

$$f(x) = w_0 + w_1 x + w_2 x^2 = \sum_{i=0}^2 w_i x^i$$

$$f(x) = \sum_{i=0}^N w_i x^i$$

w = vector of coefficients

Task 4

1. Identify the knowns and unknowns in the polynomial

w_0, w_1, w_2, x (unless provided)

2. Linear or non in w

Linear in w because w_0, w_1, w_2 involve x^i

3. Linear or non in x
non
this means Linear Regression

4. Outline Algorithm using Least squares

$$X = \begin{bmatrix} 1 & x_1 & x_1^2 \\ 1 & x_2 & x_2^2 \\ 1 & x_3 & x_3^2 \end{bmatrix} \quad Y = \begin{bmatrix} y_1 \\ y_2 \\ y_3 \end{bmatrix} \quad W = [w_0, w_1, w_2]^T$$

↓

$$W = (X^T X)^{-1} X^T Y$$

5. just extend X to $N \times N$ size
 y to N size
 w to transpose all w_i

Task 5

The projection matrix $P = A(A^T A)^{-1} A^T$
is equal to identity sometimes

1. Example of a design matrix $P = I$

$$\begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

2. Why usually not for projection?

Because a projection with identity does absolutely nothing

3. prove a condition $P = I$

$$A = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$P = A(A^T A)^{-1} A^T = I$$