Strudel: Algorithmic Patterns for the Web

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2022-12-14

ABSTRACT

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1 Introduction

This paper introduces Strudel, which began as an alternative implementation of the TidalCycles (or 'Tidal' for short) live coding system, using the JavaScript programming language.

The first tentative commit to the Strudel project was on 22nd January 2022 by Alex McLean, with the core representation implemented over the following few days. Although this was his first attempt at a JavaScript-based application, by 27th January, Alex had managed to upload the initial version to the 'npm' javascript package database, sharing with the wider community for comment. By 4th February, Felix Roos had discovered Strudel and contributed a 'REPL' user interface to it, and then contributed a scheduler the next day, so that Strudel could already make sound. At this point, Alex shared ownership to the repository with Felix, and the project has since proved to be a productive confluence of Felix's own work into music representation and visualisation, with Alex's experience with making Tidal. Felix has since become the primary contributor to Strudel, with Alex continuing to jump between developing both Strudel and Tidal. Aspects of Strudel's development has therefore fed back into TidalCycles, and both systems have maintained a shared conceptual underpinning. We plan to continue working towards feature parity between these systems, although within the syntactical trade-offs and library ecosystems of JavaScript and Haskell, some divergence is inevitable and healthy.

Over the first year of its life, Strudel is now a fully-fledged live coding environment, porting Tidal's core represention of patterns, pattern transformations, and mininotation for polymetric sequences, combined with a wealth of features for synthesising and visualising those patterns. Strudel can run entirely in the browser, opening Tidal's algorithmic patterns (Mclean 2020) up to modern audio/visual web technologies.

The main interface for Strudel is its REPL[^REPL stands for read, evaluate, print/play, loop. It is friendly jargon for an interactive programming interface from computing heritage, usually for a commandline interface but also applied to live coding editors.], a live code editor dedicated to manipulating Strudel patterns while they play. The REPL features built-in visual feedback, which highlights which elements in the patterned (mini-notation) sequences are influencing the event that is currently being played. While Strudel is written in JavaScript, as an end-user code interface the REPL is optimised for simplicity and readability by applying code transformations on the syntax tree level, allowing language operations that would otherwise be impossible.

Strudel supports several diferent options to directly output sound through the browser including a custom Web Audio Output, CSound and Tone.js, It also supports methods for triggering external software and hardware, including via OSC (Open Sound Control) messages (e.g. for use with Tidal's traditional SuperDirt synthesiser), Web Serial (so far used to work with dancing robot) and Web MIDI (for e.g. controlling synthesiser hardware or a digital audio workstation).

Strudel is split into multiple packages, allowing granular reuse in other applications. This allows Strudel to be embedded in other web-based live coding environments such as Gibber and Hydra, opening up these systems to use with the mini-notation for sequences. Apart from TidalCycles, Strudel draws inspiration from many prior existing projects like TidalVortex (McLean et al. 2022), Gibber (Roberts and Kuchera-morin 2012), Estuary (Ogborn et al. 2017), Hydra (Jack [2022] 2022), Ocarina (Solomon [2021] 2022) and Feedforward (McLean 2020).

2 From Tidal to Strudel and back

As mentioned above, the original Tidal is implemented as a domain specific language (DSL) embedded in the Haskell pure functional programming language, and takes advantage of Haskell's terse syntax and advanced, 'strong' type system. Javascript on the other hand, is a multi-paradigm programming language, with a dynamic type system. Because Tidal leans heavily on many of Haskell's more unique features, it was not always clear that it could meaningfully be ported to a multi-paradigm scripting language. However, this possibility was already demonstrated with an earlier port to Python [TidalVortex; McLean et al. (2022)], and we have now successfully implemented Tidal's pure functional representation of patterns in Strudel, including partial application, currying, and the functor, applicative and monadic structures that underlie Tidal's expressive pattern transformations. The result is a terse and highly composable system, where everything is either a pattern, or a function for combining and manipulating patterns, offering a rich creative ground for exploration.

This development process has been far from a one-way port, however. The process of porting Tidal's concepts has also opened up new possibilities, some just from revisiting every design decision, and some from the particular affordances and constraints offered by Javascript. This has lead to new features (and indeed bugfixes) that have found their way back to Tidal where appropriate, and ongoing work that we will return to in the conclusion of this paper.

3 Representing Patterns

Patterns are the essence of Tidal. Its patterns are abstract entities that represent flows of time as functions, adapting a technique called pure functional reactive programming. Taking a time span as its input, a Pattern can output a set of events that happen within that time span. It depends on the structure of the Pattern how the events are located in time. From now on, this process of generating events from a time span will be called **querying**. Example:

```
const pattern = sequence(c3, [e3, g3])
const events = pattern.queryArc(0, 1)
console.log(events.map(e => e.show()))
```

In this example, we create a pattern using the sequence function and **query** it for the time span from 0 to 1. Those numbers represent units of time called **cycles**. The length of one cycle depends on the tempo, which defaults to one cycle per second. The resulting events are:

```
[{ value: 'c3', begin: 0, end: 1/2 },
{ value: 'e3', begin: 1/2, end: 3/4 },
{ value: 'g3', begin: 3/4, end: 1 }]
```

Each event has a value, a begin time and an end time, where time is represented as a fraction. In the above case, the events are placed in sequential order, where c3 takes the first half, and e3 and g3 together take the second half. This temporal placement is the result of the sequence function, which divides its arguments equally over one cycle. If an argument is an array, the same rule applies to that part of the cycle. In the example, e3 and g3 are divided equally over the second half of the whole cycle.

The above examples do not represent how Strudel is used in practice. In the REPL, the user only has to type in the pattern itself, the querying will be handled by the scheduler. The scheduler will repeatedly query the pattern for events, which then are then scheduled as sound synthesis or other event triggers. Also, the above event data structure has been simplified for readability.

4 Making Patterns

In practice then, the end-user live coder will not deal with constructing patterns directly, but will rather build patterns using Strudel's extensive combinator library to create, combine and transform patterns.

The live coder will rarely use the sequence function as seen above, as sequencing is implicit in many functions. For example in the following, the note function constructs a pattern of notes, sequencing its arguments in the same manner as the previous example.
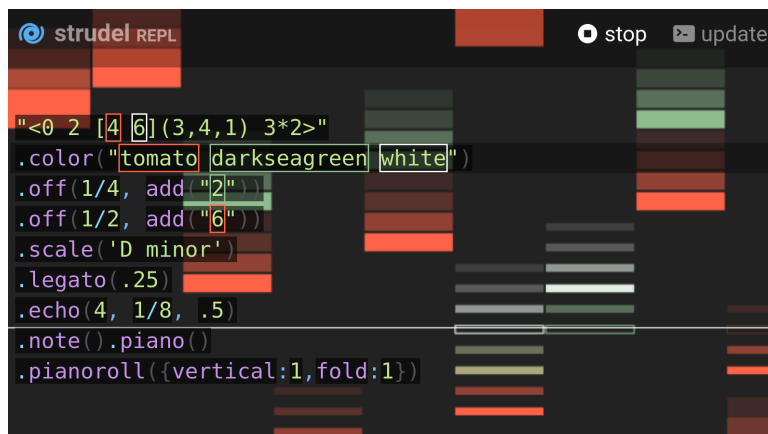
```
note(c3, [e3, g3])
```

Figure 1: Screenshot of the Strudel editor, including piano-roll visualisation.

Perhaps more often, they will use the mini-notation for even terser notation of rhythmic sequences: [ˆThis last example is also valid Tidal code, albeit the parenthesis is not required in its Haskell syntax in this case. Tidal does not support passing sequences as lists directly to the note function, however.].

```
note("c3 [e3 g3]")
```

Such sequences are often treated only a starting point for manipulation, where they then undergo pattern transformations such as repetition, symmetry, interference/combination or randomisation, potentially at multiple timescales. Because Strudel patterns are represented as pure functions of time rather than as data structures, very long and complex generative results can be represented and manipulated without having to store the resulting sequences in memory.

5 Pattern Example

The following example showcases how patterns can be utilized to create musical complexity from simple parts, using repetition and interference:

```
"<0 2 [4 6](3,4,1) 3>"
.off(1/4, add(2))
.off(1/2, add(6))
.scale('D minor')
.legato(.25)
.note().s("sawtooth square")
.delay(.8).delaytime(.125)
```

The pattern starts with a rhythm of numbers in mini notation, which are later interpreted inside the scale of D minor. This line could also be expressed without mini notation:

```
cat(0, 2, [4, 6].euclid(3, 4, 1), 3)
```

These numbers then undergo various pattern transformations. Here is a short description of all the functions used:

- cat: play elements sequentially, where each lasts one cycle
- brackets: elements inside brackets are divided equally over the time of their parent
- .euclid(p, s, o): place p pulses evenly over s steps, with offset o (Toussaint 2005)
- .off(n, f): layers a pattern on top of itself, with the new layer offset by n cycles, and with function f aplpied
- .legato(n): multiply the duration of all events in a pattern by a factor of n
- .echo(t, n, v): copy each event t times, with n cycles in between each copy, decreasing velocity by v
- .note()) interpretes values as notes
- .s(name): play back each event with the given sound
- .delay(wet): add delay
- .delaytime(t): set delay time

Much of the above will be familiar to Tidal users.

6 Ways to make Sound (and other events)

To generate sound, Strudel supports bindings for different outputs:

- Tone.js (deprecated)
- Web Audio API
- WebDirt, a js recreation of Tidal's *Dirt* sample engine (deprecated)
- OSC via osc-js, compatible with superdirt
- Csound via the Csound WebAssembly build
- MIDI via WebMIDI
- Serial via WebSerial

At first, we used Tone.js as sound output, but it proved to be limited for the use case of Strudel, where each individual event could potentially have a completely different audio graph. While the Web Audio API takes a *fire-and-forget* approach, creating a lot of Tone.js instruments and effects causes performance issues quickly. For that reason, we chose to search for alternatives.

Strudel's new default output uses the Web Audio API to create a new audio graph for each event. It currently supports basic oscillators, sample playback, various effects and an experimental support for soundfonts.

WebDirt (Ogborn [2016] 2022) was created as part of the Estuary Live Coding System (Ogborn et al. 2017), and proved to be a solid choice for handling samples in Strudel as well. We are however focused on working more directly with the Web Audio API to be able to integrate new features more tightly.

Using the OSC protocol via Strudel's provided Node.js-based OSC proxy server, it is possible to send network messages to trigger events. This is mainly used to render sound using SuperDirt (*SuperDirt* [2015] 2022), which is the well-developed Supercollider-based synthesis framework that Tidal live coders generally use as standard.

Recently, the experimental integration of Csound proved to bring a new dimension of sound design capabilities to Strudel. Thanks to the WebAssembly distribution of this classic system (**CsoundWebAssembly?**), csound 'orchestra' synthesisers can be embedded in and then patterned with Strudel code.

MIDI output can also be used to send MIDI messages to either external instruments or to other programs on the same device. Unlike OSC, Strudel is able to send MIDI directly without requiring additional proxy software, but only from web browsers that support it (at the time of writing, this means Chromium-based browsers).

Finally, Strudel supports Serial output, for example to trigger events via microcontrollers. This has already been explored for robot choreography by Kate Sicchio and Alex McLean, via a performance presented at the International Conference on Live Interfaces 2022.

7 The Strudel REPL

While Strudel can be used as a library in any JavaScript codebase, its reference implementation is the Strudel REPL, which is a browser-based live coding environment. Besides a basic UI for playback control and meta information, the main part of the interface is the code editor powered by CodeMirror. In it, the user can edit and evaluate pattern code live, using one of the outputs to create music and or sound art. The control flow of the REPL follows 3 basic steps:

1. The user writes and updates `Code`. Each update transpiles and evaluates the code to create a `Pattern` instance
2. While the REPL is running, the `Scheduler` queries the active `Pattern` by a regular interval, generating `Events` (also called `Haps` in Strudel) for the next time span.
3. For each scheduling tick, all generated `Events` are triggered by calling their `onTrigger` method, which is set by the output.

7.1 1. User Code

To create a `Pattern` from the user code, two steps are needed:

1. Transpile the JS input code to make it functional
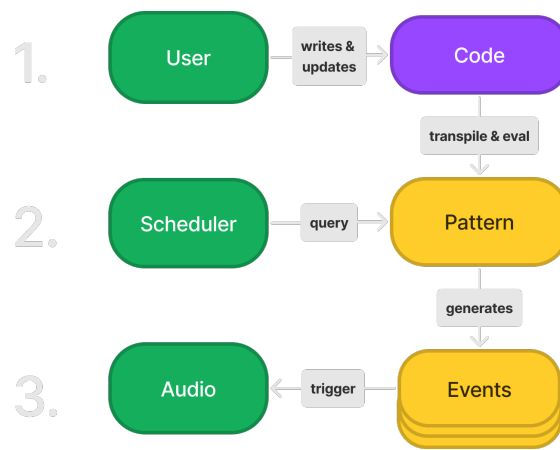2. Evaluate the transpiled code

Figure 2: repl control flow

7.1.1 Transpilation & Evaluation

In the JavaScript world, using transpilation is a common practise to be able to use language features that are not supported by the base language. Tools like `babel` will transpile code that contains unsupported language features into a version of the code without those features.

In the same tradition, Strudel can add a transpilation step to simplify the user code in the context of live coding. For example, the Strudel REPL lets the user create mini notation patterns using just double quoted strings, while single quoted strings remain what they are:

```
"c3 [e3 g3]*2"
```

is transpiled to:

```
mini("c3 [e3 g3]*2").withMiniLocation([1,0,0],[1,14,14])
```

Here, the string is wrapped in `mini`, which will create a pattern from a mini notation string. Additionally, the `withMiniLocation` method passes the original source code location of the string to the pattern, which enables highlighting active events.

Other convenient features like pseudo variables, operator overloading and top level await are possible with transpilation.

After the transpilation, the code is ready to be evaluated into a `Pattern`.

Behind the scenes, the user code string is parsed with `acorn`, turning it into an Abstract Syntax Tree (AST). The AST allows changing the structure of the code before generating the transpiled version using `escodegen`.

7.1.2 Mini Notation

While the transpilation allows JavaScript to express Patterns in a less verbose way, it is still preferable to use the Mini Notation as a more compact way to express rhythm. Strudel aims to provide the same Mini Notation features and syntax as used in Tidal.

The Mini Notation parser is implemented using peggy, which allows generating performant parsers for Domain Specific Languages (DSLs) using a concise grammar notation. The generated parser turns the Mini Notation string into an AST which is used to call the respective Strudel functions with the given structure. For example, `"c3 [e3 g3]*2"` will result in the following calls:

```
seq(
  reify('c3').withLocation([1,1,1], [1,4,4]),
  seq(
    reify('e3').withLocation([1,5,5], [1,8,8]),
    reify('g3').withLocation([1,8,8], [1,10,10]),
  ).fast(2)
)
```

7.1.3 Highlighting Locations

As seen in the examples above, both the JS and the Mini Notation parser add source code locations using `withMiniLocation` and `withLocation` methods. While the JS parser adds locations relative to the user code as a whole, the Mini Notation adds locations relative to the position of the mini notation string. The absolute location of elements within Mini Notation can be calculated by simply adding both locations together. This absolute location can be used to highlight active events in real time.

7.2 2. Scheduling Events

After an instance of `Pattern` is obtained from the user code, it is used by the scheduler to get queried for events. Once started, the scheduler runs at a fixed interval to query active pattern for events withing the current interval's time span. A simplified implementation looks like this:

```
let pattern = seq('c3', ['e3', 'g3']); // pattern from user
let interval = 0.5; // query interval in seconds
let time = 0; // beginning of current time span
let minLatency = .1; // min time before a hap should trigger
setInterval(() => {
  const haps = pattern.queryArc(time, time + interval);
  time += interval; // increment time
  haps.forEach((hap) => {
    const deadline = hap.whole.begin - time + minLatency;
    onTrigger(hap, deadline, duration);
  });
}, interval * 1000); // query each "interval" seconds
```

Note that the above code is simplified for illustrative purposes. The actual implementation has to work around imprecise callbacks of `setInterval`. More about the implementation details can be read in this blog post.

The fact that `Pattern.queryArc` is a pure function that maps a time span to a set of events allows us to choose any interval we like without changing the resulting output. It also means that when the pattern is changed from outside, the next scheduling callback will work with the new pattern, keeping its clock running.

The latency between the time the pattern is evaluated and the change is heard is between `minLatency` and `interval + minLatency`, in our example between 100ms and 600ms. In Strudel, the current query interval is 50ms with a minLatency of 100ms, meaning the latency is between 50ms and 150ms.

7.3 3. Output

The last step is to trigger each event in the chosen output. This is where the given time and value of each event is used to generate audio or any other form of time based output. The default output of the Strudel REPL is the WebAudio output. To understand what an output does, we first have to understand what control params are.

7.3.1 Control Patterns

To be able to manipulate multiple aspects of sound in parallel, so called control patterns are used to shape the value of each event. Example:

```
note("c3 e3").cutoff(1000).s('sawtooth')
  .queryArc(0, 1).map(hap => hap.value)
/* [
  { note: 'c3', cutoff: 1000, s: 'sawtooth' }
  { note: 'e3', cutoff: 1000, s: 'sawtooth' }
] */
```

Here, the control pattern functions note, cutoff and s are used, where each controls a different property in the value object. Each control param pattern accepts a primitive value, a list of values to be sequenced into a Pattern, or a Pattern. In the example, note gets a Pattern from a Mini Notation expression (double quoted), while cutoff and s are given a Number and a (single quoted) String respectively.

Strudel comes with a large default set of control pattern functions that are based on the ones used by Tidal and SuperDirt, focusing on music and audio terminology. It is however possible to create custom control params for any purpose:

```
const { x, y } = createParams('x', 'y')
x(sine.range(0, 200)).y(cosine.range(0,200))
```

This example creates the custom control params x and y which are then used to form a pattern that descibes the coordinates of a circle.

7.3.2 Outputs

Now that we know how the value of an event is manipulated using control params, we can look at how outputs can use that value to generate anything. The scheduler above was calling the onTrigger function which is used to implement the output. A very simple version of the web audio output could look like this:

```
function onTrigger(hap, deadline, duration) {
  const { note } = hap.value;
  const time = getAudioContext().currentTime + deadline;
  const o = getAudioContext().createOscillator();
  o.frequency.value = getFreq(note);
  o.start(time);
  o.stop(time + event.duration);
  o.connect(getAudioContext().destination);
}
```

The above example will create an OscillatorNode for each event, where the frequency is controlled by the note param. In essence, this is how the WebAudio API output of Strudel works, only with many more params like cutoff, resonance, attack, decay, sustain, release and many more.

8   Pattern alignment and combination

One core aspect of Strudel, inherited from Tidal, is the flexible way that patterns can be combined, irrespective of their structure. Its declarative approach means a live coder does not have to think about the details of *how* this is done, only *what* is to be done.

As a simple example, consider two number patterns "0 [1 2] 3", and "10 20". The first has three contiguous steps of equal lengths, with the second step broken down into two substeps, giving four events in total. There are a very large number of ways in which the structure of these two patterns could be combined, but the default method in both Strudel and Tidal is to line up the cycles of the two patterns, and then take events from the first pattern and match them with those in the second pattern. Therefore, the following two lines are equivalent:

```
"0 [1 2] 3".add("10 20")
"10 [11 22] 23"
```

Where the events only partially overlap, they are treated as fragments of the event in the first pattern. This is a little difficult to conceptualise, but lets start by comparing the two patterns in the following example:

```
"0 1 2".add("10 20")
"10 [11 21] 20"
```

They are similar to the previous example in that the number 1 is split in two, with its two halves added to 10 and 20 respectively. However, the 11 'remembers' that it is a fragment of that original 1 event, and so is treated as having a duration of a third of a cycle, despite only being active for a sixth of a cycle. Likewise, the 21 is also a fragment of that original 1 event, but a fragment of its second half. Because the start of its event is missing, it wouldn't actually trigger a sound (unless it underwent further pattern transformations/combinations).

In practice, the effect of this default, implicit method for combining two patterns is that the second pattern is added *in* to the first one, and indeed this can be made explicit:

```
"0 1 2".add.in("10 20")
```

This makes way for other ways to align the pattern, and several are already defined, in particular:

- in - as explained above, aligns cycles, and applies values from the pattern on the right *in* to the pattern on the left.
- out - as with in, but values are applied *out* of the pattern on the left (i.e. *in* to the one on the right).
- mix - structures from both patterns are combined, so that the new events are not fragments but are created at intersections of events from both sides.
- squeeze - cycles from the pattern on the right are squeezed into events on the left. So that e.g. "0 1 2".add.squeeze("10 20") is equivalent to "[10 20] [11 21] [12 22]".
- squeezeout - as with squeeze, but cycles from the left are squeezed into events on the right. So, "0 1 2".add.squeezeout("10 20") is equivalent to [10 11 12] [20 21 22].
- trig is similar to squeezeout in that cycles from the right are aligned with events on the left. However those cycles are not 'squeezed', rather they are truncated to fit the event. So "0 1 2 3 4 5 6 7".add.trig("10 [20 30]") would be equivalent to 10 11 12 13 20 21 30 31. In effect, events on the right 'trigger' cycles on the left.
- trigzero is similar to trig, but the pattern is 'triggered' from its very first cycle, rather than from the current cycle. trig and trigzero therefore only give different results where the leftmost pattern differs from one cycle to the next.

We will save going deeper into the background, design and practicalities of these alignment functions for future publications. However in the next section, we take them as a case study for looking at the different design affordances offered by Haskell to Tidal, and JavaScript to Strudel.

9   Comparing Strudel and Haskell in use

Unlike Haskell, JavaScript lacks the ability to define custom infix operators, or change the meaning of existing ones. So the above Strudel example of "0 1 2".add.out("10 20") is equivalent to the Tidal expression "0 1 2" +| "10 20", where the vertical bar in the operator +| stands for out (where a |+ b would be equivalent of a.add.in(b)).

From this we can already see that Tidal tends towards brevity through mixing infix operators with functions, and Strudel tends towards spelling out operations which are joined together with the . operator. This then is the design trade-off of Tidal's tersity, versus Strudel's simplicity.

To demonstrate this, consider the following Tidal pattern:

```
iter 4 $ every 3 (||+ n "10 20") $ (n "0 1 3") # s "triangle" # crush 4
```

This can be directly translated to the Strudel equivalent:

```
iter(4, every(3, add.squeeze("10 20"), n("0 1 3").s("triangle").crush(4)))
```

Although for a more canonical Strudel expression, we would reorder it as:

```
n("0 1 3").every(3, add.squeeze("10 20")).iter(4).s("triangle").crush(4)
```

The Strudel example uses the . method call operator for all operations and combinations, whereas the Tidal example has # for the default method for combining patterns and uses infix operators for other methods. The lack of parenthesis in the Tidal example is partly due to the way that arguments are applied to Haskell's functions, and partly due to the use of the $ operator as an alternative way to establish precedence and control the order of evaluation.

Considering the above, we argue that the Haskell syntax is a little cleaner, but that the Strudel syntax is easier to learn. Our informal observation is that while Haskell's dollar $ operator is very useful in making code easier to work with, it is one of the most difficult aspects of Tidal use for beginners to learn. On the other hand, the deeper levels of parenthesis in Strudel code can be difficult to keep track of, especially while coding under pressure of live musical performance. However this difficulty can be largely be mitigated by reordering expressions, and further mitigated by supporting editor features.

With Strudel, we have little choice but to embrace the affordances and constraints offered by JavaScript, and while designing a domain-specific language entirely based on method calls is a challenge, through creative adoption of functional programming techniques like partial application, we are so far very happy with the results. Tidal's functional reactive approach to pattern-making has in general translated well to JavaScript, and opportunities and constraints have overall traded off to create a very approachable and useable live coding environment.

10   The trade-off of flexible typing

We have identified one problem with porting Tidal to JavaScript where we have missed Haskell's strict typing and type inference. In both Tidal and Strudel, time is rational, where any point in time is represented as the ratio of two integers. This allows representation of musical ratios such that are impossible to represent accurately using the more common floating point numbers. However while libraries are available that support rational numbers in JavaScript, the lack of strict typing means that it is easy to implement pattern methods where computationally expensive conversion from floating point to rational numbers are performed late, and therefore often enough to overload the CPUs, due to the large number of iterative calculations required to estimate a ratio for a given floating point number. To mitigate this problem, we might consider moving to TypeScript in the future.

11   Future Outlook

The project is still young, with many features on the horizon. As general guiding principles, Strudel aims to be

1. accessible
2. consistent with Tidal's approach to pattern
3. modular and extensible

For the future, it is planned to integrate additional alternative sound engines such as Glicol (Lan [2020] 2022) and Faust (*Faust - Programming Language for Audio Applications and Plugins* [2016] 2022). To improve compatibility with Tidal, more Tidal functions are planned to be ported, as well as full compatibility with SuperDirt. Besides sound, other ways to render events are being explored, such as graphical, and choreographic output. We are also looking into alternative ways of editing patterns, including multi-user editing for network music, parsing a novel syntax to escape the constraints of javascript, and developing hardware/e-textile interfaces.

12   Links

The Strudel REPL is available at https://strudel.tidalcycles.org, including an interactive tutorial. The repository is at https://github.com/tidalcycles/strudel, all the code is open source under the AGPL-3.0 License.

13   Acknowledgments

References

10 *Faust - Programming Language for Audio Applications and Plugins*. (2016) 2022. C++. GRAME. https://github.com/grame-cncm/faust.

Jack, Olivia. (2022) 2022. *Hydra*. https://github.com/ojack/hydra.

Lan, Qichao. (2020) 2022. *Chaosprint/Glicol*. Rust. https://github.com/chaosprint/glicol.

Mclean, Alex. 2020. "Algorithmic Pattern." In *Proceedings of the International Conference on New Interfaces for Musical Expression*, 265--270. Birmingham, UK. https://zenodo.org/record/4813352.

McLean, Alex. 2020. "Feedforward." In *Proceedings of New Interfaces for Musical Expression*. Birmingham. https://zenodo.org/record/6353969.

McLean, Alex, Raphaël Forment, Sylvain Le Beux, and Damián Silvani. 2022. "TidalVortex Zero." In *Proceedings of the 7th International Conference on Live Coding*. Limerick, Ireland: Zenodo. https://doi.org/10.5281/zenodo.6456380.

Ogborn, David. (2016) 2022. *Dktr0/WebDirt*. JavaScript. https://github.com/dktr0/WebDirt.

Ogborn, David, Jamie Beverley, Luis Navarro del Angel, Eldad Tsabary, and Alex McLean. 2017. "Estuary: Browser-Based Collaborative Projectional Live Coding of Musical Patterns." In *Proceedings of the International Conference on Live Coding*, 11. Morelia.

Roberts, Charles, and Joann Kuchera-morin. 2012. "Gibber: Live Coding Audio in the Browser." In *In Proceedings of the 2012 International Computer Music Conference*.

Solomon, Mike. (2021) 2022. *Purescript-Ocarina*. PureScript. https://github.com/mikesol/purescript-ocarina.

SuperDirt. (2015) 2022. SuperCollider. musikinformatik. https://github.com/musikinformatik/SuperDirt.

Toussaint, Godfried. 2005. "The Euclidean Algorithm Generates Traditional Musical Rhythms." In *In Proceedings of BRIDGES: Mathematical Connections in Art, Music and Science*, 47–56. http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.62.231.