

Week Assignment 8

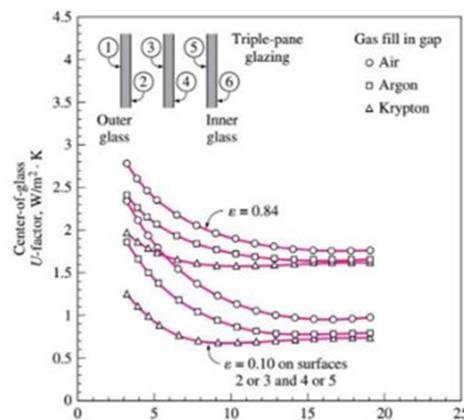
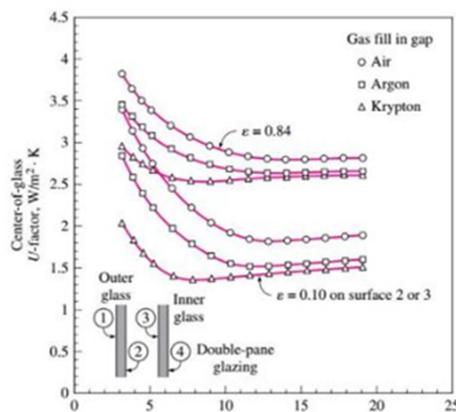
Question 1

Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating? (keep the gap thickness to be 13 mm)?

Solution

Double pane glazing ($\varepsilon=0.84$) Gap thickness = 13mm

$$U\text{-Value of a double pane glazing window if the gap is filled with air} = 2.8 \frac{W}{m^2 K}$$



ε value	0.84		0.10			0.84			0.1		
No. of panes	2	2	2	2	2	3	3	3	3	3	3
Gas	Argon	Krypton	Air	Argon	Krypton	Air	Argon	Krypton	Air	Argon	krypton
U value	2.65	2.6	1.8	1.5	1.4	1.8	1.7	1.6	1	0.8	0.7
% of change	5.4	7.2	35.7	46.4	50	35.7	39.2	42.8	64.3	71.4	75

Question 2

Consider the house that we analyzed in the last two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m² on the west, fixed 3.6 m² on the south and an operable 3.6 m² on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminum?

Solution

PIACENZA, Italy												WMO#: 160840																																										
Lat:	44.92N	Long:	9.73E	Elev:	138	StdP:	99.68	Time Zone: 1.00 (EUW)			Period: 89-10	WBAN: 99999																																										
Annual Heating and Humidification Design Conditions																																																						
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Latitude ≈ 45

Glazing Type	Glazing Layers	ID ^b	Properties ^{c,d}	Frame												
				Operable				Fixed								
				Center of Glazing	Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum Clad Wood	Wood/Vinyl	Insulated Fiberglass/Vinyl	Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum Clad Wood	Wood/Vinyl	Insulated Fiberglass/Vinyl		
Clear	1	1a	U	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35		
	2	5a	SHGC	0.86	0.75	0.64	0.64	0.64	0.78	0.64	0.78	0.75	0.75	0.75		
	3	29a	SHGC	0.76	0.67	0.57	0.57	0.57	0.61	0.53	0.61	0.58	0.58	0.58	0.58	
		SHGC	0.68	0.60	0.51	0.51	0.51	0.62	0.62	0.60	0.60	0.60	0.60	0.60	0.60	
Low-e, low-solar	2	25a	U	1.70	3.83	2.68	2.31	2.21	1.89	2.75	2.36	2.03	2.01	1.90		
		SHGC	0.41	0.37	0.37	0.31	0.31	0.31	0.38	0.38	0.38	0.36	0.36	0.36		
	3	40a	U	1.02	3.22	2.07	1.76	1.71	1.45	2.13	1.76	1.44	1.40	1.33		
		SHGC	0.27	0.25	0.25	0.21	0.21	0.21	0.25	0.25	0.24	0.24	0.24	0.24	0.24	
Low-e, high-solar	2	17a	U	1.99	4.05	2.89	2.52	2.39	2.07	2.99	2.60	2.26	2.24	2.13		
		SHGC	0.70	0.62	0.62	0.52	0.52	0.52	0.64	0.64	0.64	0.61	0.61	0.61		
	3	32c	U	1.42	3.54	2.36	2.02	1.97	1.70	2.47	2.10	1.77	1.73	1.66		
		SHGC	0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.56	0.54	0.54	0.54		
Heat-absorbing	1	1c	U	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35		
		SHGC	0.73	0.64	0.64	0.54	0.54	0.54	0.66	0.66	0.66	0.64	0.64	0.64		
	2	5c	U	2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84	2.72		
		SHGC	0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.56	0.54	0.54	0.54		
	3	29c	U	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01	1.93		
		SHGC	0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.31	0.30	0.30	0.30		
Reflective	1	11	U	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35		
		SHGC	0.31	0.28	0.28	0.24	0.24	0.24	0.29	0.29	0.29	0.27	0.27	0.27		
	2	5p	U	2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84	2.72		
		SHGC	0.29	0.27	0.27	0.22	0.22	0.22	0.27	0.27	0.27	0.26	0.26	0.26		
	3	29p	U	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01	1.93		
		SHGC	0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.31	0.30	0.30	0.30		

T_{cooling} = 24°C

T_{heating} = 20°C

$$\Delta T_{cooling} = "31.0^\circ\text{C} - 24^\circ\text{C} = 7.9^\circ\text{C}"$$

$$\Delta T_{heating} = "2^\circ\text{C} - (-4.8)^\circ\text{C} = 24.8^\circ\text{C}"$$

From the table DR = 11.9 °C

FIXED WINDOW ON WEST SIDE

Area = 14.4 m²

Table 10 Peak Irradiance, W/m²

Exposure	Latitude									
	20°	25°	30°	35°	40°	45°	50°	55°	60°	
North	E_D	125	106	92	84	81	85	96	112	136
	E_d	128	115	103	93	84	76	69	62	55
	E_t	253	221	195	177	166	162	164	174	191
Northeast/Northwest	E_D	460	449	437	425	412	399	386	374	361
	E_d	177	169	162	156	151	147	143	140	137
	E_t	637	618	599	581	563	546	529	513	498
East/West	E_D	530	543	552	558	560	559	555	547	537
	E_d	200	196	193	190	189	188	187	187	187
	E_t	730	739	745	748	749	747	742	734	724
Southeast/Southwest	E_D	282	328	369	405	436	463	485	503	517
	E_d	204	203	203	204	205	207	210	212	215
	E_t	485	531	572	609	641	670	693	715	732
South	E_D	0	60	139	214	283	348	408	464	515
	E_d	166	193	196	200	204	209	214	219	225
	E_t	166	253	335	414	487	557	622	683	740
Horizontal	E_D	845	840	827	808	776	738	691	637	574
	E_d	170	170	170	170	170	170	170	170	170
	E_t	1015	1010	997	976	946	908	861	807	744

COOLING LOAD

$$q_{\text{west window}} = A \times CF_{\text{west window}}$$

$$CF_{\text{west window(heat transfer)}} = U_{\text{west window}} (\Delta T_{\text{cooling}} - 0.46 DR)$$

$$U_{\text{west window}} = 2.84 \frac{W}{m^2 k^2}$$

$$CF_{\text{west window(heat transfer)}} = 2.84 \frac{W}{m^2 k^2} (7.9 k - 0.46 (11.9 k))$$

$$\approx 6.89 \frac{W}{m^2}$$

Table 13 Fenestration Solar Load Factors FF_s

Exposure	Single Family Detached	Multifamily
North	0.44	0.27
Northeast	0.21	0.43
East	0.31	0.56
Southeast	0.37	0.54
South	0.47	0.53
Southwest	0.58	0.61
West	0.56	0.65
Northwest	0.46	0.57
Horizontal	0.58	0.73

Irradiation

$$E_D = 559$$

$$E_d = 188$$

$$PXi_{\text{west window}} = E_D + E_d$$

$$= 559 + 188 = 747$$

Since no internal shading, so IAC = 1

$$SHGC = 0.54$$

$$FF_s = 0.56$$

$$CF_{\text{west window(irradiation)}} = PXi \times SHGC \times IAC \times FF_s$$

$$= 747 \times 0.54 \times 1 \times 0.56 = 225.89$$

$$q_{\text{west window}} = A \times CF_{\text{west window}} = \\ A \times (CF_{\text{west window(heat transfer)}} + (CF_{\text{west window(irradiation)}}))$$

$$= 14.4 m^2 \times (6.89 + 225.89) \frac{W}{m^2} = 3352.07 W$$

HEATING LOAD

$$q_{\text{west window}} = A \times HF_{\text{west window}} = A \times U_{\text{west window}} \times \Delta T_{\text{heating}}$$

$$= 14.4 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} \times 24.8 \text{ k} = 1014.22 \text{ W}$$

If the frame is aluminium

$$U'_{\text{west window}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ}$$

SHGC' = 0.56

Cooling load

$$CF'_{\text{west window(heat transfer)}} = U'_{\text{west window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$= 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} (7.9 \text{ K} - 0.46 \times 11.9 \text{ k}) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$CF'_{\text{west window(irradiation)}} = PXI \times SHGC' \times IAC \times FF_s$$

$$= 747 \times 0.56 \times 1 \times 0.56 = 234.26$$

$$q'_{\text{west window}} = A \times (CF'_{\text{west window(heat transfer)}} + CF'_{\text{west window(irradiation)}})$$

$$= 14.4 \text{ m}^2 \times (8.76 + 234.26) \frac{\text{W}}{\text{m}^2} = 3499.48 \text{ W}$$

Heating load

$$q'_{\text{west window}} = A \times HF'_{\text{west window}} = A \times U'_{\text{west window}} \times \Delta T_{\text{heating}}$$

$$= 14.4 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} \times 24.8 \text{ k} = 1289.20 \text{ W}$$

FIXED WINDOW ON SOUTH SIDE

Area = 3.6 m²

COOLING LOAD

$$q_{\text{south window}} = A \times CF_{\text{south window}}$$

$$CF_{\text{south window(heat transfer)}} = U_{\text{south window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$U_{\text{south window}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{k}^\circ}$$

$$CF_{\text{south window(heat transfer)}} = 2.84 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} (7.9 \text{ k} - 0.46 (11.9 \text{ k})) \approx 6.89 \frac{\text{W}}{\text{m}^2}$$

Irradiation

$$E_D = 348$$

$$E_d = 209$$

$$PXI_{\text{west window}} = E_D + E_d = 348 + 209 = 557$$

Since no internal shading, so IAC = 1

SHGC = 0.54

$$FF_s = 0.47$$

$$CF_{\text{south window(irradiation)}} = PXI \times SHGC \times IAC \times FF_s = 557 \times 0.54 \times 1 \times 0.47 = 141.36$$

$$q_{\text{south window}} = A \times CF_{\text{south window}} =$$

$$Ax(CF_{\text{south window(heat transfer)}} + (CF_{\text{south window(irradiation)}}))$$

$$= 3.6 \text{ m}^2 \times (6.89 + 141.36) \frac{\text{W}}{\text{m}^2} = 533.72 \text{ W}$$

HEATING LOAD

$$q_{\text{south window}} = A \times HF_{\text{south window}} = A \times U_{\text{south window}} \times \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 2.84 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} \times 24.8 \text{ k} = 253.56 \text{ W}$$

If the frame is aluminum

$$U'_{\text{south window}} = 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ}$$

SHGC' = 0.56

Cooling load

$$CF'_{\text{south window(heat transfer)}} = U'_{\text{south window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$= 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} (7.9 \text{ K} - 0.46 \times 11.9 \text{ k}) = 8.76 \frac{\text{W}}{\text{m}^2}$$

$$CF'_{\text{south window(irradiation)}} = PXI \times SHGC' \times IAC \times FF_s = 557 \times 0.56 \times 1 \times 0.47 = 146.6$$

$$q'_{\text{south window}} = A \times (CF'_{\text{south window(heat transfer)}} + (CF'_{\text{south window(irradiation)}}))$$

$$= 3.6 \text{ m}^2 \times (8.76 + 146.60) \frac{\text{W}}{\text{m}^2} = 559.30 \text{ W}$$

Heating load

$$q'_{\text{south window}} = A \times HF'_{\text{south window}} = A \times U'_{\text{south window}} \times \Delta T_{\text{heating}}$$

$$= 3.6 \text{ m}^2 \times 3.61 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} \times 24.8 \text{ k} = 322.30 \text{ W}$$

OPERABLE WINDOW ON SOUTH SIDE

Area = 3.6 m²

COOLING LOAD

$$q_{\text{south window}} = A \times CF_{\text{south window}}$$

$$CF_{\text{south window(heat transfer)}} = U_{\text{south window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR})$$

$$U_{\text{south window}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{k}^\circ}$$

$$CF_{\text{south window(heat transfer)}} = 2.87 \frac{\text{W}}{\text{m}^2 \text{k}^\circ} (7.9 \text{ k} - 0.46 (11.9 \text{ k})) \approx 6.96 \frac{\text{W}}{\text{m}^2}$$

Irradiation

E_D = 348

E_d = 209

$$PXI_{\text{south window}} = E_D + E_d = 348 + 209 = 557$$

Since no internal shading, so IAC = 1

SHGC = 0.46

$$FF_s = 0.47$$

$$CF_{\text{south window(irradiation)}} = PXI \times SHGC \times IAC \times FF_s = 557 \times 0.46 \times 1 \times 0.47 = 120.42$$

$$q_{\text{south window}} = A \times CF_{\text{south window}} = \\ A(CF_{\text{south window(heat transfer)}} + (CF_{\text{south window(irradiation)}}))$$

$$= 3.6 \text{ m}^2 \times (6.96 + 120.42) \frac{\text{W}}{\text{m}^2} = 458.58 \text{ W}$$

HEATING LOAD

$$q_{\text{south window}} = A \times HF_{\text{south window}} = A \times U_{\text{south window}} \times \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 2.87 \frac{\text{W}}{\text{m}^2 \text{K}^2} \times 24.8 \text{ K} = 256.23 \text{ W}$$

If the frame is aluminium

$$U'_{\text{south window}} = 4.62 \frac{\text{W}}{\text{m}^2 \text{K}^2}$$

$$SHGC' = 0.55$$

Cooling load

$$CF'_{\text{south window(heat transfer)}} = U'_{\text{south window}} (\Delta T_{\text{cooling}} - 0.46 \text{ DR}) \\ = 4.62 \frac{\text{W}}{\text{m}^2 \text{K}^2} (7.9 \text{ K} - 0.46 \times 11.9 \text{ K}) = 11.21 \frac{\text{W}}{\text{m}^2}$$

$$CF'_{\text{west window(irradiation)}} = PXI \times SHGC' \times IAC \times FF_s = 557 \times 0.55 \times 1 \times 0.47 = 143.98$$

$$q'_{\text{west window}} = A \times (CF'_{\text{west window(heat transfer)}} + (CF'_{\text{west window(irradiation)}})) \\ = 3.6 \text{ m}^2 \times (11.21 + 143.98) \frac{\text{W}}{\text{m}^2} = 558.70 \text{ W}$$

Heating load

$$q'_{\text{south window}} = A \times HF'_{\text{south window}} = A \times U'_{\text{south window}} \times \Delta T_{\text{heating}} \\ = 3.6 \text{ m}^2 \times 4.62 \frac{\text{W}}{\text{m}^2 \text{K}^2} \times 24.8 \text{ K} = 412.47 \text{ W}$$