

Lambda calculus

Functional models of computation

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History

- 1928 - Hilbert's *Entscheidungsproblem*
(German for *Decision problem*)
 - Is there an *algorithm* for deciding whether a proposition in first-order logic is true or false?
- 1933 - Recursive functions (*Gödel, Herbrand*)
- 1935 - Untyped λ -calculus (*Church, Kleene, Rosser*)
- 1936 - Turing machine
- 1936 - Church-Turing thesis
- 1936 - Undecidability of first-order logic
 - Halting problem of Turing machine
 - Equivalence of λ -terms

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David Hilbert

- **Haskell Curry**
- Wilhelm Ackermann
- John von Neumann
- Ernst Zermelo
- ...

Alonzo Church

- **Stephen Cole Kleene**
- **J. Barkley Rosser**
- Alan Turing
- Dana Scott
- Michael O. Rabin
- ...

$$term ::= \underbrace{var}_{\text{Variable}} \mid \underbrace{term\ term}_{\text{Application}} \mid \underbrace{\lambda var. term}_{\text{Abstraction}}$$

Examples

Conventions

Tree representation

Free and bound variables

Substitution

α -equivalence

β -conversion

β -reduction

β -abstraction

Normal order reduction

First Church-Rosser theorem

Second Church-Rosser theorem

Normal order reduction

Fixed-point combinator

Curry's Y -combinator

$$Y = \lambda f. (\lambda x. f(xx)) (\lambda x. f(xx))$$

Turing's Θ -combinator

$$\Theta = (\lambda xy. x(xxy)) (\lambda xy. x(xxy))$$

Undecidability

Church numerals

Relation to folds

Algebraic data types

Predecessor

Q&A