



# Wobbling motion in A~190 region

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Nirupama Sensharma

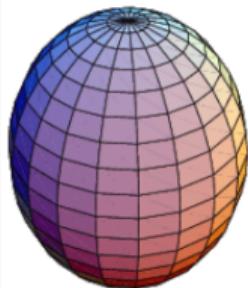
Fifth Joint Meeting of the DNP of the APS and the JPS

October 24, 2018

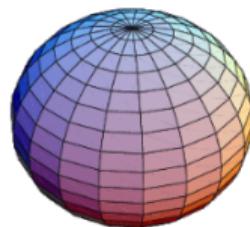
University of Notre Dame

# Nuclear Shapes

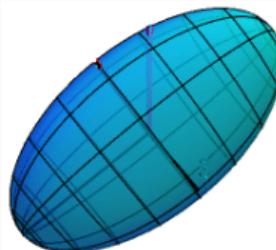
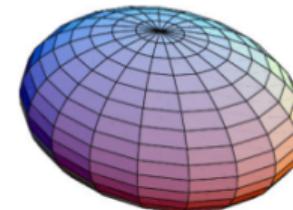
Prolate



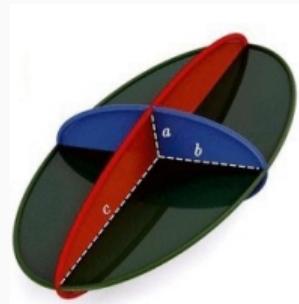
Spherical



Oblate



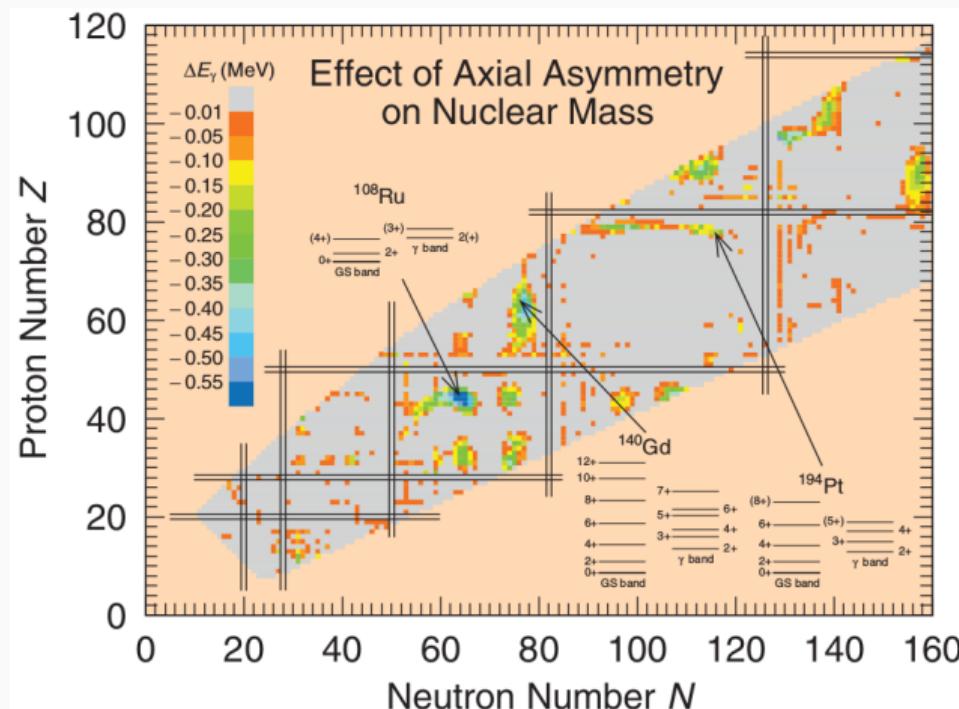
Triaxial Nucleus



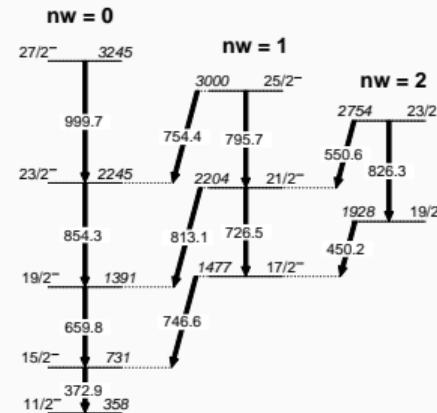
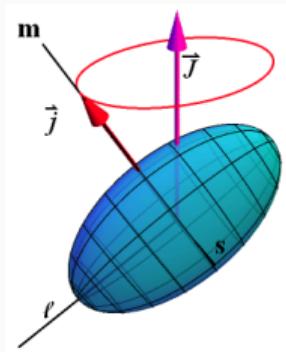
# Triaxial Region

Triaxiality - A rare phenomenon!

P. Möller et. al. PRL 97, 162502 (2006)



# Wobbling - Unique fingerprint of Triaxiality

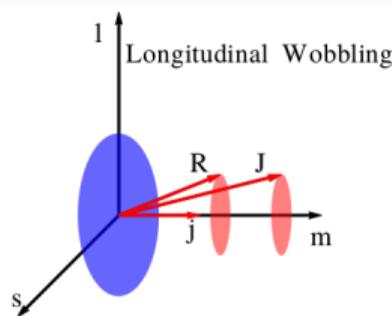


- Analog of the spinning motion of an asymmetric top.
- Oscillation of a principal axis about the space fixed  $\vec{J}$ .

## Standard fingerprints for Wobbling bands:

- Rotational bands corresponding to  $n_w = 0, 1, 2, \dots$
- Transitions from  $n_{w+1} \rightarrow n_w$  ( $\Delta n_w = +1$ )
- Interband Transitions are  $\Delta I = 1$ , E2

## Wobbling in odd-A nuclei - Types of Wobbling(1/2)

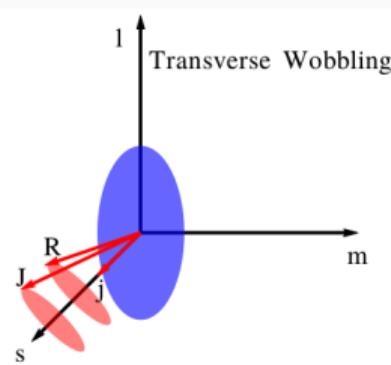


- Odd-particle aligned with axis with max. MOI ( $m$ -axis).
- $\mathcal{J}_3 > \mathcal{J}_2$  and  $\mathcal{J}_3 > \mathcal{J}_1$
- Longitudinal wobbling:  
$$\mathcal{J}_3 = \mathcal{J}_m$$

$$\text{Wobbling energy, } \hbar\omega_w = \frac{j}{\mathcal{J}_3} \left[ \left( 1 + \frac{J}{j} \left( \frac{\mathcal{J}_3}{\mathcal{J}_1} - 1 \right) \right) \left( 1 + \frac{J}{j} \left( \frac{\mathcal{J}_3}{\mathcal{J}_2} - 1 \right) \right) \right]^{1/2}$$

$\implies E_{\text{wobb}}$  increases with  $J$ .

## Wobbling in odd-A nuclei - Types of Wobbling(2/2)



- Odd-particle aligned perpendicular to axis with max. MOI (s- or l-axis).
- $\mathcal{J}_3 < \mathcal{J}_2$  and  $\mathcal{J}_3 > \mathcal{J}_1$
- Transverse wobbling:  
$$\mathcal{J}_3 = \mathcal{J}_s$$

$$\text{Wobbling energy, } \hbar\omega_w = \frac{j}{\mathcal{J}_3} \left[ \left( 1 + \frac{J}{j} \left( \frac{\mathcal{J}_3}{\mathcal{J}_1} - 1 \right) \right) \left( 1 + \frac{J}{j} \left( \frac{\mathcal{J}_3}{\mathcal{J}_2} - 1 \right) \right) \right]^{1/2}$$

$\implies E_{\text{wobb}}$  decreases with  $J$ .

## More on wobbling...

- $^{163}\text{Lu}$  - first observation of wobbling in 2001.
- For long, wobbling known in only 5 nuclei:  $^{161}\text{Lu}$ ,  $^{163}\text{Lu}$ ,  $^{165}\text{Lu}$ ,  $^{167}\text{Lu}$  and  $^{167}\text{Ta}$ .  
*Eur. Phys. J. A 24 (2005), PRL 86(2001), PLB 552 (2003), PLB 553 (2003), PRC 80 (2009)*
- All in  $A \sim 160$  region.

- Breakthrough observation in 2015 - Wobbling found in  $^{135}\text{Pr}$ .  
*J. T. Matta et. al., PRL 114 (2015)*
- Followed by reporting of wobbling bands in  $^{133}\text{La}$ .  
*S. Biswas, et al., arxiv: nucl-ex 1608 (2016) 07840v1.*

***Are there other regions of nuclear chart where wobbling bands may be observed?***

## Exploring in A~190 region

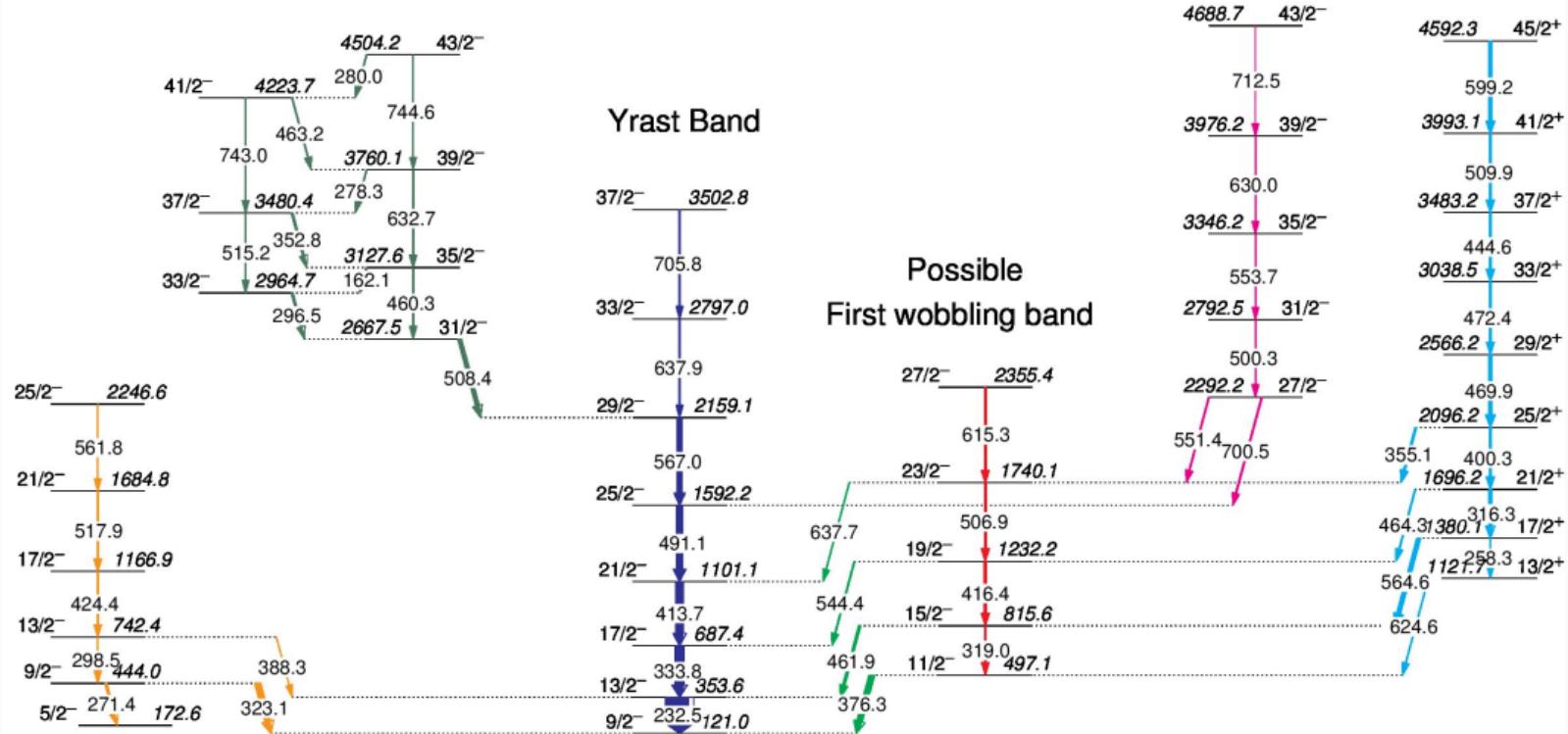
- Significant triaxiality suggested for nuclei at low spins in this mass region.  
(T. Nikšić, et. al. Part. Nucl. Phys. 66 (2011))
- Clear evidence for triaxiality provided by observation of chiral band pairs in  $^{188}\text{Ir}$ ,  $^{194}\text{Tl}$  and  $^{198}\text{Tl}$ .
- Our choice -  $^{187}\text{Au}$ 
  - The nucleus  $^{186}\text{Pt}$  known to exhibit triaxial behavior.
  - Wobbling observed so far only in odd-Z nuclei.
  - The  $\pi h_{9/2}$  orbital expected to lead to stabilization of triaxial shapes in this region.

# Experiment

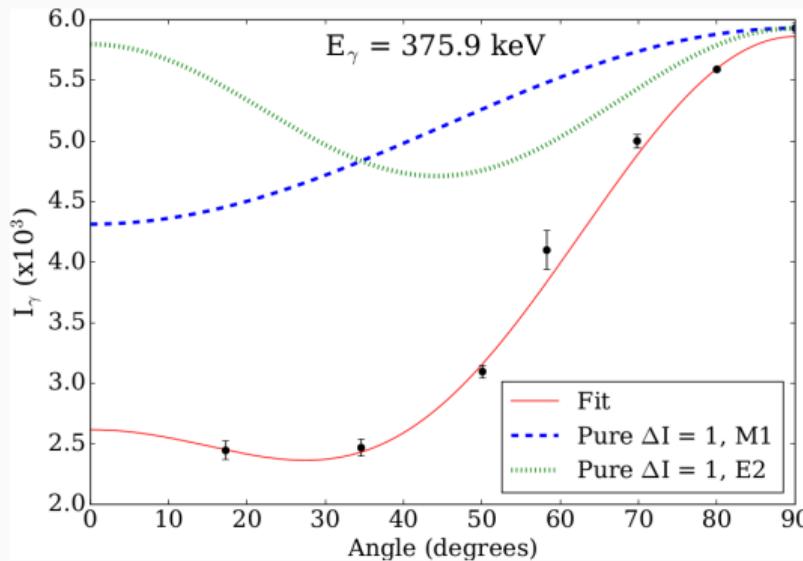
- Experiment performed using Gammasphere array at the Argonne National Laboratory.
- Reaction:  $^{174}\text{Yb}(^{19}\text{F},6\text{n})^{187}\text{Au}$  at 115 MeV.
- 73 Compton suppressed Ge detectors used.
- No. of three and higher-fold  $\gamma$ -ray coincidence events collected -  $6 \times 10^{10}$ .



# Partial Level Scheme of $^{187}\text{Au}$

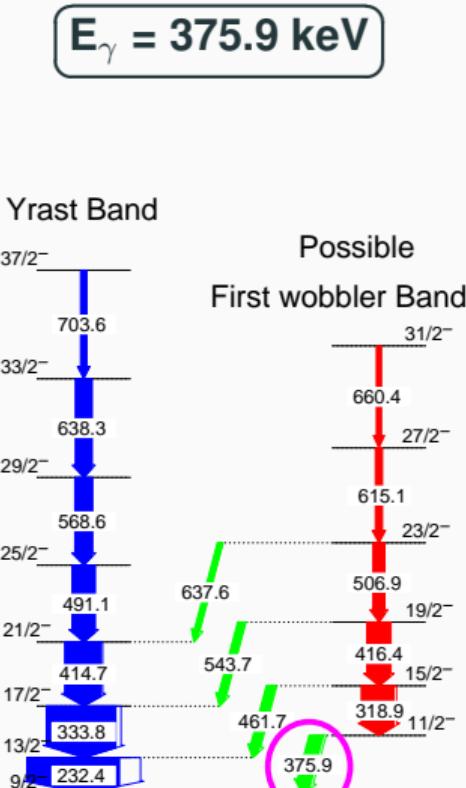


# Angular Distributions (1/4)

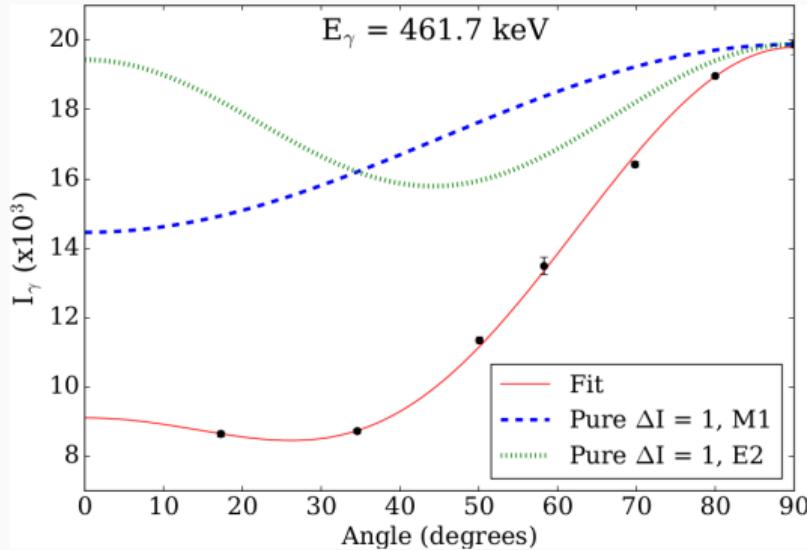


$$\delta = -2.62^{+0.09}_{-0.11}$$

$$E2\% = 87.28^{+0.93}_{-0.76}$$



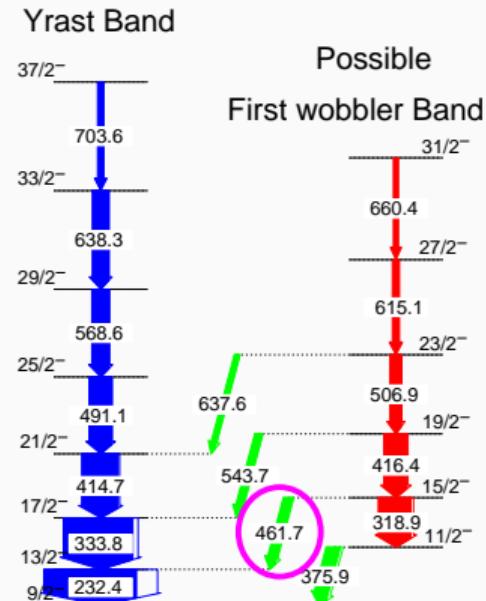
## Angular Distributions (2/4)



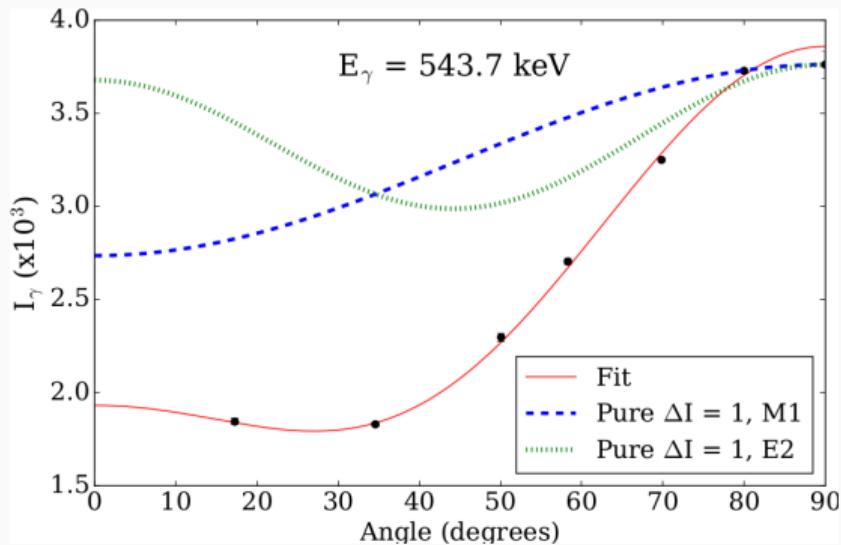
$$\delta = -2.97^{+0.04}_{-0.04}$$

$$E2\% = 89.82^{+0.25}_{-0.25}$$

$E_\gamma = 461.7 \text{ keV}$

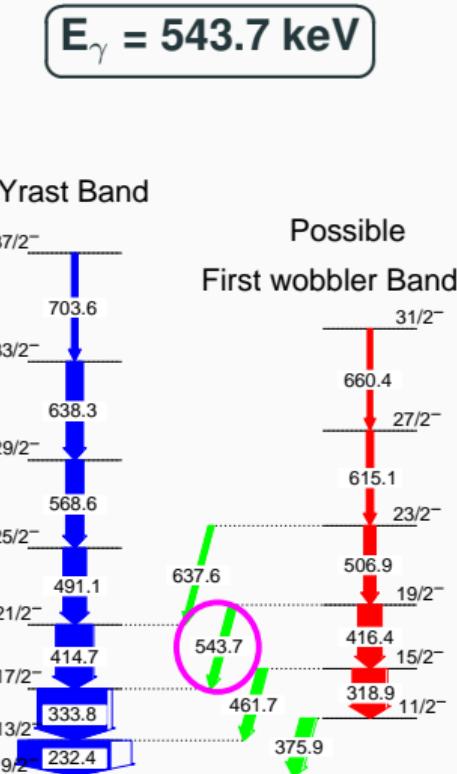


## Angular Distributions (3/4)

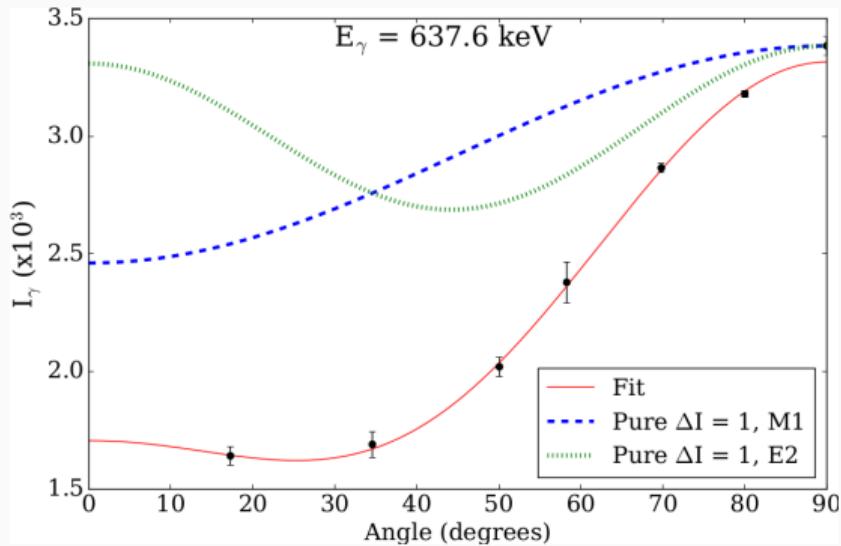


$$\delta = -3.45^{+0.05}_{-0.06}$$

$$E2\% = 92.25^{+0.25}_{-0.21}$$



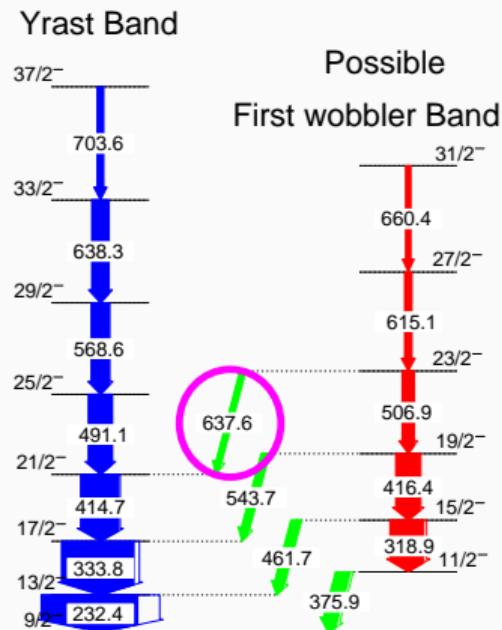
# Angular Distributions (4/4)



$$\delta = -3.82^{+0.17}_{-0.19}$$

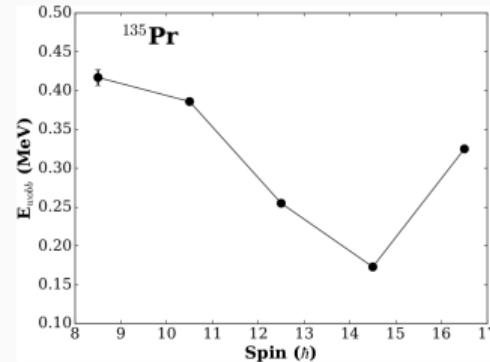
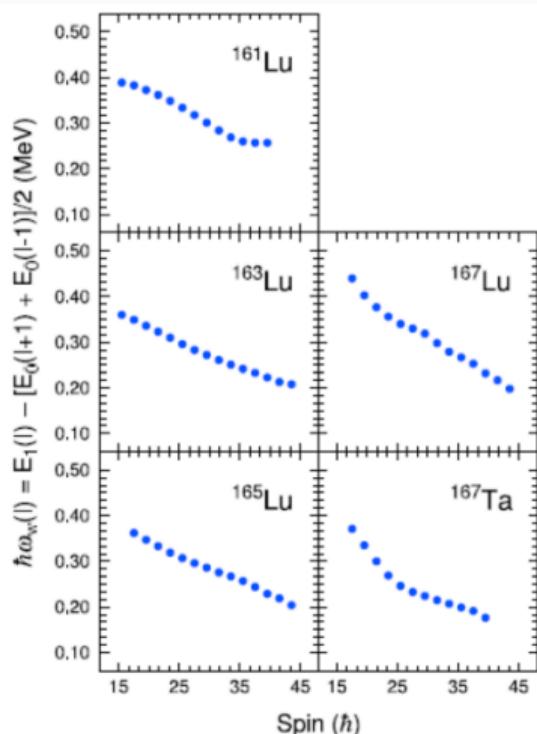
$$E2\% = 93.59^{+0.60}_{-0.53}$$

$E_\gamma = 637.6 \text{ keV}$



# Wobbling Energy (1/3)

Wobbling energy ( $E_{\text{wobb}}$ ) - energy associated with wobbling excitations.



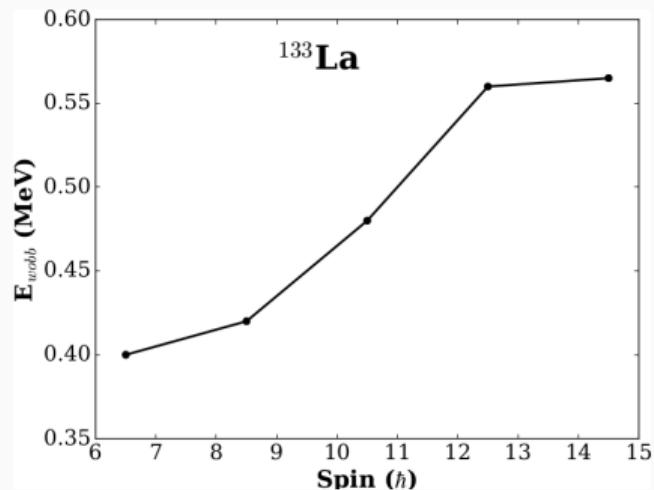
## Transverse Wobbling

*Odd particle aligns  $\perp$  to axis with maximum M.O.I*

S. Frauendorf, F. Dönau, Phys. Rev. C 89 (2014)

## Wobbling Energy (2/3)

Wobbling energy ( $E_{wobb}$ ) - energy associated with wobbling excitations.

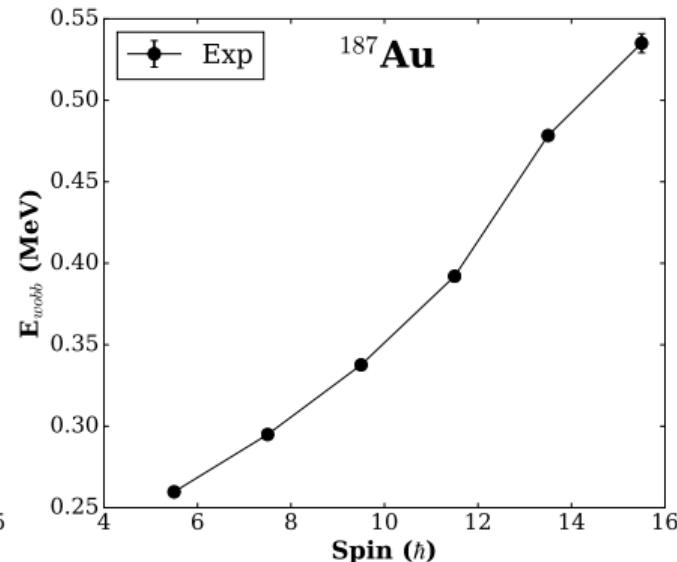
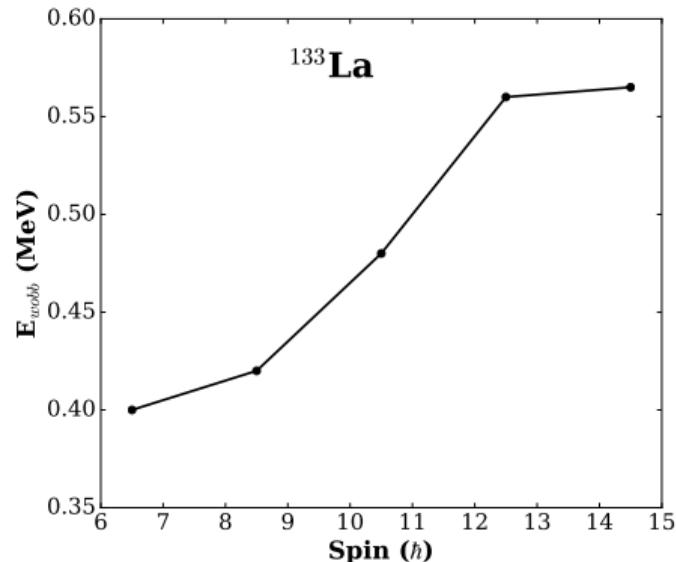


### First case of Longitudinal Wobbling

*Odd particle aligns parallel to axis with maximum M.O.I*

## Wobbling Energy (3/3)

Wobbling energy ( $E_{wobb}$ ) - energy associated with wobbling excitations.



$^{187}\text{Au}$  - Only the second case of Longitudinal Wobbling!

## Conclusion and Future Work

- Wobbling motion has been investigated in the  $A \sim 190$  region.
- $^{187}\text{Au}$  - clear observation of wobbling bands.
- $^{187}\text{Au}$  - only the second case of *Longitudinal wobbling*.
- Calculations in the framework of the Particle Rotor Model (PRM) being done to affirm experimental observations.

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