

## #Week 8

Task 1 Using the diagrams given in the presentation calculate how much (%) is the effect of applying different modifications (changing the gas, adding an extra pane, using a low emissivity coating) on the U value with respect to a benchmark case of double layer with air and no coating ? ( keep the gap thickness to be 13 mm)

Task 2 Consider the house that we analysed in the alst two examples, calculate the heating and cooling load of the other windows which are fixed 14.4 m2 on the west, fixed 3.6 m2 on the south and an operable 3.6 m2 on the south (the same window and frame type). How much does the total value change if I change the frame of the window from wooden one to aluminium ?

### Answers:

#### Task 1

Answer:

From the diagram we can see that:  
For double-pane (13mm) glazing:

$$U_{air} = 2.8 \frac{W}{m^2 \cdot K}$$

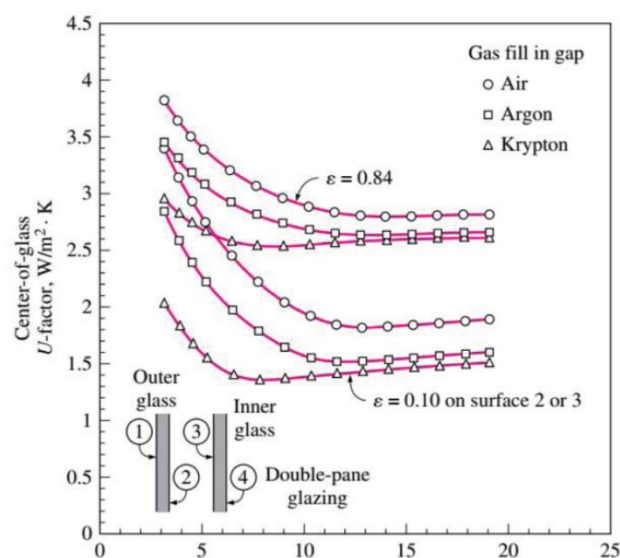
$$U_{argon} = 2.7 \frac{W}{m^2 \cdot K}$$

$$U_{krypton} = 2.6 \frac{W}{m^2 \cdot K}$$

So, when the gas is changing

Air → Argon: decrease about 4.57%

Air → Krypton: decrease about 7.14%

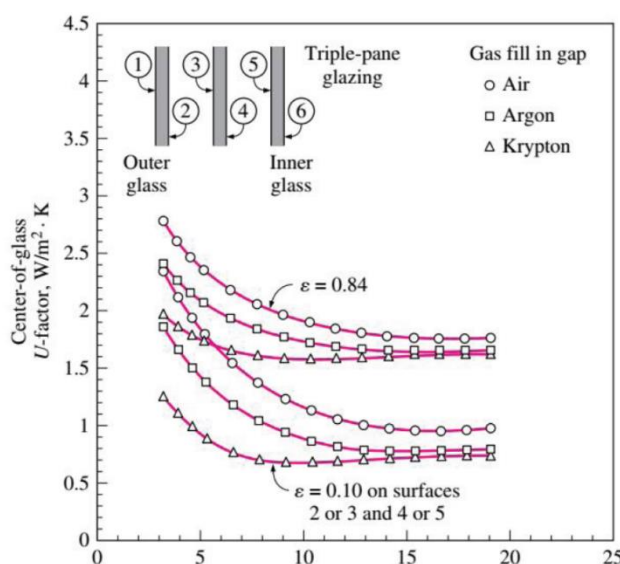


For triple-pane (13mm) glazing:

$$U_{double} = 2.8 \frac{W}{m^2 \cdot K}$$

$$U_{triple} = 1.8 \frac{W}{m^2 \cdot K}$$

So, when changing double-pane to triple-pane the U value will decrease about 35.71%



When the glass surfaces are coated with a film that has an emissivity of 0.1,

$$U_{double0.1} = 1.8 \frac{W}{m^2 \cdot K}$$

$$U_{triple0.1} = 1 \frac{W}{m^2 \cdot K}$$

So, when coating a film that has an emissivity of 0.1, the U value of double-pane decrease

about 35.71%, the U value of double-pane decrease about 44.44%.

## Task 2

Answer:

PIACENZA, Italy													WMO#: 160840		
Lat: 44.92N	Long: 9.73E	Elev: 138	StdP: 99.68	Time Zone: 1.00 (EUW)	Period: 89-10	WBAN: 99999									
Annual Heating and Humidification Design Conditions															
Coldest Month	Heating DB		Humidification DP/MCDB and HR						Coldest month WS/MCDB				MCWS/PCWD to 99.6% DB		
	99.6%	99%	99.6%			99%			0.4%		1%		MCWS	PCWD	
			DP	HR	MCDB	DP	HR	MCDB	WS	MCDB	WS	MCDB			
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(l)	(m)	(n)	(o)	
1	-6.2	-4.8	-11.6	1.4	3.1	-8.8	1.8	1.8	8.8	5.6	7.7	6.2	2.1	250	
(1)															
Annual Cooling, Dehumidification, and Enthalpy Design Conditions															
Hottest Month	Hottest Month DB Range	Cooling DB/MCWB						Evaporation WB/MCDB						MCWS/PCWD to 0.4% DB	
		0.4%		1%		2%		0.4%		1%		2%		MCWS	PCWD
		DB	MCWB	DB	MCWB	DB	MCWB	WB	MCDB	WB	MCDB	WB	MCDB		
(a)	(b)	(c)	(d)	(e)	(f)	(g)	(h)	(i)	(j)	(k)	(l)	(m)	(n)	(o)	(p)
8	11.9	33.1	22.7	31.9	22.4	30.3	21.8	24.6	30.2	23.7	29.2	22.9	28.3	2.4	90
(2)															

Table 10 Peak Irradiance, W/m<sup>2</sup>

Exposure		Latitude									
		20°	25°	30°	35°	40°	45°	50°	55°	60°	
North	$E_D$	125	106	92	84	81	85	96	112	136	
	$E_d$	128	115	103	93	84	76	69	62	55	
	$E_t$	253	221	195	177	166	162	164	174	191	
Northeast/Northwest	$E_D$	460	449	437	425	412	399	386	374	361	
	$E_d$	177	169	162	156	151	147	143	140	137	
	$E_t$	637	618	599	581	563	546	529	513	498	
East/West	$E_D$	530	543	552	558	560	559	555	547	537	
	$E_d$	200	196	193	190	189	188	187	187	187	
	$E_t$	730	739	745	748	749	747	742	734	724	
Southeast/Southwest	$E_D$	282	328	369	405	436	463	485	503	517	
	$E_d$	204	203	203	204	205	207	210	212	215	
	$E_t$	485	531	572	609	641	670	695	715	732	
South	$E_D$	0	60	139	214	283	348	408	464	515	
	$E_d$	166	193	196	200	204	209	214	219	225	
	$E_t$	166	253	335	414	487	557	622	683	740	
Horizontal	$E_D$	845	840	827	806	776	738	691	637	574	
	$E_d$	170	170	170	170	170	170	170	170	170	
	$E_t$	1015	1010	997	976	946	908	861	807	744	

Table 13 Fenestration Solar Load Factors FF<sub>s</sub>

Exposure	Single Family Detached	Multifamily
North	0.44	0.27
Northeast	0.21	0.43
East	0.31	0.56
Southeast	0.37	0.54
South	0.47	0.53
Southwest	0.58	0.61
West	0.56	0.65
Northwest	0.46	0.57
Horizontal	0.58	0.73

Glazing Type	Glazing Layers	ID <sup>b</sup>	Property <sup>c,d</sup>	Center of Glazing	Frame									
					Operable					Fixed				
					Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum Clad Wood	Wood/Vinyl	Insulated Fiberglass/Vinyl	Aluminum	Aluminum with Thermal Break	Reinforced Vinyl/Aluminum Clad Wood	Wood/Vinyl	Insulated Fiberglass/Vinyl
Clear	1	1a	$U$	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35
			SHGC	0.86	0.75	0.75	0.64	0.64	0.64	0.78	0.78	0.75	0.75	0.75
	2	5a	$U$	2.73	4.62	3.42	3.00	2.87	5.83	3.61	3.22	2.86	2.84	2.72
			SHGC	0.76	0.67	0.67	0.57	0.57	0.57	0.69	0.69	0.67	0.67	0.67
	3	29a	$U$	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01	1.93
			SHGC	0.68	0.60	0.60	0.51	0.51	0.51	0.62	0.62	0.60	0.60	0.60
Low-e, low-solar	2	25a	$U$	1.70	3.83	2.68	2.33	2.21	1.89	2.75	2.36	2.03	2.01	1.90
			SHGC	0.41	0.37	0.37	0.31	0.31	0.31	0.38	0.38	0.36	0.36	0.36
	3	40c	$U$	1.02	3.22	2.07	1.76	1.71	1.45	2.13	1.76	1.44	1.40	1.33
			SHGC	0.27	0.25	0.25	0.21	0.21	0.21	0.25	0.25	0.24	0.24	0.24
	2	17c	$U$	1.99	4.05	2.89	2.52	2.39	2.07	2.99	2.60	2.26	2.24	2.13
			SHGC	0.70	0.62	0.62	0.52	0.52	0.52	0.64	0.64	0.61	0.61	0.61
Low-e, high-solar	3	32c	$U$	1.42	3.54	2.36	2.02	1.97	1.70	2.47	2.10	1.77	1.73	1.66
			SHGC	0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.54	0.54	0.54
	1	1c	$U$	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35
			SHGC	0.73	0.64	0.64	0.54	0.54	0.54	0.66	0.66	0.64	0.64	0.64
	2	5c	$U$	2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84	2.72
			SHGC	0.62	0.55	0.55	0.46	0.46	0.46	0.56	0.56	0.54	0.54	0.54
Heat-absorbing	3	29c	$U$	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01	1.93
			SHGC	0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.30	0.30	0.30
	1	1l	$U$	5.91	7.24	6.12	5.14	5.05	4.61	6.42	6.07	5.55	5.55	5.35
			SHGC	0.31	0.28	0.28	0.24	0.24	0.24	0.29	0.29	0.27	0.27	0.27
	2	5p	$U$	2.73	4.62	3.42	3.00	2.87	2.53	3.61	3.22	2.86	2.84	2.72
			SHGC	0.29	0.27	0.27	0.22	0.22	0.22	0.27	0.27	0.26	0.26	0.26
Reflective	3	29c	$U$	1.76	3.80	2.60	2.25	2.19	1.91	2.76	2.39	2.05	2.01	1.93
			SHGC	0.34	0.31	0.31	0.26	0.26	0.26	0.31	0.31	0.30	0.30	0.30

$$q_{fen} = A \times CF_{fen}$$

$$CF_{fen} = U(\Delta t - 0.46DR) + PXI \times SHGC \times IAC \times FF_s$$

where

$q_{fen}$  = fenestration cooling load, W

$A$  = fenestration area (including frame), m<sup>2</sup>

$CF_{fen}$  = surface cooling factor, W/m<sup>2</sup>

$U$  = fenestration NFRC heating U-factor, W/(m<sup>2</sup>·K)

$\Delta t$  = cooling design temperature difference, K

$PXI$  = peak exterior irradiance, including shading modifications, W/m<sup>2</sup> [see Equations (26) or (27)]

$SHGC$  = fenestration rated or estimated NFRC solar heat gain coefficient

$IAC$  = interior shading attenuation coefficient, Equation (29)

$FF_s$  = fenestration solar load factor, [Table 13](#)

$$\Delta T_{cooling} = 31.9 - 24 = 7.9^\circ\text{C}$$

$$\Delta T_{heating} = 20 - (-4.8) = 24.8^\circ\text{C}$$

$$DR = 11.9^\circ\text{C}$$

**Wood Frames**

**Window1 (east, wood frame, fixed)**

$$A_{window1} = 14.4 \text{ m}^2$$

Heating:

$$U_{window1} = 2.84 \frac{\text{W}}{\text{m}^2} \cdot \text{K}$$

$$HF_{window1} = U_{window1} \cdot \Delta T_{cooling} = 2.84 \cdot 24.8 = 70.44 \text{ W/m}^2$$

$$Q_{window1} = HF_{window1} \cdot A_{window} = 70.44 \cdot 14.4 = 1014.2 \text{ W}$$

Cooling:

Heat transfer:

$$CF_{window1} = U_{window1}(\Delta T_{cooling} - 0.46 \cdot DR) = 2.84(7.9 - 0.46 \cdot 11.9) = 6.9 \text{ W/m}^2$$

Irradiation:

$$E_D = 559, E_d = 188, FF_{seast} = 0.31$$

$$PXI_{window1} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window1} = PXI \cdot SHGC \cdot IAC \cdot FF_{seast} = 747 \cdot 0.54 \cdot 1 \cdot 0.31 = 125.1$$

$$CF_{fenestration1} = U_{window1}(\Delta T_{cooling} - 0.46 \cdot DR) + PXI \cdot SHGC \cdot IAC \cdot FF_{seast}$$

$$= 6.9 + 125.1 = 132 \text{ W/m}^2$$

$$\dot{Q}_{window1} = CF_{fenestration1} \cdot A_{window1} = 132 \cdot 14.4 = 1900.8 \text{ W}$$

**Window2 (west, wood frame, fixed)**

$$A_{window2} = 14.4 \text{ m}^2$$

Heating:

$$U_{\text{window2}} = 2.84 \text{ w/m}^2 \cdot \text{K}$$

$$HF_{\text{window2}} = U_{\text{window2}} * \Delta T_{\text{cooling}} = 2.84 * 24.8 = 70.44 \text{ w/m}^2$$

$$Q_{\text{window2}} = HF_{\text{window2}} * A_{\text{window}} = 70.44 * 14.4 = 1014.2 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{\text{window2}} = U_{\text{window2}} (\Delta T_{\text{cooling}} - 0.46 * DR) = 2.84 (7.9 - 0.46 * 11.9) = 6.9 \text{ w/m}^2$$

Irradiation:

$$E_D = 559, E_d = 188, FF_{\text{swest}} = 0.56$$

$$PXI_{\text{window1}} = E_D + E_d = 559 + 188 = 747$$

$$CF_{\text{window2}} = PXI * SHGC * IAC * FF_{\text{swest}} = 747 * 0.54 * 1 * 0.56 = 225.9$$

$$CF_{\text{fenestration2}} = U_{\text{window2}} (\Delta T_{\text{cooling}} - 0.46 * DR) + PXI * SHGC * IAC * FF_{\text{swest}} \\ = 6.9 + 225.9 = 232.8 \text{ W/m}^2$$

$$\dot{Q}_{\text{window2}} = CF_{\text{fenestration2}} * A_{\text{window2}} = 232.8 * 14.4 = 3352.32 \text{ w}$$

### Window3 (south, wood frame, fixed)

$$A_{\text{window3}} = 3.6 \text{ m}^2$$

Heating:

$$U_{\text{window3}} = 2.84 \text{ w/m}^2 \cdot \text{K}$$

$$HF_{\text{window3}} = U_{\text{window3}} * \Delta T_{\text{cooling}} = 2.84 * 24.8 = 70.44 \text{ w/m}^2$$

$$Q_{\text{window3}} = HF_{\text{window3}} * A_{\text{window}} = 70.44 * 3.6 = 253.6 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{\text{window3}} = U_{\text{window3}} (\Delta T_{\text{cooling}} - 0.46 * DR) = 2.84 (7.9 - 0.46 * 11.9) = 6.9 \text{ w/m}^2$$

Irradiation:

$$E_D = 348, E_d = 209, FF_{\text{ssouth}} = 0.47$$

$$PXI_{\text{window3}} = E_D + E_d = 348 + 209 = 557$$

$$CF_{\text{window3}} = PXI * SHGC * IAC * FF_{\text{ssouth}} = 557 * 0.54 * 1 * 0.47 = 141.4$$

$$CF_{\text{fenestration3}} = U_{\text{window3}} (\Delta T_{\text{cooling}} - 0.46 * DR) + PXI * SHGC * IAC * FF_{\text{ssouth}} \\ = 6.9 + 141.4 = 148.3 \text{ W/m}^2$$

$$\dot{Q}_{\text{window3}} = CF_{\text{fenestration3}} * A_{\text{window3}} = 148.3 * 3.6 = 533.88 \text{ w}$$

### Window4 (south, wood frame, openable)

$$A_{\text{window3}} = 3.6 \text{ m}^2$$

Heating:

$$U_{window4} = 2.87 \text{ w/m}^2 \cdot K$$

$$HF_{window4} = U_{window4} * \Delta T_{cooling} = 2.87 * 24.8 = 71.17 \text{ w/m}^2$$

$$Q_{window4} = HF_{window4} * A_{window} = 71.17 * 3.6 = 256.2 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{window4} = U_{window4}(\Delta T_{cooling} - 0.46 * DR) = 2.87(7.9 - 0.46 * 11.9) = 6.96 \text{ w/m}^2$$

Irradiation:

$$E_D = 348, E_d = 209, SHGC = 0.46, FF_{ssouth} = 0.47$$

$$PXI_{window4} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window4} = PXI * SHGC * IAC * FF_{ssouth} = 557 * 0.46 * 1 * 0.47 = 120.4$$

$$CF_{fenestration4} = U_{window4}(\Delta T_{cooling} - 0.46 * DR) + PXI * SHGC * IAC * FF_{ssouth} \\ = 6.9 + 120.4 = 127.3 \text{ W/m}^2$$

$$\dot{Q}_{window4} = CF_{fenestration4} * A_{window4} = 127.3 * 3.6 = 458.28 \text{ w}$$

$$\dot{Q}_{totalcoolingwood} = 1900.8 + 3352.32 + 533.88 + 458.28 = 6245.3 \text{ w}$$

$$\dot{Q}_{totalheatingwood} = 1014.2 + 1014.2 + 253.6 + 256.2 = 2538.2 \text{ w}$$

## Aluminum Frames

### Window1 (south, aluminum frame, fixed)

Heating:

$$U_{window1} = 3.61 \text{ w/m}^2 \cdot K$$

$$HF_{window1} = U_{window1} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52 \text{ w/m}^2$$

$$Q_{window1} = HF_{window1} * A_{window} = 89.52 * 14.4 = 1289.1 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{window1} = U_{window1}(\Delta T_{cooling} - 0.46 * DR) = 3.61(7.9 - 0.46 * 11.9) = 8.7 \text{ w/m}^2$$

Irradiation:

$$E_D = 559, E_d = 188, SHGC = 0.56, FF_{seast} = 0.31$$

$$PXI_{window1} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window1} = PXI * SHGC * IAC * FF_{seast} = 747 * 0.56 * 1 * 0.31 = 129.6$$

$$CF_{fenestration1} = U_{window1}(\Delta T_{cooling} - 0.46 * DR) + PXI * SHGC * IAC * FF_{seast} \\ = 8.7 + 129.6 = 138.3 \text{ W/m}^2$$

$$\dot{Q}_{window1} = CF_{fenestration1} * A_{window1} = 138.3 * 14.4 = 1991.5 \text{ w}$$

### Window2 (west, aluminum frame, fixed)

$$A_{window2} = 14.4 \text{ m}^2$$

Heating:

$$U_{window2} = 3.61 \text{ w/m}^2 \cdot K$$

$$HF_{window2} = U_{window2} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52 \text{ w/m}^2$$

$$Q_{window2} = HF_{window2} * A_{window} = 89.52 * 14.4 = 1289.1 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{window2} = U_{window2}(\Delta T_{cooling} - 0.46 * DR) = 3.61(7.9 - 0.46 * 11.9) = 8.7 \text{ w/m}^2$$

Irradiation:

$$E_D = 559, E_d = 188, FF_{swest} = 0.56$$

$$PXI_{window1} = E_D + E_d = 559 + 188 = 747$$

$$CF_{window2} = PXI * SHGC * IAC * FF_{swest} = 747 * 0.56 * 1 * 0.56 = 234.26$$

$$CF_{fenestration2} = U_{window2}(\Delta T_{cooling} - 0.46 * DR) + PXI * SHGC * IAC * FF_{swest}$$

$$= 8.7 + 234.26 = 242.96 \text{ W/m}^2$$

$$\dot{Q}_{window2} = CF_{fenestration2} * A_{window2} = 242.96 * 14.4 = 3498.6 \text{ w}$$

#### Window3 (south, aluminum frame, fixed)

$$A_{window3} = 3.6 \text{ m}^2$$

Heating:

$$U_{window3} = 3.61 \text{ w/m}^2 \cdot K$$

$$HF_{window3} = U_{window3} * \Delta T_{cooling} = 3.61 * 24.8 = 89.52 \text{ w/m}^2$$

$$Q_{window3} = HF_{window3} * A_{window} = 89.52 * 3.6 = 322.2 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{window3} = U_{window3}(\Delta T_{cooling} - 0.46 * DR) = 3.61(7.9 - 0.46 * 11.9) = 8.7 \text{ w/m}^2$$

Irradiation:

$$E_D = 348, E_d = 209, FF_{ssouth} = 0.47$$

$$PXI_{window3} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window3} = PXI * SHGC * IAC * FF_{ssouth} = 557 * 0.56 * 1 * 0.47 = 146.6$$

$$CF_{fenestration3} = U_{window3}(\Delta T_{cooling} - 0.46 * DR) + PXI * SHGC * IAC * FF_{ssouth}$$

$$= 8.7 + 146.6 = 155.3 \text{ W/m}^2$$

$$\dot{Q}_{window3} = CF_{fenestration3} * A_{window3} = 155.3 * 3.6 = 559.08 \text{ w}$$

#### Window4 (south, aluminum frame, operable)

$$A_{window3} = 3.6 \text{ m}^2$$

Heating:

$$U_{window4} = 4.62 \text{ w/m}^2 \cdot K$$

$$HF_{window4} = U_{window4} * \Delta T_{cooling} = 4.62 * 24.8 = 114.57 \text{ w/m}^2$$

$$Q_{window4} = HF_{window4} * A_{window} = 114.57 * 3.6 = 412.4 \text{ w}$$

Cooling:

Heat transfer:

$$CF_{window4} = U_{window4}(\Delta T_{cooling} - 0.46 * DR) = 4.62(7.9 - 0.46 * 11.9) = 11.2 \text{ w/m}^2$$

Irradiation:

$$E_D = 348, E_d = 209, SHGC = 0.55, FF_{ssouth} = 0.47$$

$$PXI_{window4} = E_D + E_d = 348 + 209 = 557$$

$$CF_{window4} = PXI * SHGC * IAC * FF_{ssouth} = 557 * 0.55 * 1 * 0.47 = 143.98$$

$$\begin{aligned} CF_{fenestration4} &= U_{window4}(\Delta T_{cooling} - 0.46 * DR) + PXI * SHGC * IAC * FF_{ssouth} \\ &= 11.2 + 143.98 = 155.18 \text{ W/m}^2 \end{aligned}$$

$$\dot{Q}_{window4} = CF_{fenestration4} * A_{window4} = 155.18 * 3.6 = 558.65 \text{ w}$$

$$\dot{Q}_{totalcoolingaluminum} = 1991.5 + 3498.6 + 559.08 + 558.65 = 6607.8 \text{ w}$$

$$\dot{Q}_{totalheatingaluminum} = 1289.1 + 1289.1 + 322.2 + 412.4 = 3312.8 \text{ w}$$

$$\begin{aligned} \frac{\dot{Q}_{totalcoolingwood}}{\dot{Q}_{totalcoolingaluminum}} &= \frac{6245.3}{6607.8} = 94.5\% \\ \frac{\dot{Q}_{totalheatingwood}}{\dot{Q}_{totalheatingaluminum}} &= \frac{2538.2}{3312.8} = 76.6\% \end{aligned}$$

### Conclusion:

It can be seen that window with wooden frame has better resistance in cooling and heating, aluminum frame window has 94.5% cooling and 76.6% heating resistance of a wooden one.