

# **STA130H1F**

## **Class #3**

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**2018-24-09**

# Welcome back to STA130



## Today's class

- Statistical data
- Tidy data
- Data wrangling

 Transforming data

- Boxplots

# Statistical data

# What is statistical data?

- Statistical data is obtained by observing (random) variables.
- A random variable can be given a precise mathematical definition that we will cover later in the course.
- In this class we will discuss examples.

# Observing a few variables on STA130 students

- What is your height?
- How many years have been at UofT?
- What is your eye colour?

Collecting this data will generate three variables: `height`, `years`, and `eye_colour`.

# Enter variables on STA130 students

```
{ height <- c()  
  years <- c()  
  eye_colour <- c()  
    c(150, 175, 146, ...)  
    vectors}
```

Put the variables into an R data frame.

NB: `data_frame` is the `tidyverse` version of base R `data.frame`.

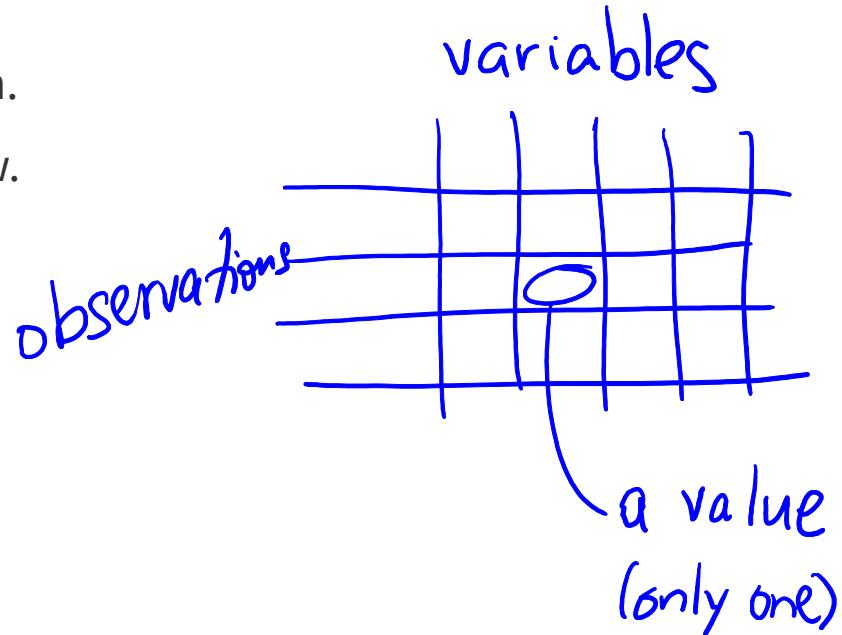
```
sta130_dat <- data_frame(height, years, eye_colour)
```

We could have entered this in a spreadsheet program like MS Excel, saved it as a CSV file, then imported the file into R.

# Tidy data

There are three interrelated rules which make a dataset tidy:

1. Each variable must have its own column.
2. Each observation must have its own row.
3. Each value must have its own cell.



# Tidy data: Eye colour example

Suppose that a first year class of 250 students has the following distribution of eye colour.

Colour	N	
Brown	105	✓
Green	55	✓
Blue	75	✓
Other	15	✓

# Tidy data: Eye colour example

Suppose that a first year class of 250 students has the following distribution of eye colour.

Colour	N
Brown	105
Green	55
Blue	75
Other	15

We can create a tidy data set with a categorical variable `eye_col`.

250 rows

	brown	green	blue	other
1	yes	no	no	no
2				
3				
:				
250				

One option :

st# eye-colour

1	brown
2	blue
3	blue
:	green
250	

second option

# Tidy data: Eye colour example

Suppose that a first year class of 250 students has the following distribution of eye colour.

Colour	N
Brown	105
Green	55
Blue	75
Other	15

*rep("Brown", 105)*

*↳ vector with "Brown" repeated 105 times*

We can create a tidy data set with a categorical variable `eye_col`.

```
library(tidyverse)
blue_eye <- rep("Brown", 105)
hazel_eye <- rep("Green", 55)
green_eye <- rep("Blue", 75)
other_eye <- rep("Other", 15)
eye_col = c(blue_eye, hazel_eye,
            green_eye, other_eye)
eye_data <- data_frame(stnum = 1:250, eye_col)
glimpse(eye_data)
```

*R code for tidy data*

# Tidy data: Eye colour

*glimpse(eye\_data)*

```
## Observations: 250  
## Variables: 2  
## $ stnum    <int> 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, ...  
## $ eye_col <chr> "Brown", "Brown", "Brown", "Brown", "Brown", "Brown", ...
```

# Tidy data

var1      var2  
cases/population

Which data set is tidy?

```
## # A tibble: 6 x 4
##   country     year   cases population
##   <chr>       <int>   <int>      <int>
## 1 Afghanistan 1999    745  19987071
## 2 Afghanistan 2000   2666  20595360
## 3 Brazil       1999  37737 172006362
## 4 Brazil       2000  80488 174504898
## 5 China        1999 212258 1272915272
## 6 China        2000 213766 1280428583
```

```
## # A tibble: 6 x 3
##   country     year   rate
##   <chr>       <int> <chr>
## 1 Afghanistan 1999 745/19987071
## 2 Afghanistan 2000 2666/20595360
## 3 Brazil       1999 37737/172006362
## 4 Brazil       2000 80488/174504898
## 5 China        1999 212258/1272915272
## 6 China        2000 213766/1280428583
```

each cell contains one piece of information.

2 pieces of information

# Tidy data

"For a given dataset, it is usually easy to figure out what are observations and what are variables, but it is surprisingly difficult to precisely define variables and observations in general." (Wickham, 2014)

A general rule of thumb:

- It is easier to describe functional relationships between variables (e.g., z is a linear combination of x and y, density is the ratio of weight to volume) than between rows.
- It is easier to make comparisons between groups of observations (e.g., average of group a vs. average of group b) than between groups of columns.

(Wickham, 2014)

# Data Wrangling

# Data wrangling

- The `ggplot` library implements a grammar of graphics.
  - Similarly the `dplyr` library presents a **grammar for data wrangling**.
- both included in tidyverse*

# The Economic Guide to Picking a Major

**FiveThirtyEight**

Politics   Sports   Science & Health   **Economics**   Culture

SEP. 12, 2014 AT 7:37 AM

## The Economic Guide To Picking A College Major

By [Ben Casselman](#)

Filed under [Higher Education](#)

Get the data on [GitHub](#)



Students walk across the campus of UCLA in Los Angeles. KEVORK DJANSEZIAN / GETTY IMAGES

"...A college degree is no guarantee of economic success. But through their choice of major, they can take at least some steps toward boosting their odds."

# The Economic Guide to Picking a Major

- The data used in the article is from the American Community Survey 2010-2012 Public Use Microdata Series.
- We can use the fivethirtyeight library in R.

`library(fivethirtyeight)`

# Data behind the article

```
→ library(fivethirtyeight) # load the library  
→ glimpse(college_recent_grads)
```

```
## Observations: 173 # of rows  
## Variables: 21 # of columns  
## $ rank  
## $ major_code  
## $ major  
## $ major_category  
## $ total  
## $ sample_size  
## $ men  
## $ women  
## $ sharewomen  
## $ employed  
## $ employed_fulltime  
## $ employed_parttime  
## $ employed_fulltime_yearround  
## $ unemployed  
## $ unemployment_rate  
## $ p25th  
## $ median  
## $ p75th
```

<int>	1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11,...
<int>	2419, 2416, 2415, 2417, 2405, 2418...
<chr>	"Petroleum Engineering", "Mining A..."
<chr>	"Engineering", "Engineering", "Eng..."
<int>	2339, 756, 856, 1258, 32260, 2573,...
<int>	36, 7, 3, 16, 289, 17, 51, 10, 102...
<int>	2057, 679, 725, 1123, 21239, 2200,...
<int>	282, 77, 131, 135, 11021, 373, 166...
<dbl>	0.1205643, 0.1018519, 0.1530374, 0...
<int>	1976, 640, 648, 758, 25694, 1857, ...
<int>	1849, 556, 558, 1069, 23170, 2038,...
<int>	270, 170, 133, 150, 5180, 264, 296...
<int>	1207, 388, 340, 692, 16697, 1449, ...
<int>	37, 85, 16, 40, 1672, 400, 308, 33...
<dbl>	0.018380527, 0.117241379, 0.024096...
<dbl>	95000, 55000, 50000, 43000, 50000, ...
<dbl>	110000, 75000, 73000, 70000, 65000...
<dbl>	125000, 90000, 105000, 80000, 75000...

# Select variables/columns using

`select()` → used to view only certain columns in a dataset

To retrieve a data frame with only major, number of male and female graduates we use the `select()` function in the `dplyr` library.

```
select(college_recent_grads, major, men, women)
## # A tibble: 173 x 3
##   major
##   <chr>
## 1 Petroleum Engineering
## 2 Mining And Mineral Engineering
## 3 Metallurgical Engineering
## 4 Naval Architecture And Marine Engineering
## 5 Chemical Engineering
## 6 Nuclear Engineering
## 7 Actuarial Science
## 8 Astronomy And Astrophysics
## 9 Mechanical Engineering
## 10 Electrical Engineering
## # ... with 163 more rows
## # ... with 3 variables: men <int>, women <int>, and 1 other
```

*dataframe*

*columns we want to keep*

major	men	women
Petroleum Engineering	2057	282
Mining And Mineral Engineering	679	77
Metallurgical Engineering	725	131
Naval Architecture And Marine Engineering	1123	135
Chemical Engineering	21239	11021
Nuclear Engineering	2200	373
Actuarial Science	2110	1667
Astronomy And Astrophysics	832	960
Mechanical Engineering	80320	10907
Electrical Engineering	65511	16016

# Select observations/rows using filter() → used to view certain rows only

If we want to retrieve only those observations (rows) that pertain to engineering majors then we need to specify that the value of the major variable is Electrical Engineering.

data

```
# == is a test for equality and is different than !=.  
EE <- filter(college_recent_grads,  
              major == "Electrical Engineering")  
glimpse(EE)
```

```
## Observations: 1  
## Variables: 21  
## $ rank                      <int> 10  
## $ major_code                 <int> 2408  
## $ major                      <chr> "Electrical Engineering"  
## $ major_category             <chr> "Engineering"  
## $ total                      <int> 81527  
## $ sample_size                <int> 631  
## $ men                        <int> 65511  
## $ women                      <int> 16016  
## $ sharewomen                 <dbl> 0.1964503  
## $ employed                   <int> 61928
```

# Combine select() and filter()

- We can drill down to get certain pieces of information using filter() and select() together.
- The median variable is median salary.

```
select(filter(college_recent_grads, median >= 60000),  
       major, men, women)
```

*these three variables*

*only majors with median  
salary of at least  
60k*

(1) Which students, and (2) which variables are in this data frame?

Respond at PollEv.com/loop  Text LOOP to (780) 800-5606 once to join, then A, B, C, D, or E

(1) All students in the original data set; (2) all variables in the original data set

A

(1) All students in the original data set in a major where the median salary is at least \$60,000; (2) all variables in the data set

B

(1) All students in the original data set in a major where the median salary is at least \$60,000; (2) three variables: major, men, women

C

(1) All students in the original data set in a major where the median salary is at most \$60,000; (2) all variables in the original data set

D

(1) All students in the original data set in a major where the median salary is at most \$60,000; (2) three variables: major, men, women

E

Total Results: 0

# The pipe operator %>%

pipe

In the code:

```
select(filter(college_recent_grads, median >= 60000),  
      major, men, women)
```

} previous slide

filter is nested inside select.

The pipe operator allows is an alternative to nesting and yields easier to read code.

The same expression can be written with the pipe operator

```
[ college_recent_grads %>%  
  filter(median >= 60000) %>%  
  select(major, men, women)
```

first keep only rows for  
majors with med.  
income >= 60k

} with piping.

↳ next we keep only these  
3 variables

# Create new variables from existing variables using mutate()

What percentage of graduates from each major where the median earnings is at least \$60,000 are men ?

✓ data

```
college_recent_grads %>%  
  filter(median >= 60000) %>% → only keep majors w income ≥ 60k  
  select(major, men, women) %>% → only keep these 3 variables  
  mutate(total = men + women,  
        pct_male = round((men / total)*100, 2))
```

Compare to nested code:

↳ 5 variables: major, men, women, total, pct\_male

```
mutate(select(filter(college_recent_grads, median >= 60000),  
          major, men, women),  
      total = men + women,  
      pct_male = round((men / total)*100, 2))
```

||

# Create new variables from existing variables using mutate()

```
knitr::kable(college_recent_grads %>%  
  filter(median >= 60000) %>%  
  select(major, men, women) %>%  
  mutate(total = men + women,  
         pct_male = round((men / total)*100, 2)),  
  format = "html")
```

} from prev. slide  
new vars.

major	men	women	total	pct_male
Petroleum Engineering	2057	282	2339	87.94
Mining And Mineral Engineering	679	77	756	89.81
Metallurgical Engineering	725	131	856	84.70
Naval Architecture And Marine Engineering	1123	135	1258	89.27
Chemical Engineering	21239	11021	32260	65.84
Nuclear Engineering	2200	373	2573	85.50

# Create new variables from existing variables using `mutate()` and `ifelse()`

- Suppose that we would like to create a categorical variable to identify majors with between 45% and 55% women (ie., approximately equal numbers of males and females).
- We can use `ifelse()` in a `mutate()` statement.

The format of an `ifelse()` statement in R is: `ifelse(test, yes, no)`

logical: T/F  
↗

# Create new variables from existing variables using `mutate()` and `ifelse()`

- Suppose that we would like to create a categorical variable to identify majors with between 45% and 55% women (ie., approximately equal numbers of males and females).
- We can use `ifelse()` in a `mutate()` statement.

The format of an `ifelse()` statement in R is: `ifelse(test, yes, no)`

```
people <- c("Don", "Lei", "Francois", "Fanny")
ifelse(people == "Lei" | people == "Fanny", "Female", "Male")
```

female OR female

test

$\hookrightarrow c(FALSE, TRUE, FALSE, TRUE)$

$\rightarrow c('Male', 'Female', 'Male', 'Female')$

# Create new variables from existing variables using `mutate()` and `ifelse()`

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- We can use `ifelse()` in a `mutate()` statement.

The format of an `ifelse()` statement in R is: `ifelse(test, yes, no)`

```
people <- c("Don", "Lei", "Francois", "Fanny")
ifelse(people == "Lei" | people == "Fanny", "Female", "Male")
```

```
## [1] "Male"    "Female"   "Male"    "Female"
```

```

college_recent_grads %>%
  select(major, men, women) %>%
  mutate(total = men + women,
        pct_female = round((women / total)*100, 1),
        sex.equal = ifelse(pct_female >= 45 & pct_female <= 55,
                           yes="Yes", no="No")) %>%
  select(major, sex.equal)

```

COPY into  
R

	sex.equal
	<chr>
## 1 Petroleum Engineering	Yes <b>No</b>
## 2 Mining And Mineral Engineering	Yes <b>No</b>
## 3 Metallurgical Engineering	Yes :
## 4 Naval Architecture And Marine Engineering	Yes <b>wrong.</b>
## 5 Chemical Engineering	Yes
## 6 Nuclear Engineering	Yes <b>NO</b>
## 7 Actuarial Science	Yes <b>NO</b>
## 8 Astronomy And Astrophysics	Yes <b>YES</b>
## 9 Mechanical Engineering	Yes <b>NO.</b>
## 10 Electrical Engineering	Yes <b>R</b>
## # ... with 163 more rows	

# Rename variables using rename()

- It's considered bad practice in R to use periods in variable names.
- We can use `rename()` to change the name of sex.equal to sex\_equal.

*same as before*

```
my_college_dat <- college_recent_grads %>%  
  select(major, men, women, median) %>%  
  mutate(total = men + women,  
         pct_female = round((women / total)*100, 2),  
         sex.equal = ifelse(pct_female >= 45 &  
                             pct_female <= 55, yes="Yes", no="No")) %>%  
  select(major, sex.equal, median)
```

```
my_college_dat <- my_college_dat %>%  
  rename(sex_equal = sex.equal, salary_median = median)  
glimpse(my_college_dat)
```

*new name*

*old name*

*new*

```
## Observations: 173  
## Variables: 3  
## $ major          <chr> "Petroleum Engineering", "Mining And Mineral Eng..."  
## $ sex_equal      <chr> "No", "No", "No", "No", "No", "No", "Yes", ...  
## $ salary_median <dbl> 110000, 75000, 73000, 70000, 65000, 65000, 62000...
```

# Sort a data frame using arrange()

↳ used to sort the rows in dataframe

```
my_college_dat %>%  
  select(major, salary_median) %>%  
  arrange(desc(salary_median))
```

↳ descending order

```
## # A tibble: 173 x 2  
##   major           salary_median  
##   <chr>          <dbl>  
## 1 Petroleum Engineering      110000  
## 2 Mining And Mineral Engineering 75000  
## 3 Metallurgical Engineering    73000  
## 4 Naval Architecture And Marine Engineering 70000  
## 5 Chemical Engineering       65000  
## 6 Nuclear Engineering        65000  
## 7 Actuarial Science          62000  
## 8 Astronomy And Astrophysics 62000  
## 9 Mechanical Engineering     60000  
## 10 Electrical Engineering    60000  
## # ... with 163 more rows
```

# Summarize a data frame using summarize()

The average number of female grads and the total number of majors in the data set.

```
college_recent_grads %>%  
  select(major, men, women) %>%  
  summarise(femgrad_mean = mean(women, na.rm = T), N = n())  
  
## # A tibble: 1 x 2  
##   femgrad_mean     N  
##       <dbl> <int>  
## 1      22647.    173
```

mean & of women  
grads in each major

exclude NAs from  
calculation.

total # of majors

# Summarize groups in a data frame using `summarize()` and `group_by()`

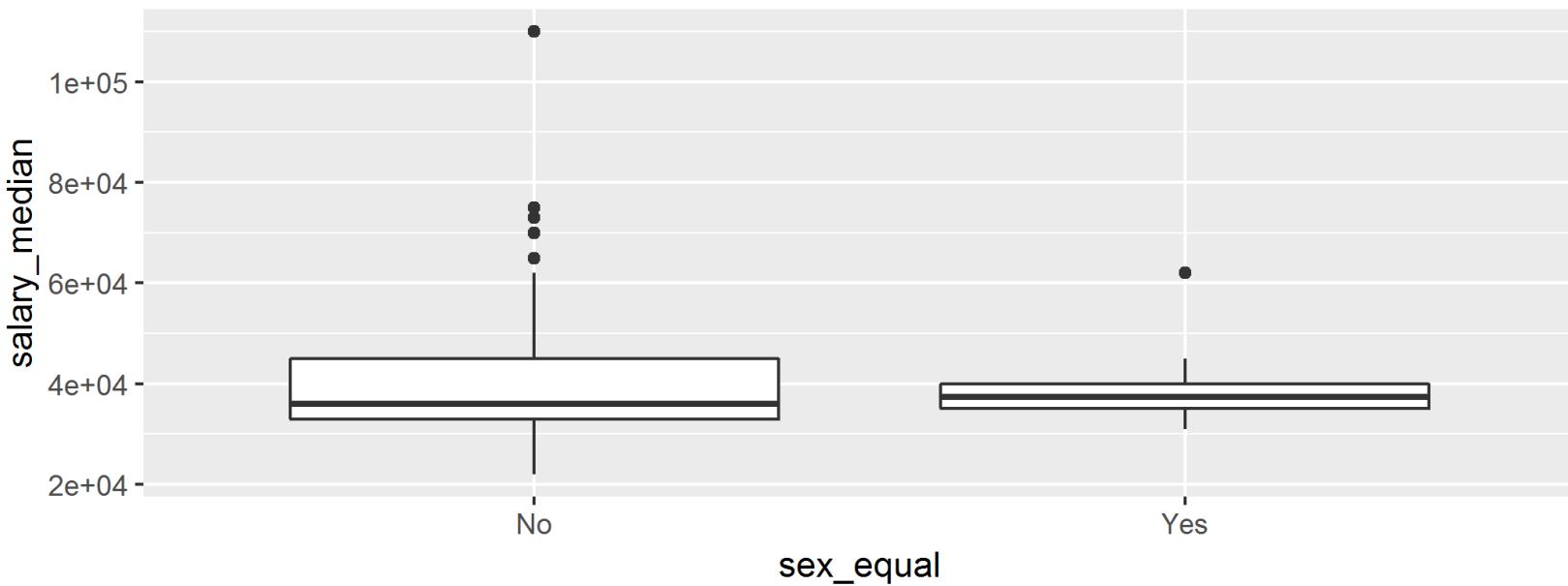
The median salary in majors with 45%-55% female students.

```
my_college_dat %>%  
  group_by(sex_equal) %>%  
  summarise(median(salary_median))
```

```
## # A tibble: 3 x 2  
##   sex_equal `median(salary_median)`  
##   <chr>          <dbl>  
## 1 No            36000  
## 2 Yes           37400  
## 3 <NA>          53000
```

# Boxplots to compare distribution of salary in majors with balanced vs unbalanced sex distributions

```
my_college_dat %>% filter(is.na(sex_equal) == FALSE) %>%
  ggplot(aes(x = sex_equal, y = salary_median)) + geom_boxplot()
```



# What is a boxplot?

# What is a boxplot?

A boxplot summarizes the distribution of a quantitative (numerical) variable using five statistics, while also plotting unusual observations (outliers)

The elements of a boxplot are:

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The elements of a boxplot are:

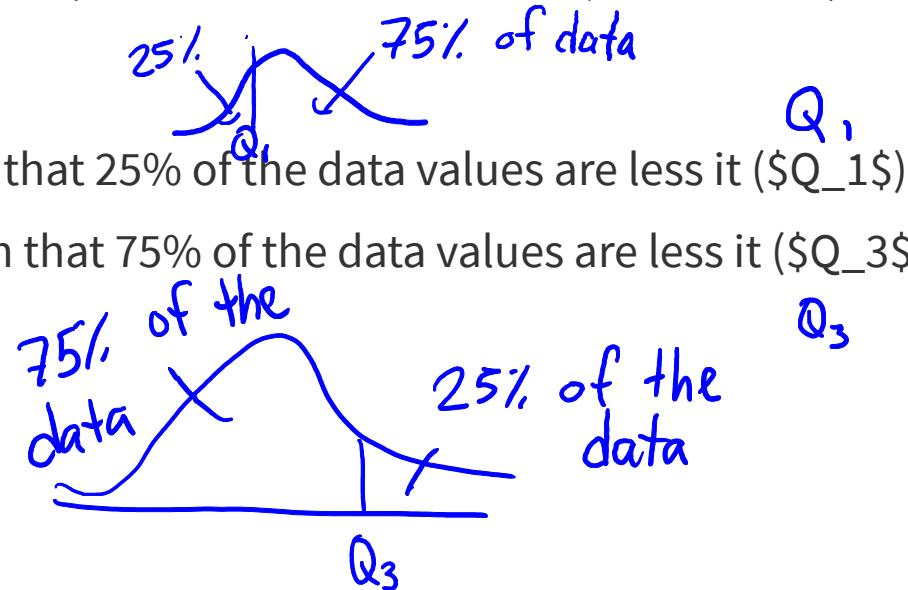
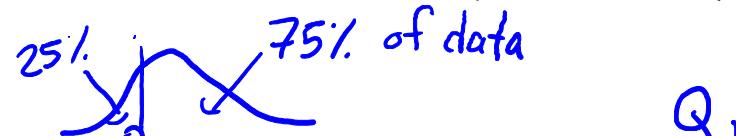
- Line in the middle of the box:
  - **median**: middle data value (50% of data values above, 50% below)

# What is a boxplot?

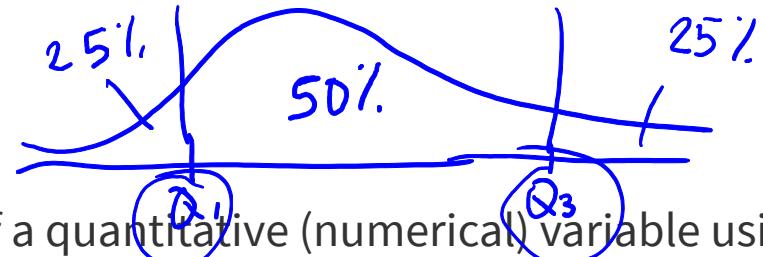
A boxplot summarizes the distribution of a quantitative (numerical) variable using five statistics, while also plotting unusual observations (outliers)

The elements of a boxplot are:

- Line in the middle of the box:
  - **median**: middle data value (50% of data values above, 50% below)
- Edges of the box:
  - **1st quartile**: value such that 25% of the data values are less it ( $Q_1$ )
  - **3rd quartile** - value such that 75% of the data values are less it ( $Q_3$ )

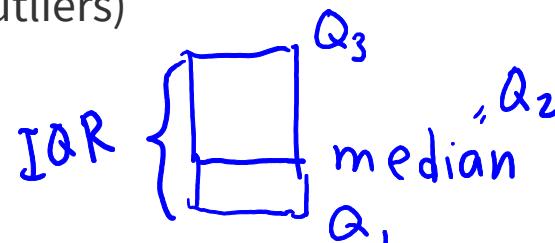


# What is a boxplot?



A boxplot summarizes the distribution of a quantitative (numerical) variable using five statistics, while also plotting unusual observations (outliers)

The elements of a boxplot are:



- Line in the middle of the box:
  - **median**: middle data value (50% of data values above, 50% below)
- Edges of the box:
  - **1st quartile**: value such that 25% of the data values are less than it ( $Q_1$ )
  - **3rd quartile** - value such that 75% of the data values are less than it ( $Q_3$ )
- Length of the box is the Interquartile Range (IQR) = 3rd quartile - 1st quartile
  - gives an indication of how spread out the data are  $Q_3 - Q_1$

# What is a boxplot?

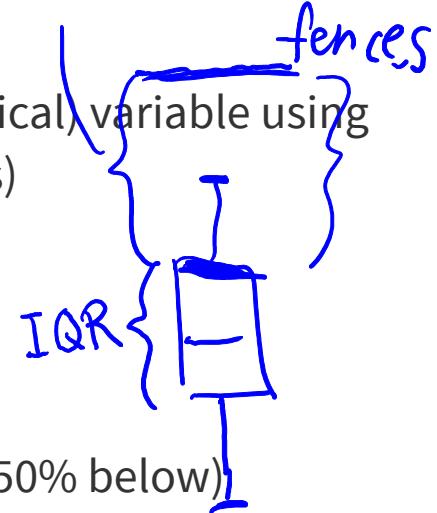
$$Q_3 + 1.5 \text{ IQR}$$

$$Q_3 + 1.5 \text{ IQR}$$

A boxplot summarizes the distribution of a quantitative (numerical) variable using five statistics, while also plotting unusual observations (outliers)

The elements of a boxplot are:

- Line in the middle of the box:
  - **median**: middle data value (50% of data values above, 50% below)
- Edges of the box:
  - **1st quartile**: value such that 25% of the data values are less it ( $Q_1$ )
  - **3rd quartile** - value such that 75% of the data values are less it ( $Q_3$ )
- Length of the box is the Interquartile Range (IQR) = 3rd quartile - 1st quartile
  - gives an indication of how spread out the data are
- Whiskers on the box extend to the most extreme value that is outside of the box but within  $1.5 \times \text{IQR}$ 
  - whiskers can't go beyond the fences*



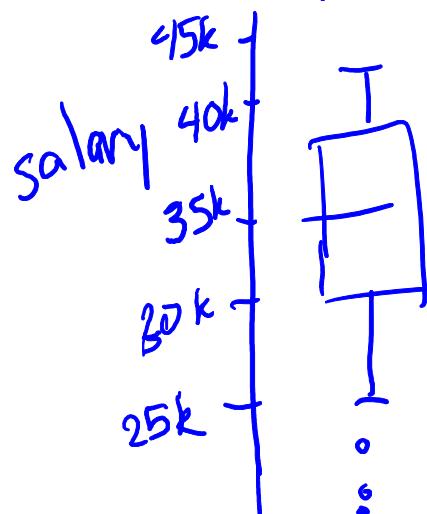
# Outliers – unusual values

An outlier is a value which is beyond the whiskers, that is either

- less than  $Q_1 - 1.5 \times IQR$  OR
- more than  $Q_3 + 1.5 \times IQR$

The whiskers of the boxplot capture data which is outside the box, but not beyond  $1.5 \times IQR$  on either side

↳ outliers are represented on the plot with dots



# Example

x

*n=10*

```
## [1] 0.14 0.15 0.15 0.44 0.54 0.76 0.96 1.18 1.23 2.89
```

# Example

x

```
## [1] 0.14 0.15 0.15 0.44 0.54 0.76 0.96 1.18 1.23 2.89
```

quantile(x, 0.25)

```
## 25%  
## 0.2225
```

$Q_1$

quantile(x, 0.50)

```
## 50%  
## 0.65
```

$Q_2$  = median

quantile(x, 0.75)

```
## 75%  
## 1.125
```

$Q_3$

quantile(x, 0.75) -  
quantile(x, 0.25)

```
## 75%  
## 0.9025
```

$IQR = Q_3 - Q_1$

# Example

x

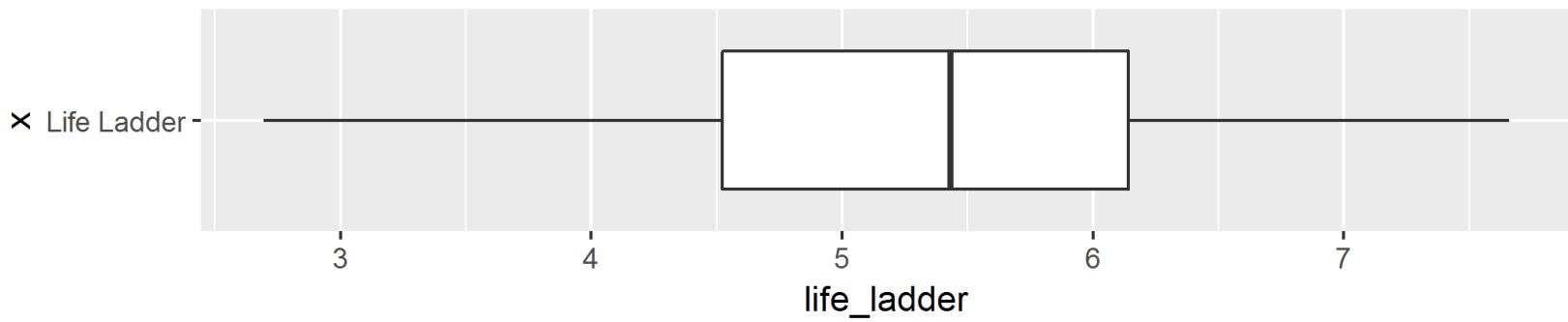
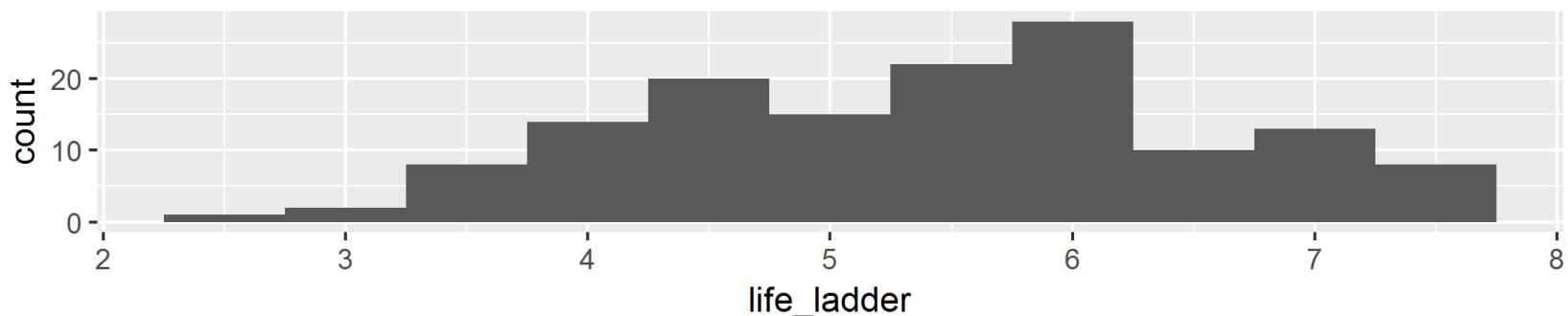
```
## [1] 0.14 0.15 0.15 0.44 0.54 0.76 0.96 1.18 1.23 2.89
```

```
data_frame(x) %>%
  ggplot(aes(x = "", y = x)) +
  geom_boxplot()
```

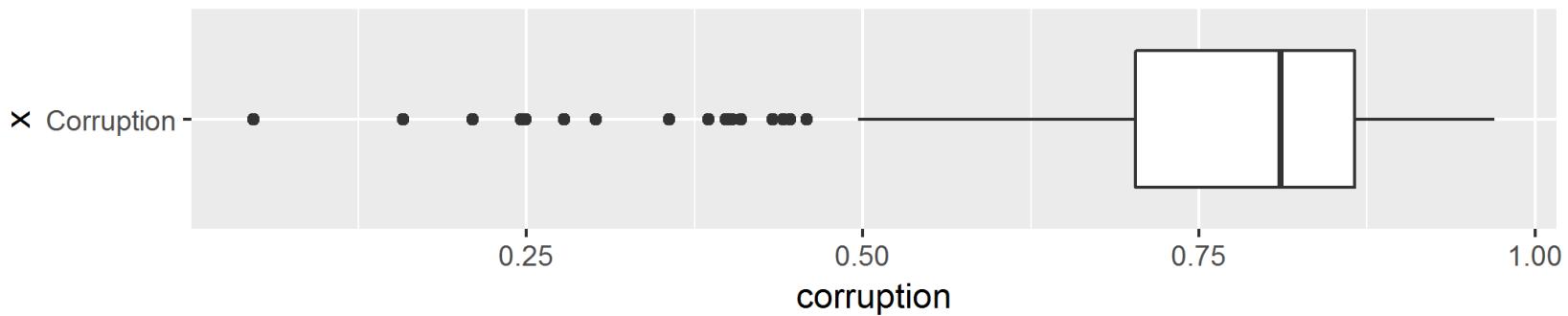
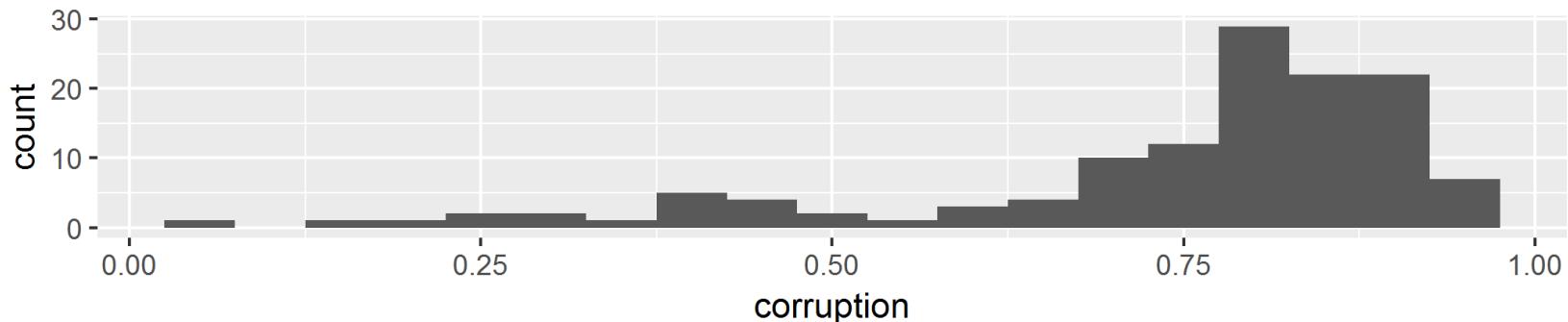
in ggplot4



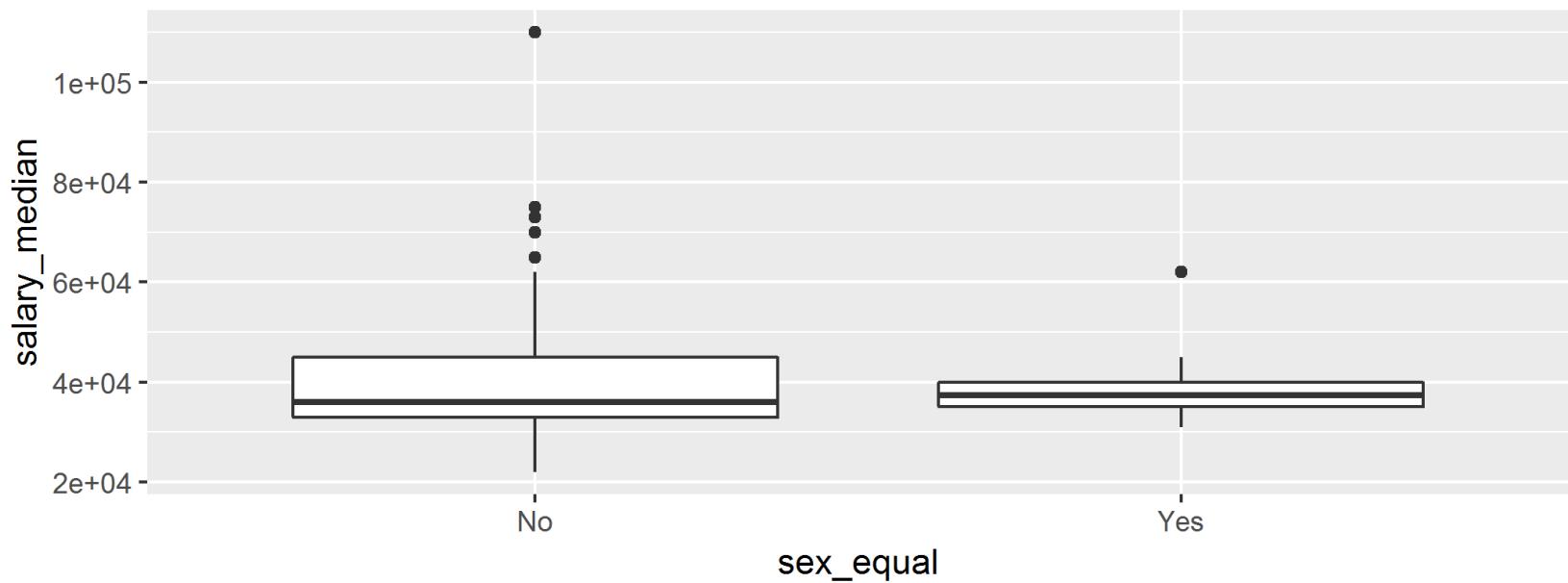
# Example: Histogram vs boxplot



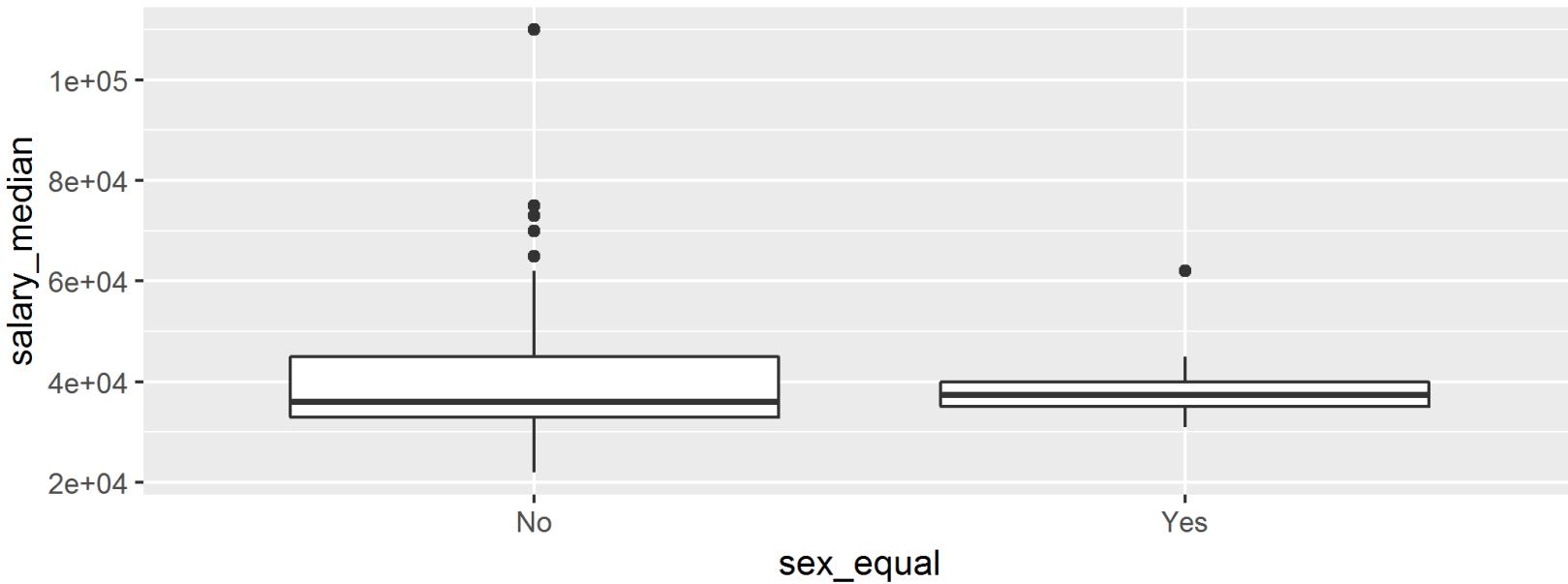
# Example: Histogram vs boxplot



# Back to the salary example...



# Back to the salary example...



- Similar medians? ↗ Yes

- Range / variability?

↳ look at the height of the boxes

↳ whiskers and outliers

variability is different across the two levels of sex-equals

# Boxplots to compare distribution of salary in majors with mostly men vs mostly women vs balanced

