17

19

## 1 A Toy Example

Define a simple objective function which calculates the sum of a penalty term and the squared error between the DataRemix reconstruction and the original input matrix. The input matrix is a 100-by-9 matrix with random values. In this case, we know that when k=9,p=1 or  $\mu=1$ , p=1, it achieves the maximal value which is qual to the penalty term.

```
> eval <- function(X_reconstruct, X, penalty){</pre>
    return(-sum((X-X_reconstruct)^2)+penalty)
+ }#eval
Genrate a random matrix with dimension 100-by-9 and perform the SVD de-
composition.
> set.seed(1)
> num_of_row <- 100
> num_of_col <- 9
> X <- matrix(rnorm(num_of_row*num_of_col), nrow = num_of_row, ncol = num_of_col)
> svdres <- svd(X)
Set mt to be 2000.
> basis_short <- omega[1:2000,]</pre>
Infer the optimal combinations of k, p and \mu. Here X and penalty are additional
inputs for the eval() function.
> DataRemix.res <- DataRemix(svdres, eval, k_limits = c(1, length(svdres$d)),
                   p_{limits} = c(-1,1), mu_{limits} = c(1e-12,1),
                   num_of_initialization = 5, num_of_thompson = 50,
                   basis = basis_short, xi = 0.1, full = T, verbose = F,
                   X = X, penalty = 100)
> knitr::kable(cbind(1:55,DataRemix.res$para), align = "l",
               col.names = c("Iteration", "k", "p", "mu", "Eval"))
|Iteration |k |p
                                       |Eval
                            mu
|:----|:--|:--|
           |8 |0.9343941 |0.8669163 |80.133470
11
              |-0.6161244 | 0.0822944 | -774.549343 |
12
           14
13
           |6 |-0.8592770 |0.5276627 |-674.508131
               |-0.9036173 | 0.5945408 | -595.209680
14
15
           |8 |0.1977374 |0.0279159 |-608.454077 |
16
           11
              I-0.8864492 | 0.0000000 | -857.307510 |
```

|0.9710026 |1.0000000 |95.796992

```
18
            19
                10.5652128
                             |1.0000000 |-294.183178 |
19
            12
                10.3076150
                             |0.0000000 |-762.471773
110
            19
                11.0000000
                             |0.0213327 |100.000000
|11
            18
                10.8987462
                             |0.2482674 | 24.395734
112
            19
                10.7693587
                             |0.0307309 |-68.911583
            14
                11.0000000
                             |0.2702496 |-119.556864
|13
|14
            15
                10.6702578
                             |0.6061702 |-148.365491
                10.9714513
                             10.4360788 | 27.620644
|15
            16
|16
            18
                11.0000000
                             |0.0115548 |40.546538
|17
            18
                0.9275926
                             |0.0010597 |16.749705
|18
            17
                |-0.8048691 | 0.0000000 | -837.884176
|19
            1
                10.8895300
                             |0.4589730 |-143.745379
120
            11
                0.2451882
                             |0.5008529 |-215.580317
|21
            15
                1.0000000
                             |1.0000000 |100.000000
122
            16
                0.9021402
                             |0.0021875 |-149.272093
123
            19
                1.0000000
                             |0.1065941 |100.000000
124
            18
                11.0000000
                             |0.0000000 |39.148407
125
            15
                10.1647886
                             |0.0208602 |-687.531413
           17
126
                10.7651296
                             |0.0000000 |-189.425162
127
            14
                10.9763708
                             |0.0003240 |-313.770572
            15
128
                10.6015909
                             |1.0000000 |-154.939640
                11.0000000
                             10.0000000 | 39.148404
129
            18
130
            19
                10.8481905
                             |0.0000000 |13.019424
131
            15
                11.0000000
                             |0.0000000 |-201.782435
132
            16
                10.4246590
                             |0.0000000 |-536.224365
133
            18
                10.8861626
                             |0.0000000 |-11.472133
           17
                1.0000000
|34
                             1.0000000 | 100.000000
135
            19
                10.8752923
                             10.3208530 | 37.626562
136
            17
                1.0000000
                             |0.0968655 |-11.613634
           12
                1.0000000
                             |1.0000000 |100.000000
|37
138
           13
                10.7020952
                             |0.3133165 |-267.634044
            18
139
                10.8898831
                             |0.0000000 |-8.621272
140
            19
                1.0000000
                             0.0000000 | 100.000000
|41
            18
                11.0000000
                             |0.0000002 |39.148434
142
            17
                10.9423744
                             |0.0000000 |-50.562141
143
            19
                10.9474766
                             |0.0000000 |86.947638
|44
            15
                10.9509870
                             |1.0000000 |91.602471
145
                |-0.0133796 | 0.0000000 | -836.453933
            1
146
            19
                             |0.0000016 |100.000000
                11.0000000
|47
            19
                11.0000000
                             |0.000000 |100.00000
148
            1
                10.9430562
                             |0.0001217 |-702.783740
|49
           17
                10.7776872
                             |0.0000448 |-177.336161
150
            19
                10.8566499
                             |0.0000002 | 20.964082
            15
                10.8830432
                             |0.0253040 |-227.421134
|51
152
            12
                11.0000000
                             0.1112699 |-417.742749
                10.8240095
                            |0.0000018 |-10.793403
|53
            19
```