

## WEEK 8

Monday, December 16, 2019 2:31 AM

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- Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? ( keep the gap thickness to be 13 mm)

	BENCHMARK	1	2	3
GAP	13mm	13mm	13mm	13mm
e	0,84	0,84	0,1	0,84
N° PANE	2	2	2	3
GAS	AIR	KRYPTON	AIR	AIR
UFACTOR	2,8 W/m <sup>2</sup> K	2,6 W/m <sup>2</sup> K	1,8 W/m <sup>2</sup> K	1,8 W/m <sup>2</sup> K
%	100%	93%	64%	64%

- Consider the house that we analysed in the alst two examples, calculate the heating and cooling load of the other windows which are fixed  
m<sup>2</sup> on the west, fixed 3.6 m<sup>2</sup> on the south and an operable 3.6 m<sup>2</sup> on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium ?

**PIACENZA LAT:** 44,92 N

**LONG:** 9,73 E

**ELEV :**138

**TSUMMER:** 24°

**TWINTER:** 20°

**HEATING DB 99%:** - 4,8

**COOLING DB/MCWB 1%:** 31,9

$$DT_{cooling} = 31.9 - 24 = 7.9^{\circ}\text{C}$$

$$DT_{heating} = 20 - (-4.8) = 24.8^{\circ}\text{C} \quad DR = 11.9^{\circ}\text{C}$$

### Wood Frames

Window1(east, wood frame, fixed)

$$A_{window1} = 14.4 \text{ m}^2$$

### Heating:

$$U_{window1} = 2.84 \text{ W/m}^2 \cdot \text{K}$$

$$HF_{window1} = U_{window1} \cdot DT_{cooling} = 2.84 \cdot 24.8 = 70.44 \text{ W / m}^2$$

$$Q_{window1} = HF_{window1} \cdot A_{window} = 70.44 \cdot 14.44 = 1014.2 \text{ W}$$

**Cooling:****Heat transfer:**

$$CF_{\text{window1}} = U_{\text{window1}} (DT_{\text{cooling}} - 0.46DR) = 2.84(7.9 - 0.46 \cdot 11.9) = 6.9 \text{ W / m}^2$$

Irradiation:

$$ED = 559,$$

$$Ed = 188,$$

$$FF_{\text{seast}}$$

$$= 0.31$$

$$PXL_{\text{window1}} = ED + Ed = 559 + 188 = 747$$

$$CF_{\text{window1}} = PXL \cdot SHGC \cdot IAC \cdot FF_{\text{seast}} = 747 \cdot 0.54 \cdot 1 \cdot 0.31 = 125.1$$

$$CF_{\text{fenestration1}} = U_{\text{window1}} (DT_{\text{cooling}} - 0.46DR) + PXL \cdot SHGC \cdot IAC \cdot FF_{\text{seast}} \\ = 6.9 + 125.1 = 132 \text{ W / m}^2$$

$$Q\&_{\text{window1}} = CF_{\text{fenestration1}} \cdot A_{\text{window1}} = 132 \cdot 14.4 = 1900.8 \text{ W}$$

**Window2(west, wood frame, fixed)**

$$A_{\text{window2}} = 14.4 \text{ m}^2$$

**Heating:**

$$U_{\text{window2}} = 2.84 \text{ W / m}^2 \cdot \text{K}$$

$$HF_{\text{window2}} = U_{\text{window2}} \cdot DT_{\text{cooling}} = 2.84 \cdot 24.8 = 70.44 \text{ W / m}^2$$

$$Q_{\text{window2}} = HF_{\text{window2}} \cdot A_{\text{window2}} = 70.44 \cdot 14.4 = 1014.2 \text{ W}$$

**Cooling:****Heat transfer:**

$$CF_{\text{window2}} = U_{\text{window2}} (DT_{\text{cooling}} - 0.46DR) = 2.84(7.9 - 0.46 \cdot 11.9) = 6.9 \text{ W / m}^2$$

Irradiation:

$$ED = 559, Ed = 188,$$

$$FF_{\text{swest}} = 0.56,$$

$$PXL_{\text{window1}} = ED + Ed = 559 + 188 = 747$$

$$CF_{\text{window2}} = PXL \cdot SHGC \cdot IAC \cdot FF_{\text{swest}} = 747 \cdot 0.56 \cdot 1 \cdot 0.56 = 225.9$$

$$CF_{\text{fenestration2}} = U_{\text{window2}} (DT_{\text{cooling}} - 0.46DR) + PXL \cdot SHGC \cdot IAC \cdot FF_{\text{swest}} \\ = 6.9 + 225.9 = 232.8 \text{ W / m}^2$$

$$Q\&_{\text{window2}} = CF_{\text{fenestration2}} \cdot A_{\text{window2}} = 232.8 \cdot 14.4 = 3352.32 \text{ W}$$

**Window3(south, wood frame, fixed)**

$$A_{\text{window3}} = 3.6 \text{ m}^2$$

**Heating:**

$$U_{\text{window3}} = 2.84 \text{ W / m}^2 \cdot \text{K}$$

$$HF_{\text{window3}} = U_{\text{window3}} \cdot DT_{\text{cooling}} = 2.84 \cdot 24.8 = 70.44 \text{ W / m}^2 \\ Q_{\text{window3}} = HF_{\text{window3}} \cdot A_{\text{window3}} = 70.44 \cdot 3.6 = 253.6 \text{ W}$$

**Cooling:****Heat transfer:**

$$CF_{\text{window3}} = U_{\text{window3}} (DT_{\text{cooling}} - 0.46DR) = 2.84(7.9 - 0.46 \cdot 11.9) = 6.9 \text{ W / m}^2$$

Irradiation:

$$ED=348, Ed=209,$$

$$FF_{ssouth}=0.47$$

$$Pxl_{window3}=ED+Ed=348+209=557$$

$$CF_{window3}=Pxl \cdot SHGC \cdot IAC \cdot FF_{ssouth}=557 \cdot 0.54 \cdot 1 \cdot 0.47=141.4$$

$$CF_{fenestration3}=U_{window3}(DT_{cooling}-0.46DR)+Pxl \cdot SHGC \cdot IAC \cdot FF_{ssouth}$$

$$=6.9+141.4=148.3W/m^2$$

$$Q_{window3}=CF_{fenestration3} \cdot A_{window3}=148.3 \cdot 3.6=533.88W$$

#### Window4(south, wood frame, openable)

$$A_{window4}=3.6m^2$$

##### Heating:

$$U_{window4}=2.87W/m^2 \cdot K$$

$$HF_{window4}=U_{window4} \cdot DT_{cooling}=2.87 \cdot 24.8=71.17W/m^2$$

$$Q_{window4}=HF_{window4} \cdot A_{window4}=71.17 \cdot 3.6=256.2W$$

##### Cooling:

##### Heat transfer:

$$CF_{window4}=U_{window4}(DT_{cooling}-0.46DR)=2.87(7.9-0.46 \cdot 11.9)=6.96W/m^2$$

Irradiation:

$$ED=348, Ed=209, S_{Rom}=0.46,$$

$$FF_{ssouth}=0.47$$

$$Pxl_{window4}=ED+Ed=348+209=557$$

$$CF_{window4}=Pxl \cdot SHGC \cdot IAC \cdot FF_{ssouth}=557 \cdot 0.46 \cdot 1 \cdot 0.47=120.4$$

$$CF_{fenestration4}=U_{window4}(DT_{cooling}-0.46DR)+Pxl \cdot SHGC \cdot IAC \cdot FF_{ssouth}$$

$$=6.9+120.4=127.3W/m^2$$

$$Q_{window4}=CF_{fenestration4} \cdot A_{window4}=127.3 \cdot 3.6=458.28W$$

$$Q_{totalcoolingwood}=1900.8+3352.32+533.88+458.28=6245.3W$$

$$Q_{totalheatingwood}=1014.2+1014.2+253.6+256.2=2538.2W$$

Aluminum Frames

#### Window1(south, aluminum frame, fixed)

$$A_{window1}=14.4m^2$$

##### Heating:

$$U_{window1}=3.61W/m^2 \cdot K$$

$$HF_{window1}=U_{window1} \cdot DT_{cooling}=3.61 \cdot 24.8=89.52W/m^2$$

$$Q_{window1}=HF_{window1} \cdot A_{window1}=89.52 \cdot 14.4=1289.1W$$

##### Cooling:

##### Heat transfer:

$$CF_{window1}=U_{window1}(DT_{cooling}-0.46DR)=3.61(7.9-0.46 \cdot 11.9)=8.7W/m^2$$

Irradiation:

$$ED=559,$$

$$Ed=188, S_{Rom}=0.56$$

$$FF_{seast}=0.31$$

$$PXI_{window1} = ED + Ed = 559 + 188 = 747$$

$$CF_{window1} = PXI \cdot SHGC \cdot IAC \cdot FF_{seast} = 747 \cdot 0.56 \cdot 1 \cdot 0.31 = 129.6$$

$$CF_{fenestration1} = U_{window1} (DT_{cooling} - 0.46DR) + PXI \cdot SHGC \cdot IAC \cdot FF_{seast} \\ = 8.7 + 129.6 = 138.3 \text{ W} / \text{m}^2$$

$$Q_{window1} = CF_{fenestration1} \cdot A_{window1} = 138.3 \cdot 14.4 = 1991.5 \text{ W}$$

### Window2(west, aluminum frame, fixed)

$$A_{window2} = 14.4 \text{ m}^2$$

#### Heating:

$$U_{window2} = 3.61 \text{ W} / \text{m}^2 \cdot \text{K}$$

$$HF_{window2} = U_{window2} \cdot DT_{cooling} = 3.61 \cdot 24.8 = 89.52 \text{ W} / \text{m}^2$$

$$Q_{window2} = HF_{window2} \cdot A_{window2} = 89.52 \cdot 14.4 = 1289.1 \text{ W}$$

#### Cooling:

##### Heat transfer:

$$CF_{window2} = U_{window2} (DT_{cooling} - 0.46DR) = 3.61(7.9 - 0.46 \cdot 11.9) = 8.7 \text{ W} / \text{m}^2$$

Irradiation:

$$ED = 559, Ed = 188,$$

$$FF_{swest} = 0.56$$

$$PXI_{window2} = ED + Ed = 559 + 188 = 747$$

$$CF_{window2} = PXI \cdot SHGC \cdot IAC \cdot FF_{swest} = 747 \cdot 0.56 \cdot 1 \cdot 0.56 = 234.26$$

$$CF_{fenestration2} = U_{window2} (DT_{cooling} - 0.46DR) + PXI \cdot SHGC \cdot IAC \cdot FF_{swest} \\ = 8.7 + 234.26 = 242.96 \text{ W} / \text{m}^2$$

$$Q_{window2} = CF_{fenestration2} \cdot A_{window2} = 242.96 \cdot 14.4 = 2398.6 \text{ W}$$

### Window3(south, aluminum frame, fixed)

$$A_{window3} = 3.6 \text{ m}^2$$

#### Heating:

$$U_{window3} = 3.61 \text{ W} / \text{m}^2 \cdot \text{K}$$

$$HF_{window3} = U_{window3} \cdot DT_{cooling} = 3.61 \cdot 24.8 = 89.52 \text{ W} / \text{m}^2$$

$$Q_{window3} = HF_{window3} \cdot A_{window3} = 89.52 \cdot 3.6 = 322.2 \text{ W}$$

#### Cooling:

##### Heat transfer:

$$CF_{window3} = U_{window3} (DT_{cooling} - 0.46DR) = 3.61(7.9 - 0.46 \cdot 11.9) = 8.7 \text{ W} / \text{m}^2$$

Irradiation:

$$ED = 348, Ed = 209,$$

$$FF_{ssouth} = 0.47$$

$$P_{Xlwindow3} = ED + Ed = 348 + 209 = 557$$

$$CF_{window3} = P_{Xl} \cdot SHGC \cdot IAC \cdot FF_{ssouth} = 557 \cdot 0.56 \cdot 1 \cdot 0.47 = 146.6$$

$$CF_{fenestration3} = U_{window3} (DT_{cooling} - 0.46DR) + P_{Xl} \cdot SHGC \cdot IAC \cdot FF_{ssouth} \\ = 8.7 + 146.6 = 155.3 \text{ W} / \text{m}^2$$

$$Q_{\&window3} = CF_{fenestration3} \cdot A_{window3} = 155.3 \cdot 3.6 = 559.08 \text{ W}$$

#### Window4(south, aluminum frame, openable)

$$A_{window4} = 3.6 \text{ m}^2$$

##### Heating:

$$U_{window4} = 4.62 \text{ W} / \text{m}^2 \cdot \text{K} \quad R$$

$$HF_{window4} = U_{window4} \cdot DT_{cooling} = 4.62 \cdot 24.8 = 114.57 \text{ W} / \text{m}^2$$

$$Q_{window4} = HF_{window4} \cdot A_{window4} = 114.57 \cdot 3.6 = 412.4 \text{ W}$$

##### Cooling:

##### Heat transfer:

$$CF_{window4} = U_{window4} (DT_{cooling} - 0.46DR) = 4.62(7.9 - 0.46 \cdot 11.9) = 11.2 \text{ W} / \text{m}^2$$

Irradiation:

$$ED = 348, Ed = 209, SR_{om} = 0.55,$$

$$FF_{ssouth} = 0.47$$

$$P_{Xlwindow4} = ED + Ed = 348 + 209 = 557$$

$$CF_{window4} = P_{Xl} \cdot SHGC \cdot IAC \cdot FF_{ssouth} = 557 \cdot 0.55 \cdot 1 \cdot 0.47 = 143.98$$

$$CF_{fenestration4} = U_{window4} (DT_{cooling} - 0.46DR) + P_{Xl} \cdot SHGC \cdot IAC \cdot FF_{ssouth} \\ = 11.2 + 143.98 = 155.18 \text{ W} / \text{m}^2$$

$$Q_{\&window4} = CF_{fenestration4} \cdot A_{window4} = 155.18 \cdot 3.6 = 558.65 \text{ W} \quad Q_{\&totalcoolingaluminum} \\ = 1991.5 + 3498.6 + 559.08 + 558.65 = 6607.8 \text{ W} \quad Q_{\&totalheatingaluminum} \\ = 1289.1 + 1289.1 + 322.2 + 412.4 = 3312.8 \text{ W}$$

#### Conclusion:

$$Q_{\&totalcoolingwood}$$

$$/ Q_{\&totalcoolingaluminum} = 6245.3 / 6607.8 = 94.5\%$$

$$Q_{\&totalheatingwood} / Q_{\&totalheatingaluminum} = 2538.2 / 3312.8 = 76.6\%$$

From the result we can conclude that window with wooden frame has better resistance than aluminum frame. 94.5% for cooling and 76.6% for heating.