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## A Toy Example

Define a simple objective function which calculates the sum of a penalty term and the squared error between the DataRemix reconstruction and the original input matrix. The input matrix is a 100-by-9 matrix with random values. In this case, we know that when k=9,p=1 or  $\mu=1, p=1$ , it achieves the maximal value which is qual to the penalty term.

```
> eval <- function(X_reconstruct, X, penalty){</pre>
    return(-sum((X-X_reconstruct)^2)+penalty)
+ }#eval
Genrate a random matrix with dimension 100-by-9 and perform the SVD de-
composition.
> set.seed(1)
> num_of_row <- 100
> num_of_col <- 9
> X <- matrix(rnorm(num_of_row*num_of_col), nrow = num_of_row, ncol = num_of_col)
> svdres <- svd(X)
Set mt to be 2000.
> basis_short <- omega[1:2000,]</pre>
Infer the optimal combinations of k, p and \mu. Here X and penalty are additional
inputs for the eval() function.
> DataRemix.res <- DataRemix(svdres, eval, lower_limit = c(1,-1,0),
                   upper_limit = c(length(svdres$d), 1,1), num_of_initialization = 5,
                   num_of_thompson = 50, basis = basis_short, xi = 0.1, full = T,
                   verbose = F, X = X, penalty = 100)
> knitr::kable(cbind(1:55,DataRemix.res$para), align = "l",
               col.names = c("Iteration", "k", "p", "mu", "Eval"))
|Iteration |k |p
|:----|:--|:--|:----
           18
               0.9343941
                           |0.8669163 |80.13347
1
12
               |-0.6161244 | 0.0822944 | -774.54934 |
              |-0.8592770 | 0.5276627 | -674.50813 |
13
```

|-0.9036173 | 0.5945408 | -595.20968 |

|0.1977374 |0.0279159 |-608.45408 |

|0.7600058 |0.7491820 |-57.75474

10.9732232 10.7962543 166.09687 |2 |0.6264308 |0.8342587 |-30.90262

```
19
            15
                10.9392592
                             |0.7591503 |69.95399
110
            19
                11.0000000
                             |1.0000000 |100.00000
|11
                10.1871164
                             |0.7129497 |-343.61286
|12
           12
                11.0000000
                             |0.9781217 |99.68624
113
            12
                10.6365943
                             |0.4338173 |-219.30523
            |1
                10.5156579
                             |0.7223355 |-41.68571
|14
|15
           17
                11.0000000
                             10.7208022 | 89.33314
                10.4294922
                             |0.5433661 |-407.64110
|16
           18
|17
            19
                1.0000000
                             0.6235153 | 100.00000
           15
                0.5461408
                             |0.9202155 |-197.56072 |
|18
|19
           18
                10.9772540
                             10.9936968 | 97.49998
120
           14
                1.0000000
                             |0.5460449 |15.03810
|21
            11
                |-0.0173672 |1.0000000 |-36.59617
122
            1
                0.9025561
                             |0.6182613 |-24.26296
123
           18
                0.8715479
                             |0.3022851 |8.03090
124
           18
                10.9828520
                             |0.6873251 |92.61232
125
            18
                10.9454568
                             |0.1996929 |47.69907
126
            1
                10.5610817
                             |0.9933571 |27.84442
127
           13
                10.3069788
                             |0.9803562 |-189.58190
128
            12
                |0.9187318
                             |0.0457580 |-507.27793
            12
                11.0000000
                             |0.7288770 |51.81555
129
                |-0.0317688 |1.0000000 |-697.04950
130
            19
|31
           14
                10.9620278
                             10.6540939 | 46.30062
                11.0000000
                             |0.1181146 |-68.91236
132
            16
133
            13
                11.0000000
                             10.8792390 192.25942
134
           14
                0.9115363
                             |0.8683955 |71.85496
135
           14
                1.0000000
                             1.0000000 | 100.00000
136
            16
                10.9603441
                             |0.5743332 |54.42460
                11.0000000
                             |0.4080560 |52.05165
|37
            17
138
                10.8956883
                             |1.0000000 |91.35505
           11
139
           19
                11.0000000
                             |0.1709873 |100.00000
           19
                1.0000000
                             |0.4663211 |100.00000
140
|41
            18
                1.0000000
                             0.1373955 | 54.72115
142
            19
                10.9790435
                             10.0000000 | 97.76288
143
            18
                11.0000000
                             |0.5319136 |86.66712
|44
            18
                10.7708451
                             |0.6429106 |-66.45776
145
            13
                10.9880974
                             |0.9615625 |98.85134
                11.0000000
146
           15
                             |0.9478538 |99.17939
147
                10.4824335
                             |0.8224709 |-10.65728
            1
148
            16
                10.9907425
                             |0.8281591 |93.22178
149
           17
                10.9866542
                             10.7967908 | 93.53178
|50
           14
                11.0000000
                             |0.9221451 |97.50097
           17
                             |0.9049580 |75.03276
|51
                10.9224287
                                                      1
            19
                1.0000000
                             0.2967019 | 100.00000
152
153
            19
                10.9003347
                             10.0943662 | 57.83476
                1.0000000
                             |0.0935604 |100.00000
154
            19
```