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lmtp: An R Package for Non-Parametric Causal Effects Based on Modified Treatment Policies

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Abstract

The majority of causal inference methods consider treatment effects based on counterfactual outcomes where exposure is deterministically established. When exposure is continuous, deterministic treatment effects may be irrelevant and impossible to bring about. As a solution, modified treatment policies offer a non-parametric alternative to deterministic treatment effects that allow for the study of feasible interventions and offer a safegaurd against positivity violations. The **lmtp** package implements the estimators of Diaz, Williams, Hoffman, and Schenck (2020) for estimating causal effects based on non-parametric modified treatment policies in R. The provided methods can be applied to both point-treatment and longitudinal settings, and can account for time-varying exposure, covariates, and right censoring. Additionally, two of the provided estimators can incorporate flexible data-adaptive algorithms for estimation while maintaining valid statistical inference.

Keywords: causal inference, non-parametric, modified treatment policies, R.

1. Introduction

Most modern causal inference methods consider the effects of a exposure on a population mean outcome under interventions that set the treatment value deterministically. For example, the average treatment effect (ATE) considers the hypothetical difference in a population mean outcome if a dichotomous exposure was applied to all observations versus if it was applied to none. In the case of a categorical or continuous exposure, it is unlikely any policy could bring this about. Furthermore, the estimation of causal effects requires the so called positivity assumption which states that all observations have a greater than zero chance of experiencing the exposure levels (Rosenbaum and Rubin 1983). This assumption is often violated when evaluating the effects of deterministic interventions and is usually exacerbated with longitudinal data.

First introduced by Haneuse and Rotnitzky (2013), and building off work by Muñoz and van der Laan (2012), modified treatment policies (MTPs) are stochastic treatment regimes that can be formulated to avoid violations of the positivity assumption. Diaz et al. (2020) later extended MTPs to the longitudinal setting with time-varying treatment, covariates, and right-censoring of the outcome.

The package <code>lmtp</code> implements four methods for estimating the effects of MTPs. Two of these estimators, a targeted minimum-loss based estimator (Laan and Rose 2011; Laan and Rubin 2006) and a sequentially doubly-robust estimator (Buckley and James 1979; Fan and Gijbels 1994; van der Laan and Dudoit 2003; Rotnitzky, Faraggi, and Schisterman 2006; Rubin and Laan 2006; Kennedy, Ma, McHugh, and Small 2017), are multiply-robust. In addition to MTPs, the package naturally allows for estimation of the ATE, causal risk ratio, and causal odds ratio and can thus be used for a variety of causal inference problems. In this article we describe how <code>lmtp</code> can be used for estimating the causal effects of MTPs and both static and dynamic deterministic treatment effects. The package may be download from CRAN at <code>cran.r-project.org/package=lmtp</code>.

2. Notation and modified treatment policies

2.1. Data structure

In this article, we will use the notation of Diaz et al. (2020) with slight modification. Let i be the index of an observation from a data set with n total units and t be the index of time for a total time of τ . The observed data for observation Z_i may be denoted as

$$Z_i = (W, L_1, A_1, L_2, A_2, ..., L_{\tau}, A_{\tau}, Y_{\tau+1}) \tag{1}$$

where W denotes baseline covariates, L_t denotes time-varying covariates, A_t denotes a vector of exposure variables and Y denotes an outcome at the end of study follow-up. We observe n i.i.d. copies of Z with distribution P. We use $A_t = a_t$ to denote a realization of a random variable. If right-censoring exists, A_t can be adapted so that $A_t = (A_{1,t}, A_{2,t})$ where $A_{1,t}$ equals one if an observation is still in the study at time t and zero otherwise, and $A_{2,t}$ denotes the exposure at time t. We use an overbar to indicate the history of a variable up until time t. We then use $H_t = (\bar{L}_t, \bar{A}_{t-1})$ to denote the history of all variables up until just before A_t .

2.2. Modified treatment policies

We will use the potential outcomes framework to define the causal effect of interest using our established data structure. We consider a hypothetical policy where \bar{A} is set to a regime d defined as $A_t^d = d_t(A_t, H_t^d)$, where $H_t^d = (\bar{L}_t, \bar{A}_t^d - 1)$, for a set of user-given regimes $d_t : t \in \{1, ..., \tau\}$. The defining characteristic that makes regime d_t a modified treatment policy is that it depends on the *natural value* of \bar{A}_t and \bar{L}_t .

Formally, consider a longitudinal study with loss-to-follow-up. Let $A_t = (A_{1,t}, A_{2,t})$ where $A_{1,t}$ equals one if an observation is still in the study at time t and zero otherwise, and $A_{2,t}$ denote a continuous exposure at time t that can be changed through some intervention. A

modified treatment policy that decreases A_t is then

$$d_t(a_t, h_t) = \begin{cases} (1, a_{2,t} - \delta_t) & \text{if } a_{2,t} > u_t(h_t) + \delta_t \\ (1, a_{2,t}) & \text{if } a_{2,t} \le u_t(h_t) + \delta_t \end{cases}$$
(2)

where $0 < \delta_t < u_t(h_t)$ is a user-defined value and A_t is supported in the data. Notice that the hypothetical exposure after intervention, A_t^d depends on the actually observed exposure, A_t . This is in contrast to a deterministic intervention where A_t^d would be set to some arbitrary value with probability one. If right-censoring did not exist in the data, the MTP d would simplify to removing $A_{1,t}$ from the MTP definition. In analogue to Diaz $et\ al.\ (2020)$, in this article we will focus on estimating the the causal effect of MTP d on outcome Y, using lmtp, through the causal parameter

$$\theta = \mathsf{E}\{Y(A^d)\},\tag{3}$$

where $Y(A^d)$ is the potential outcome in a world, contrary to fact, where \bar{A} was modified according to the MTP d. When Y is continuous, θ is the mean population value of Y under MTP d; when Y is dichotomous, θ is the population proportion of event Y under MTP d. Similarly, when Y is a survival outcome, θ is defined as the cumulative incidence of Y under MTP d.

2.3. Identification

Causal interpretation of θ requires identifying an expression of θ as a function of the data generating distribution P using only the observed data Z. A full review of these identification assumptions is outside the scope of this article. Briefly, the following standard assumptions must hold

Assumption 1 (Consistency) $\bar{A} = \bar{a} \implies Y = Y(\bar{a}) \text{ for all } \bar{a} \in \text{supp } \bar{A}$

Assumption 2 (Exchangeability) If $(a_t, h_t) \in \text{supp}\{A_t, H_t\}$ then $(d(a_t, h_t), h_t) \in \text{supp}\{A_t, H_t\}$ for $t \in \{1, ..., \tau\}$

Assumption 3 (Positivity) $A_t \perp \!\!\!\perp Y(\bar{a}) | H_t \text{ for all } \bar{a} \in \text{supp } \bar{A} \text{ and } t \in \{1, ..., \tau\}$

The consistency assumption states that the potential outcome for an observation under their observed exposure is the value of the outcome that we did actually observe. Assumption 2, the exchangeability assumption, is often also referred to as the no-unmeasured confounding assumption; it is satisfied if all common causes of the exposure and outcome are measured and adjusted for. Of particular importance to this article is the positivity assumption which states that the distribution of the exposure under the MTP is supported in the data. Concretely, in a study with a continuous exposure and loss-to-follow-up, the positivity assumption states that if an observation with covariate history h_t and exposure a_t who was not lost-to-follow-up at time t exists then there is also an observation with covariate history h_t who was not lost-to-follow-up at time t but whose exposure was observed as $d(a_t, h_t)$ that also exists.

The strength of MTPs is that they may be formulated to avoid violations of the positivity assumption, which is often an issue when working with continuous exposures.

3. Estimating modified treatment policy effects

3.1. Estimation methods

The **lmtp** package implements four estimation methods: a targeted minimum-loss based estimator (TMLE), a sequential doubly-robust estimator (SDR), an estimator based on the parametric G-formula, and an inverse probability weighted (IPW) estimator. We will only describe the use of TMLE, lmtp_tmle, and SDR, lmtp_sdr, as their use is strongly suggested over the others.

Targeted minimum-loss based estimation is a general framework for constructing asymptotically linear estimators with an optimal bias-variance tradeoff of the target causal parameter (INSERT A CITATION FOR THIS). In general, TMLE is constructed from a factorization of the target parameter into an outcome regression and a treatment mechanism. Using the outcome regression, an initial estimate of the target parameter is constructed and then *de-biased* by a fluctuation that depends on a function of the treatment mechanism. The sequential doubly-robust estimator is based on a unbiased transformation of the efficient influence function of the target estimand. For a thorough discussion of TMLE and SDR, we recommend the following articles (INSERT THESE ARTICLES).

Both TMLE and SDR are multiply-robust. Specifically, TMLE is considered $\tau + 1$ -multiply robust while SDR is robust under 2^{τ} -configurations. EXPLAIN WHAT THIS MEANS.

It is important to note that it is possible for the SDR to produce an estimate of $\hat{\theta}$ outside of the bounds of the parameter space. Taking into account that for a single time-point the TMLE and SDR have equivalent robustness, we recommend use of TMLE for the case of a single time-point, while we recommend use of SDR for the longitudinal setting. All examples in this article will use both estimators.

3.2. Required data structure

Data is passed to **lmtp** estimators through the data argument, and should be in wide format with one column per variable per time point under study (i.e., there should be one column for every variable in Z). These columns do not have to be in any specific order and the data set may contain variables that won't be used in estimation. The names of treatment variables, censoring variables, baseline covariates, and time-varying covariates are specified using the trt, cens, baseline, and time_vary arguments respectively. The trt, cens, and baseline arguments accept character vectors and the trt and cens arguments should be ordered according to the time-ordering of the data generating mechanism. The time_vary argument accepts an unnamed list ordered according to the time-ordering of the model with each index containing the name of the time-varying covariates for the given time. The outcome variable is specified through the outcome argument.

The provided estimators can work with dichotomous, continuous, or survival outcomes. In the case of a dichotomous or continuous outcome, only a single variable name should be passed to the outcome argument. For survival outcomes, a vector containing the names of the intermediate outcome and final outcome variables ordered according to time should be passed to the outcome argument. Dichotomous and survival outcomes should be coded using zero's and one's where one indicates the occurrence of an event and zero otherwise. The outcome_type argument should be set to "continuous" for continuous outcomes and "binomial" for dichotomous and survival outcomes. If missingness is present in the outcome variable, the cens argument must be provided. Censoring indicators should be coded using zero's and one's where one indicates an observation is observed at the next time and zero indicates loss-to-follow-up. Once an observation's censoring status is switched to zero it cannot change back to one. Missing data before an observation is lost-to-follow-up is not allowed

The k argument controls a Markov assumption of the data. With k = Inf, the entire history H_t will be used for estimation at time t while k = 0 will restrict the set of variables in H_t used for estimation to time-varying covariates at time t - 1. Baseline confounders are always included in estimation. The create_node_list function may be used to inspect how variables will be used for estimation. It is specified with the same trt, baseline, time_vary, and k arguments as lmtp estimators and is used internally to create a "node list" that encodes which variables should be used at each time point of estimation. For example, consider a study with the observed data structure

$$Z = (W_1, W_2, L_{1,1}, L_{1,2}, A_1, L_{2,1}, L_{2,2}, A_2, Y_3)$$

$$\tag{4}$$

We can translate this data structure to R with

```
R> baseline <- c("W_1", "W_2")
R > trt <- c("A_1", "A_2")
R> time_vary <- list(c("L_11", "L_12"),</pre>
                     c("L_21", "L_22"))
R+
R> create_node_list(trt = trt, baseline = baseline,
R+
                    time_vary = time_vary, tau = 2)
$trt
$trt[[1]]
[1] "W_1"
           "W_2" "L_11" "L_12" "A_1"
$trt[[2]]
           "W_2" "L_11" "L_12" "L_21" "L_22" "A_1" "A_2"
[1] "W_1"
$outcome
$outcome[[1]]
[1] "W_1" "W_2" "L_11" "L_12" "A_1"
$outcome[[2]]
           "W_2" "L_11" "L_12" "A_1" "L_21" "L_22" "A_2"
```

A list of lists is returned with the names of the variables in H_t to be used for estimation of the outcome regression and the treatment mechanism at every time t. Notice that variables

 A_1 and A_2 are included for their own estimation. The **lmtp** package recasts the density ratio nuisance parameter estimation into a classification problem based on a 2n observations augmented data set where an indicator variable Λ is used as a pseudo outcome (Cheng and Chu 2004; Qin 1998). In the augmented data set, the data structure at time t is redefined as

$$(H_{\lambda,i,t}, A_{\lambda,i,t}, \Lambda_{\lambda,i} : \lambda = 0, 1; i = 1, ..., n)$$

$$(5)$$

where $\Lambda_{\lambda,i} = \lambda_i$ indexes the duplicate values. For all duplicated observations $i \in \{1, ..., 2n\}$, $H_{\lambda,i,t}$ is the same. While, for $i \in \{1, ..., n\}$ duplicated observations $A_{0,i,t}$ are the observed exposure values and $A_{1,i,t}$ for $i \in \{n+1, ..., 2n\}$ are the exposure values under the MTP d, A_t^d .

3.3. Creating modified treatment policies

Treatment policies are specified using the **shift** argument, which accepts a user-defined function that returns a vector of exposure values modified according to the policy of interest. Shift functions should take two arguments, the first for specifying a data set and the second for specifying the current exposure variable. For example, a possible MTP may increase exposure by 2 units if the natural exposure value was below 5 units and do nothing otherwise. A shift function for this MTP would look like

```
R> function(data, trt) {
R+ (data[[trt]] < 5)*(data[[trt]] + 2) + (data[[trt]] >= 5)*data[[trt]]
R+ }
```

This framework is flexible and allows for specifying complex treatment regimes that can also depend on time and covariates. In the case of a binary exposure, two shift functions are installed with the package: static_binary_on which sets $A_{i,t} = 1$, and static_binary_off which sets $A_{i,t} = 0$.

3.4. The estimation engine

An attractive property of multiply-robust estimators is that they can incorporate flexible machine-learning algorithms for the estimation of nuisance parameters while remaining \sqrt{n} -consistent. The super learner algorithm is an ensemble learner than incorporates a set of candidate models through a weighted convex-combination based on cross-validation (Laan, Polley, and Hubbard 2007). Asymptotically, this weighted combination of models, called the meta-learner, will outperform any single one of its components.

Access to the super learner is provided by the sl3 package (Coyle, Hejazi, Malenica, and Sofrygin 2020). Analysts must create sl3 learner stacks which are then included in lmtp_tmle and lmtp_sdr calls with the lrnrs_trt and lrnrs_outcome arguments. The outcome variable type should guide users on selecting the appropriate candidate learners for use with the lrnrs_outcome argument. Regardless of whether an exposure is continuous, dichotomous, or categorical, the exposure mechanism is estimated using classification, users should thus only include candidate learners capable of binary classification with the lrnrs_trt argument.

Candidate learners that rely on cross-validation for the tuning of hyper-parameters should support grouped data if used with lrnrs_trt. Because estimation of the treatment mech-

anism relies on the augmented 2n duplicated data set, duplicated observations must be put into the same fold during sample-splitting.

User's may install sl3 from https://github.com/tlverse/sl3. Because sl3 is not available for installation from a standard repository, it is not required to use lmtp. Instead, the lrnrs_trt and lrnrs_outcomes arguments can be set equal to NULL and nuisance parameters will be estimated using a generalized linear model (GLM) with the glm function from the stats package (INSERT STATS PACKAGE CITATION).

3.5. Additional arguments

Sample-splitting and cross-fitting is used with all methods (Zheng and van der Laan 2011; Chernozhukov, Chetverikov, Demirer, Duflo, Hansen, Newey, and Robins 2018), and the number of folds can be set with the folds argument; the minimum number of allowed folds is two. If data has a hierarchical structure, the id argument is used to indicate the name of a variable in the data set indicating unique groups. These identifiers will be used for generation of cross-validation folds and will be accounted for in standard error calculations.

3.6. Contrasts

In addition to the MTP effect, researchers may be interested in a comparison of the MTP effect and the outcome under the observed exposures, or other treatment policies. This is the role of the lmtp_contrast function. Users may specify any number of objects returned by calls to lmtp_tmle or lmtp_sdr to be compared to a single a reference value or a single reference MTP, specified using the ref argument. Depending on the outcome type, contrasts may be either additive (type = "additive"), an odds ratio (type = "or"), or the relative risk (type = "rr")

3.7. Examples

Example 1: Longitudinal MTP with no loss-to-follow-up

We have simulated data on n=5000 observations over a 5-month period. Each observation has a continuous exposure (A_1, A_2, A_3, A_4) and covariate (L_1, L_2, L_3, L_4) recorded at months one through four and a dichotomous outcome (Y) at month five. We assume no loss-to-follow-up and no Markov property. This data set is installed with the package and is stored in the object sim_t4 .

For this example, we are interested in the effect of a longitudinal MTP where at each month an observation's exposure decreases by one only if their observed exposure wouldn't be less than one if modified. Our data structure has no baseline confounders and we will use only GLMs for estimation so the only objects we must specify are the treatment variables, the time-varying covariates, the outcome variable, and the MTP shift function.

```
R> trt <- c("A_1", "A_2", "A_3", "A_4")

R> time_vary <- list(c("L_1"), c("L_2"), c("L_3"), c("L_4"))

R> y <- "Y"

R> shift <- function(data, trt) {

R+ (data[[trt]] - 1) * (data[[trt]] - 1 >= 1) +
```

```
R+
       data[[trt]] * (data[[trt]] - 1 < 1)</pre>
R+ }
R> lmtp_tmle(sim_t4, trt, y, time_vary = time_vary, shift = shift)
LMTP Estimator: TMLE
   Trt. Policy: (shift)
Population intervention effect
      Estimate: 0.2646
    Std. error: 0.019
        95% CI: (0.2274, 0.3019)
R> lmtp_sdr(sim_t4, trt, y, time_vary = time_vary, shift = shift)
LMTP Estimator: SDR
   Trt. Policy: (shift)
Population intervention effect
      Estimate: 0.2608
    Std. error: 0.021
        95% CI: (0.2196, 0.3019)
```

Example 2: Longitudinal MTP, right-censoring, and the super learner

For this example, we have a simulated dataset of n=1000 observations. Data was simulated for three time points with a continuous time-varying exposure at times $t \in \{1,2\}$ (A1, A2), a dichotomous time-varying covariate at times $t \in \{1,2\}$ (L1, L2), and a dichotomous outcome (Y) at time t=3. Loss-to-follow-up is present after time t=1 so the data set contains censoring indicators (C1, C2). This data is installed with the package and is stored in the object sim_cens.

Suppose we are interested in the additive effect of an MTP where exposure is increased by 0.5 at every time point for all observations. Instead of using a linear model, we will estimate the outcome regression and treatment mechanism using a super learner composed of a GLM, a random forest (Wright and Ziegler 2017), and multivariate adaptive regression splines (Milborrow 2019).

```
R> tml <- lmtp_tmle(sim_cens, trt, y, time_vary = time_vary,</pre>
R.+
                     cens = cen, shift = mtp, learners_trt = lrnrs,
                     learners_outcome = lrnrs, folds = 3)
R+
R> print(tml)
LMTP Estimator: TMLE
   Trt. Policy: (mtp)
Population intervention effect
      Estimate: 0.9011
    Std. error: 0.0094
        95% CI: (0.8826, 0.9196)
R> sdr <- lmtp_sdr(sim_cens, trt, y, time_vary = time_vary,</pre>
R+
                    cens = cen, shift = mtp, learners_trt = lrnrs,
R+
                    learners_outcome = lrnrs, folds = 3)
R> print(sdr)
LMTP Estimator: SDR
   Trt. Policy: (mtp)
Population intervention effect
      Estimate: 0.8995
    Std. error: 0.0095
        95% CI: (0.881, 0.918)
```

If loss-to-follow-up exists, we can estimate the population mean outcome under the observed exposures by specifying shift = NULL. This estimate can then be used as the reference value for calculating the additive effect of the MTP compared to the observed exposures.

```
R> tml_obs <- lmtp_tmle(sim_cens, trt, y, time_vary = time_vary,</pre>
R+
                         cens = cen, shift = NULL, learners_trt = lrnrs,
R+
                         learners_outcome = lrnrs, folds = 3)
R> lmtp_contrast(tml, ref = tml_obs)
  LMTP Contrast: additive
Null hypothesis: theta == 0
  theta shift ref std.error conf.low conf.high p.value
1 0.104 0.901 0.797
                      0.00607
                                 0.0918
                                           0.116 < 0.001
R> sdr_obs <- lmtp_sdr(sim_cens, trt, y, time_vary = time_vary,</pre>
R+
                        cens = cen, shift = NULL, learners_trt = lrnrs,
R+
                       learners_outcome = lrnrs, folds = 3)
R> lmtp_contrast(sdr, ref = sdr_obs)
```

```
LMTP Contrast: additive
Null hypothesis: theta == 0

theta shift ref std.error conf.low conf.high p.value
1 0.0998 0.899 0.8 0.00612 0.0878 0.112 <0.001
```

Example 3: Survival analysis and deterministic effects

The Imtp package may also be used to estimate deterministic causal effects, such as the causal relative risk. Suppose we have data on n=2000 observations with a time-invariant binary exposure followed for a period of seven days. We wish to estimate the causal relative risk of experiencing an event by day seven. This data is installed with the package and is stored in the object $\operatorname{sim_point_surv}$.

```
R> trt <- "trt"
R> baseline <- c("W1", "W2")</pre>
R> cens <- paste0("C.", 0:5)
R> y <- paste0("Y.", 1:6)
R> tml1 <- lmtp_tmle(sim_point_surv, trt, y, baseline, cens = cens,</pre>
R+
                     learners_trt = lrnrs, learners_outcome = lrnrs,
                     shift = static_binary_on, folds = 3)
R> tml0 <- lmtp_tmle(sim_point_surv, trt, y, baseline, cens = cens,
                      learners_trt = lrnrs, learners_outcome = lrnrs,
R+
R+
                     shift = static_binary_off, folds = 3)
R> lmtp_contrast(tml1, ref = tml0, type = "rr")
  LMTP Contrast: relative risk
Null hypothesis: theta == 1
                ref std.error conf.low conf.high p.value
  theta shift
1 1.22 0.812 0.665
                       0.0341
                                   1.14
                                             1.31 < 0.001
R> sdr1 \leftarrow lmtp\_sdr(sim\_point\_surv, trt, y, baseline, cens = cens,
R+
                   learners_trt = lrnrs, learners_outcome = lrnrs,
                   shift = static_binary_on, folds = 3)
R+
R> sdr0 <- lmtp_sdr(sim_point_surv, trt, y, baseline, cens = cens,
                   learners_trt = lrnrs, learners_outcome = lrnrs,
R+
R+
                   shift = static_binary_off, folds = 3)
R> lmtp_contrast(sdr1, ref = sdr0, type = "rr")
  LMTP Contrast: relative risk
Null hypothesis: theta == 1
  theta shift ref std.error conf.low conf.high p.value
1 1.21 0.809 0.667
                                   1.14
                       0.0338
                                              1.3 < 0.001
```

3.8. Extra features

Computation time can rapidly increase with many time points and when using the super learner. As a solution, **Imtp** can utilize parallel processing provided by the **future** package (Bengtsson 2020a). In addition, **Imtp** is compatible with the **progressr** package (Bengtsson 2020b) for producing progress bars by wrapping estimator calls in with_progress. For users familiar with the **broom** package (Robinson and Hayes 2020), **Imtp** contains a tidy method.

4. Reference Manual

4.1. lmtp_tmle and lmtp_sdr

Syntax 1

Arguments

- data: A data frame in wide format.
- trt: A vector containing the column names of the treatment variables ordered by time.
- outcome: The column name of the outcome variable. In the case of time-to-event analysis, a vector containing the column names of the intermediate outcome variables and the final outcome variable ordered by time. Only numeric values are allowed. If the outcome type is binary, data should be coded as zeroes and ones.
- baseline: An optional vector containing the columns names of baseline covariates to be included for adjustment at every time-point.
- time_vary: A list the same length as the number of time points of observation. The list should be ordered following the time ordering of the model. Each index of the list should be a vector containing the column names of the time-varying covariates at that time-point.
- cens: An optional vector, the same length as time_vary, containing the column names of censoring indicators. Must be provided if there is missingness in the outcome or if a time-to-event analysis.
- shift: A two argument function that specifies how treatment variables should be shifted.
- k: An integer controlling the Markov property of the data generating mechanism. If k
 Inf (default) the history H_t will contain all previous time-point variables. If k = 0
 the history will only contain baseline variables and time-varying covariates at t 1.
- outcome_type: The outcome variable type. Valid options are "continuous" and "binomial".
- id: An optional column name containing cluster-level identifiers.

- bounds: An optional vector of length two containing the upper and lower bounds for a continuous outcome. If NULL the bounds will be taken as the minimum and maximum of the observed data; ignored if outcome_type = "binomial"
- learners_outcome: An optional sl3 learner stack to be used for estimation of the outcome regression. If NULL, estimation will default to using a generalized linear model.
- learners_trt: An optional sl3 learner stack to be used for estimation of the treatment mechanism. If NULL, estimation will default to using a generalized linear model.
- folds: The number of folds to be used for cross-fitting. The minimum number of allowed folds is two.
- bound: Determines that maximum and minimum values (scaled) predictions will be bounded to. The default is 1e-5, bounding predictions between 1×10^{-5} and 0.9999.

Returns

Objects returned from calls to lmtp_tmle or lmtp_sdr will contain:

- \bullet estimator:
- theta:
- standard_error:
- low:
- high:
- eif:
- shift:
- outcome_reg:
- density_ratios:
- weights_m:
- weights_r:
- outcome_type:

4.2. lmtp_contrast

Syntax

Arguments

- One entry in the list
- Another entry in the list

Returns

- One entry in the list
- Another entry in the list

4.3. create_node_list

Syntax

Arguments

- One entry in the list
- Another entry in the list

Returns

- One entry in the list
- Another entry in the list

References

- Bengtsson H (2020a). future: Unified Parallel and Distributed Processing in R for Everyone. R package version 1.18.0, URL https://CRAN.R-project.org/package=future.
- Bengtsson H (2020b). progressr: A Inclusive, Unifying API for Progress Updates. R package version 0.6.0, URL https://CRAN.R-project.org/package=progressr.
- Buckley J, James I (1979). "Linear Regression with Censored Data." *Biometrika*, **66**(3), 429–436. ISSN 0006-3444. doi:10.2307/2335161. Publisher: [Oxford University Press, Biometrika Trust], URL https://www.jstor.org/stable/2335161.
- Cheng KF, Chu CK (2004). "Semiparametric Density Estimation under a Two-Sample Density Ratio Model." *Bernoulli*, **10**(4), 583–604. ISSN 1350-7265. Publisher: International Statistical Institute (ISI) and Bernoulli Society for Mathematical Statistics and Probability, URL https://www.jstor.org/stable/3318817.

- Chernozhukov V, Chetverikov D, Demirer M, Duflo E, Hansen C, Newey W, Robins J (2018). "Double/debiased machine learning for treatment and structural parameters." *The Econometrics Journal*, **21**(1), C1–C68. ISSN 1368-423X. doi:10.1111/ectj.12097. _eprint: https://onlinelibrary.wiley.com/doi/pdf/10.1111/ectj.12097, URL https://onlinelibrary.wiley.com/doi/abs/10.1111/ectj.12097.
- Coyle JR, Hejazi NS, Malenica I, Sofrygin O (2020). sl3: Pipelines for Machine Learning and Super Learning. doi:10.5281/zenodo.1342293. R package version 1.3.8, URL https://github.com/tlverse/sl3.
- Diaz I, Williams N, Hoffman KL, Schenck EJ (2020). "Non-parametric causal effects based on longitudinal modified treatment policies." arXiv:2006.01366. ArXiv: 2006.01366 version: 2, URL http://arxiv.org/abs/2006.01366.
- Fan J, Gijbels I (1994). "Censored Regression: Local Linear Approximations and Their Applications." Journal of the American Statistical Association, 89(426), 560–570. ISSN 0162-1459. doi:10.2307/2290859. Publisher: [American Statistical Association, Taylor & Francis, Ltd.], URL https://www.jstor.org/stable/2290859.
- Haneuse S, Rotnitzky A (2013). "Estimation of the effect of interventions that modify the received treatment." *Statistics in Medicine*, **32**(30), 5260–5277. ISSN 1097-0258. doi:10. 1002/sim.5907. _eprint: https://onlinelibrary.wiley.com/doi/pdf/10.1002/sim.5907, URL https://onlinelibrary.wiley.com/doi/abs/10.1002/sim.5907.
- Kennedy EH, Ma Z, McHugh MD, Small DS (2017). "Nonparametric methods for doubly robust estimation of continuous treatment effects." *Journal of the Royal Statistical Society.* Series B, Statistical methodology, **79**(4), 1229–1245. ISSN 1369-7412. doi:10.1111/rssb. 12212. URL https://www.ncbi.nlm.nih.gov/pmc/articles/PMC5627792/.
- Laan MJvd, Polley EC, Hubbard AE (2007). "Super Learner." Statistical Applications in Genetics and Molecular Biology, 6(1). ISSN 1544-6115, 2194-6302. doi:10.2202/1544-6115.1309. Publisher: De Gruyter Section: Statistical Applications in Genetics and Molecular Biology, URL https://www.degruyter.com/view/journals/sagmb/6/1/article-sagmb.2007.6.1.1309.xml.xml.
- Laan MJvd, Rose S (2011). Targeted Learning: Causal Inference for Observational and Experimental Data. Springer Series in Statistics. Springer-Verlag, New York. ISBN 978-1-4419-9781-4. doi:10.1007/978-1-4419-9782-1. URL https://www.springer.com/us/book/9781441997814.
- Laan MJvd, Rubin D (2006). "Targeted Maximum Likelihood Learning." The International Journal of Biostatistics, 2(1). ISSN 1557-4679. doi:10.2202/1557-4679.1043. Publisher: De Gruyter Section: The International Journal of Biostatistics, URL https://www.degruyter.com/view/journals/ijb/2/1/article-ijb.2006.2.1.1043.xml.xml.
- Milborrow S (2019). earth: Multivariate Adaptive Regression Splines. R package version 5.1.2, URL https://CRAN.R-project.org/package=earth.
- Muñoz ID, van der Laan M (2012). "Population intervention causal effects based on stochastic interventions." *Biometrics*, **68**(2), 541–549. ISSN 1541-0420. doi:10.1111/j.1541-0420. 2011.01685.x.

- Qin J (1998). "Inferences for Case-Control and Semiparametric Two-Sample Density Ratio Models." *Biometrika*, **85**(3), 619–630. ISSN 0006-3444. Publisher: [Oxford University Press, Biometrika Trust], URL https://www.jstor.org/stable/2337391.
- Robinson D, Hayes A (2020). broom: Convert Statistical Analysis Objects into Tidy Tibbles. R package version 0.5.6, URL https://CRAN.R-project.org/package=broom.
- Rosenbaum PR, Rubin DB (1983). "The Central Role of the Propensity Score in Observational Studies for Causal Effects." *Biometrika*, **70**(1), 41–55. ISSN 0006-3444. doi:10.2307/2335942. Publisher: [Oxford University Press, Biometrika Trust], URL https://www.jstor.org/stable/2335942.
- Rotnitzky A, Faraggi D, Schisterman E (2006). "Doubly Robust Estimation of the Area Under the Receiver-Operating Characteristic Curve in the Presence of Verification Bias." *Journal of the American Statistical Association*, **101**(475), 1276–1288. ISSN 0162-1459, 1537-274X. doi:10.1198/016214505000001339. URL http://www.tandfonline.com/doi/abs/10.1198/016214505000001339.
- Rubin D, Laan Mvd (2006). "Doubly Robust Censoring Unbiased Transformations." *U.C. Berkeley Division of Biostatistics Working Paper Series.* URL https://biostats.bepress.com/ucbbiostat/paper208.
- van der Laan M, Dudoit S (2003). "Unified Cross-Validation Methodology For Selection Among Estimators and a General Cross-Validated Adaptive Epsilon-Net Estimator: Finite Sample Oracle Inequalities and Examples." U.C. Berkeley Division of Biostatistics Working Paper Series. URL https://biostats.bepress.com/ucbbiostat/paper130.
- Wright MN, Ziegler A (2017). "ranger: A Fast Implementation of Random Forests for High Dimensional Data in C++ and R." *Journal of Statistical Software*, **77**(1), 1–17. doi: 10.18637/jss.v077.i01.
- Zheng W, van der Laan MJ (2011). "Cross-Validated Targeted Minimum-Loss-Based Estimation." In MJ van der Laan, S Rose (eds.), Targeted Learning: Causal Inference for Observational and Experimental Data, Springer Series in Statistics, pp. 459–474. Springer, New York, NY. ISBN 978-1-4419-9782-1. doi:10.1007/978-1-4419-9782-1_27. URL https://doi.org/10.1007/978-1-4419-9782-1_27.

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