

# ANALOG SYSTEMS : PROBLEM SET 8

## Problem 1

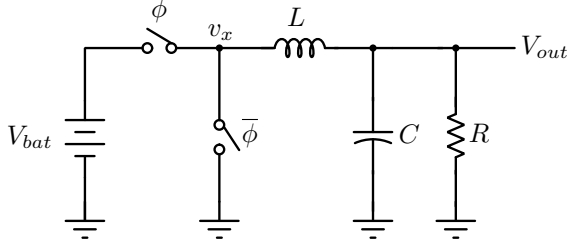


Figure 1: Circuit for Problem 1.

Fig. 1 shows a buck converter. The battery voltage  $V_{bat}$  is 5 V.  $\phi$  and  $\bar{\phi}$  are complementary switch drive signals. The duty cycle of  $\phi$  is denoted by  $D$ . The switching frequency is 1.5 MHz.  $L = 2.2 \mu\text{H}$  and  $C = 22 \mu\text{F}$ . The load resistor  $R = 10 \Omega$ .

- Determine  $D$  needed to achieve  $\overline{V_{out}} = 3.3 \text{ V}$ .
- Determine the transfer function from  $v_x$  to  $V_{out}$ .
- Using the observation that the pole frequency of the LC filter is much lower than the switching frequency, determine the ripple in the inductor current and output voltage.
- Sketch the current waveforms in the inductor and capacitor in steady state.
- Sketch the voltage waveform  $V_{out}$  in steady state.

## Problem 2

In class, we saw that the response of a “slow” linear time-invariant system to a rapidly varying input like  $v_i$  in Fig. ?? is approximately the same as that due to  $\hat{v}_i$ . In this problem, we will convince ourselves of this by working a specific example.

Assume that  $v_i$  has a frequency of 1 MHz, and a duty cycle of 10%.  $RC = 1 \text{ mS}$ . On the same graph, plot  $v_o(t)$  when the input is  $v_i(t)$ , and when it is  $\hat{v}_i(t)$ .

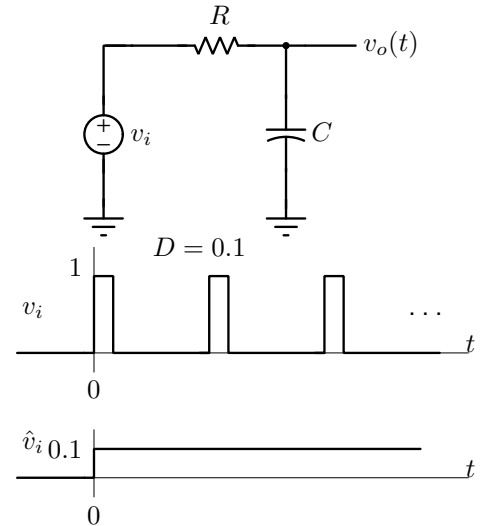


Figure 2: Circuit for Problem 2.