

Lists

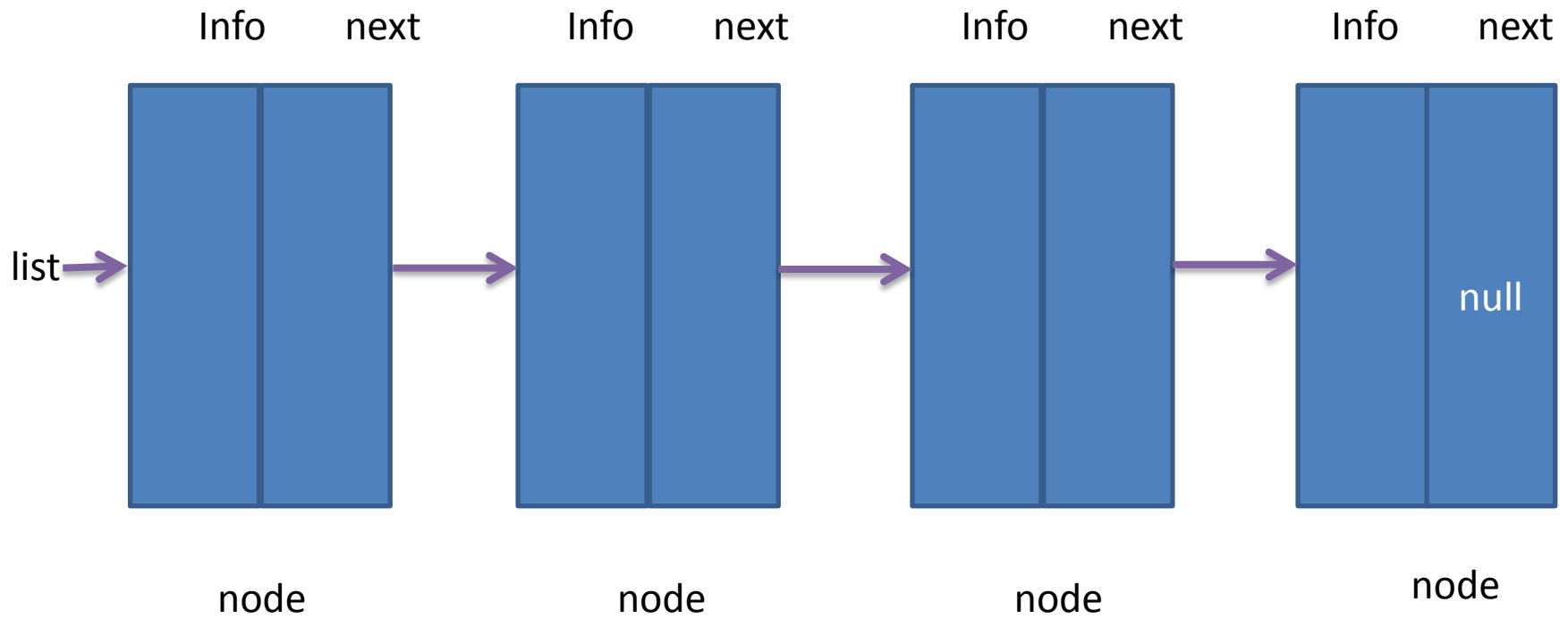
Unit 4

Introduction to Linked Linear Lists

- What are the **drawbacks of using sequential storage** to represent stacks and queues?
- One major drawback is that a **fixed amount of storage** remains allocated to the stack or queue even when the structure is actually using a smaller amount or possibly no storage at all.
- **In a sequential representation, the items of stack or queue are implicitly ordered** by the sequential order of storage.
- Thus if $q.items[x]$ represents an element of a queue.
- The next element will be $q.items[x + 1]$ (or if x equals $MAXQUEUE - 1$, $q.items[0]$).
- **It provides relationship of physical adjacency**

Introduction

- ***linked linear list is a data structure which provides Explicit Ordering. (Logical adjacency)***
- Each item in the list is called a **node** and contains two fields, **an information field and a next address field**.
- **info** - The information field holds the actual elements on the list.
- **next** - The next address field contains the address of the next node in the list.
- Such an address, which is used to access a particular node, is known as a **pointer**.



LINEAR LINKED LIST

Introduction

- The entire list is accessed from an ***external pointer – list (or First)*** that points to the ***first node*** in the list
 - list contains the address of the ***first node*** in the list.
- The ***next*** field of the ***last*** node in the list contains a special value known as ***null***.
- Null pointer signals the end of the list
- The list with no nodes is called an ***empty list*** or ***null list***.

Few Notations

- If **p** is a **pointer** to a node, **node(p)** refers to the node pointed to by p, **info(p)** refers to the information portion of that node, and **next(p)** refers to the next address portion and is therefore a pointer.
- Thus, if **next(p)** is not null, **info(next(p))** refers to the information portion of the node that follows node(p) in the list.

Types of lists

- Types of lists
 - Singly Linked List
 - Doubly Linked List
 - Circular Linked List

Linked Linear Lists

- A list is a dynamic data structure.
- The **number of nodes on a list may vary dramatically** as elements are inserted and removed.
- The dynamic nature of a list may be contrasted with the static nature of an array, whose size remains constant.

Inserting Nodes into a List

- Obtains empty nodes and then adds them to the existing nodes.
- The mechanism for obtaining the empty nodes is ***p=getnode();***.
- It sets the contents of a variable named p to the address of that node.
- The value of p is then a pointer to this newly allocated node.
- The next step is to insert the integer 6 into info portion of the newly allocated node. This is done by operation
- `info(p) = 6;`

Inserting Nodes into a List

- After setting the info portion of node(p), it is necessary to set the next portion of that node.
- Since node(p) is to be inserted at the front of the list. this node should point to the current first node
- **next(p) = list;**
- This operation places the value of list into the next field of node(p).
- At this point, p points to list with the additional item included.
- The external pointer ***list*** should now point to the new additional node since it is at the beginning of the list.
- **list = p;**
- Which changes the value of list to the value of p.

Inserting Nodes into a List

- *p* is an auxiliary variable which is used during the process of modifying the list.
- The value of *p* is not necessary after the process of modifying. It can be reused.
- The pseudo code for this insertion in general is
 - *p=getnode();*
 - *info(p)=x;*
 - *next(p)=list;*
 - *list = p;*
 - where x is the value of the node to be inserted

Removing Nodes from a List

- The following operation are performed:

p = list

list = next(p);

x = info(p);

- The first node has been removed from list, and x has been set to the desired value.
- The variable p is used as an auxiliary variable during the process of removing the first node from the list.
- The list make no reference to p.
- **freenode(p);**

Removing Nodes from a List

Once this operation has been performed, it becomes illegal to reference `node(p)`, since the node is no longer allocated.

- Since the value of `p` is a pointer to a node that has been freed, any reference to that value is also illegal.
- Another way of thinking of `getnode` and `freenode` is that `getnode` creates a new node whereas `freenode` destroys a node.

Representing Linked Lists in C

- Use the self referential structures to define a node's structure.
- To create new nodes when it is needed.
 - malloc function
- To remove the nodes that are no longer needed.
 - free function

Representing Linked Lists in C

- The general syntax is

struct node

{

int info1, info2, info3.....;

struct node * link;

};

typedef struct node NODE;

- Create a ***start*** pointer to the struct node called ***NODE***.

NODE * start;

Create a Node

- Create a node dynamically using ***malloc ()***.

☞ ***start= (NODE*) malloc (sizeof (NODE));***

✗ This obtains a memory area that is sufficient to store the node and assign its address to the pointer variable ***start***.

✗ This pointer indicates the beginning of the linked list.

Store data information

- start → info = 100;
- start → link = NULL;
 - The **link** part of the last node in a **singly linked list** should always contain **NULL**.
- To traverse the list or to display the nodes, the **start** pointer should always point to the first node.
- Initially when the list is empty start = NULL;

Insert at the beginning of the List

Pseudo code:

- Step 1: Start
- Step 2 : [Create a new node that is to be inserted]
 - newnode = getnode();
- Step 3:[Assign the item into the info field of the newnode]
 - Info [newnode]=ITEM
- Step 4:[Assign the link field of the newnode]
 - link[newnode]=Start
 - [It makes a link from NEWNODE to the previous first node.

Insert at the beginning of the List

- Step 5 : Reassign 'start' with the NEWNODE so that a link is developed between start and newnode.
- start = newnode
- Step 6: Return

Delete at the beginning

Pseudo code:

- Step 1: Start
- Step 2: An auxiliary variable **temp** should point to start.
- **temp = start**
- Step 3: Assign item as the value of info field of first node
- **item= info[start] // or item = info(temp)**

Delete at the beginning

- Step 4: Reassign start with the next node so that the first node is removed.
- **start = link[start] // or start = link(temp)**
- Step 5: Free the node that is being pointed by temp
- **freenode(temp)**
- Step 6: Exit

GETNODE AND FREENODE OPERATIONS

- The getnode operation finds one new node from the pool of available nodes and makes it available to the algorithm.
- Thus each time that getnode is invoked, it presents its caller with a brand new node, different from all the nodes previously in use.
- The function of freenode is to make a node that is no longer being used in its current context available for reuse in a different context.

GETNODE AND FREENODE OPERATIONS

- This available pool cannot be accessed by the programmer except through the getnode and freenode returns a node to the pool.
- It makes no difference which node is retrieved by getnode or where within the pool a node is placed by freenode.

GETNODE AND FREENODE OPERATIONS

- The available memory can be viewed as the list which is linked together by next field in each node
- The getnode operation removes the first node from this list and makes it available for use.
- The freenode operation adds a node to front of the list for reallocation by the next getnode.
- **The list of available nodes is called the available list.**

GETNODE AND FREENODE OPERATIONS

```
p = getnode(); can be implemented by  
    if (avail == null) {  
        printf("overflow");  
        exit(1);  
    }  
    p = avail;  
    avail = next(avail);
```

GETNODE AND FREENODE OPERATIONS

- The implementation of freenode(p) is straightforward:

next(p) = avail;

avail = p;

LINKED IMPLEMENTATION of STACKS

- The operation of adding an element to the front of a linked list is quite similar to that of pushing an element onto a stack.
- A stack may be represented by a linear linked list.
- The first node of the list is the top of the stack.
- If an external pointer *s* points to such a linked list, the operation `push(s,x)` may be implemented by

```
p = getnode();
```

```
info(p) = x;
```

```
next(p) = s;
```

```
s = p;
```

LINKED IMPLEMENTATION of STACKS

- The operation `empty(s)` is merely a test of whether `s` equals null.
- The operation `x = pop(s)` removes the first node from a nonempty list and signals underflow if the list is empty.

```
if (empty(s)) {  
    printf('stack underflow');  
    exit(1);  
}  
else{  
    p = s;  
    s = next(p);  
    x = info(p);  
    freenode(p);  
} /* end if */
```

Arrays v/s Linked lists

- The **disadvantages of representing a stack or queue by a linked list**
- A node in a linked list occupies **more storage** than a corresponding element in an array.
- Since two pieces of information per element are necessary in a list node.
- Only one piece of information is needed in the array implementation.
- An **array implementation allows access** to the n th item in a group using a **single operation**, whereas a list implementation requires n operations.
- It is necessary to pass through each of the first $n-1$ elements (Traversal) before reaching the n th element.

- **The advantage of a list over an array occurs when it is necessary to insert or delete an element in the middle of a group of other elements.**

Suppose the item are stored as a list.

- If p points to an element of the list, inserting a new element after $\text{node}(p)$ involves allocating a node, inserting the information, and adjusting two pointers.
- The amount of work required is independent of the size of the list.

Traversing a Linked List

Step 1: Start

Step 2: [Underflow condition]

if start = null then display linked list is empty and return

Step 3: Assign start to currptr // curr = start

Step 4: while curr!= null

process info[curr]

assign link[curr] to curr // curr = link(curr)

Step 5: Return

Displaying a Linked List

Step 1: Start

Step 2: [Underflow condition]

if start = null then display linked list is empty and return

Step 3: Assign start to curr // curr = start

Step 4: while curr!= null

display info[curr]

assign link[curr] to curr // curr = link(curr)

Step 5: Return

Insert at End

Step 1 : Start

Step 2 : Assign result of `getnode()` to `newnode`

Step 3: Assign item to `info[newnode]`

Step 4 : Assign null to `link[newnode]`

Step 5: [Empty List]

if `start = null` then Insert at beginning and
return // `start = newnode`

Insert at End

Step 6: Assign start to curr

Step 7: [Traverse] while link[curr] != null

Assign link[curr] to curr

Step 8: Assign newnode to link[curr]

Step 9: Return

Insert at End

Pseudo Code:

```
p = getnode();  
info(p) = x;  
link(p) = NULL;  
If (start == NULL)  
    start = p, return  
else  
    curr = start;  
    while (link(curr) != NULL)  
        curr = link(curr)  
    link(curr) = p  
return
```

Delete from end of list

Step 1: Start

Step 2: [Empty List]

if start = NULL then display Empty List and return

Step 3: [One element in list]

if link[start] = null then

assign null to start and free node and return

// curr = start, start = NULL, free(curr)

Step 4: [More than one element in list]

Assign start to curr // curr = start

Delete from end of list

Step 5: Assign NULL to prev // prev = NULL

Step 6: while link[curr]!=NULL

Assign curr to prev // prev = curr

Assign link[curr] to curr // curr = link(curr)

Step 7: Assign NULL to link[prev] // link(prev) = NULL

Step 8: free(curr)

Step 9: Return

Insert a node at a particular position in the linked list

Step 1: Start

Step 2: read pos

Step 3: newnode = getnode()

Step 4: Assign item to info[newnode]

Step 5: if pos = 1 Insert at beginning

link(newnode) = start

start = newnode

return

Step 6: Assign start to curr // curr = start

Step 7: count = 1

Insert a node at a particular position in the linked list

Step 8: from beginning to pos -1 assign link[curr] to curr

while count < (pos-1)

curr = link(curr)

count ++

Step 9: If curr = null

display not possible to insert and return

Step 10: Assign link[curr] to link[newnode]

link(newnode) = link(curr)

Step 11: Assign newnode to link[curr]

link(curr) = newnode

Step 12: Return

Delete from a particular position

Step 1: Start

Step 2: Read pos

Step 3: If pos =1 then delete from beginning and return

// curr = start, start = link(start), free(curr)

Step 4: Assign start to curr // curr = start

Step 5: Assign NULL to prev // prev = NULL

Step 6: count = 1

Delete from a particular position

Step 7: from 1 to pos

Assign curr to prev, Assign link[curr] to curr

while count < pos

prev = curr

curr = link(curr)

count ++

Step 8: Assign link[curr] to link[prev]

link(prev) = link(curr)

Step 9: free curr

Step 10: return

Insertion after node p and deletion of a node after node p from a list

insafter(p, x)

```
q = getnode();  
info(q) = x;  
link(q) = link(p);  
link(p) = q;
```

delafter(p, x)

```
q = link(p);  
x = info(q);  
link(p) = link(q);  
freenode(q);
```

Assignment

- Delete all nodes whose info field is x
- Insert into an ordered linked list
- Count the number of nodes whose info field is ≥ 60

Other Types of lists

- Lists with header nodes
- Noninteger lists

```
struct node {  
    char info[100];  
    struct node * next;  
};
```

```
struct node {  
    char name[30];  
    char id[10];  
    char addr[100];  
    float cgpa;  
    char stream[20];  
    struct node * next;  
};
```

CIRCULAR LINKED LIST

Introduction

- In a single linked list, the link part of the last node contains a ***NULL*** value.
- In a ***circular*** linked list, the link of the last node points to the first node of the linked list.
- **Advantage : Any node of the linked list can be accessed without going back and traversing again from the first node.**
- There is no first and last node in the linked list.
- A pointer **last** is considered during the processing of a circular linked list. (address of any one node usually the last node)
- Then next node is info(next(last))
- **If last == Null then empty list**

Create a CLL

- Step 1: Start
- Step 2: `newnode = getnode()`
- Step 3: assign item to `info[newnode]`
- Step 4: if `last = NULL`
 - assign `newnode` to `last`
 - assign `last` to `link[newnode]`
- Step 5: Return

Insert at Beginning - CLL

- Step 1: Start
- Step 2: `newnode = getnode()`
- Step 3: Assign item to `info[newnode]`
- Step 4: Assign `link[last]` to `link[newnode]`
- Step 5: Assign `newnode` to `link[last]`
- Step 6: Return

Insert at end- CLL – last node

- Step 1: Start
- Step 2: `newnode = getnode()`
- Step 3: assign item to `info[newnode]`
- Step 4: if `last = null` create_CLL and return
- Step 5: assign `link[last]` to `link[newnode]`
- Step 6: assign `newnode` to `link[last]`
- Step 7: assign `newnode` to `last`
- Step 8: Return

Delete from beginning - CLL

- Step 1: Start
- Step 2: if last = null
 - display empty linked list and return
- Step 3: assign link[last] to curptr
- Step 4: assign link[curptr] to link[last]
- Step 5: Display info[curptr] and free curptr
- Step 6: Return

Delete from end - CLL

- Step 1: Start
- Step 2: if last = null display empty linked list and return
- Step 3: assign link[last] to curptr, last to prevptr
- Step 4: while [curptr]!=last
 - assign curptr to prevptr
 - assign link[curptr] to curptr
- Step 6: assign link[last] to link[prevptr]
- Step 7: Display info[curptr] and free curptr
- Step 8: Return

Home work

1. Count the nodes in a CLL
2. Insert at a specific position
3. Delete from a specific position

??

DOUBLY LINKED LIST

Introduction

- In a SLL one could traverse only in one direction. To overcome this we can make use of DLL.
- A list that allows traversal in either the ***forward*** or ***backward*** direction is called ***doubly linked list***.
- This increases the performance and efficiency of the algorithms.

Introduction

- It contains two link fields –

☞ ***prev***

pointer that contains the address of the previous node

☞ ***Next***

Pointer that contains the address of the next node

PREV	INFO	NEXT
------	------	------

- The ***prev*** field of the ***first*** node and the ***next*** field of the ***last*** node always contains ***NULL***

DLL – Advantages / Disadvantages

- It can be traversed in either forward or backward direction.
- If a particular node's address is known, it is easy to know both the ***predecessor*** and the ***successor*** node address.
 - This makes it easy to insert and delete which is not possible in SLL
- It simplifies list management.
- But **Extra memory** is required by each node to store the ***prev*** pointer.
- Like SLL and CLL, here also we may have **header nodes** with global information about the list.

Representation of DLL in C

```
struct node
{
    int info1, info2, info3.....;
    struct node * prev;
    struct node * next;
};
```

- typedef struct node *NODE;

Some Observations

- Note that if P is the address of a given node then $\text{prev}[p]$ – previous node of p
 $\text{next}[\text{prev}[p]] = p$ // node p itself

Similarly $\text{next}[p]$ – next node of p
 $\text{prev}[\text{next}[p]] = p$ // node p itself
 $\text{next}[\text{prev}[p]] = p = \text{prev}[\text{next}[p]]$

DLL - Creation

- Step 1: Start
- Step 2: `newnode = getnode()`
- Step 3: `info[newnode] = item`
- Step 4: `start = newnode`
- Step 5: `prev[start] = null`
`next[start] = null`

NULL	ITEM	NULL
------	------	------

Insert at beginning

- Step 1: Start
- Step 2: newnode=getnode()
- Step 3: info[newnode] = item
- Step 4: prev[newnode] = null
- Step 5: next[newnode] = start
- Step 5: prev[start] = newnode
- Step 6: start = newnode
- Step 7: Return

DLL – Insert at End

- Step 1: Start
- Step 2: newnode = getnode()
- Step 3: info[newnode] = item
- Step 4: curr = start
- Step 5: If curr == null
 - insert at beginning and return
- Step 5: While next[curr] != null
 - curr = next[curr]
- Step 6: next[curr] = newnode
- Step 7: prev[newnode] = curr
- Step 8: next[newnode] = null
- Step 9: Return

DLL – Delete from Beginning

- Step 1: Start
- Step 2: curr = start
- Step 3: If curr == null
 - display empty list and return
- Step 4: Display info[curr]
- Step 5: If next[curr] == null
 - start = null
 - else
 - start = next[curr]
 - prev[start] = null
- Step 6: free curr
- Step 7: Return

DLL – Delete at End

- Step 1: Start
- Step 2: curr = start
- Step 3: If curr == null
 - display empty list and return
- Step 4: if next[curr] == null // one node
 - display info[curr]
 - start = null
 - return
- Step 5: While next[curr] != null // more than one node
 - curr = next[curr]
- Step 6: next[prev[curr]] = null
- Step 7: Display info[curr]
- Step 8: Free curr
- Step 9: Return

DLL – Insert at a specific position

- Step 1: Start
- Step 2: newnode =getnode()
- Step 3: info[newnode] = item
- Step 4: if pos = 1
 - insert at beginning and return
- Step 5: l = 1
 - curr = start
- Step 6: while l is less than pos -1 and curr!=null
 - curr = next[curr]
 - increment l

- Step 7: If `curr == null`
- display invalid position and return
- Step 8: `next[newnode] = next[curr]`
- Step 9: `prev[newnode] = curr`
- Step 10: `prev[next[curr]] = newnode`
- Step 11: `next[curr] = newnode`
- Step 12: Return

DLL – Delete from a specific position

- Step 1: Start
- Step 2: curr = start
- Step 3: If curr == null
 - display empty list and return
- Step 4: l = 1
- Step 5: while i < pos and curr != null
 - curr = next[curr]
 - Increment l

- Step 6: `next[prev[curr]] = next[curr]`
- Step 7: `prev[next[curr]] = prev[curr]`
- Step 8: `display info[curr]`
- Step 9: `free curr`
- Step 10: Return

C routine for Deleting a node with address P

- This operation is not possible in SLL

```
void delete(NODE * P, int * x)
{
    NODE * l, *r;
    if (p == NULL)
    {
        printf(" deletion not possible\n");
        return;
    }
    *x = p->info;
    l = p->prev;
    r = p->next;
    l->next = r;
    r->prev = l;
    free(p);
    return;
}
```

Assignment

- Addition of two long integers using DLL

- Thank You