

# Research Proposal: Exploring Topological Narrative Structures

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## 1 23.tex - Mathematical Terms and Definitions

### 1.1 Topology

- **Topological Space:** A set equipped with a topology, which is a collection of open sets satisfying certain axioms.
- **Topological Invariant:** A property of a topological space that remains unchanged under continuous transformations (e.g., homeomorphisms). Examples include connectedness, compactness, and homotopy groups.
- **Manifold:** A topological space that locally resembles Euclidean space.
- **Chirality (in topology):** A property of a topological space that is asymmetric under certain transformations (e.g., reflection). A chiral space cannot be superimposed on its mirror image.
- **Orthogonality (in vector spaces):** Two vectors are orthogonal if their dot product is zero. This represents independence in vector spaces.
- **Cosine Similarity:** The cosine of the angle between two vectors, measuring their similarity in direction. It is given by the dot product of the two vectors divided by the product of their magnitudes.
- **Hamming Distance:** The number of positions at which two vectors differ. Used to measure the distance between binary vectors representing narratives.
- **Shortest Path Length:** In a graph, the shortest distance between two nodes, considering only the edges and edge weights.
- **Persistent Homology:** A technique in topological data analysis that identifies topological features (e.g., connected components, loops, voids) at multiple scales.
- **Topological Distance:** A measure of distance between two points in a topological space, reflecting their topological relationships.

## 1.2 Linear Algebra

- **Vector:** An ordered collection of numbers.
- **Dot Product:** A measure of the similarity between two vectors. For vectors  $u, v \in \mathbb{R}^n$ ,  $u \cdot v = \sum_{i=1}^n u_i v_i$ .
- **Cross Product (in  $\mathbb{R}^3$ ):** A binary operation on two vectors in  $\mathbb{R}^3$  producing a vector orthogonal to both inputs.
- **Matrix:** A rectangular array of numbers.
- **Matrix Multiplication (matmul):** A binary operation on two matrices under certain dimensional compatibility constraints.
- **Projection Operator:** A linear transformation that projects a vector onto a subspace.
- **Rotation Matrix:** A matrix representing a rotation in space.

## 1.3 Calculus and Optimization

- **Gradient:** A vector pointing in the direction of the steepest ascent of a function.
- **Gradient Descent:** An iterative optimization algorithm that moves in the direction of the negative gradient to minimize a function.
- **Learning Rate:** A parameter controlling the step size in gradient descent.
- **Loss Function:** A function measuring the difference between predictions and actual values.
- **Convergence (of optimization algorithm):** An algorithm converges if it reaches a minimum or stationary point of the function being optimized.
- **Local Minimum:** A point that is a minimum within a local neighborhood.
- **Global Minimum:** The absolute minimum value of a function.

## 1.4 Information Theory

- **Mutual Information:** A measure of the mutual dependence between two random variables.
- **Entropy:** A measure of uncertainty in a random variable.
- **Information Gain:** The reduction in uncertainty achieved by observing a random variable.

## 1.5 Graph Theory

- **Graph:** A mathematical structure representing relationships between objects (nodes or vertices) connected by edges.
- **Directed Graph:** A graph where edges have a direction.
- **Weighted Graph:** A graph where edges have associated weights.
- **Node Centrality:** A measure of a node's importance in a graph. Different centrality measures exist, capturing various aspects of importance.
- **Community Structure (in graphs):** The division of nodes into groups or communities based on connectivity patterns.
- **Shortest Path:** The shortest sequence of edges connecting two nodes in a graph.
- **Path Length:** The number of edges in a path.

## 1.6 Reinforcement Learning

- **Agent:** An entity that learns to interact with an environment.
- **Environment:** The system the agent interacts with.
- **State:** A representation of the environment.
- **Action:** A decision made by the agent.
- **Reward:** A scalar value reflecting the desirability of a state or action.
- **Policy:** A strategy that maps states to actions.
- **Value Function:** A function estimating the expected cumulative reward from a given state.
- **Q-value:** The expected cumulative reward for taking a given action in a given state.
- **Learning Rate (in RL):** A parameter controlling the speed of learning in the reinforcement learning algorithm.
- **Discount Factor (in RL):** A parameter controlling the relative importance of immediate rewards versus future rewards.

## 2 Mathematical Formulas

### 2.1 Chiral Gradient Descent (CGD) Formulas

1. Equation:

$$\boldsymbol{\theta}_{t+1} = \boldsymbol{\theta}_t - \alpha \nabla L(\boldsymbol{\theta}_t) + \beta \sum_{i,j \in C} s(w_{ij}, \mathbf{c}_{ij})(\nabla L(\boldsymbol{\theta}_t) \times \mathbf{c}_{ij})$$

2. Equation:

$$\boldsymbol{\theta}_{t+1} = \boldsymbol{\theta}_t - \alpha \nabla L(\boldsymbol{\theta}_t) + \beta \sum_{i,j \in C(\boldsymbol{\theta}_t)} \frac{\|\mathbf{c}_{ij}\|}{1 + e^{-\gamma d_{ij}}} (\nabla L(\boldsymbol{\theta}_t) \times \mathbf{c}_{ij})$$

3. Chirality Score:

$$C_i(t) = \sum_{j \in N(i)} w_{ij} \times A(v_i, v_j)$$

4. Learning Rate Update:

$$\eta_i(t+1) = \eta_i(t) \times (1 + \beta \times C_i(t))$$

5. Chiral Similarity:

$$CS(N_i, N_j) = w_f \times \text{sim}(F_i, F_j) + w_c \times \text{sim}(C_i, C_j) + w_t \times |T_i - T_j|$$

6. Orthogonal Similarity:

$$OS(N_i, N_j) = 1 - |CS(N_i, N_j)|$$

7. Q-Learning Update:

$$Q(s, a) = Q(s, a) + \alpha \times [R(s, a, s') + \gamma \times \max_{a'} Q(s', a') - Q(s, a)]$$

## 3 Conjectures

### 3.1 Chiral Convergence Conjecture

In a multi-agent system performing narrative synthesis, the presence of both chiral and orthogonal narratives, coupled with local explanations, strictly increases the rate of convergence towards the ground truth embedding, compared to systems utilizing only chiral or only orthogonal narratives, when measured relative to the resources consumed. This increase in convergence is not merely due to the increased number of narratives but arises from the synergistic interaction of chiral and orthogonal information, especially in high-dimensional narrative spaces with complex topological features.

## 4 24.tex - Mathematical Terms and Definitions (Continued)

### 4.1 Bayesian Inference

- **Prior Probability:** The probability of an event before observing any data.
- **Likelihood:** The probability of observing the data given a particular event.
- **Posterior Probability:** The probability of an event after observing the data. Calculated using Bayes' theorem.
- **Bayes' Theorem:** A theorem relating prior probability, likelihood, and posterior probability.
- **Bayesian Update:** The process of updating a probability distribution based on new data.
- **Variational Inference:** An approximation method for performing Bayesian inference in complex models.

### 4.2 Fuzzy Logic

- **Fuzzy Set:** A set where elements have degrees of membership (between 0 and 1).
- **Membership Function:** A function defining the degree of membership of an element in a fuzzy set.
- **Fuzzy Logic Operations:** Logical operations (AND, OR, NOT) extended to fuzzy sets.
- **Fuzzy Truth Value:** A truth value between 0 and 1, representing degrees of belief or uncertainty.

### 4.3 Spatiotemporal Digests

- **Spatiotemporal Region ( $X_r$ ):** A subset of spacetime.
- **Raster Recording ( $R$ ):** A function mapping a spatiotemporal region to a set of data values.
- **Spatiotemporal Digest ( $S$ ):** A function mapping a spatiotemporal region to a digest value, typically a cryptographic hash, that is computationally infeasible to invert.
- **Strong Verification ( $V$ ):** A function that compares a raster recording with a spatiotemporal digest to verify authenticity.

## 4.4 Additional Terms

- **Confidence Score ( $T_i$ ):** A scalar value in the range  $[0, 1]$ , representing the degree of belief in the truthfulness of a narrative.
- **Asymmetry Function ( $A(v_i, v_j)$ ):** A function measuring the degree of asymmetry between two nodes in a network.
- **Neighborhood ( $N(i)$ ):** The set of nodes directly connected to node  $i$  in a graph.
- **Sigmoid Function:** A function that maps a real number to a value between 0 and 1. Often used to introduce non-linearity in neural networks.

## 5 Mathematical Formulas (Continued)

### 5.1 Additional Formulas

1. **Convergence Rate:**

$$CR(N_i, T, t) = -\frac{d}{dt}[d(F_i(t), F_t(t))]$$

2. **Chiral Score (refined):**

$$CS(N_i, N_j) = w_f \text{sim}(F_i, F_j) + w_c \text{sim}(C_i, C_j) + w_t |T_i - T_j|$$

3. **Orthogonal Score (refined):**

$$OS(N_i, N_j) = 1 - |CS(N_i, N_j)|$$

## 6 Conjectures (Continued)

### 6.1 Chiral Convergence Conjecture (refined)

In a multi-agent system performing narrative synthesis, the convergence towards a higher confidence shared understanding of truth is accelerated by the presence and resolution of chiral and orthogonal relationships between narratives, where these relationships are defined by a combination of feature similarity, contextual similarity, and confidence discrepancies. Furthermore, this convergence is optimized through a reinforcement learning process that rewards agents for increasing narrative confidence, synthesizing higher-confidence narratives, resolving chiral tensions, and integrating orthogonal perspectives.

## 7 25.tex - Mathematical Terms and Definitions (Continued)

### 7.1 Reinforcement Learning (Continued)

- **Multi-Agent Reinforcement Learning (MARL):** Reinforcement learning extended to multiple interacting agents.
- **Decentralized RL:** MARL where agents do not have a central controller or global knowledge of the environment.
- **Multi-Objective RL:** RL where the agent has multiple goals or reward functions to optimize.
- **Adversarial RL:** RL where two or more agents compete against each other.
- **Meta-Learning (in RL):** Learning to learn; an RL agent learns to adapt its learning strategy based on experience.

### 7.2 Local Interpretable Model-agnostic Explanations (LIME)

- **Local Explanation:** An explanation of a single prediction made by a machine learning model.
- **Interpretable Model:** A model whose predictions are easily understandable by humans (e.g., linear model, decision tree).
- **Model-Agnostic:** A method that can be applied to any machine learning model, regardless of its internal structure.
- **Submodular Pick (SP-LIME):** A method for selecting a representative subset of instances to explain a model's global behavior.

### 7.3 Additional Terms

- **Narrative Space (NS):** The set of all possible narratives, considered as a high-dimensional topological space.
- **Narrative Refinement ( $\Delta N_i$ ):** A change in a narrative based on feedback and interaction with other narratives. Represented as a vector in narrative space.
- **Truth Value ( $T_i$ ):** A measure of the truthfulness of a narrative, represented as a probability or confidence score.
- **Global Chirality Parameter ( $\beta$ ):** Controls the overall effect of chirality on gradient descent.

- **Scaling Parameter ( $\gamma$ ):** Controls the steepness of the sigmoid function, determining how topological distance affects the chiral influence.

## 8 Mathematical Formulas (Continued)

### 8.1 Additional Formulas

1. **Weighted Averaging of Embeddings (during synthesis):**

$$F_k = \frac{T_i F_i + T_j F_j}{T_i + T_j}$$

2. **Reward Function (example):**

$$R(s, a, s') = w_c \textit{Coherence}(s') + w_r \textit{Resolution}(s, a, s') + w_t \textit{Convergence}(s', T) - w_r \textit{RC}(a)$$

3. **Average Confidence Score:**

$$\frac{1}{n} \sum_{i=1}^n T_i(t)$$

## 9 26.md - Introspection Process: Formalizing Implicit Conjectures

### 9.1 Bayesian Narrative Representation

The core idea is to represent narratives as probability distributions over possible world states  $W$ . A narrative  $N_i$  is thus a conditional probability distribution:  $N_i \equiv P(W|N_i)$ . This allows explicit modeling of uncertainty and incorporates prior knowledge.

### 9.2 Synthesis as Bayesian Updating

Narrative synthesis is viewed as a Bayesian update. The posterior distribution over world states, given narratives  $N_i$  and  $N_j$ , is  $P(W|N_i, N_j)$ . This posterior captures combined information. Assuming conditional independence between narratives given the world state (a common simplification), and a uniform prior  $P(W)$ , we have:

$$P(W|N_i, N_j) \propto P(N_i|W)P(N_j|W)$$

However, for high-dimensional  $W$ , calculating this product is computationally expensive. Variational inference or approximations are needed for scalability. The proportionality



constant is omitted as it is a normalization constant. Note that this is a conditional independence assumption, which may or may not be true in practice.

### 9.3 Chirality and Orthogonality in Bayesian Terms

- **Chirality:** High divergence (KL or JS divergence) between  $P(W|N_i)$  and  $P(W|N_j)$  indicates chirality.
- **Orthogonality:** Low mutual information  $I(N_i; N_j)$  between  $N_i$  and  $N_j$  indicates orthogonality.

### 9.4 Conjectures

**Conjecture 1** (Bayesian Narrative Synthesis). *If  $N_i$  and  $N_j$  are two narratives with confidence scores  $T_i$  and  $T_j$  respectively, and  $N_k = \text{Synth}(N_i, N_j)$  is their synthesis, then  $T_k \geq \max(T_i, T_j)$ . This formalizes that combining information increases confidence.*

**Conjecture 2** (Chiral Narrative Convergence). *If  $N_i$  and  $N_j$  are chiral narratives (high divergence), their synthesis  $N_k$  converges faster to the truth  $T$  than individual narratives. This formalizes the idea that resolving chiral tensions accelerates progress.*

**Conjecture 3** (Orthogonal Narrative Complementarity). *If  $N_i$  and  $N_j$  are orthogonal narratives (low mutual information), then the confidence score of their synthesis  $N_k$  is higher than either individual narrative:  $T_k > \max(T_i, T_j)$ . This formalizes the idea that independent perspectives provide complementary information.*

## 10 26.tex - Bayesian Narrative Representation

A narrative  $N_i$  is represented as a conditional probability distribution over world states  $W$ :

$$N_i \equiv P(W|N_i)$$

## 11 Narrative Synthesis

The synthesis of two narratives  $N_i$  and  $N_j$  is represented as a Bayesian update:

$$\text{Synth}(N_i, N_j) = N_k \equiv P(W|N_i, N_j)$$

Assuming conditional independence between narratives given the world state, and given a uniform prior  $P(W)$ , we have:

$$P(W|N_i, N_j) \propto P(W|N_i)P(W|N_j)$$

## 12 Chirality and Orthogonality

- **Chirality:** Two narratives  $N_i$  and  $N_j$  are chiral if their probability distributions have high divergence (e.g., measured by KL or JS divergence).
- **Orthogonality:** Two narratives  $N_i$  and  $N_j$  are orthogonal if they have low mutual information about the world state  $W$ .

## 13 Conjectures

**Conjecture 4** (Bayesian Narrative Synthesis). *If  $N_i$  and  $N_j$  are two narratives with confidence scores  $T_i$  and  $T_j$  respectively, then the confidence score  $T_k$  of the synthesized narrative  $N_k = \text{Synth}(N_i, N_j)$  satisfies:*

$$T_k \geq \max(T_i, T_j)$$

**Conjecture 5** (Chiral Narrative Convergence). *If  $N_i$  and  $N_j$  are chiral narratives with high divergence, their synthesis  $N_k$  will converge faster towards the truth  $T$  compared to the individual narratives.*

**Conjecture 6** (Orthogonal Narrative Complementarity). *If  $N_i$  and  $N_j$  are orthogonal narratives with low mutual information, their synthesis  $N_k$  will have a higher confidence score than either individual narrative:*

$$T_k > \max(T_i, T_j)$$

## 14 27 - Chiral Narrative Synthesis: A Mathematical Framework

Document 27.tex formalizes the core mathematical concepts and conjectures of Chiral Narrative Synthesis (CNS), a framework for multi-agent reinforcement learning designed to accelerate scientific discovery by leveraging chiral and orthogonal relationships between narratives. We define narratives as structured representations of hypotheses, introduce measures for chirality and orthogonality, and propose a reinforcement learning approach to guide narrative synthesis towards a shared understanding of truth. We also explore Bayesian perspectives and the implications of spatiotemporal digests for verifying truth claims.

## 15 Mathematical Terms and Definitions

### 15.1 Narratives and Truth

- **Narrative ( $N_i$ ):** A structured representation of a hypothesis, perspective, or theory, represented as a tuple:  $N_i = (G_i, F_i, C_i, T_i)$ , where:
  - $G_i$ : Graph embedding of the narrative structure (e.g., using GCNs).
  - $F_i$ : Feature embedding capturing the semantic content.
  - $C_i$ : Embedding of contextual features (including spatiotemporal digests).
  - $T_i$ : Confidence score  $\in [0, 1]$ .
- **Truth Embedding ( $T$ ):** The current best approximation of ground truth, represented similarly to a narrative:  $T = (G_t, F_t, C_t, T_t)$ , where  $T_t$  is the overall confidence in the current understanding of truth.
- **Narrative Space (NS):** The set of all possible narratives, conceptualized as a high-dimensional topological space.

### 15.2 Relationships between Narratives

- **Chiral Narratives:** Narratives representing opposing but partially correct perspectives relative to  $T$ .
- **Orthogonal Narratives:** Narratives providing independent, potentially complementary information.
- **Chiral Similarity ( $CS$ ):** Measures the degree of opposition between two narratives, incorporating feature, context, and confidence differences:

$$CS(N_i, N_j) = w_f \cdot \text{sim}(F_i, F_j) + w_c \cdot \text{sim}(C_i, C_j) + w_t \cdot |T_i - T_j|$$

where  $\text{sim}$  denotes cosine similarity and  $w_f, w_c, w_t$  are weights.

- **Orthogonal Similarity ( $OS$ ):** Measures the degree of independence between narratives:

$$OS(N_i, N_j) = 1 - |CS(N_i, N_j)|$$

### 15.3 Spiral Descent and Refinement

- **Narrative Refinement ( $\Delta N_i$ ):** A change in a narrative based on feedback and interaction, represented as a vector in NS.
- **Spiral Descent Function:** Guides narrative refinement using gradients, chiral/orthogonal influences, and local explanations (LIME):

$$\Delta N_i = g(\nabla_{NS} L(N_i), CS(N_i, N_j), OS(N_i, N_k), \text{LIME}(N_i), \dots)$$

where  $g$  is a function to be defined, and  $L(N_i)$  is a loss function in narrative space.

## 15.4 Spatiotemporal Digests

- **4D Timeline ( $X$ ):** 4-dimensional spacetime.
- **Raster Recording ( $R$ ):**  $R : X_r \rightarrow D$ , maps a spatiotemporal region  $X_r \subset X$  to data values  $D$ .
- **Spatiotemporal Digest ( $S$ ):**  $S : X_r \rightarrow H$ , maps  $X_r$  to a digest value  $H$  (e.g., cryptographic hash).
- **Strong Verification ( $V$ ):**  $V(R, S) \rightarrow \{\text{True}, \text{False}\}$ , verifies if  $S$  is a valid digest for  $R$ .
- **Levels of Truth ( $T_n$ ):** A hierarchy of truth levels based on verification methods (digest, multi-witness, contextual).

## 15.5 Other Relevant Concepts

- **Bayesian Narrative Representation:**  $N_i \equiv P(W|N_i)$ , the probability distribution over world states  $W$  given narrative  $N_i$ .
- **Narrative Synthesis (Bayesian):**  $Synth(N_i, N_j) = N_k \equiv P(W|N_i, N_j)$ .
- **Kullback-Leibler (KL) Divergence:** Measures the difference between two probability distributions.
- **Jensen-Shannon (JS) Divergence:** A symmetrized and smoothed version of KL divergence.
- **Mutual Information:** Measures the mutual dependence between two random variables.
- **Graph Convolutional Networks (GCNs):** Neural networks designed to operate on graph-structured data.
- **Locality Sensitive Hashing (LSH):** Technique for efficient approximate nearest neighbor search in high-dimensional spaces.

# 16 Mathematical Formulas and Algorithms

## 16.1 Core CNS Formulas

1. Narrative Synthesis (embedding-based):

$$F_k = \frac{T_i F_i + T_j F_j}{T_i + T_j}$$

## 2. Reinforcement Learning Update:

$$Q(s, a) = Q(s, a) + \alpha[R(s, a, s') + \gamma \max_{a'} Q(s', a') - Q(s, a)]$$

## 3. Bayesian Narrative Synthesis:

$$P(W|N_i, N_j) \propto P(N_i|W)P(N_j|W)$$

## 16.2 Chiral Pair Identification Algorithm (Illustrative)

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### Algorithm 1 Chiral Pair Identification

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**Require:** Graph  $G = (V, E)$ , Feature embeddings  $F$ , Chirality threshold  $\tau$

- 1: Initialize empty set of chiral pairs  $C$
  - 2: **for** each pair of nodes  $(v_i, v_j) \in V \times V$  **do**
  - 3:    $S_{ij} \leftarrow \text{ChiralScore}(F_i, F_j)$   $\triangleright$  Using a defined Chiral Score function
  - 4:   **if**  $S_{ij} > \tau$  **then**
  - 5:      $C \leftarrow C \cup \{(v_i, v_j)\}$
  - 6:   **end if**
  - 7: **end for** **return**  $C$
- 

## 17 Core Conjectures

**Conjecture 7** (Chiral Convergence Conjecture). *The presence and resolution of chiral and orthogonal relationships between narratives, coupled with local explanations, accelerates convergence towards a higher confidence shared understanding of truth in a multi-agent narrative synthesis system.*

**Conjecture 8** (Bayesian Narrative Synthesis). *If  $N_i$  and  $N_j$  are two narratives, the confidence score  $T_k$  of the synthesized narrative  $N_k = \text{Synth}(N_i, N_j)$  satisfies  $T_k \geq \max(T_i, T_j)$ .*

**Conjecture 9** (Chiral Narrative Convergence). *If  $N_i$  and  $N_j$  are chiral narratives with high divergence, their synthesis  $N_k$  will converge faster towards the truth  $T$  compared to the individual narratives.*

**Conjecture 10** (Orthogonal Narrative Complementarity). *If  $N_i$  and  $N_j$  are orthogonal narratives with low mutual information, their synthesis  $N_k$  will have a higher confidence score than either individual narrative:  $T_k > \max(T_i, T_j)$ .*

## 18 28.tex - Algorithms

Document 28.tex details various algorithms for identifying chiral pairs within the Chiral Narrative Synthesis (CNS) framework. We explore different approaches based on feature embeddings, graph structures, contextual information, and confidence scores. We also consider hierarchical and multi-agent implementations, emphasizing scalability and practical considerations for real-world applications.

## 19 Chiral Pair Identification Algorithms

### 19.1 Basic Chiral Pair Identification (using cosine similarity)

This algorithm identifies chiral pairs based on high cosine distance between feature embeddings and individual convergence towards the truth embedding.

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**Algorithm 2** Basic Chiral Pair Identification

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**Require:** Feature embeddings  $F = \{F_1, \dots, F_n\}$ , Truth embedding  $T$ , Distance threshold  $\tau_d$ , Similarity threshold  $\tau_s$

- 1: Initialize empty set of chiral pairs  $C$
- 2: **for** each pair of narratives  $(N_i, N_j)$  **do**
- 3:     **if**  $d(F_i, F_j) > \tau_d$  and  $\text{sim}(F_i, T) > \tau_s$  and  $\text{sim}(F_j, T) > \tau_s$  **then**
- 4:          $C \leftarrow C \cup \{(N_i, N_j)\}$
- 5:     **end if**
- 6: **end for** **return**  $C$

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Where  $d(F_i, F_j)$  is the cosine distance and  $\text{sim}(F_i, T)$  is the cosine similarity.

### 19.2 Chiral Pair Identification with Context and Confidence

This algorithm extends the basic approach by incorporating contextual similarity and confidence score differences.

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**Algorithm 3** Chiral Pair Identification with Context and Confidence

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**Require:** Narratives  $N = \{N_1, \dots, N_n\}$ , Truth embedding  $T$ , Weights  $w_f, w_c, w_t$ , Chirality threshold  $\tau_c$

- 1: Initialize empty set of chiral pairs  $C$
- 2: **for** each pair of narratives  $(N_i, N_j)$  **do**
- 3:      $CS_{ij} \leftarrow w_f \cdot \text{sim}(F_i, F_j) + w_c \cdot \text{sim}(C_i, C_j) + w_t \cdot |T_i - T_j|$
- 4:     **if**  $CS_{ij} > \tau_c$  and  $T_i > 0$  and  $T_j > 0$  **then** ▷ Require non-zero confidence
- 5:          $C \leftarrow C \cup \{(N_i, N_j)\}$
- 6:     **end if**
- 7: **end for** **return**  $C$

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### 19.3 Hierarchical Chiral Pair Identification

This algorithm recursively identifies chiral pairs within subgraphs, capturing chirality at multiple levels.

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**Algorithm 4** Hierarchical Chiral Pair Identification

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**Require:** Graph  $G$ , Feature embeddings  $F$ , Truth embedding  $T$ , Thresholds  $\tau_d, \tau_s$

```
1: function FINDCHIRALPAIRS( $G, F, T, \tau_d, \tau_s$ )
2:    $C \leftarrow$  BasicChiralPairIdentification( $F, T, \tau_d, \tau_s$ )
3:   for each subgraph  $G_s$  of  $G$  do
4:      $F_s \leftarrow$  Embeddings for  $G_s$ 
5:      $T_s \leftarrow$  Truth embedding for  $G_s$  ▷ Potentially adjusted for subgraph
6:      $C_s \leftarrow$  FindChiralPairs( $G_s, F_s, T_s, \tau_d, \tau_s$ )
7:      $C \leftarrow C \cup C_s$ 
8:   end for return  $C$ 
9: end function
```

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## 19.4 Multi-Agent Chiral Pair Identification

This algorithm distributes the chiral pair identification process among multiple agents.

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**Algorithm 5** Multi-Agent Chiral Pair Identification

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**Require:** Narratives  $N$ , Truth embedding  $T$ , Number of agents  $k$

```
1: Partition  $N$  into  $k$  subsets  $N_1, \dots, N_k$ 
2: for each agent  $i$  do
3:    $C_i \leftarrow$  ChiralPairIdentification( $N_i, T$ ) ▷ Using any chiral pair identification method
4: end for
5:  $C \leftarrow \bigcup_{i=1}^k C_i$ 
6: ▷ Optional: Resolve conflicts or inconsistencies between  $C_i$  return  $C$ 
```

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## 19.5 Chiral Pair Identification with LIME

This algorithm uses LIME to explain chiral relationships and guide the identification process.

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**Algorithm 6** Chiral Pair Identification with LIME

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**Require:** Narratives  $N$ , Truth embedding  $T$ , LIME explainer

```
1: Initialize empty set of chiral pairs  $C$ 
2: for each pair of narratives  $(N_i, N_j)$  do
3:    $CS_{ij} \leftarrow$  ChiralScore( $N_i, N_j$ )
4:   if  $CS_{ij}$  is high then
5:      $Explanation \leftarrow$  LIME( $N_i, N_j, T$ )
6:     if  $Explanation$  indicates a meaningful chiral relationship then
7:        $C \leftarrow C \cup \{(N_i, N_j)\}$ 
8:     end if
9:   end if
10: end for return  $C$ 
```

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## 19.6 Chiral Pair Identification with Spiral Descent Feedback

This algorithm incorporates feedback from the spiral descent process to dynamically adjust the chiral pair selection.

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**Algorithm 7** Chiral Pair Identification with Spiral Descent Feedback

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**Require:** Narratives  $N$ , Truth embedding  $T$ , Spiral descent parameters

- 1: Initialize chiral pairs  $C$
  - 2: **repeat**
  - 3:     Perform spiral descent using  $C$
  - 4:     Analyze narrative changes and convergence rates
  - 5:     Update  $C$  based on feedback (e.g., prioritize pairs contributing to faster convergence)
  - 6: **until** Convergence criteria met **return**  $C$
-