

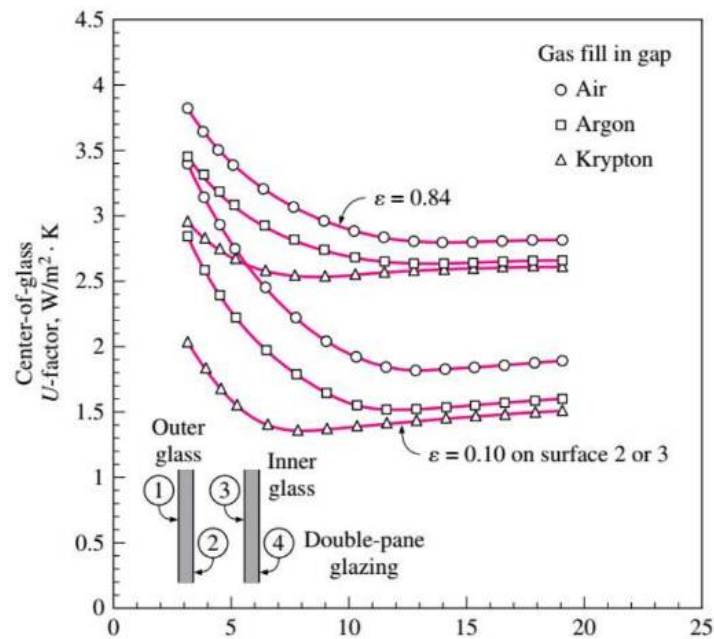
# WEEK 8 ASSIGNMENT

oalha

## QUESTION 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? (Keep the gap thickness to be 13 mm)

ANSWER:



With Double pane glazing (  $\epsilon = 0.84$  ) & gap thickness 13mm

U- Value of a double pane glazing window if the gap is filled with air is 2.8

$$\frac{w}{m^2 k}$$

$\epsilon$ value	0.84		0.10			0.84			0.1		
No. of panes	2	2	2	2	2	3	3	3	3	3	3
Gas	Argon	Krypton	Air	Argon	Krypton	Air	Argon	Krypton	Air	Argon	krypton
U value	2.65	2.6	1.8	1.5	1.4	1.8	1.7	1.6	1	0.8	0.7
% of change	5.4	7.2	35.7	46.4	50	35.7	39.2	42.8	64.3	71.4	75

## QUESTION 2

Consider the house that we analysed in the last two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m<sup>2</sup> on the west, fixed 3.6 m<sup>2</sup> on the south and an operable 3.6 m<sup>2</sup> on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium?

**ANSWER:**

Latitude ≈ 45

T<sub>cooling</sub> = 24°C

T<sub>heating</sub> = 20°C

$$\Delta T_{cooling} = 31.9^{\circ}\text{C} - 24^{\circ}\text{C} = 7.9^{\circ}\text{C}$$

$$\Delta T_{heating} = 20^{\circ}\text{C} - (-4.8)^{\circ}\text{C} = 24.8^{\circ}\text{C}$$

From the table DR = 11.9 °C

### FIXED WINDOW ON WEST SIDE

Area = 14.4 m<sup>2</sup>

### COOLING LOAD

$$q_{west\ window} = A \times CF_{west\ window}$$

$$\Delta T_{cooling} - 0.46\text{ DR}$$

$$CF_{west\ window(heat\ transfer)} = U_{west\ window} \dot{V}$$

$$U_{west\ window} = 2.84 \frac{W}{m^2 K}$$

$$7.9\text{ K} - 0.46 (11.9\text{ K})$$

$$CF_{west\ window(heat\ transfer)} = 2.84 \frac{W}{m^2 K} \dot{V}$$

$$\approx 6.89 \frac{W}{m^2}$$

Irradiation

$$E_D = 559$$

$$E_d = 188$$

$$PXI_{west\ window} = E_D + E_d$$

$$= 559 + 188 = 747$$

Since no internal shading, so IAC = 1

$$SHGC = 0.54$$

$$FF_s = 0.56$$

$$CF_{west\ window(irradiation)} = PXI \times SHGC \times IAC \times FF_s$$

$$= 747 \times 0.54 \times 1 \times 0.56 = 225.89$$

Glazing Type	Glazing Layers	ID <sup>b</sup>	Property <sup>c,d</sup>	Center of Glazing	Frame									
					Operable					Fixed				
					Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum	Reinforced Vinyl/Aluminum Clad Wood	Wood/Vinyl	Insulated Fiberglass/Vinyl	Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum	Reinforced Vinyl/Aluminum Clad Wood
Clear	1	1a	U	SHGC	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55
					0.86	0.75	0.75	0.64	0.64	0.64	0.78	0.78	0.75	0.75
					2.73	4.62	3.42	3.00	2.87	5.83	3.61	3.22	2.86	2.84
	2	5a	U	SHGC	0.76	0.67	0.67	0.57	0.57	0.57	0.69	0.69	0.67	0.67
					1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01
					0.68	0.60	0.60	0.51	0.51	0.51	0.62	0.62	0.60	0.60
Low-e, low-solar	2	25a	U	SHGC	1.70	3.83	2.68	2.33	2.21	1.89	2.75	2.36	2.03	2.01
					0.41	0.37	0.37	0.31	0.31	0.31	0.38	0.38	0.36	0.36
					1.02	3.22	2.07	1.76	1.71	1.45	2.13	1.76	1.44	1.40
	3	40c	U	SHGC	0.27	0.25	0.25	0.21	0.21	0.21	0.25	0.25	0.24	0.24
					1.99	4.05	2.89	2.52	2.39	2.07	2.99	2.60	2.26	2.24
					0.70	0.62	0.62	0.52	0.52	0.52	0.64	0.64	0.61	0.61
Low-e, high-solar	3	32c	U	SHGC	1.42	3.54	2.36	2.02	1.97	1.70	2.47	2.10	1.77	1.73
					0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.54	0.54
					5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55
Heat-absorbing	1	1c	U	SHGC	0.73	0.64	0.64	0.54	0.54	0.54	0.66	0.66	0.64	0.64
					2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84
					0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.54	0.54
	2	5c	U	SHGC	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01
					0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.30	0.30
					5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55
Reflective	1	1i	U	SHGC	0.31	0.28	0.28	0.24	0.24	0.24	0.29	0.29	0.27	0.27
					2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84
					0.29	0.27	0.27	0.22	0.22	0.22	0.27	0.27	0.26	0.26
	2	5p	U	SHGC	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01
					0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.30	0.30
					5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55

Table 10 Peak Irradiance, W/m<sup>2</sup>

Exposure	Latitude	Latitude									
		20°	25°	30°	35°	40°	45°	50°	55°	60°	
North	E <sub>D</sub>	125	106	92	84	81	85	96	112	136	
	E <sub>d</sub>	128	115	103	93	84	76	69	62	55	
	E <sub>t</sub>	253	221	195	177	166	162	164	174	191	
Northeast/Northwest	E <sub>D</sub>	460	449	437	425	412	399	386	374	361	
	E <sub>d</sub>	177	169	162	156	151	147	143	140	137	
	E <sub>t</sub>	637	618	599	581	563	546	529	513	498	
East/West	E <sub>D</sub>	530	543	552	558	560	559	555	547	537	
	E <sub>d</sub>	200	196	193	190	189	188	187	187	187	
	E <sub>t</sub>	730	739	745	748	749	747	742	734	724	
Southeast/Southwest	E <sub>D</sub>	282	328	369	405	436	463	485	503	517	
	E <sub>d</sub>	204	203	203	204	205	207	210	212	215	
	E <sub>t</sub>	485	531	572	609	641	670	695	715	732	
South	E <sub>D</sub>	0	60	139	214	283	348	408	464	515	
	E <sub>d</sub>	166	193	196	200	204	209	214	219	225	
	E <sub>t</sub>	166	253	335	414	487	557	622	683	740	
Horizontal	E <sub>D</sub>	845	840	827	806	776	738	691	637	574	
	E <sub>d</sub>	170	170	170	170	170	170	170	170	170	
	E <sub>t</sub>	1015	1010	997	976	946	908	861	807	744	

Table 13 Fenestration Solar Load Factors FF<sub>s</sub>

Exposure	Single Family Detached	Multifamily
North	0.44	0.27
Northeast	0.21	0.43
East	0.31	0.56
Southeast	0.37	0.54
South	0.47	0.53
Southwest	0.58	0.61
West	0.56	0.65
Northwest	0.46	0.57
Horizontal	0.58	0.73

$$\begin{aligned}
 & \text{CF} \\
 & (\text{west window irradiation}) \\
 q_{\text{west window}} &= A \times CF_{\text{west window}} = A \times \text{CF} \\
 &= 14.4 \text{ m}^2 \times (6.89 + 225.89) \frac{\text{W}}{\text{m}^2} = 3352.07 \text{ W}
 \end{aligned}$$

## HEATING LOAD

$$\begin{aligned}
 q_{\text{west window}} &= A \times HF_{\text{west window}} = A \times U_{\text{west window}} \times \Delta T_{\text{heating}} \\
 &= 14.4 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 1014.22 \text{ W}
 \end{aligned}$$

## If the frame is aluminium

$$U'_{\text{west window}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{SHGC}' = 0.56$$

## Cooling load

$$\begin{aligned}
 & \Delta T_{\text{cooling}} - 0.46 \text{ DR}) \\
 CF'_{\text{west window (heat transfer)}} &= U'_{\text{west window}} \text{CF} \\
 &= 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 8.76 \frac{\text{W}}{\text{m}^2}
 \end{aligned}$$

$$\begin{aligned}
 CF'_{\text{west window (irradiation)}} &= \text{PFI} \times \text{SHGC}' \times \text{IAC} \times \text{FF}_s \\
 &= 747 \times 0.56 \times 1 \times 0.56 = 234.26
 \end{aligned}$$

$$\begin{aligned}
 & CF' \\
 & (\text{west window irradiation}) \\
 q'_{\text{west window}} &= A \times \text{CF}' \\
 &= 14.4 \text{ m}^2 \times (8.76 + 234.26) \frac{\text{W}}{\text{m}^2} = 3499.48 \text{ W}
 \end{aligned}$$

## Heating load

$$\begin{aligned}
 q'_{\text{west window}} &= A \times HF'_{\text{west window}} = A \times U'_{\text{west window}} \times \Delta T_{\text{heating}} \\
 &= 14.4 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 1289.20 \text{ W}
 \end{aligned}$$

## FIXED WINDOW ON SOUTH SIDE

$$\text{Area} = 3.6 \text{ m}^2$$

## COOLING LOAD

$$\begin{aligned}
 q_{\text{south window}} &= A \times CF_{\text{south window}} \\
 & \Delta T_{\text{cooling}} - 0.46 \text{ DR}) \\
 CF_{\text{south window (heat transfer)}} &= U_{\text{south window}} \text{CF} \\
 U_{\text{south window}} &= 2.84 \frac{\text{W}}{\text{m}^2 \text{K}}
 \end{aligned}$$

$$7.9 \text{ K} - 0.46 (11.9 \text{ K}) \approx 6.89 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{south window (heat transfer)}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{K}}$$

Irradiation

$$E_D = 348$$

$$E_d = 209$$

$$P_{\text{XI west window}} = E_D + E_d = 348 + 209 = 557$$

Since no internal shading, so IAC = 1

$$\text{SHGC} = 0.54$$

$$FF_s = 0.47$$

$$CF_{\text{south window (irradiation)}} = P_{\text{XI}} \times \text{SHGC} \times \text{IAC} \times FF_s = 557 \times 0.54 \times 1 \times 0.47 = 141.36$$

$$(q_{\text{south window (irradiation)}})$$

$$q_{\text{south window}} = A \times CF_{\text{south window}} = A \times (6.89 + 141.36) \frac{\text{W}}{\text{m}^2} = 3.6 \text{ m}^2 \times (6.89 + 141.36) \frac{\text{W}}{\text{m}^2} = 533.72 \text{ W}$$

HEATING LOAD

$$q_{\text{south window}} = A \times HF_{\text{south window}} = A \times U_{\text{south window}} \times \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 253.56 \text{ W}$$

If the frame is aluminium

$$U'_{\text{south window}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{SHGC}' = 0.56$$

Cooling load

$$\Delta T_{\text{cooling}} = 0.46 \text{ DR}$$

$$CF'_{\text{south window (heat transfer)}} = U'_{\text{south window}}$$

$$= 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$CF'_{\text{south window (irradiation)}} = P_{\text{XI}} \times \text{SHGC}' \times \text{IAC} \times FF_s = 557 \times 0.56 \times 1 \times 0.47 = 146.6$$

$$(q'_{\text{south window (irradiation)}})$$

$$q'_{\text{south window}} = A \times (8.76 + 146.60) \frac{\text{W}}{\text{m}^2}$$

$$= 3.6 \text{ m}^2 \times (8.76 + 146.60) \frac{\text{W}}{\text{m}^2} = 559.30 \text{ W}$$

Heating load

$$q'_{\text{south window}} = A \times HF'_{\text{south window}} = A \times U'_{\text{south window}} \times \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 322.30 \text{ W}$$

## OPERABLE WINDOW ON SOUTH SIDE

$$\text{Area} = 3.6 \text{ m}^2$$

## COOLING LOAD

$$q_{\text{south window}} = A \times CF_{\text{south window}}$$

$$\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$CF_{\text{south window (heat transfer)}} = U_{\text{south window}} \dot{Q}$$

$$U_{\text{south window}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$7.9 \text{ K} - 0.46 (11.9 \text{ K})) \approx 6.96 \frac{\text{W}}{\text{m}^2}$$

$$CF_{\text{south window (heat transfer)}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{K}} \dot{Q}$$

## Irradiation

$$E_D = 348$$

$$E_d = 209$$

$$P_{\text{XI south window}} = E_D + E_d = 348 + 209 = 557$$

Since no internal shading, so IAC = 1

$$\text{SHGC} = 0.46$$

$$FF_s = 0.47$$

$$CF_{\text{south window (irradiation)}} = P_{\text{XI}} \times \text{SHGC} \times \text{IAC} \times FF_s = 557 \times 0.46 \times 1 \times 0.47 = 120.42$$

$$CF$$

$$(\dot{Q}_{\text{south window (irradiation)}})$$

$$q_{\text{south window}} = A \times CF_{\text{south window}} = A \dot{Q}$$

$$= 3.6 \text{ m}^2 \times (6.96 + 120.42) \frac{\text{W}}{\text{m}^2} = 458.58 \text{ W}$$

## HEATING LOAD

$$q_{\text{south window}} = A \times HF_{\text{south window}} = A \times U_{\text{south window}} \times \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 2.87 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 256.23 \text{ W}$$

## If the frame is aluminium

$$U'_{\text{south window}} = 4.62 \frac{\text{W}}{\text{m}^2 \text{K}}$$

$$\text{SHGC}' = 0.55$$

## Cooling load

$$\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$CF'_{\text{south window (heat transfer)}} = U'_{\text{south window}} \dot{Q}$$

$$= 4.62 \frac{\text{W}}{\text{m}^2 \text{K}} (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 11.21 \frac{\text{W}}{\text{m}^2}$$

$$CF'_{\text{west window (irradiation)}} = PXI \times SHGC' \times IAC \times FF_s = 557 \times 0.55 \times 1 \times 0.47 = 143.98$$

$$CF'_{\text{west window (irradiation)}} \\ q'_{\text{west window}} = A \times i$$

$$= 3.6 \text{ m}^2 \times (11.21 + 143.98) \frac{\text{W}}{\text{m}^2} = 558.70 \text{ W}$$

Heating load

$$q'_{\text{south window}} = A \times HF'_{\text{south window}} = A \times U'_{\text{south window}} \times \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 4.62 \frac{\text{W}}{\text{m}^2 \text{K}} \times 24.8 \text{ K} = 412.47 \text{ W}$$