

SPICE Problem Set#2

p-n Junction Diode

At 300 K assume

$E_g = 1.12$ eV, $N_C = 2.8 \times 10^{19}/\text{cm}^3$, $N_V = 10^{19}/\text{cm}^3$, $\mu_n = 1500$ cm²/V-s, $\mu_p = 500$ cm²/V-s, $\epsilon_{r,\text{Si}} = 11.9$, $\tau_n = \tau_p = 1$ μs for Si,

$E_g = 0.66$ eV, $N_C = 1 \times 10^{19}/\text{cm}^3$, $N_V = 6 \times 10^{18}/\text{cm}^3$, $\mu_n = 3900$ cm²/V-s, $\mu_p = 1900$ cm²/V-s, $\epsilon_{r,\text{Ge}} = 16$, $\tau_n = \tau_p = 1$ μs for Ge,

$E_g = 1.42$ eV, $N_C = 4.7 \times 10^{17}/\text{cm}^3$, $N_V = 7 \times 10^{18}/\text{cm}^3$, $\mu_n = 8500$ cm²/V-s, $\mu_p = 400$ cm²/V-s, $\epsilon_{r,\text{GaAs}} = 13.1$, $\tau_n = \tau_p = 0.1$ μs for GaAs,

and $kT = 0.0259$ eV, $\epsilon_0 = 8.85 \times 10^{-14}$ F/cm.

Diode cross-sectional area $A = 1$ μm^2 , p-sided acceptor doping as $N_A = 10^{18}/\text{cm}^3$ and n-sided donor doping as $N_D = 10^{16}/\text{cm}^3$.

Q1. Separately implement Si, Ge and GaAs p-n junction diodes with a voltage dependent current source as

$$I = I_0 \left(\exp\left(\frac{V}{\eta_1 V_T}\right) - 1 \right) \quad \text{with} \quad \eta_1 = 1. \quad \text{Use} \quad I_0 \quad \text{as} \quad I_0 = qA \left(\frac{D_p p_{n0}}{L_p} + \frac{D_n n_{p0}}{L_n} \right), \quad L_n = \sqrt{D_n \tau_n},$$

$$L_p = \sqrt{D_p \tau_p}.$$

For all three diodes, plot current I as a function of voltage V varying from 0 to 0.75 V in a semilog axis (linear x-axis and logarithmic y-axis) for $T = 300$ K. Estimate the values of the parameters I_0 from the plot and check if the values match well with the ones used in the simulation. Also plot the I - V characteristics of these diodes for $T = 200$ K and $T = 400$ K.

Q2. Simulate Full Wave Bridge rectifier circuits with (a) Ge, (b) Si and (c) GaAs p-n diodes and 1 k Ω load resistances. Apply (i) 10 V p-p, (ii) 100 V p-p input sine waves at 50 Hz. Observe the output waveforms in time domain when (i) $T = 300$ K, (ii) 400 K and (iii) 500 K. Under what kind of input voltages and temperatures, will you use Ge, Si or GaAs diodes in this rectification purpose?

Q3. Implement a Si p-n junction diode with voltage dependent current source as

$$I = I_0 \left(\exp\left(\frac{V}{\eta_1 V_T}\right) - 1 \right) + I_{0r} \left(\exp\left(\frac{V}{\eta_2 V_T}\right) - 1 \right) \quad \text{with} \quad \eta_1 = 1 \quad \text{and} \quad \eta_2 = 2. \quad \text{Find} \quad I_0 \quad \text{following the expression in Q1}$$

and use I_{0r} as $I_{0r} = \frac{qA n_i W}{2\tau}$ with W as the space charge width and $\tau = \tau_p = \tau_n$.

Plot current I as a function of voltage V varying from 0 to 0.75 V in a semilog axis at $T = 300$ K. Estimate the values of the parameters I_0 and I_{0r} from the combined plot and check if these values match with the ones used in the simulation. Repeat this problem for Ge and GaAs p-n junction diodes and compare the I - V characteristics.

Q4. Add a series resistor $R = 10$ m Ω in the diode implementation of **Q3** so that the current equation becomes implicit as

$$I = I_0 \left(\exp\left(\frac{V - IR}{\eta_1 V_T}\right) - 1 \right) + I_{0r} \left(\exp\left(\frac{V - IR}{\eta_2 V_T}\right) - 1 \right). \quad \text{Use the parameter values obtained in Q3. Plot current } I \text{ as}$$

a function of voltage V varying from 0 to 0.75 V in a semilog axis at $T = 300$ K for a Si p-n diode. Vary the resistance values from 1 m Ω to 10 Ω and show the difference in the plots.

Q5. For a Si p-n diode, implement the charging current $\frac{dQ_j}{dt}$ in parallel with the current source given in **Q1**

where Q_j is obtained as $Q_j = \int_0^V C_j dV = \int_0^V \left(\frac{C_{j0}}{\sqrt{1 - \frac{V}{V_{bi}}}} \right) dV$. Run a fixed frequency AC simulation at $f=2$

MHz to find out the Y-parameter and plot the junction capacitance versus voltage varying from -2 V to 0.75 V. Also plot $1/C_j^2$ versus V to extract the parameters C_{j0} and V_{bi} and check if they match with the calculated values.

Q6. From the simulation of **Q5**, plot the conductance versus current for a Si p-n diode. If the current source expression in **Q5** is taken from **Q4** with $R=1 \Omega$, plot the conductance versus current and compare with the previous plot. If one varies R from $1 \text{ m}\Omega$ to 10Ω , how this conductance plot changes?

Q7. In the problem of **Q5** for a Si p-n diode, implement one additional parallel charging current component as

$\frac{dQ_{diff}}{dt}$ where $Q_{diff} = I \tau$ with $\tau = \tau_p = \tau_n$. Now run a fixed frequency AC simulation at $f=2$ MHz to find out the Y-parameter and plot the junction capacitance versus voltage for voltage varying from -2 V to 0.75 V. Compare this plot with the one obtained from **Q5**. Plot the diffusion and junction capacitance components separately.