

P8110 Homework Two

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Problem 1

(a)

$$\hat{t}_{0.5} = \min\{t_j : \hat{S}(t_j) < 0.5\}$$

1: identify \hat{t}_j such that $\hat{S}(t_j) < 0.5$

\hat{t}_j	$\hat{S}(t_j)$
t_6	0.0000
t_5	0.2667
t_4	0.4000

2: identify minimum $\hat{t}_j : \hat{t}_4 = 5$

$$\begin{aligned}
 95\% \text{CI} &= \text{all } t_j \text{CI} \ni 0.5 \\
 &= t_1, t_2, t_3, t_4, t_5 \\
 &= [0.4, 1.2), [1.2, 4.3), [4.3, 5.0), [5.0, 5.1), [5.1, 7.1) \\
 &= [0.4, 7.1)
 \end{aligned}$$

We estimate that 50% of patients will survive for more than 5 years. Furthermore, we are 95% confident that the true median survival time is between 0.4 and 7.1 years.

(b)

$$\begin{aligned}
 \hat{\mu}_{t_j} &= \sum_{j=1}^J \hat{S}(t_{j-1})(t_j - t_{j-1}) \\
 &= 1(0.4) + 0.9(1.2 - 0.4) + 0.8(4.3 - 1.2) + 0.6667(5.0 - 4.3) + 0.4(5.1 - 5.0) + 0.2667(7.1 - 5.1) \\
 &= 0.4 + 0.72 + 2.48 + 0.4667 + 0.04 + 0.5334 \\
 &= 4.64
 \end{aligned}$$

The estimated average survival time is 4.64 years.

(c) $\hat{\mu}_1$ will be bigger. If $\hat{\mu}_2$ is the mean survival time where all the listed points are events, then 2 more events are occurring before $\hat{\mu}_1 = (4.64)$ and thus the average survival time will decrease.