

Thermal Excitation of Carriers

We want to calculate the number of charge carriers at a temperature T in a simple semiconductor. The probability that a state at energy ε is occupied is

$$f(\varepsilon) = \frac{1}{e^{(\varepsilon - \mu)/k_B T}}.$$

The value of μ is fixed to give the correct number of particles in the system. We will also need the density of states for the conduction and valence band:

$$\text{conduction band} \quad g(\varepsilon) = \frac{V}{2\pi^2 \hbar^3} (2m_e)^{3/2} \sqrt{\varepsilon - E_G}$$

and

$$\text{valence band} \quad g(\varepsilon) = \frac{V}{2\pi^2 \hbar^3} (2m_h)^{3/2} \sqrt{-\varepsilon}.$$

Sketch the density of states and the Fermi function as function of energy on a single plot.

If $\varepsilon - \mu \gg k_B T$ find an approximation for $f(\varepsilon)$. Use this to calculate the number of electrons in the conduction band

$$n = \frac{1}{V} \int_{E_G}^{\infty} f(\varepsilon) g(\varepsilon) d\varepsilon,$$

and write the answer in terms of $N_C = 2(2\pi m_e k_B T / h^2)^{3/2}$. Next calculate the number of holes in the valence band

$$p = \frac{1}{V} \int_{-\infty}^0 [1 - f(\varepsilon)] g(\varepsilon) d\varepsilon,$$

and write the answer in terms of $N_V = 2(2\pi m_h k_B T / h^2)^{3/2}$.

Show that np is independent of the value of the chemical potential μ .