## 1 A Toy Example

Define a simple objective function which calculates the squared error between the DataRemix reconstruction and the original input matrix and the reconstruction error comes with a penalty term. The maximal value should be the same as penalty.

```
> reconstruct <- function(X_reconstruct, X, penalty){</pre>
    return(-sum((X-X_reconstruct)^2)+penalty)
+ }#reconstruct
Genrate a random matrix with dimension 100-by-9 and perform the SVD de-
composition.
> set.seed(1)
> num_of_row <- 100
> num_of_col <- 9
> X <- matrix(rnorm(num_of_row*num_of_col), nrow = num_of_row, ncol = num_of_col)
> svdres <- svd(X)
Set mt to be 2000.
> basis_short <- basis[1:2000,]</pre>
Infer the optimal combinations of k, p and \mu
> DataRemix.res <- DataRemix(svdres, reconstruct, lower_limit = c(1,-1,0), upper_limit = c(1,-1,0)
[1]
      1.0000000
                  6.0000000
                              0.7600058
                                          0.7491820 -57.7547434
[1]
    2.0000000 1.0000000 0.9732232 0.7962543 66.0968707
[1]
      3.0000000
                  2.0000000
                              0.6264308
                                          0.8342587 -30.9026157
[1]
    4.0000000 5.0000000 0.9392592 0.7591503 69.9539900
[1]
          9
              1
                  1 100
[1]
       6.000000
                    4.0000000
                                 0.1871164
                                              0.7129497 -343.6128577
    7.0000000 2.0000000 1.0000000 0.9781217 99.6862375
[1]
[1]
       8.0000000
                    2.0000000
                                 0.6365943
                                              0.4338173 -219.3052342
[1]
      9.000000
                  1.0000000
                              0.5156579
                                          0.7223355 -41.6857087
[1] 10.0000000 7.0000000 1.0000000 0.7208022 89.3331418
[1]
      11.0000000
                    8.0000000
                                 0.4294922
                                              0.5433661 -407.6411023
   12.0000000
                              1.0000000
[1]
                  9.0000000
                                          0.6235153 100.0000000
[1]
      13.0000000
                    5.0000000
                                 0.5461408
                                              0.9202155 -197.5607230
[1] 14.0000000 8.0000000 0.9772540 0.9936968 97.4999840
[1] 15.0000000 4.0000000 1.0000000 0.5460449 15.0380954
[1] 16.00000000
                   1.00000000 -0.01736721
                                             1.00000000 -36.59616861
[1] 17.0000000
                  1.0000000
```

```
[1] 18.0000000 8.0000000 0.8715479 0.3022851 8.0308999
[1] 19.0000000 8.0000000 0.9828520 0.6873251 92.6123180
```

- [1] 20.0000000 8.0000000 0.9454568 0.1996929 47.6990694
- [1] 21.0000000 1.0000000 0.5454500 0.1550525 47.0550054 [1] 21.0000000 1.0000000 0.5610817 0.9933571 27.8444243
- [1] 22.0000000 3.0000000 0.3069788 0.9803562 -189.5818971
- [1] 23.0000000 2.0000000 0.9187318 0.0457580 -507.2779252
- [1] 24.000000 2.000000 1.000000 0.728877 51.815549
- [1] 25.00000000 9.00000000 -0.03176877 1.00000000 -697.04950018
- [1] 26.0000000 4.0000000 0.9620278 0.6540939 46.3006161
- [1] 27.0000000 6.0000000 1.0000000 0.1181146 -68.9123575
- [1] 28.000000 3.000000 1.000000 0.879239 92.259421
- [1] 29.0000000 4.0000000 0.9115363 0.8683955 71.8549594
- [1] 30 4 1 1 100
- [1] 31.0000000 6.0000000 0.9603441 0.5743332 54.4245994
- [1] 32.000000 7.000000 1.000000 0.408056 52.051646
- [1] 33.0000000 1.0000000 0.8956883 1.0000000 91.3550476
- [1] 34.0000000 9.0000000 1.0000000 0.1709873 100.0000000
- [1] 35.0000000 9.0000000 1.0000000 0.4663211 100.0000000
- [1] 36.0000000 8.0000000 1.0000000 0.1373955 54.7211458
- [1] 37.0000000 9.0000000 0.9790435 0.0000000 97.7628833
- [1] 38.0000000 8.0000000 1.0000000 0.5319136 86.6671161
- [1] 39.0000000 8.0000000 0.7708451 0.6429106 -66.4577644
- [1] 40.0000000 3.0000000 0.9880974 0.9615625 98.8513362
- [1] 41.0000000 5.0000000 1.0000000 0.9478538 99.1793856
- [1] 42.0000000 1.0000000 0.4824335 0.8224709 -10.6572787
- [1] 43.0000000 6.0000000 0.9907425 0.8281591 93.2217789
- [1] 44.0000000 7.0000000 0.9866542 0.7967908 93.5317794
- [1] 45.0000000 4.0000000 1.0000000 0.9221451 97.5009747
- [1] 46.0000000 7.0000000 0.9224287 0.9049580 75.0327600
- [1] 47.0000000 9.0000000 1.0000000 0.2967019 100.0000000
- [1] 49.0000000 9.0000000 1.0000000 0.09356036 100.00000000 [1] 50.000000 1.000000 0.8545062 0.9146200 78.9340674