Lambda calculus

Functional models of computation

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Lambda calculus

- History

Syntax

$$term ::= \underbrace{var}_{\text{Variable}} \mid \underbrace{term\ term}_{\text{Application}} \mid \underbrace{\lambda var.\, term}_{\text{Abstraction}}$$

Examples

Conventions

Tree representation

α-conversion

Free and bound variables

Substitution

α-equivalence

β-conversion

β-reduction

β-abstraction

η-conversion

Convertibility

Normal order reduction

First Church-Rosser theorem

Second Church-Rosser theorem

Normal order reduction

Recursion

Fixed-point combinator

Curry's Y-combinator

$$Y = \lambda f.\,(\lambda x.\,f(xx))\ (\lambda x.\,f(xx))$$

Turing's Θ-combinator

$$\Theta = (\lambda xy.\,x(xxy))\ (\lambda xy.\,x(xxy))$$

Church-Turing thesis

Undecidability

Church numerals

Relation to folds

Algebraic data types

Predecessor

Q&A