

Homework#2

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R Markdown

Lab #1

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Possible Protocol 1 (PP1): roll once; if get 6 then conclude the dice is not fair; if roll any other number conclude the dice is fair

-Once we rolled the dice and ran the code, we "rolled" a "1". This would indicate that the dice is fair

```
dice = c("1", "2", "3", "4", "5", "6")
sample(x = dice, size = 1, replace = TRUE)
a<-sample(1:6,size=1,replace = T)
print(a)
table(a)
[1] "1"
```

Then, we rolled the tampered dice to see if the roll is consistent with the code.

We rolled a "5" initially with the tampered dice, which makes this consistent with the fair dice portion of the code. As the dice is fair, the probability of it being judged as unfair is $1/6$ or 16.67%. Rolling a six is the only way to conclude the dice is unfair.

Depending on if the dice was unfair, the probability of them being deemed as fair is still $5/6$ or 83.3%.

PP2: roll the dice 30 times. Group can specify a decision rule to judge that dice is fair or unfair. Code below.

-As we rolled the tampered dice, we had a range of different outcomes. The format for the distribution of outcomes is as follows:

As seen in the tampered dice with the outcome of 2:6, two rolls cannot equal a six which will prove its tampered.

When we run code in R, the values follow rule for judging fairness. If a fair die is rolled 30 times, the outcomes will be as follows:

```
dice = c("1", "2", "3", "4", "5", "6")
sample(x = dice, size = 30, replace = TRUE)
a<-sample(1:6,size=30,replace = T)
print(a)
table(a)
1 2 3 4 5 6
1 6 7 5 9 2
[1] "5" "3" "3" "4" "3" "1" "4" "2" "3" "4" "3" "5" "5" "2" "3" "2" "6" "4" "4"
[20] "5" "5" "5" "2" "5" "5" "2" "2" "5" "6" "3"
outcomes <- c(5,3,3,4,3,1,4,2,3,4,3,5,5,2,3,2,6,4,4,5,5,5,2,5,5,2,2,5,6,3)
count1 <- length(which(outcomes == 1))
1
count2 <- length(which(outcomes == 2))
6
```

```
count3 <- length(which(outcomes == 3))
7
count4 <- length(which(outcomes == 4))
5
count5 <- length(which(outcomes == 5))
9
count6 <- length(which(outcomes == 6))
2
```

If the dice is being judged unfairly, it must be because any value appears at an alarmingly higher rate.

PP3: roll 100 times and specify decision rules. Some cases are easy: if every roll comes to 6 then might

-From what we believe, our sample size is now much greater from 30, so we can expect the number of 6's in

```
sample(x = dice, size = 100, replace = TRUE)
```

```
a<-sample(1:6,size=100,replace = T)
```

```
print(a)
```

```
table(a)
```

```
 1  2  3  4  5  6
12 17 23 16 15 17
[1] "3" "4" "3" "4" "3" "6" "6" "4" "1" "2" "3" "3" "4" "5" "4" "3" "4" "3" "6"
[20] "4" "5" "2" "2" "4" "2" "1" "3" "6" "1" "6" "4" "1" "6" "5" "5" "3" "3" "5"
[39] "1" "4" "5" "2" "4" "1" "1" "5" "5" "2" "2" "4" "6" "3" "3" "3" "4" "6" "6"
[58] "4" "2" "6" "6" "2" "6" "3" "3" "3" "6" "1" "5" "5" "3" "6" "1" "3" "3" "1"
[77] "6" "5" "1" "1" "2" "5" "2" "2" "5" "2" "3" "6" "4" "5" "2" "2" "3" "4" "6"
[96] "3" "5" "2" "3" "2"
```

```
outcomes <- c(5,3,3,4,3,1,4,2,3,4,3,5,5,2,3,2,6,4,4,5,5,5,2,5,5,2,2,5,6,3)
```

```
count1 <- length(which(outcomes == 1))
```

```
12
```

```
count2 <- length(which(outcomes == 2))
```

```
17
```

```
count3 <- length(which(outcomes == 3))
```

```
23
```

```
count4 <- length(which(outcomes == 4))
```

```
16
```

```
count5 <- length(which(outcomes == 5))
```

```
15
```

```
count6 <- length(which(outcomes == 6))
```

```
17
```

Ultimately, this proves the fairness of the dice where not one single number is appearing at a rate significantly different from the expected rate.

EP1: What is a reasonable number of times to roll your experiment dice? (given time available in class,

-"Rolling" a single 100 times for 5 rounds, (500 times) with replacements as the rolls are independent

We will then take the average of the experimental probability of the 5 separate trials. For the average

```
sample(x = dice, size = 500, replace = TRUE)
```

```
a<-sample(1:6,size=500,replace = T)
```

```
print(a)
```

```
[1] 3 5 1 5 5 1 2 1 5 6 4 1 3 2 5 3 1 2 2 5 3 4 5 3 6 6 4 6 5 2 6 6 3 2 3 4 4 3 5
[40] 5 6 6 5 3 5 2 1 3 2 4 5 3 6 3 4 3 3 1 2 1 5 5 2 5 5 3 2 1 4 1 1 5 1 5 6 3 4 3
[79] 1 4 3 5 1 4 4 1 5 5 3 3 4 6 2 5 4 5 6 4 1 2 5 4 6 2 1 6 4 1 1 3 4 1 6 4 5 5 3
[118] 4 3 2 5 4 2 3 4 2 5 6 6 3 3 4 1 5 2 3 3 3 4 5 5 1 5 5 5 5 4 2 3 2 3 6 2 6 2 3
[157] 4 6 3 3 2 3 4 4 2 2 2 1 1 5 2 4 3 5 5 4 6 2 2 5 2 2 2 4 5 5 5 3 5 2 1 1 3 4 6
[196] 2 3 5 2 6 6 4 2 1 5 2 2 1 4 3 3 2 5 2 6 3 6 3 4 3 4 6 3 3 2 2 3 5 4 3 3 6 3 2
[235] 1 6 3 2 1 2 3 3 1 3 6 5 1 3 6 1 3 2 6 4 1 1 3 1 5 4 4 3 2 1 1 3 3 1 6 1 1 3 1
[274] 3 4 2 6 2 2 1 2 5 2 1 3 2 5 5 2 4 2 2 6 2 3 2 4 3 1 6 1 5 5 4 4 1 1 5 2 3 5 2
```

```
[313] 1 2 3 2 1 4 1 3 3 2 1 6 4 5 6 2 4 6 2 4 2 1 3 5 6 5 3 3 2 2 6 2 5 2 3 4 5 6 2
[352] 2 6 4 6 6 2 4 5 1 1 5 3 4 1 1 3 5 3 1 1 5 5 1 1 1 4 4 4 3 2 5 6 5 3 6 4 6 6 5
[391] 5 5 2 2 5 5 3 5 1 5 4 2 3 3 1 3 2 2 4 2 2 1 4 5 3 5 2 2 2 5 6 2 4 2 4 2 2 5 2
[430] 4 3 4 1 4 2 1 4 5 1 4 6 2 5 6 5 6 4 3 6 6 6 4 4 5 2 1 2 6 3 1 5 5 5 5 3 6 1 2
[469] 3 6 6 2 6 6 5 3 1 6 4 4 4 3 4 2 5 2 1 2 6 3 4 5 1 4 5 2 6 5 1 6
```

```
table(a)
```

```
 1  2  3  4  5  6
75 99 91 76 93 66
```

```
library(ggplot2)
```

```
qplot(a,binwidth=1)
```

```
mean(a)
```

```
[1] 3.422
```

```
mode(a)
```

```
[1] 2
```

```
median(a)
```

```
[1] 3
```

```
var(a)
```

```
[1] 2.709335
```

```
sqrt(var(a))
```

```
[1] 1.646006
```

```
summary(a)
```

```
   Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
 1.000  2.000   3.000   3.422   5.000   6.000
```

```
sd(a,na.rm=TRUE)
```

```
[1] 1.646006]
```

```
hist(a)
```

We see here that the average is 3.422 with a standard deviation of 1.646006. The fairness of the dice is