Finding Extreme Points: Takeaways 🖻

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Concepts

- A derivative is the slope of the tangent line at any point along a curve.
- Let x be a point on the curve and h be the distance between two points, then the mathematical formula for the slope as h approaches zero is given as:

$$f'(x) = \lim_{h \to 0} \frac{f(x+h) - f(x)}{h}$$

- Differentiation is the process of finding a function's derivative.
- Finding the derivative of: $f(x) = -(x)^2 + 3x 1$:

•
$$y' = \lim_{h \to 0} \frac{(-(x+h)^2 + 3(x+h) - 1) - (-(x)^2 + 3x - 1)}{h}$$

•
$$y' = \lim_{h \to 0} \frac{-x^2 - 2xh - h^2 + 3x + 3h - 1 + x^2 - 3x + 1}{h}$$

•
$$y' = \lim_{h \to 0} \frac{h(-2x-h+3)}{h}$$

•
$$y' = \lim_{h \to 0} -2x - h + 3$$

•
$$y' = -2x + 3$$

• Three ways of notating a curve's derivative:

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$$y' = -2x + 3$$

•
$$f'(x) = -2x + 3$$
 *Only use if derivative is a function

•
$$\frac{d}{dx}[-x^2+3x-1]=-2x+3$$

- A critical point is a point where the slope changes direction from negative slope to positive slope or vice-versa. Critical points represent extreme values, which can be classified as a minimum or extreme value.
- ullet Critical points are found by setting the derivative function to 0 and solving for x
- Critical point classification:
 - When the slope changes direction from positive to negative it can be a maximum value.
 - When the slope changes direction from negative to positive, it can be a minimum value.
 - If the slope doesn't change direction, like at x=0 for $y=x^3$, then it can't be a minimum or maximum value.

- Each maximum or minimum value points are known as local extrema.
- Classifying local extrema:
 - A point is a relative minimum if a critical point is the lowest point in a given interval.
 - A point is a relative maximum if a critical point is the highest point in a given interval.
- Instead of using the definition of the derivative, we can apply derivative rules to easily calculate the derivative functions.
- Derivative rules:
 - Power rule: Let r be some power, then $f'(x) = rx^{r-1}$
 - Example: Let $f(x)=x^2$ In our function, r would be 2. Using the power rule, it's derivative would be $f'(x)=2x^{2-1}$ or f'(x)=2x
 - Sum rule: $rac{d}{dx}[f(x)+g(x)]=rac{d}{dx}[f(x)]+rac{d}{dx}[g(x)]$
 - Example: $\frac{d}{dx}[-x^3+x^2] = \frac{d}{dx}[-x^3] + \frac{d}{dx}[x^2] = -3x^2 + 2x$
 - Constant factor rule: $rac{d}{dx}[3x]=3rac{d}{dx}x=3\dot{1}=3$
- Derivative of x is always 1 and derivative of 1 is always 0.
- Once you found the critical points of a function, you can analyze the direction of the slope around the points using a sign chart to classify the point as a minimum or maximum. We can test points around our points of interest to see if there is a sign change as well as what the change is.

Resources

- Derivative rules
- Sign chart



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