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# Probing pairing correlations in nuclei with (t,p) reactions

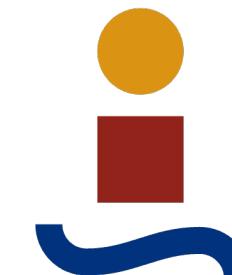
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Gregory Potel Aguilar

December 17, 2025



UNIVERSIDAD  
DE SEVILLA  
1505

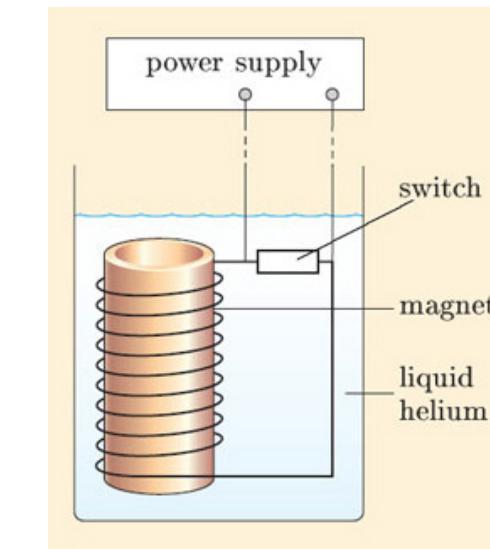
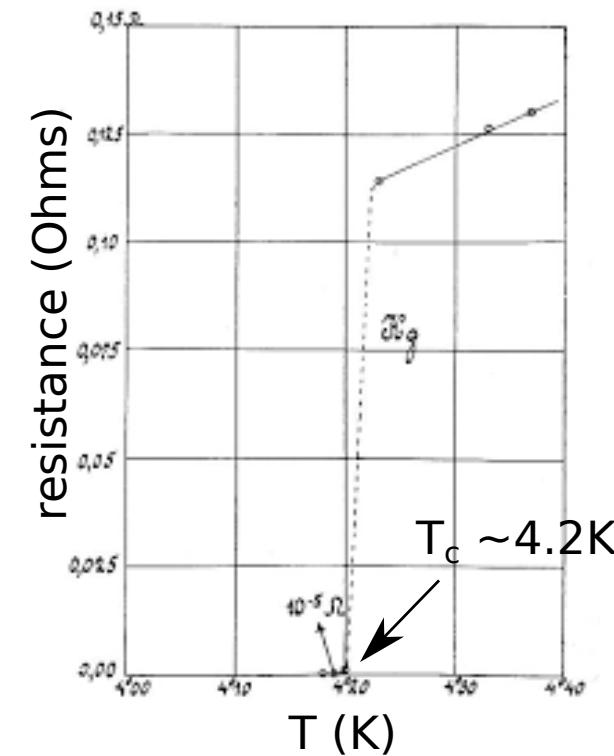


Escuela Técnica Superior de  
**INGENIERÍA DE SEVILLA**

# Introduction: superconductivity in metals

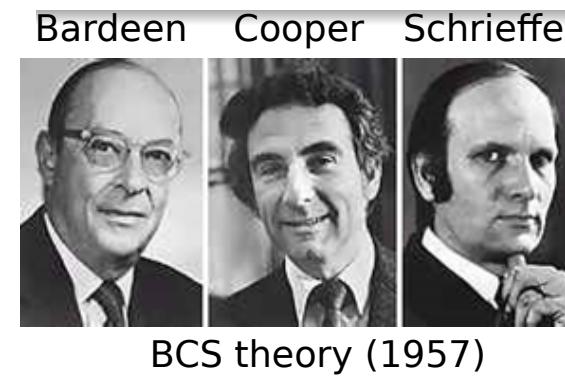


H. Kamerlingh Onnes

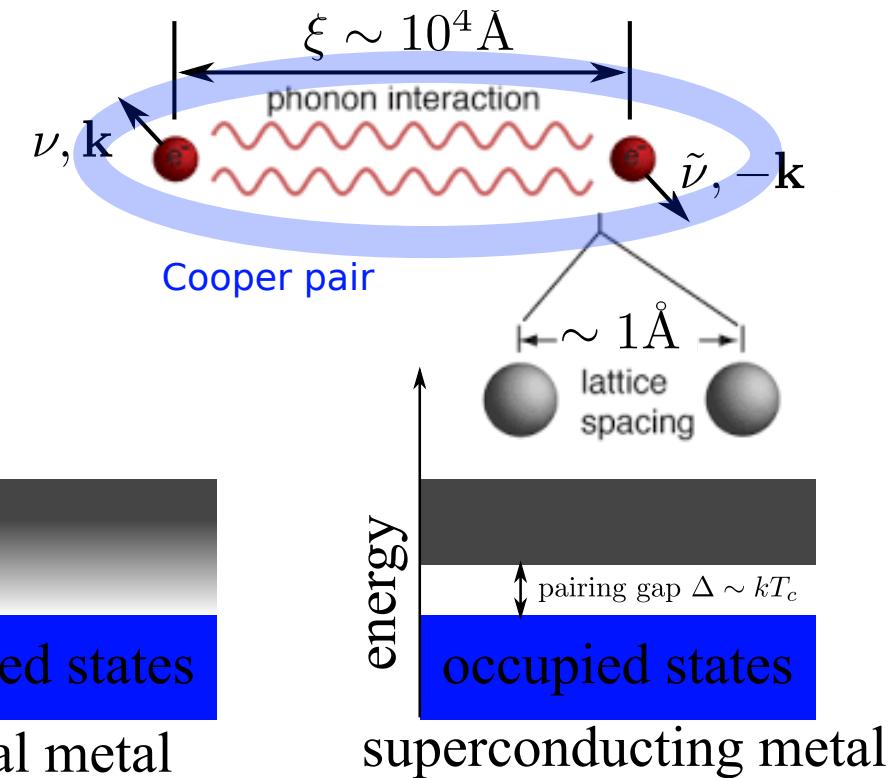
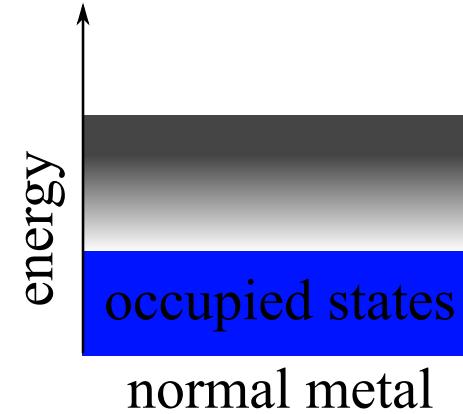


- In 1911, H. K. Onnes liquefies Helium and discovers superconductivity in mercury.
- When cooled below a critical temperature (e.g.  $T_c = 7.26\text{ K}$  for lead,  $T_c = 3.69\text{ K}$  for tin), many metals become superconductors.
- Persistent supercurrents can be induced in superconducting coils.

# BCS theory and Cooper pairs



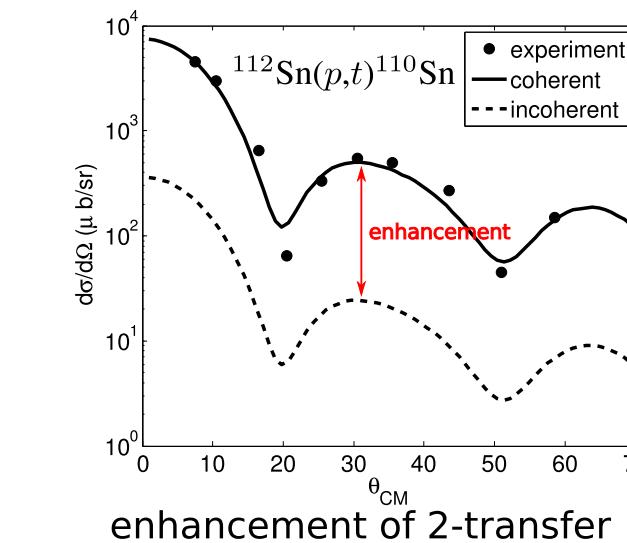
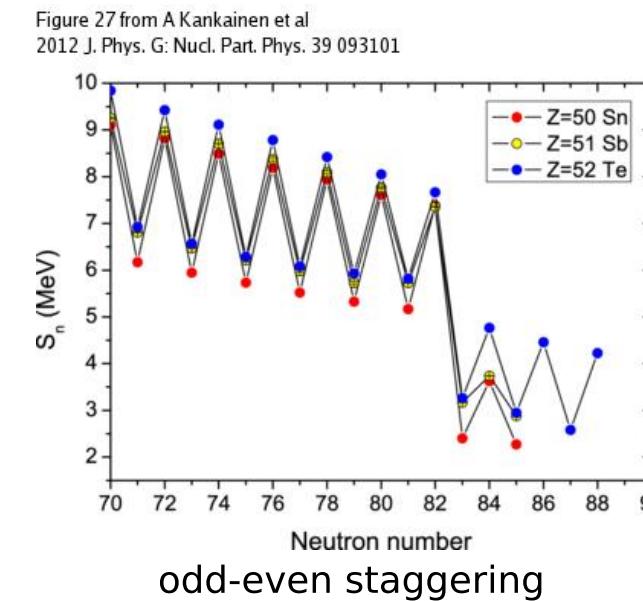
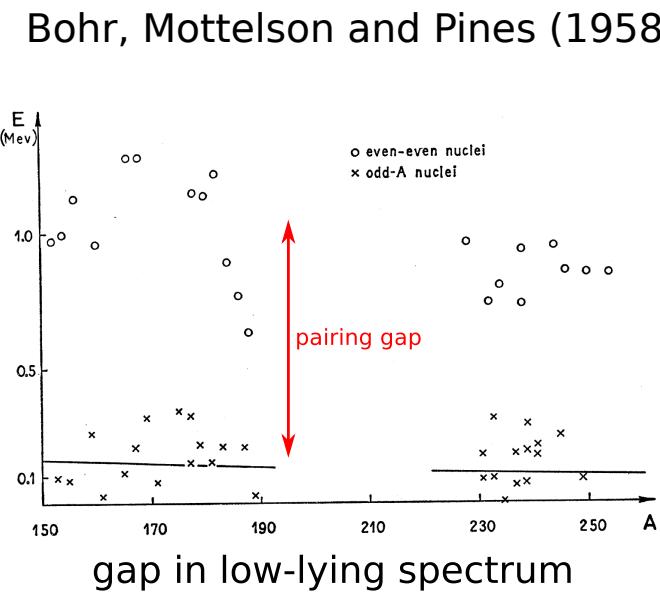
More than 40 years later  
arrives the theoretical  
breakthrough!



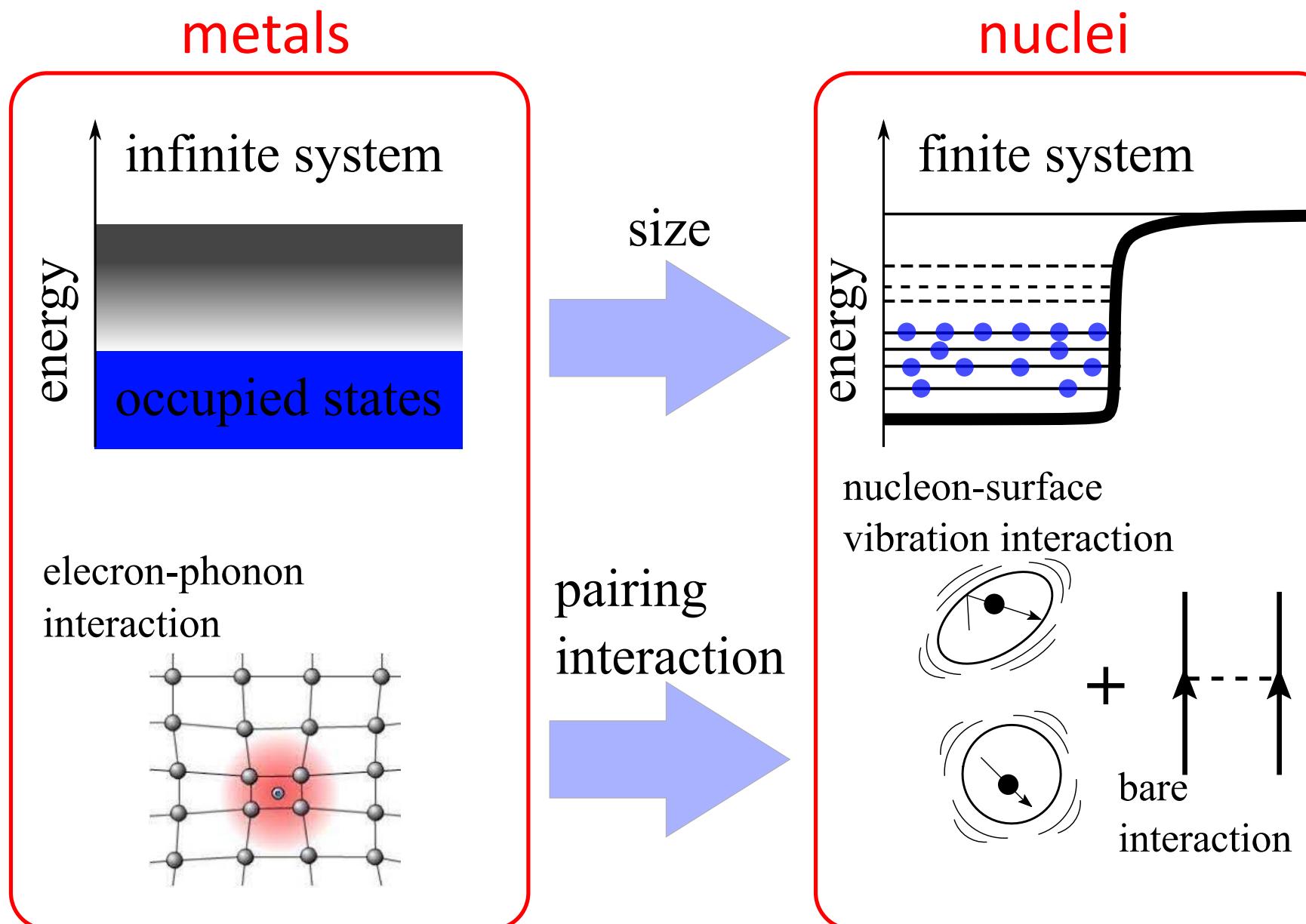
- Below  $T_c$ , electrons form **enormous** (correlation length  $\xi \sim 10^4 \text{ \AA}$ ) quasi-bosons (**Cooper pairs**).
  - The binding interaction results from the **screening** of the Coulomb force and the exchange of **lattice phonons**.
  - An **energy gap** develops in the low-lying spectrum.
  - The Cooper pairs form a condensate
- $$|BCS\rangle = \prod_{\nu} \left( U_{\nu} + V_{\nu} e^{i\phi} a_{\nu}^{\dagger} a_{\tilde{\nu}}^{\dagger} \right) |0\rangle$$

# Some experimental evidence of nuclear superfluidity

- Gap in the spectrum of even–even nuclei associated with the breaking of a Cooper pair.
- Odd–even mass staggering: enhanced binding for even number of nucleons.
- Enhanced two–nucleon transfer reactions due to the coherence of the Cooper pair wave function.



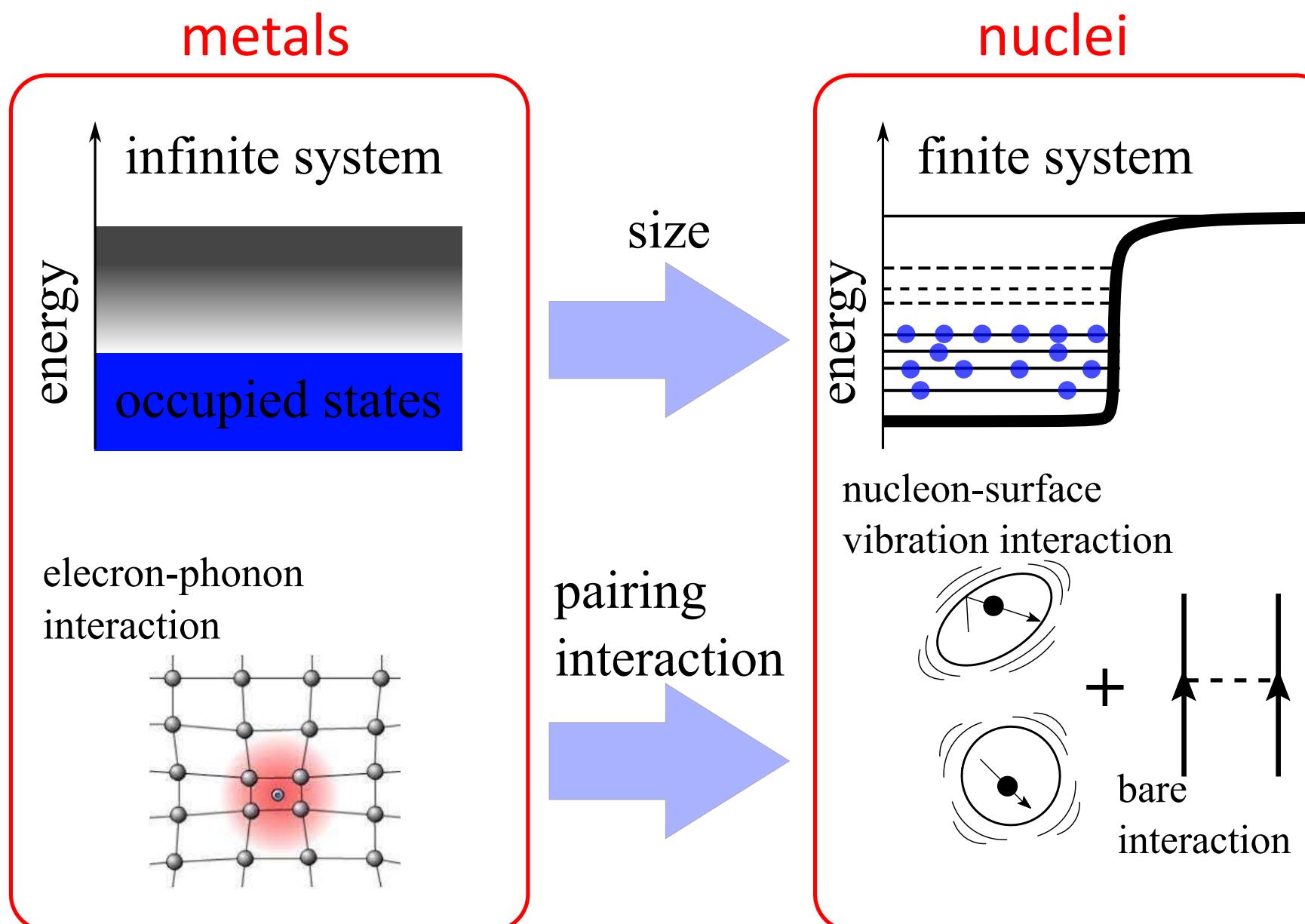
# But, metals and nuclei are quite different, aren't they?



questions still arise

- Can we observe Cooper pairs in nuclei?
- How do we make a quantitative assessment of pair correlations in nuclei?
- How do we export our knowledge of nuclear superfluidity to nuclear matter?

# But, metals and nuclei are quite different, aren't they?

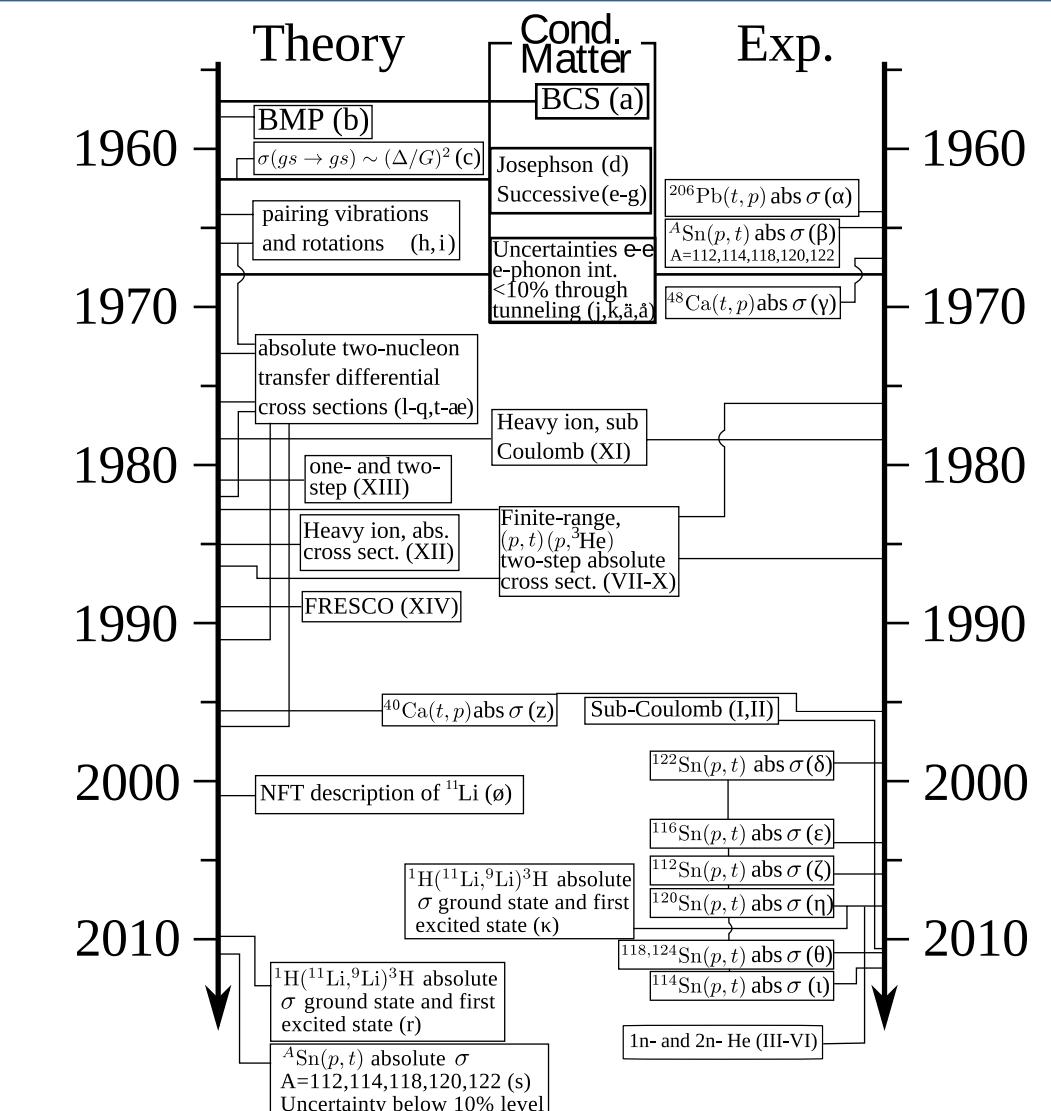
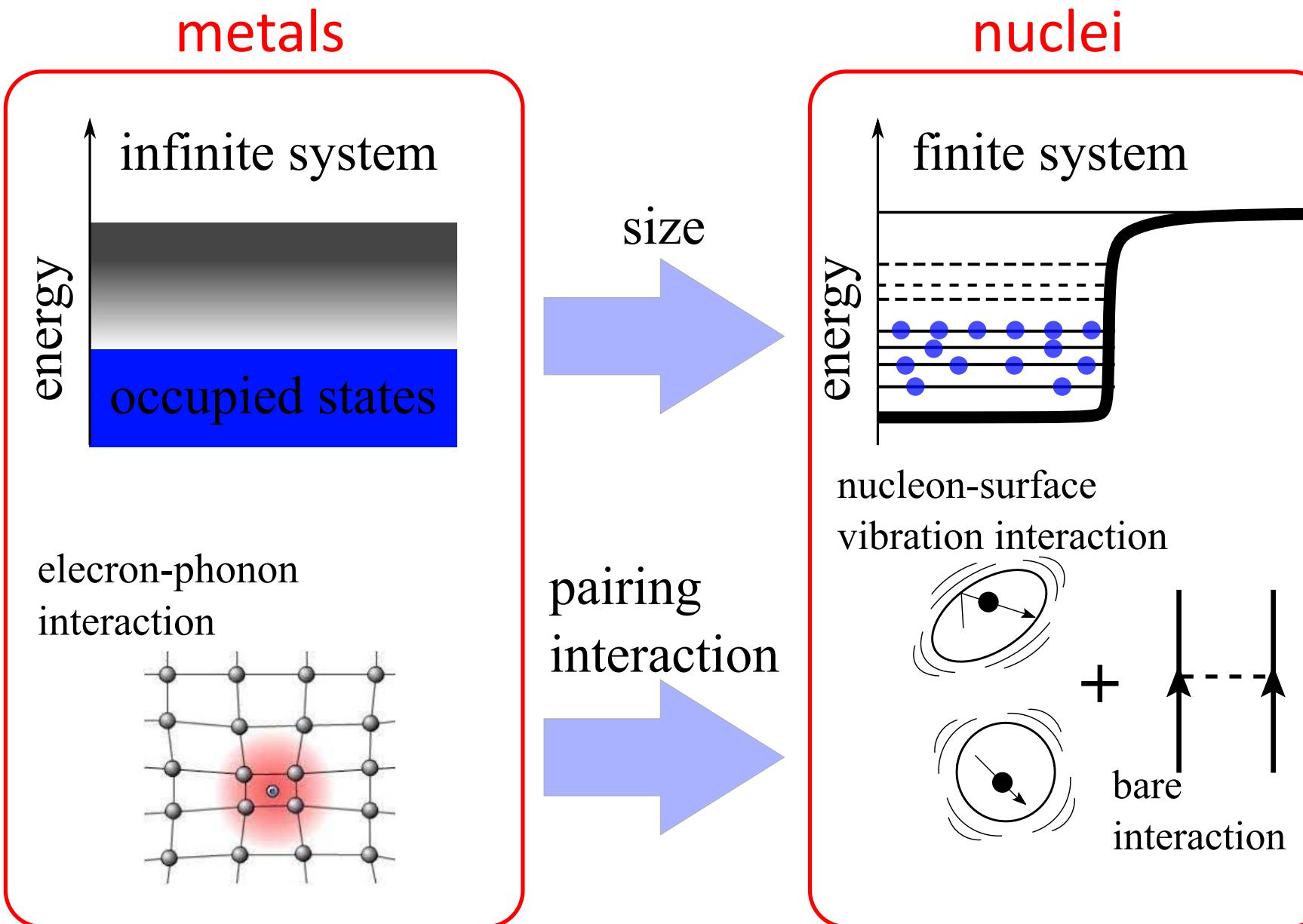


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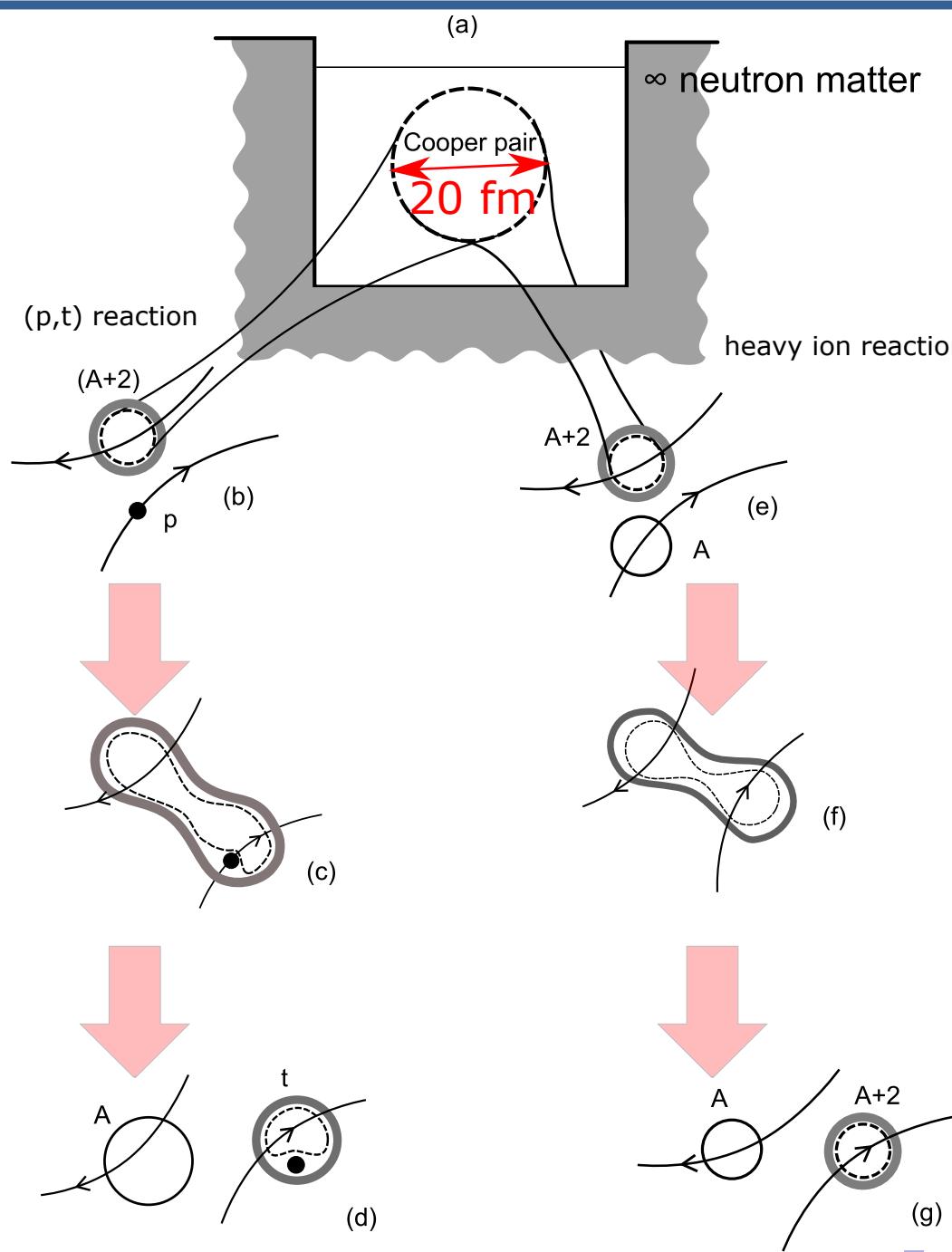
(t,p) reactions are a specific probe of nuclear pairing correlations

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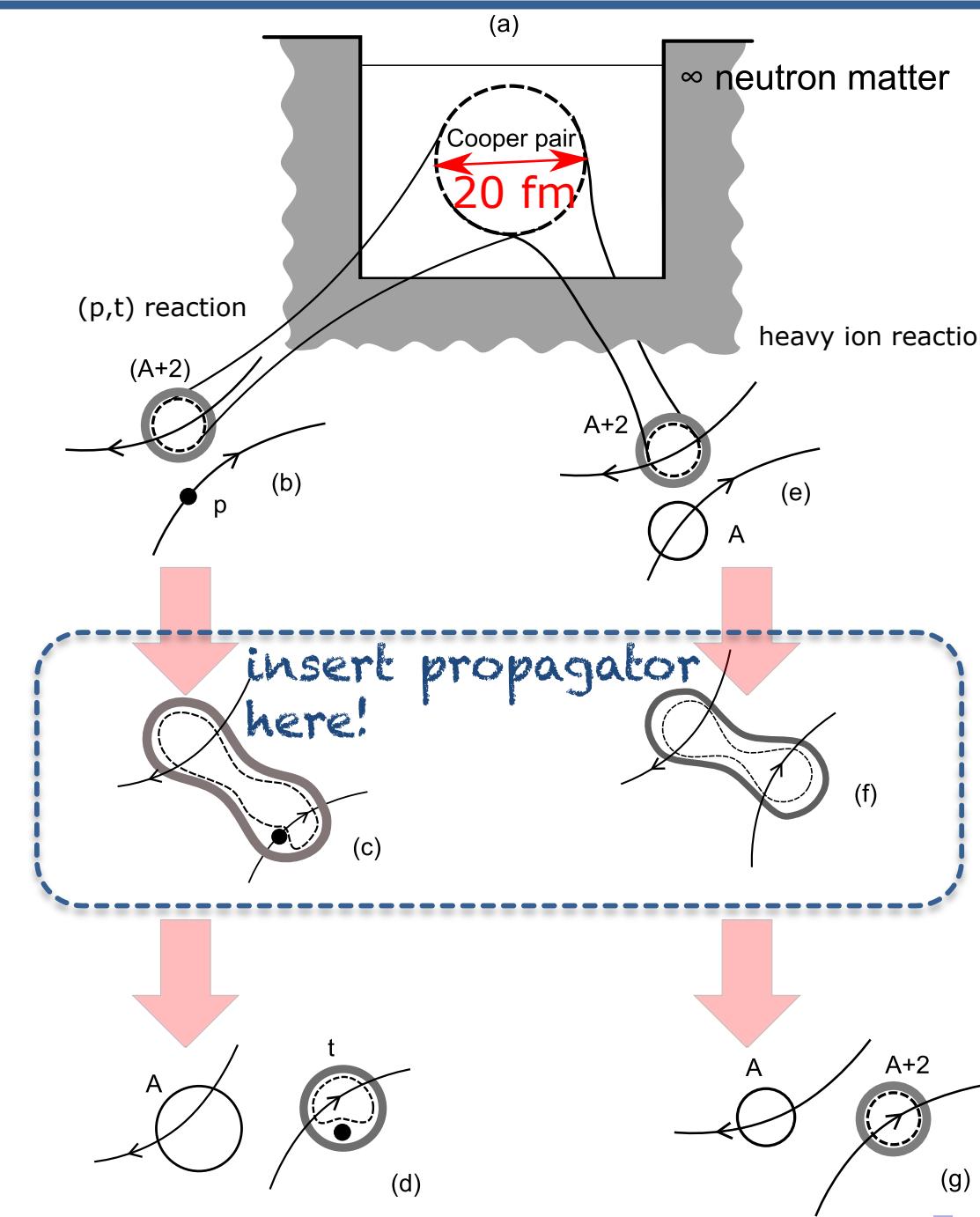


Rep. Prog. Phys. **76** (2013) 106301  
GP, Idini, Barranco, Vigezzi, Broglia

# The 2 neutron transfer process is very delocalized

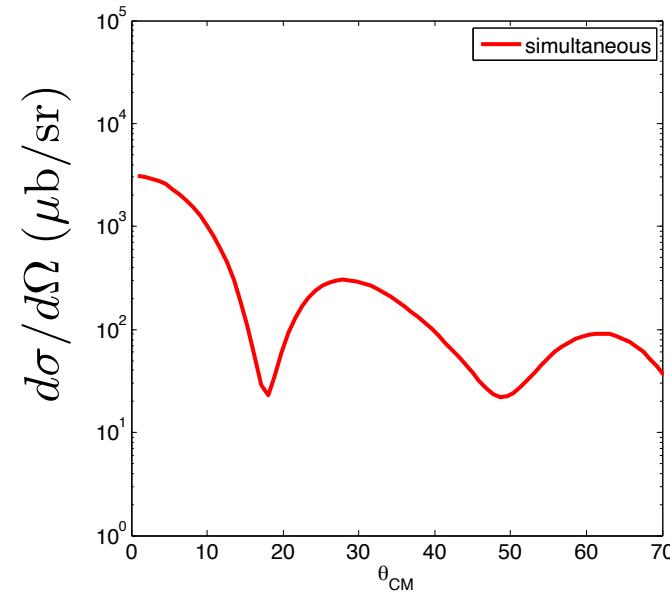


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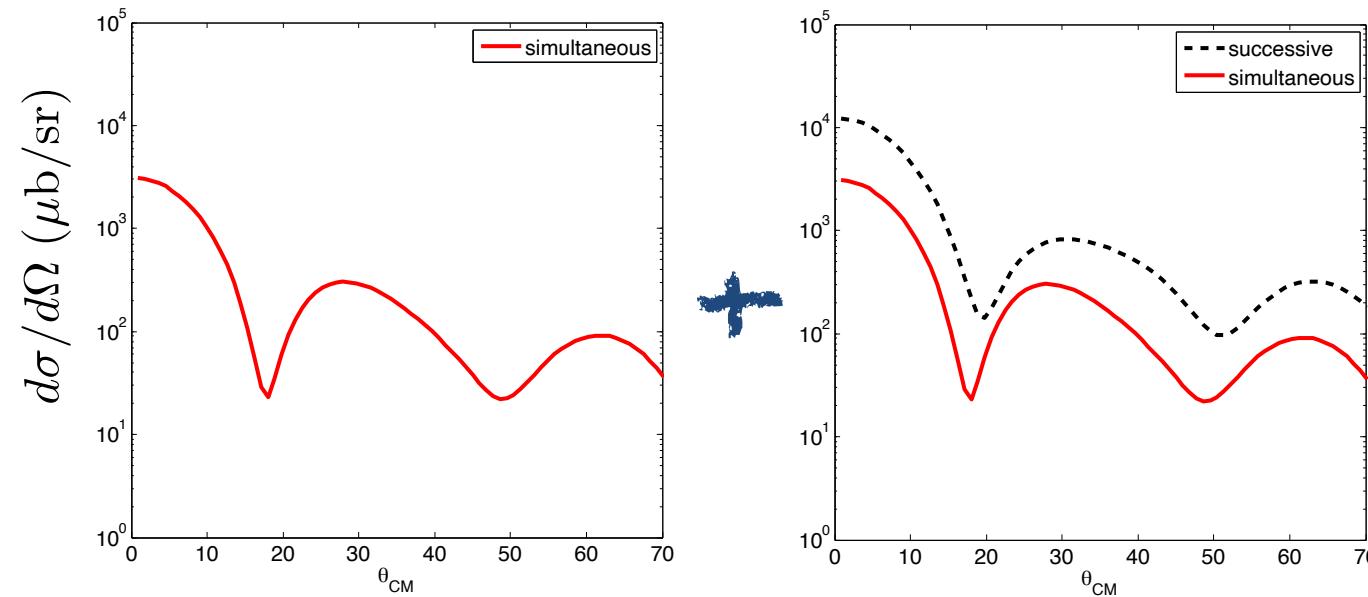


# Computing $^{112}\text{Sn}(p,t)^{110}\text{Sn}$ in second order DWBA

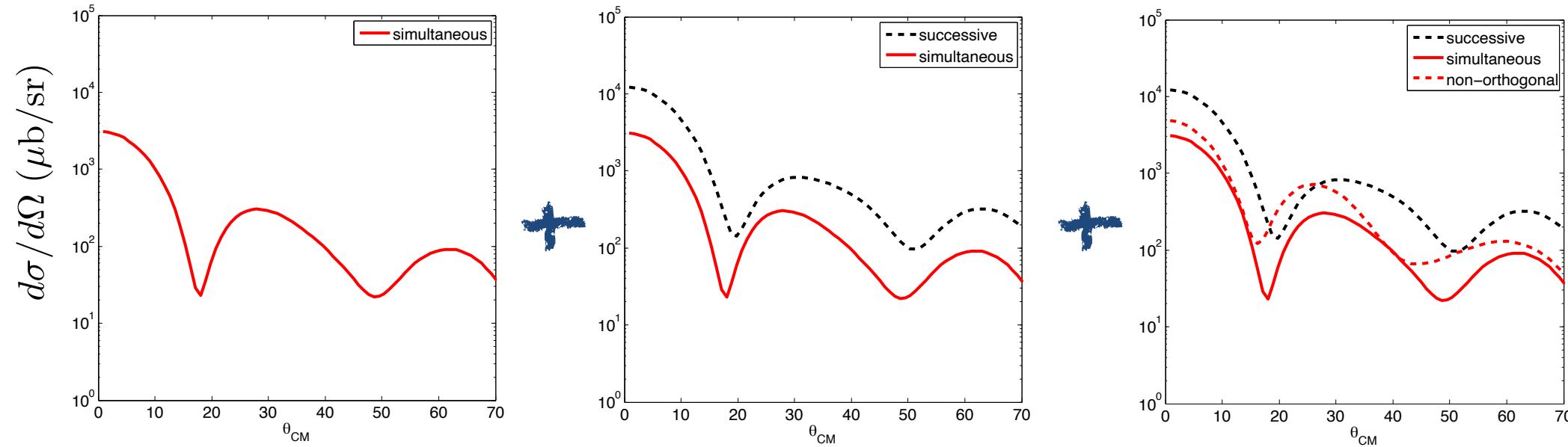
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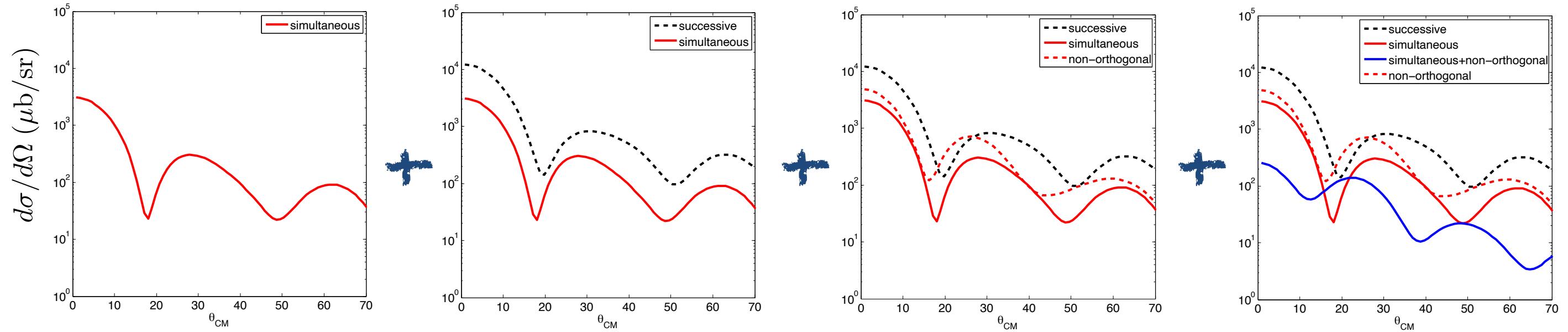
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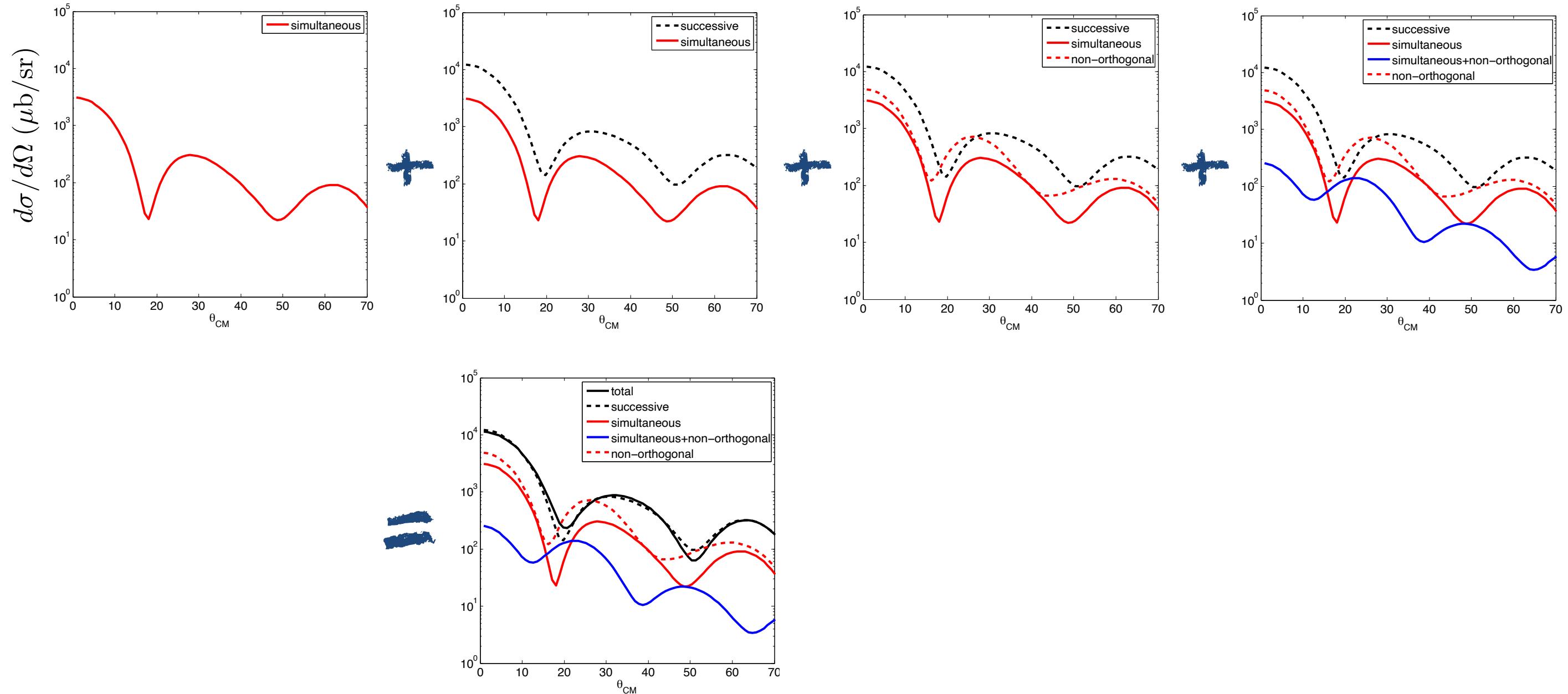
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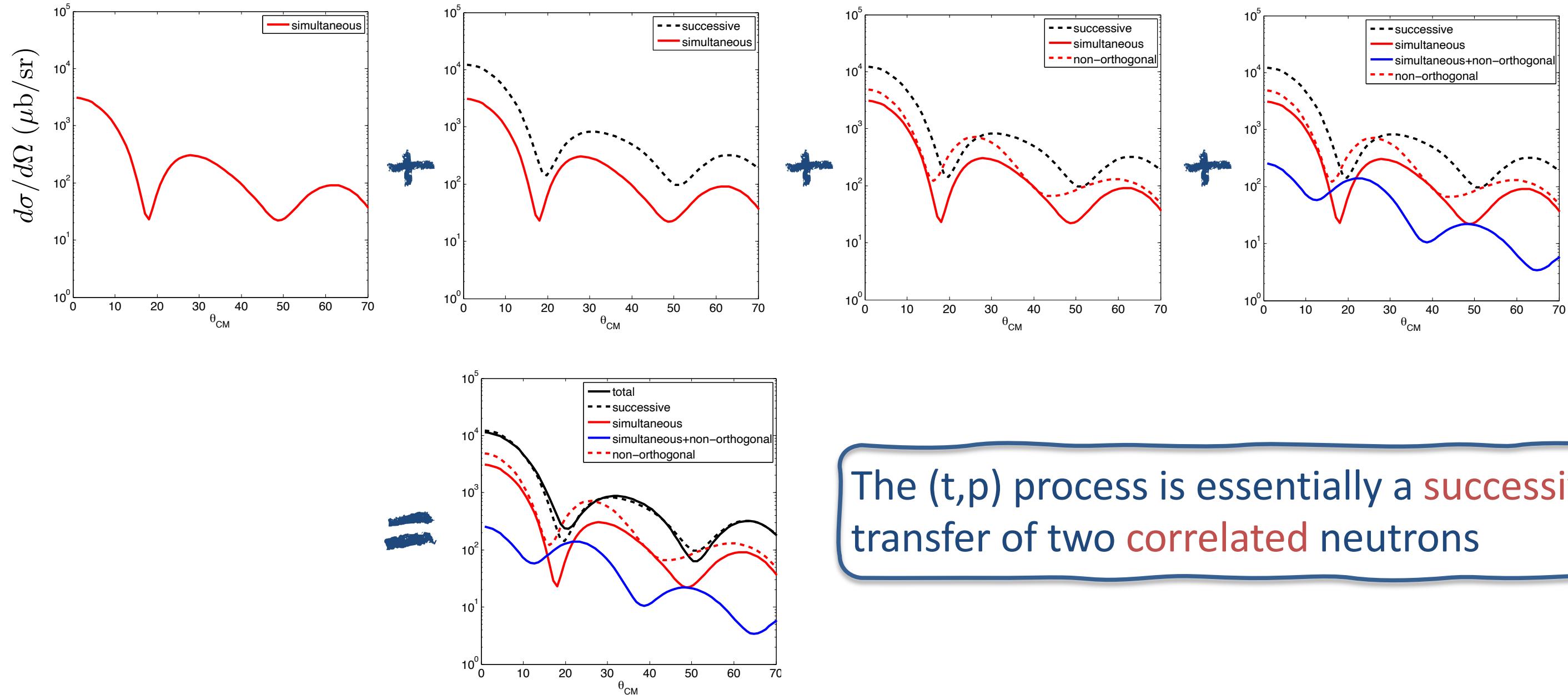
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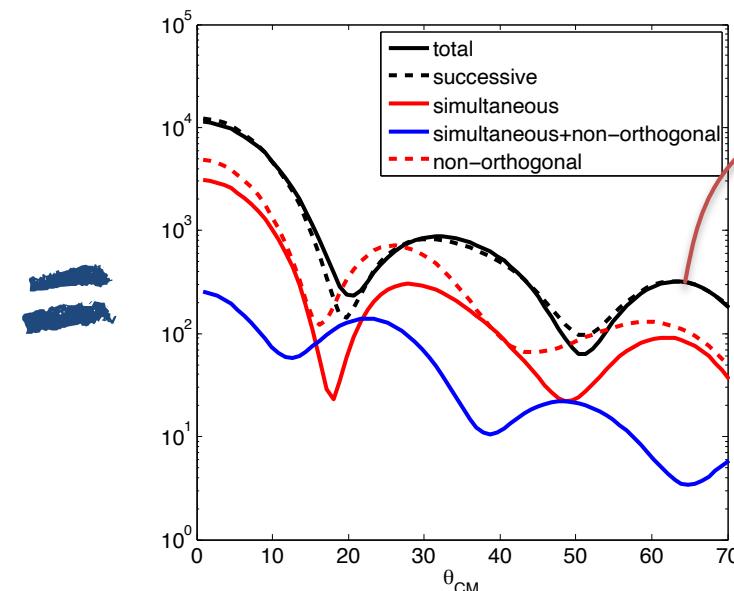
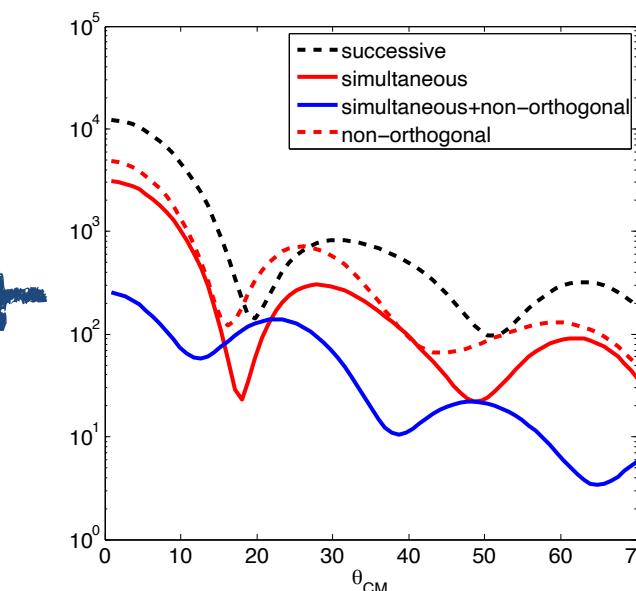
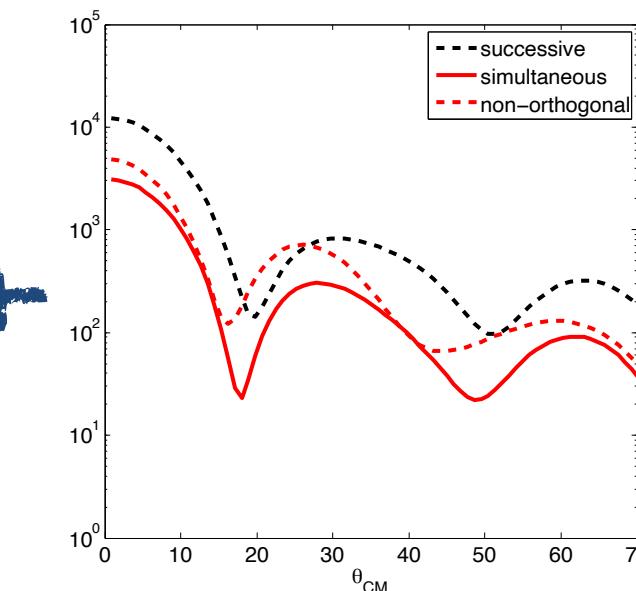
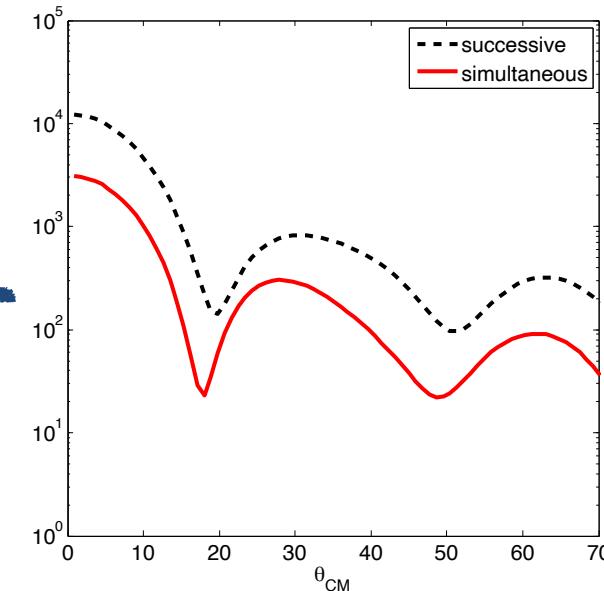
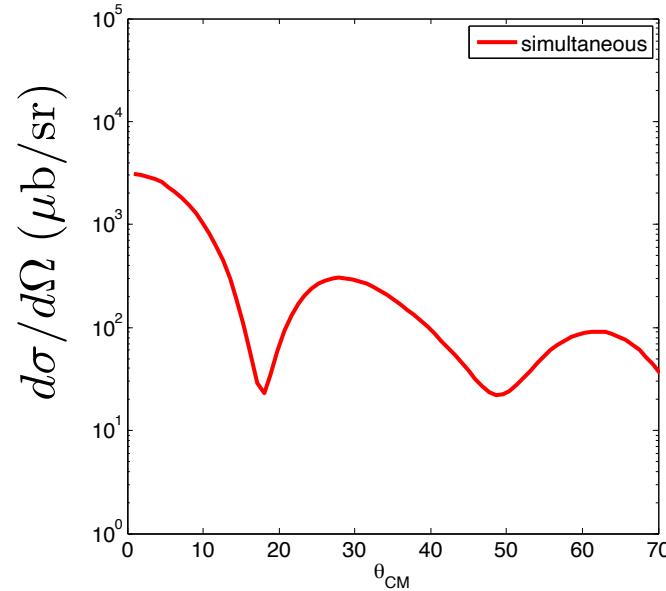


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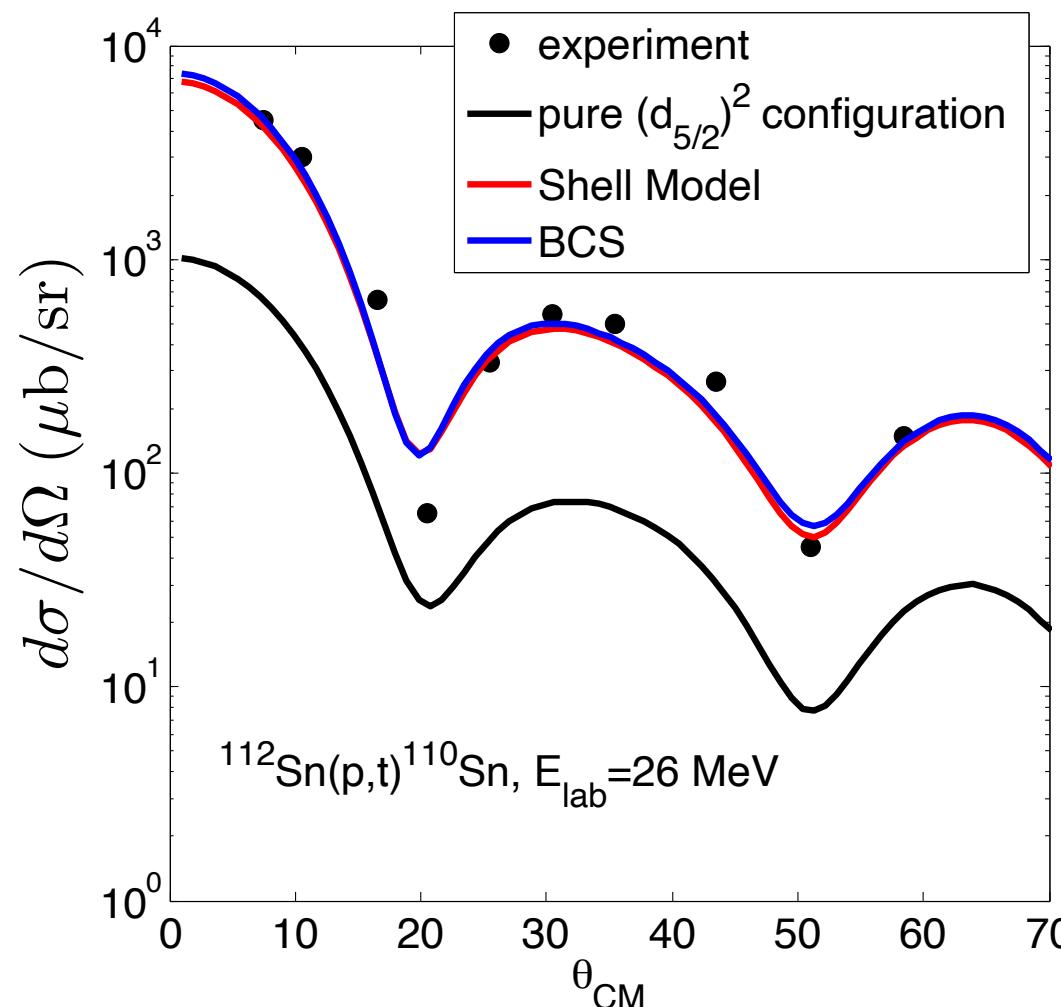
The  $(t,p)$  process is essentially a successive transfer of two correlated neutrons

# Computing $^{112}\text{Sn}(\text{p},\text{t})^{110}\text{Sn}$ in second order DWBA



The  $(\text{t},\text{p})$  process is essentially a **successive** transfer of two **correlated neutrons**

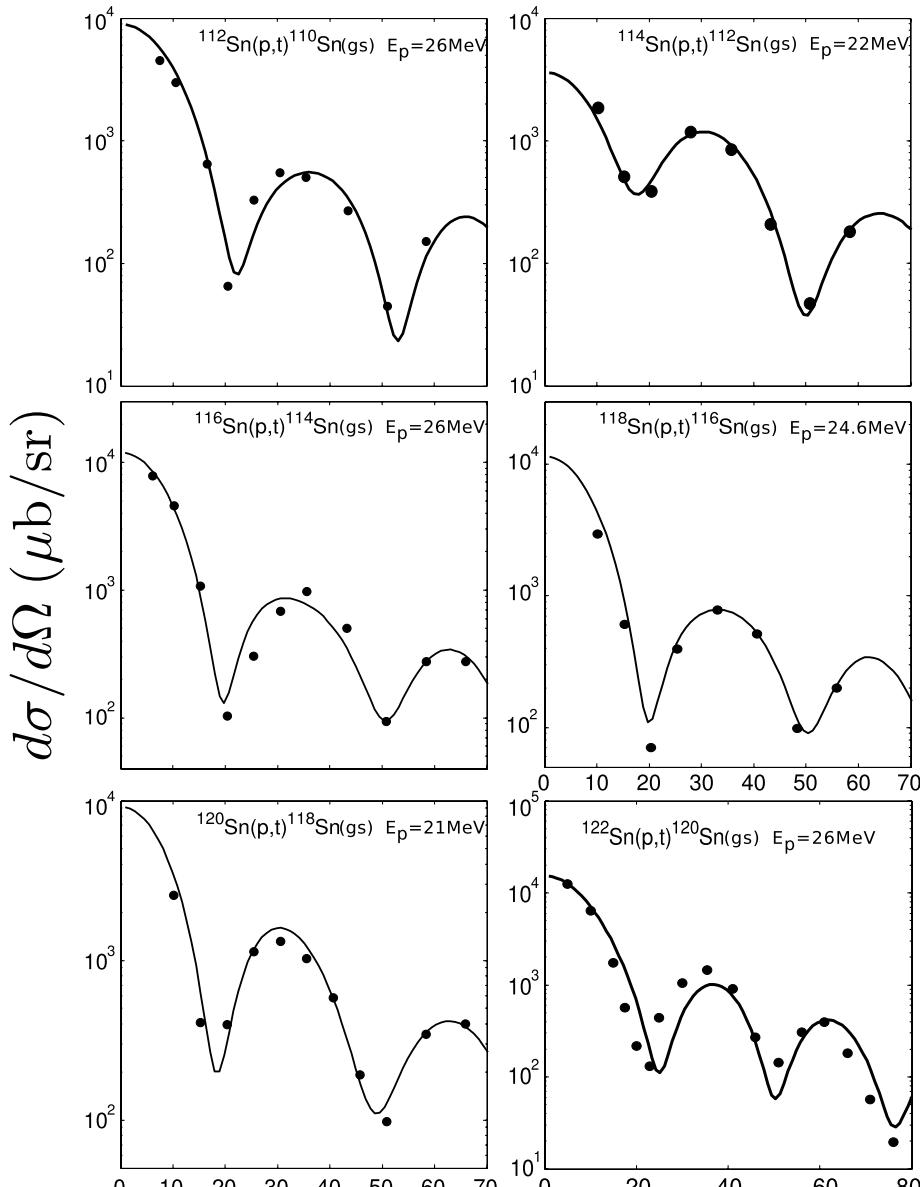
# Theory should account for the *absolute value* of the cross section



enhancement factor with  
respect to the transfer of  
uncorrelated neutrons:  
 $\varepsilon = 20.6$

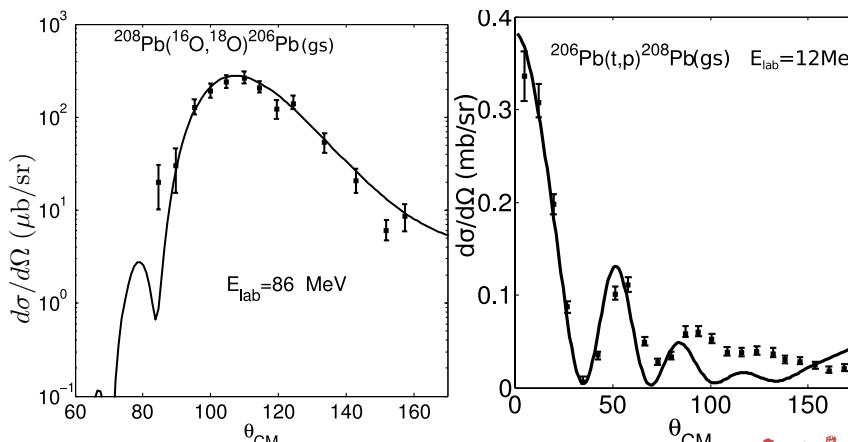
Experimental data and shell model wavefunction from Guazzoni *et al.*  
PRC 74 054605 (2006)

# Reaction+Structure theory works well across the nuclear chart



Sn isotopes (BCS)

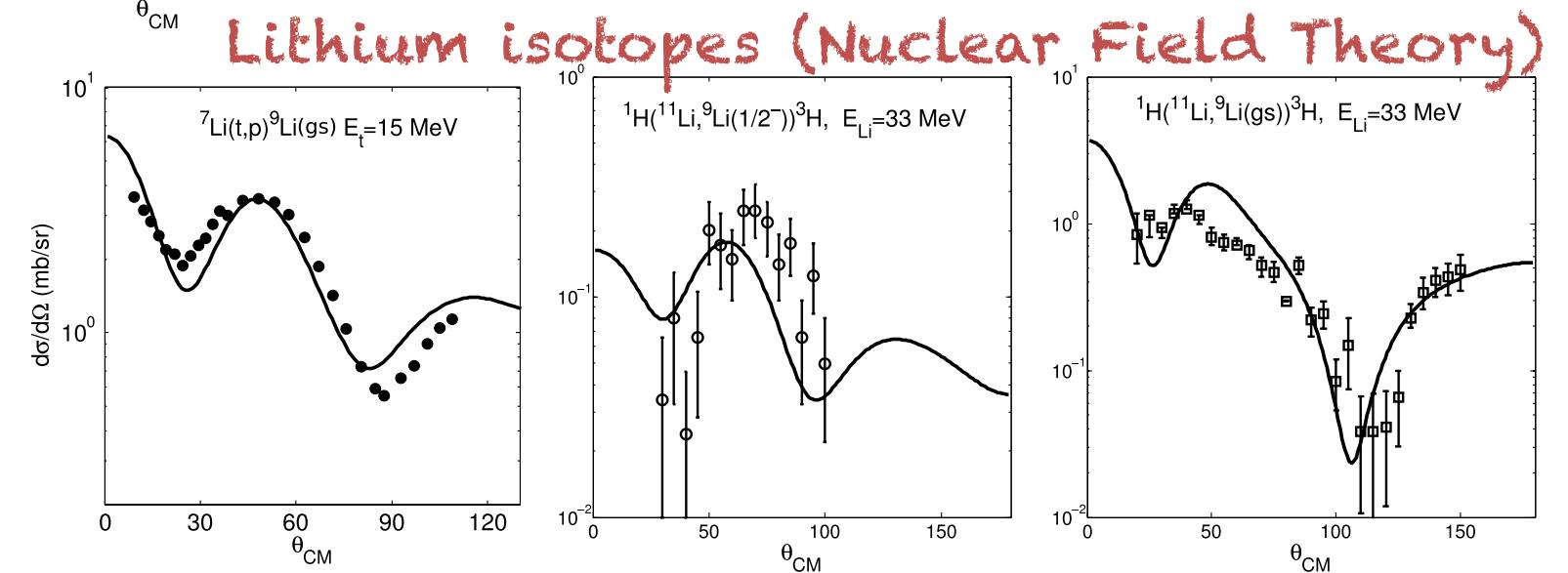
Pb ground state and excited states (QRPA)



Rep. Prog. Phys. **76** (2013) 106301 (21pp)

## Cooper pair transfer in nuclei

G Potel<sup>1</sup>, A Idini<sup>2,3,4</sup>, F Barranco<sup>5</sup>, E Vigezzi<sup>4</sup> and R A Broglia<sup>3,4,6,7</sup>



Lithium isotopes (Nuclear Field Theory)

# Looking for something new in the nuclear spectrum: The Giant Pairing Vibration (GPV)

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Volume 69B, number 2

PHYSICS LETTERS

1 August 1977

## HIGH-LYING PAIRING RESONANCES\*

R.A. BROGLIA

*The Niels Bohr Institute, University of Copenhagen, DK-2100 Copenhagen Ø, Denmark<sup>1</sup>  
State University of New York, Department of Physics, Stony Brook, New York 11794, USA*

and

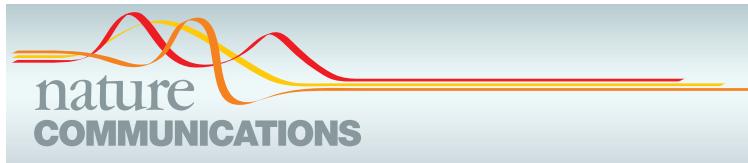
D.R. BES<sup>2</sup>

*NORDITA, DK-2100 Copenhagen Ø, Denmark*

Pairing vibrations based on the excitation of pairs of particles and holes across major shells are predicted at an excitation energy of about  $70/A^{1/3}$  MeV and carrying a cross section which is 20%–100% the ground state cross section.

Collective pairing mode predicted almost 50 years ago, awaiting experimental confirmation?

# (t,p) is an ideal process to populate the elusive Giant Pairing Vibration



## ARTICLE

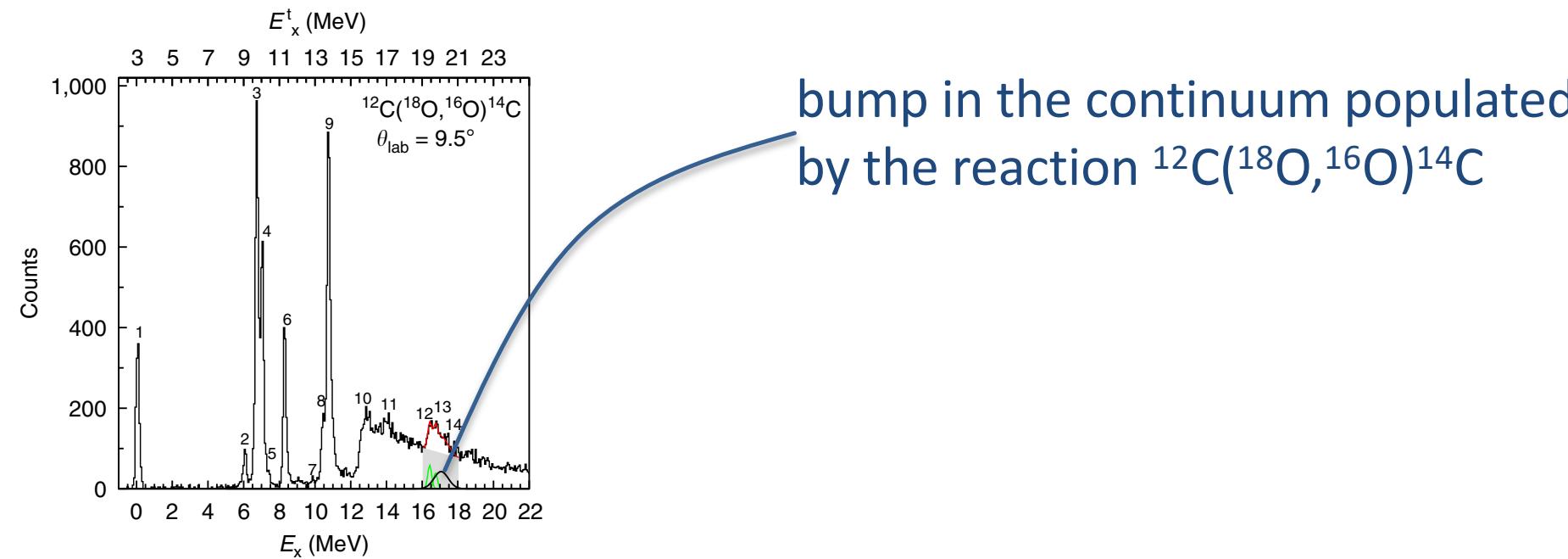
Received 28 Dec 2014 | Accepted 24 Feb 2015 | Published 27 Mar 2015

DOI: 10.1038/ncomms7743

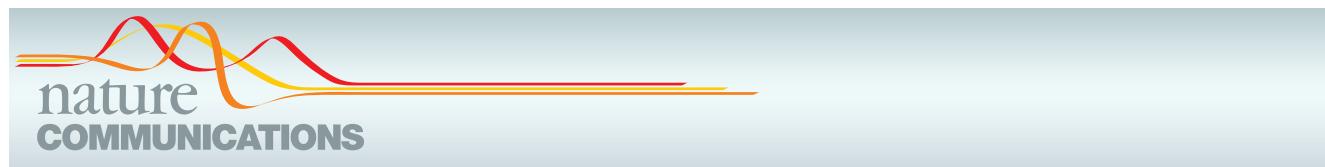
OPEN

## Signatures of the Giant Pairing Vibration in the $^{14}\text{C}$ and $^{15}\text{C}$ atomic nuclei

F. Cappuzzello<sup>1,2</sup>, D. Carbone<sup>2</sup>, M. Cavallaro<sup>2</sup>, M. Bondi<sup>1,2</sup>, C. Agodi<sup>2</sup>, F. Azaiez<sup>3</sup>, A. Bonaccorso<sup>4</sup>, A. Cunsolo<sup>2</sup>, L. Fortunato<sup>5,6</sup>, A. Foti<sup>1,7</sup>, S. Franchoo<sup>3</sup>, E. Khan<sup>3</sup>, R. Linares<sup>8</sup>, J. Lubian<sup>8</sup>, J.A. Scarpaci<sup>9</sup> & A. Vitturi<sup>5,6</sup>



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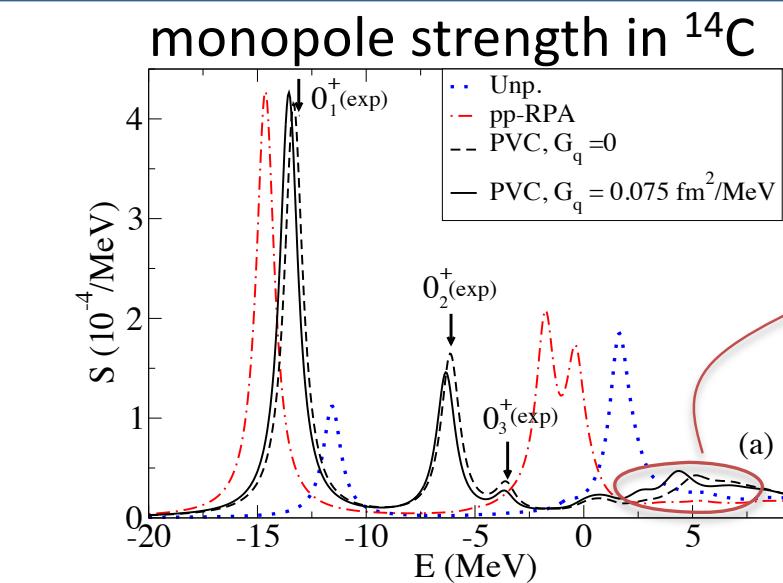
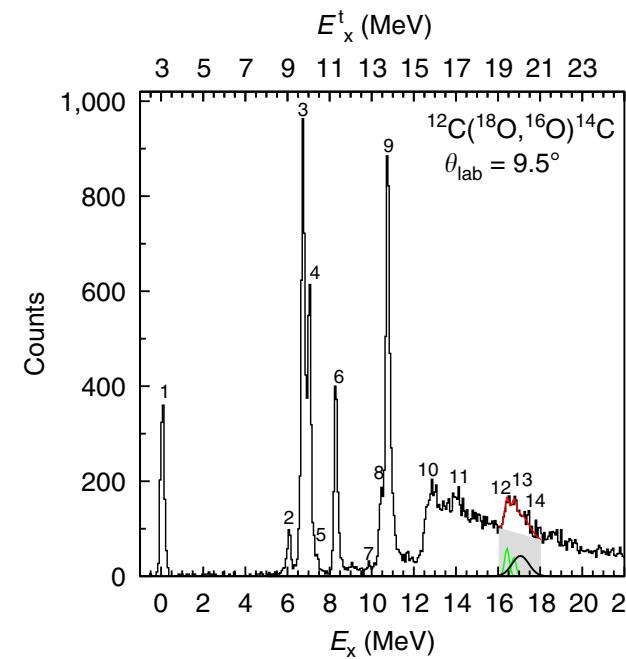
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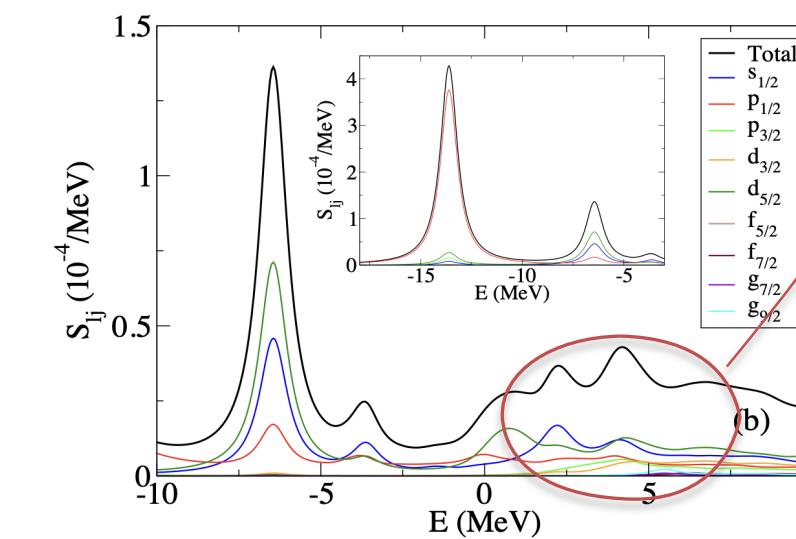
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we predict a rather broad  
structure in the continuum

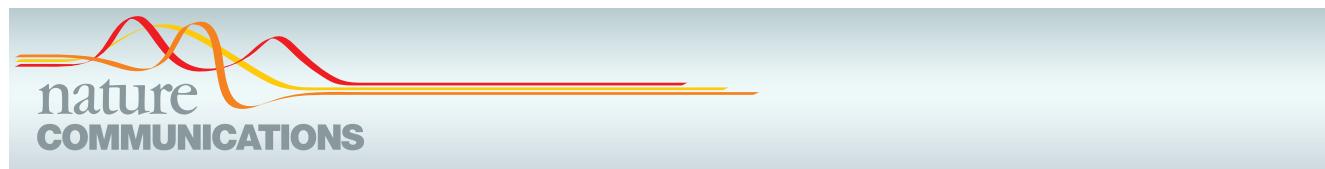


PHYSICAL REVIEW LETTERS 134, 062501 (2025)

## Fragmentation of the Giant Pairing Vibration in $^{14}\text{C}$ Induced by Many-Body Processes

F. Barranco<sup>1</sup>, G. Potel<sup>1,2</sup> and E. Vigezzi<sup>3</sup>

# (t,p) is an ideal process to populate the elusive Giant Pairing Vibration



ARTICLE

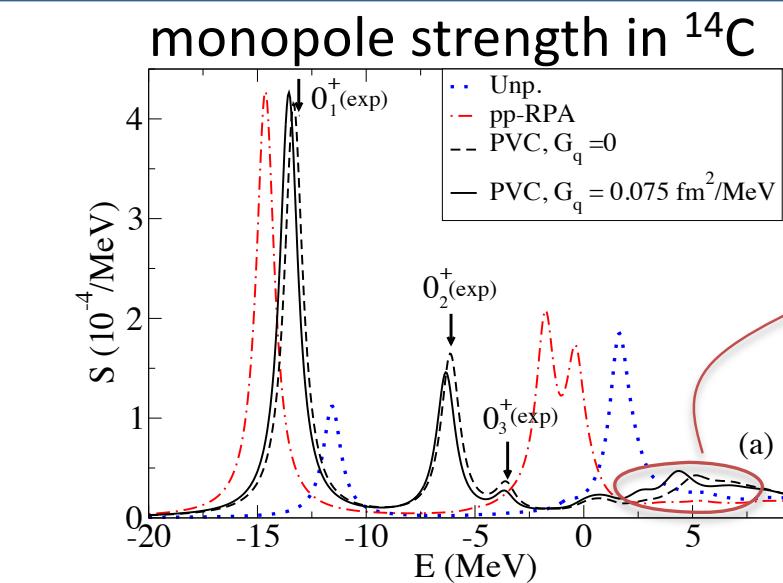
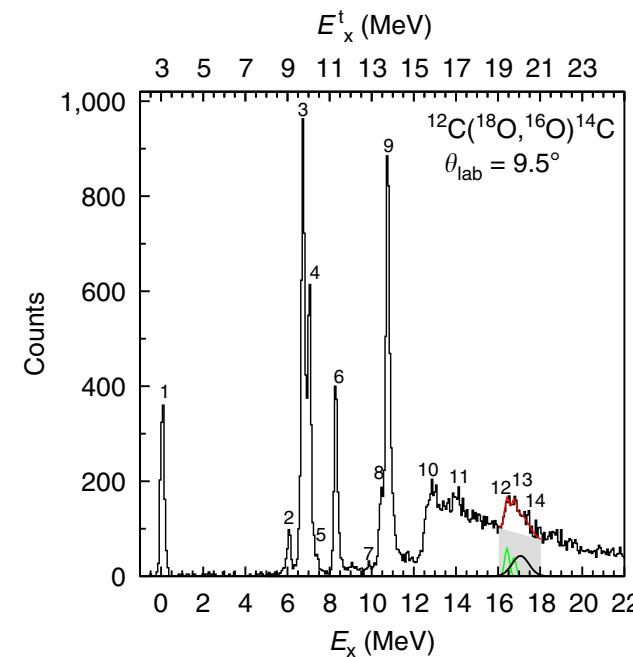
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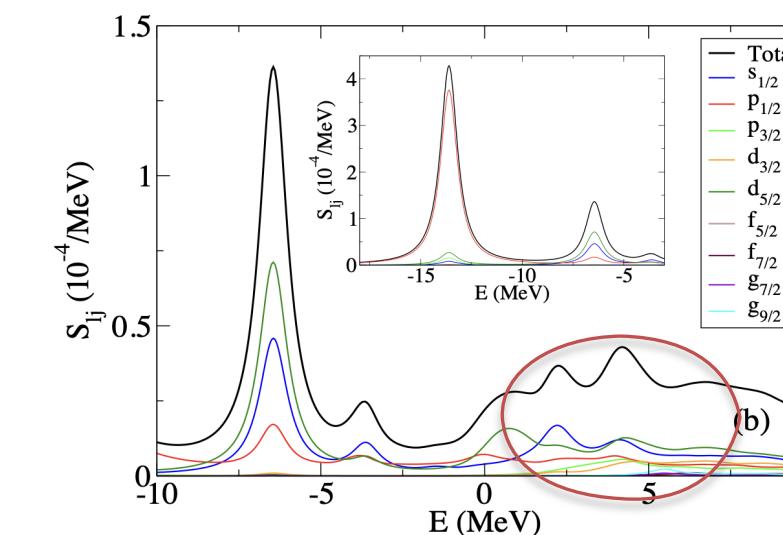
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we predict a rather broad structure in the continuum



working on a theoretical estimate of  $^{12}\text{C}(\text{t},\text{p})^{14}\text{C}(\text{GPV})$

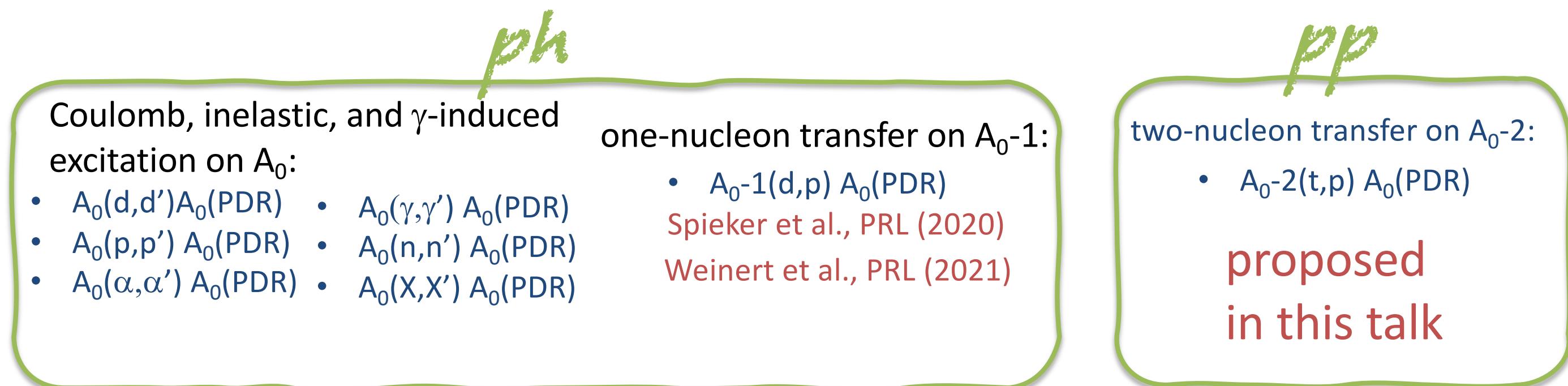
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F. Barranco<sup>1</sup>, G. Potel<sup>1,2</sup> and E. Vigezzi<sup>3</sup>

# The Pygmy Dipole Resonance (PDR) as a two-quasiparticle mode

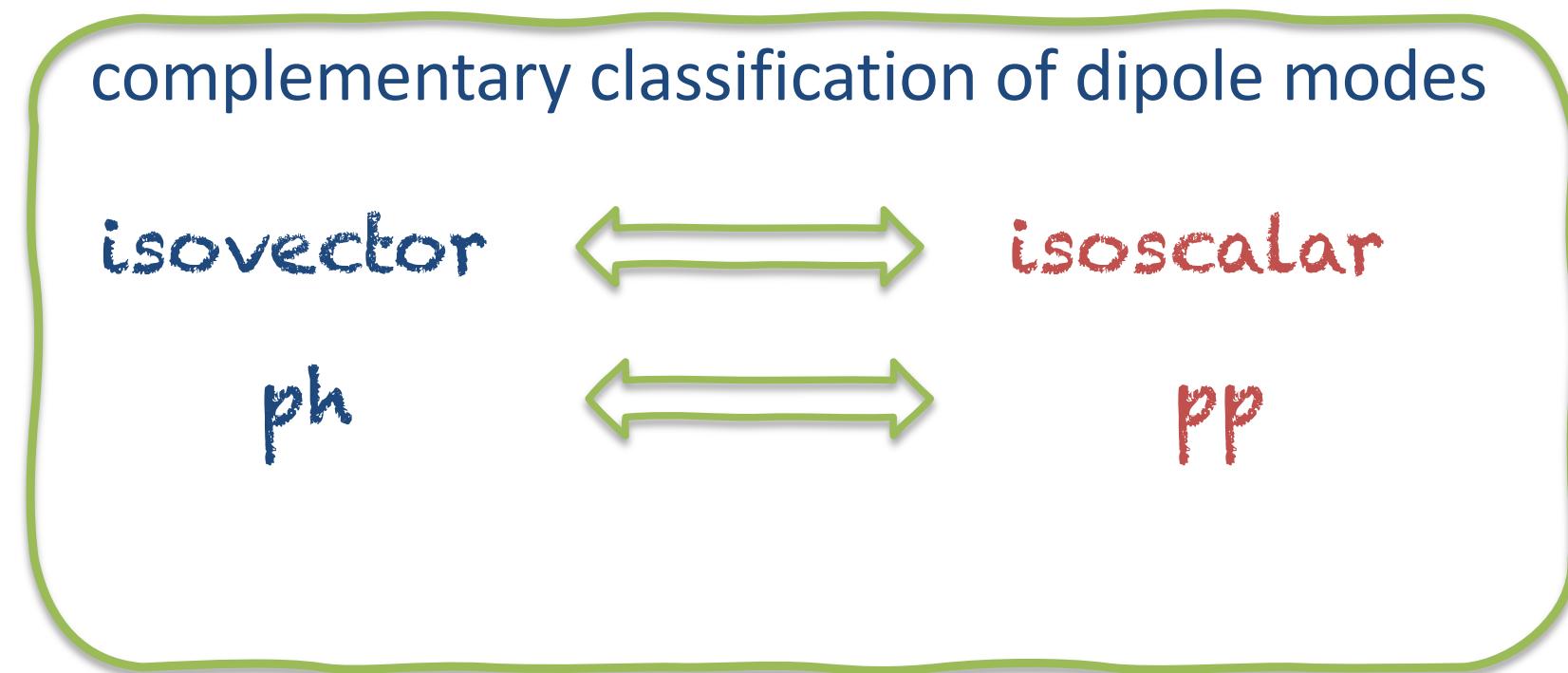
- The PDR is rather well described in the harmonic approximation (RPA, QRPA) as a two-quasiparticle mode.
- Therefore, PDR in a nucleus  $A_0$  can be better probed with two-quasiparticle fields, i.e., particle-hole ( $ph$ ), particle-particle ( $pp$ ), and hole-hole ( $hh$ ) fields.



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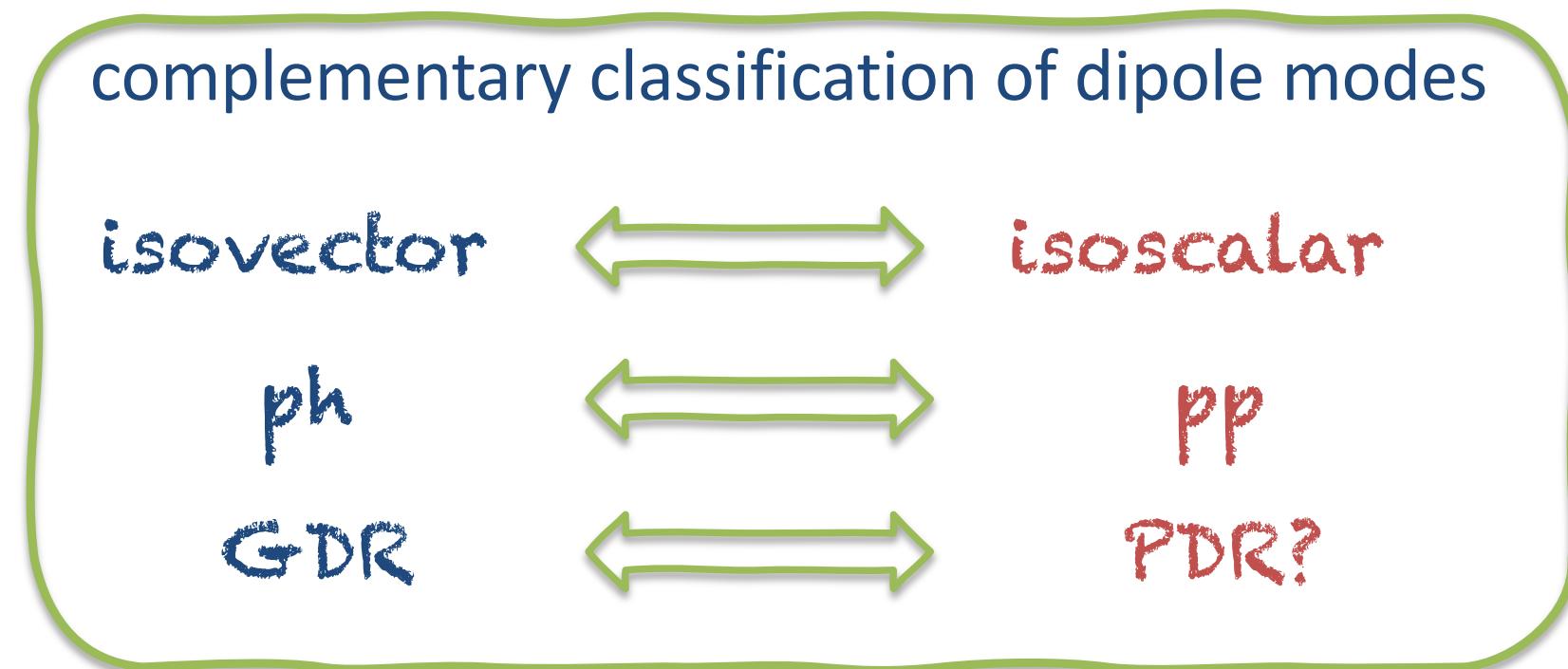
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# Probing the $^{11}\text{Li}$ PDR with 2-neutron transfer

Eur. Phys. J. A (2019) 55: 243  
DOI 10.1140/epja/i2019-12789-y

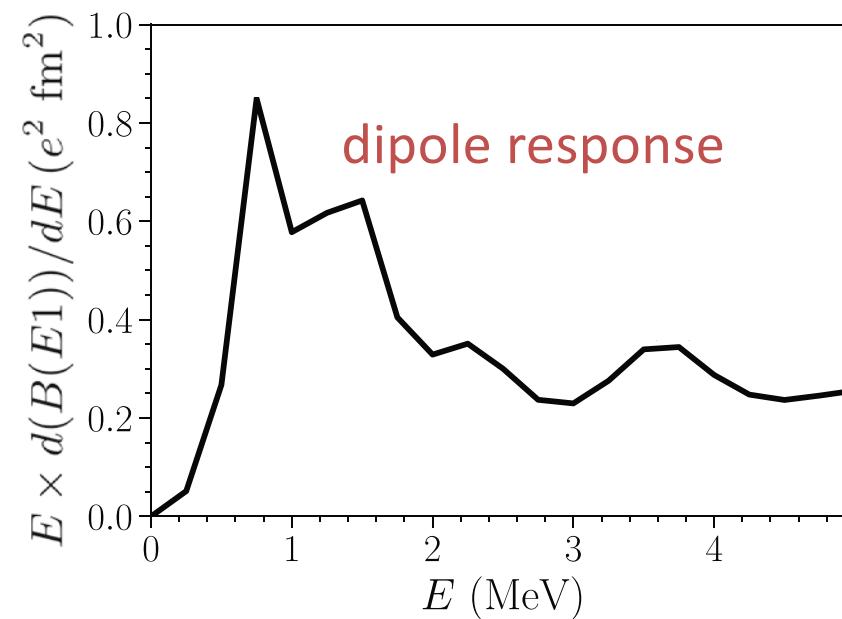
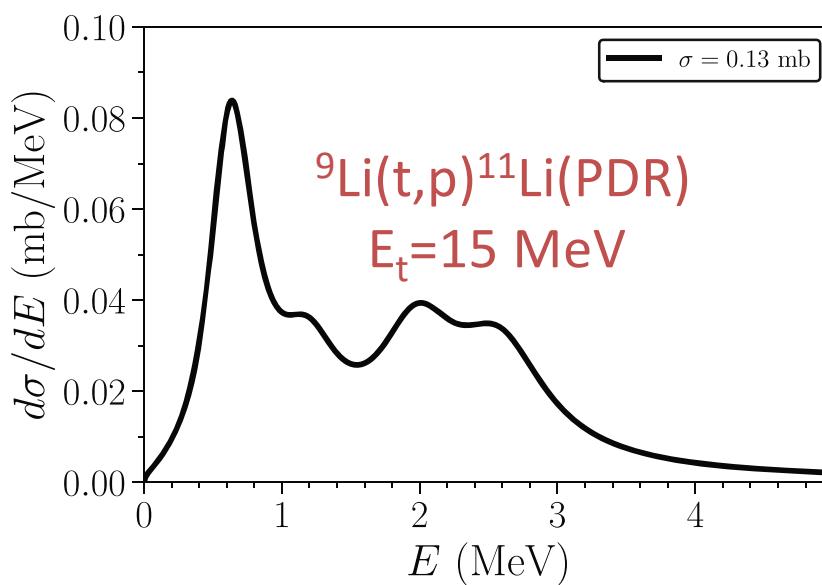
THE EUROPEAN  
PHYSICAL JOURNAL A

Regular Article – Theoretical Physics

EUROPEAN ORGANIZATION FOR NUCLEAR RESEARCH

## Characterization of vorticity in pygmy resonances and soft-dipole modes with two-nucleon transfer reactions\*

R.A. Broglia<sup>1,2</sup>, F. Barranco<sup>3</sup>, G. Potel<sup>4,a</sup>, and E. Vigezzi<sup>5</sup>



Probing the  $^{11}\text{Li}$  low-lying dipole strength via  $^{9}\text{Li}(\text{t},\text{p})$  with the ISS

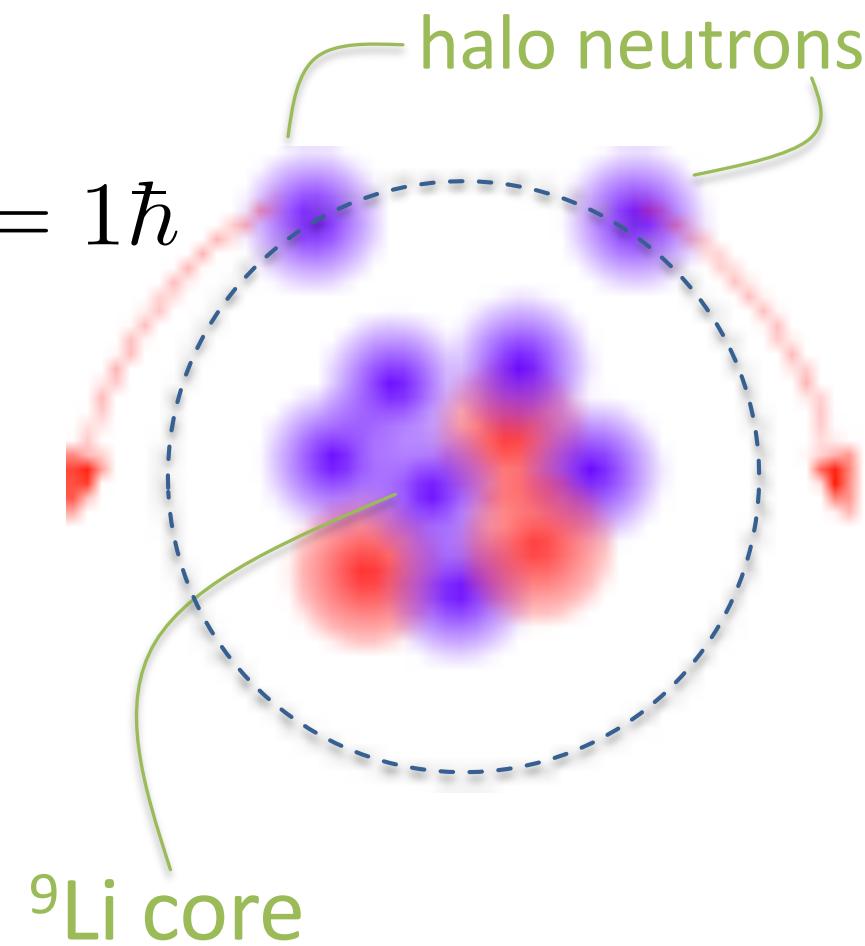
Y. Ayyad<sup>1</sup>, E. Vigezzi<sup>2</sup>, G. Potel<sup>3</sup>, R. Broglia<sup>4,5</sup>, B.P. Kay<sup>6</sup>,  
A.O. Macchiavelli<sup>7</sup>, H. Alvarez-Pol<sup>8</sup>, F. Barranco<sup>9</sup>, D. Bazin<sup>1,10</sup>, M. Caamaño<sup>8</sup>,  
A. Ceulemans<sup>11</sup>, J. Chen<sup>1</sup>, H.L. Crawford<sup>7</sup>, B. Fernández-Domínguez<sup>8</sup>, S.J. Freeman<sup>12</sup>,  
L.P. Gaffney<sup>13</sup>, C.R. Hoffman<sup>6</sup>, R. Kanungo<sup>14</sup>, C. Morse<sup>7</sup>, O. Poleshchuk<sup>11</sup>, R. Raabe<sup>11</sup>,  
C.A. Santamaría<sup>7</sup>, D.K. Sharp<sup>12</sup>, T. L. Tang<sup>6</sup>, K. Wimmer<sup>15</sup>, A.H. Wuosmaa<sup>16</sup>

experiment approved at ISOLDE facility  
(CERN). Spokepersons: Ayyad, Vigezzi

# the $^{11}\text{Li}$ PDR has the structure of an elementary quantum vortex

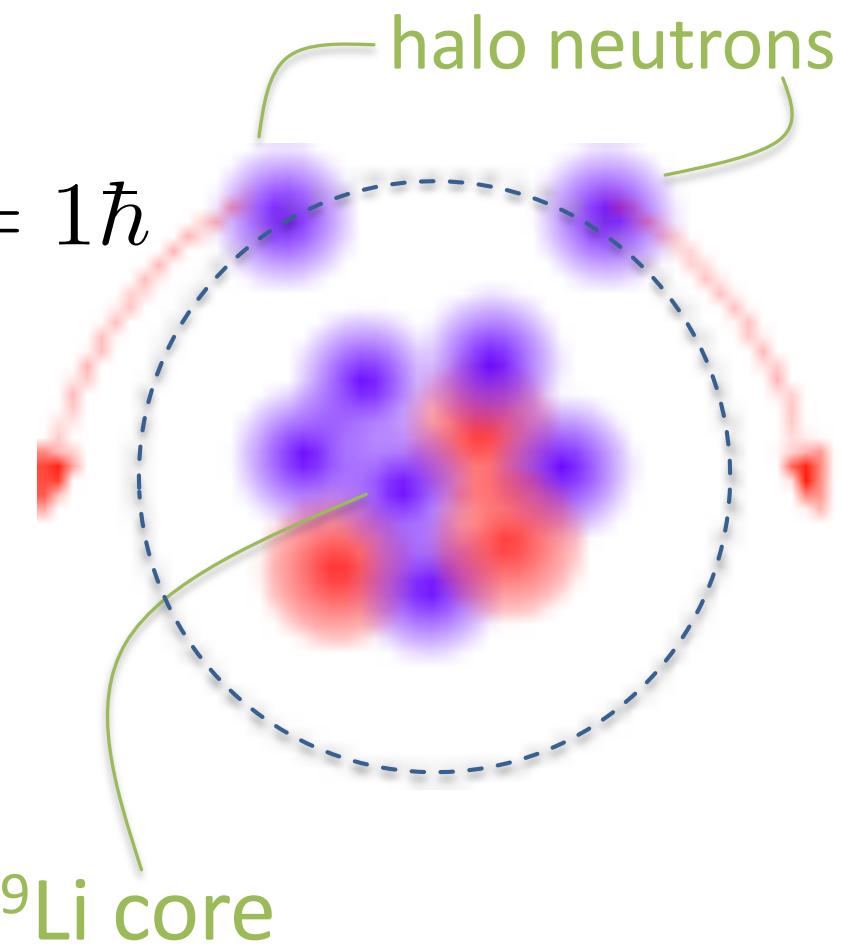
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structure of a multipolar ( $1^-$ ) Cooper pair:  
elementary quantum vortex



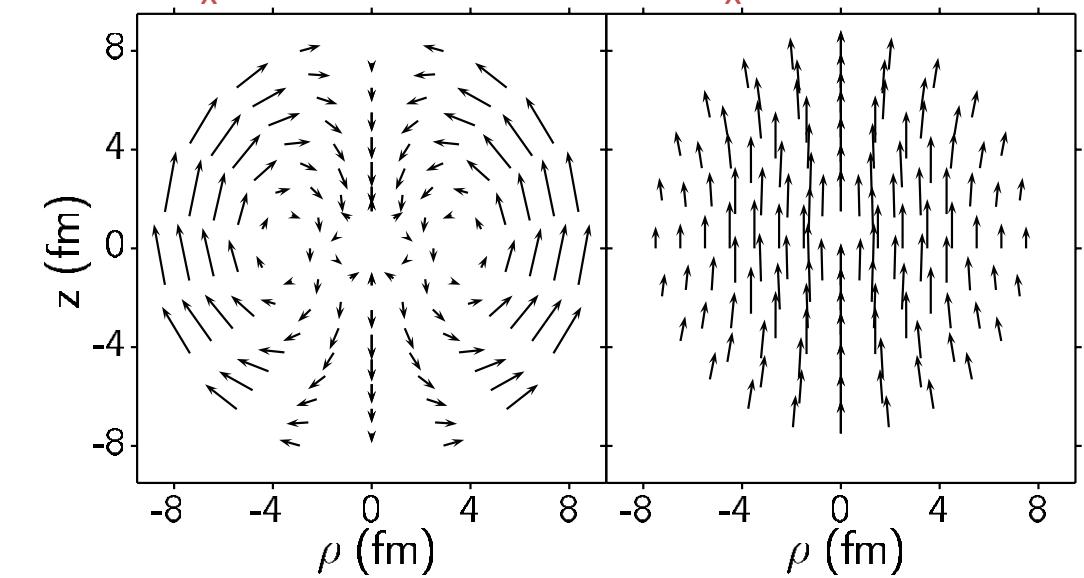
# the $^{11}\text{Li}$ PDR has the structure of an elementary quantum vortex

structure of a multipolar ( $1^-$ ) Cooper pair:  
elementary quantum vortex



velocity field of  $^{208}\text{Pb}$  dipole states

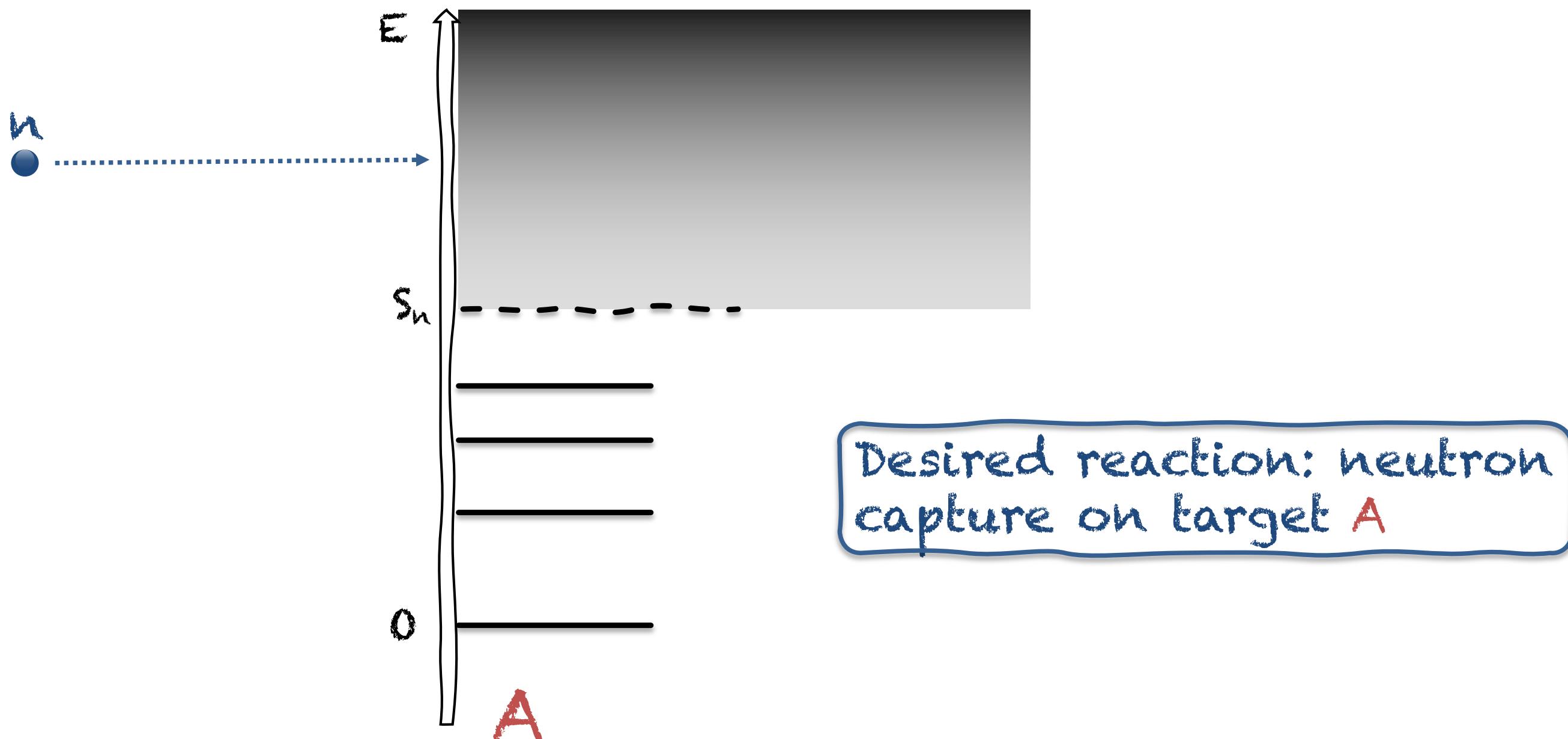
$E_x = 6.5\text{-}10.5 \text{ MeV}$        $E_x > 10.5 \text{ MeV}$



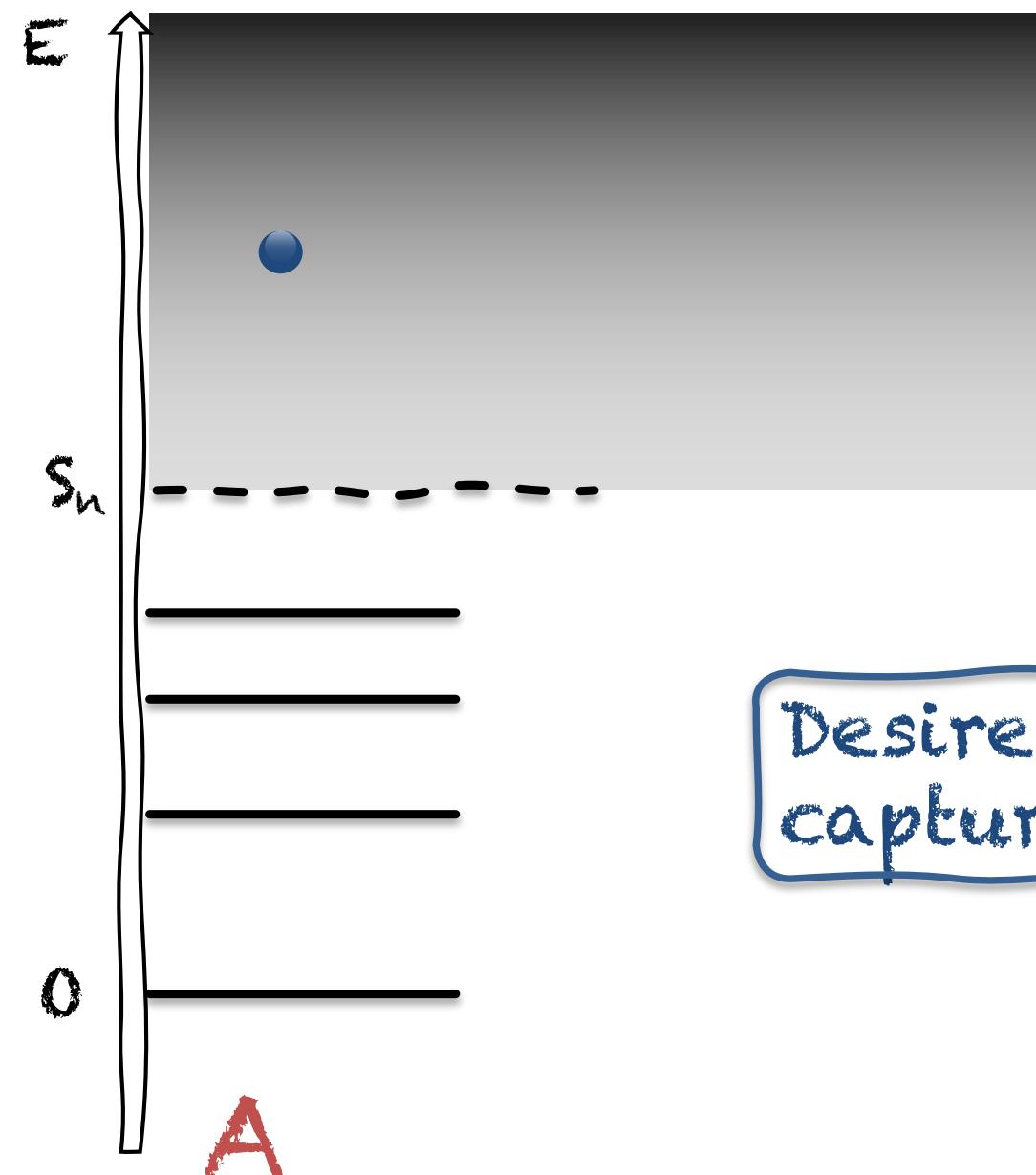
Ryezayeva *et al.* PRL 89 (2002) 272502

- Is vorticity a signature of PDR?
- Is there an experimental signature for it?

# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(\text{n},\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(\text{d,p}\gamma){}^{A+1}\text{X}$

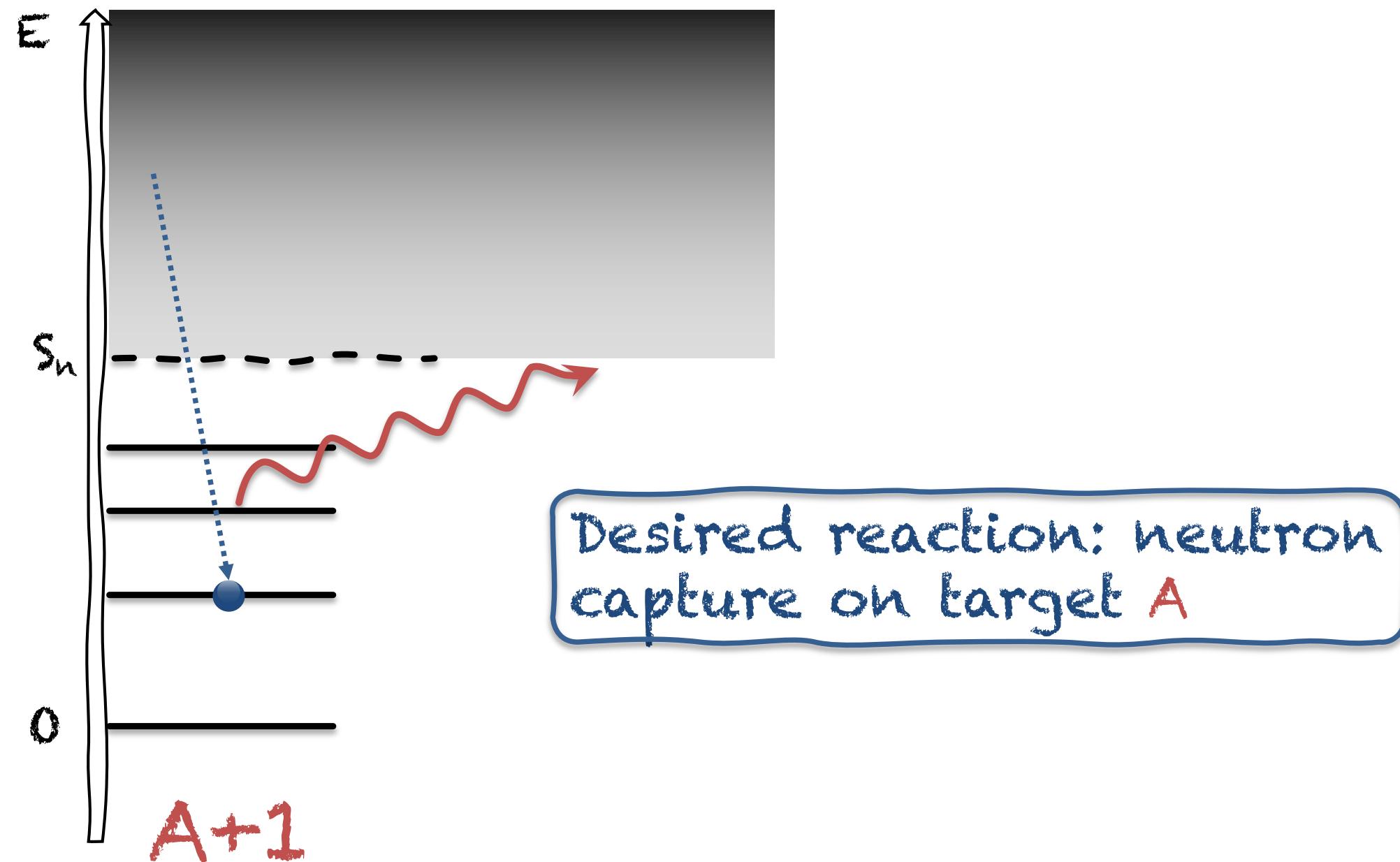


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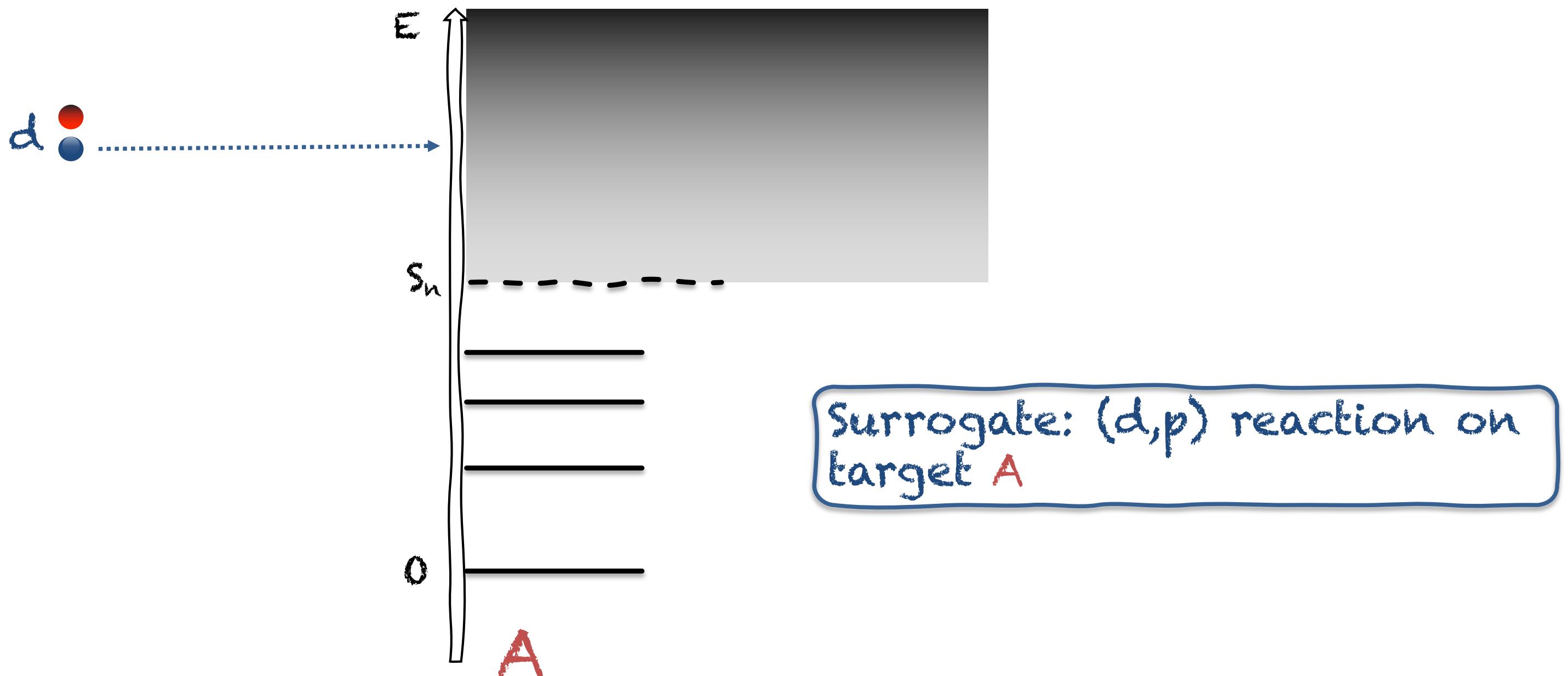


Desired reaction: neutron capture on target A

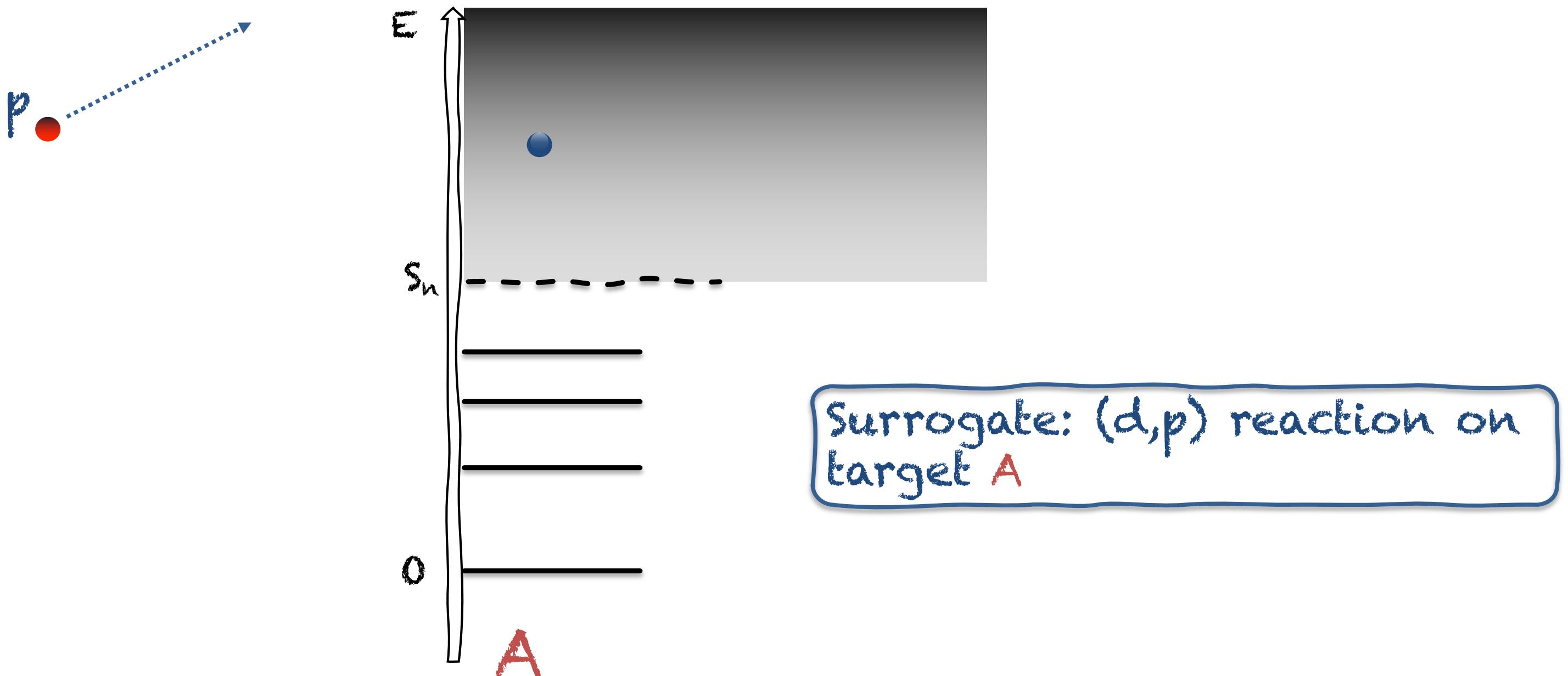
# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(\text{n},\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(\text{d,p}\gamma){}^{A+1}\text{X}$



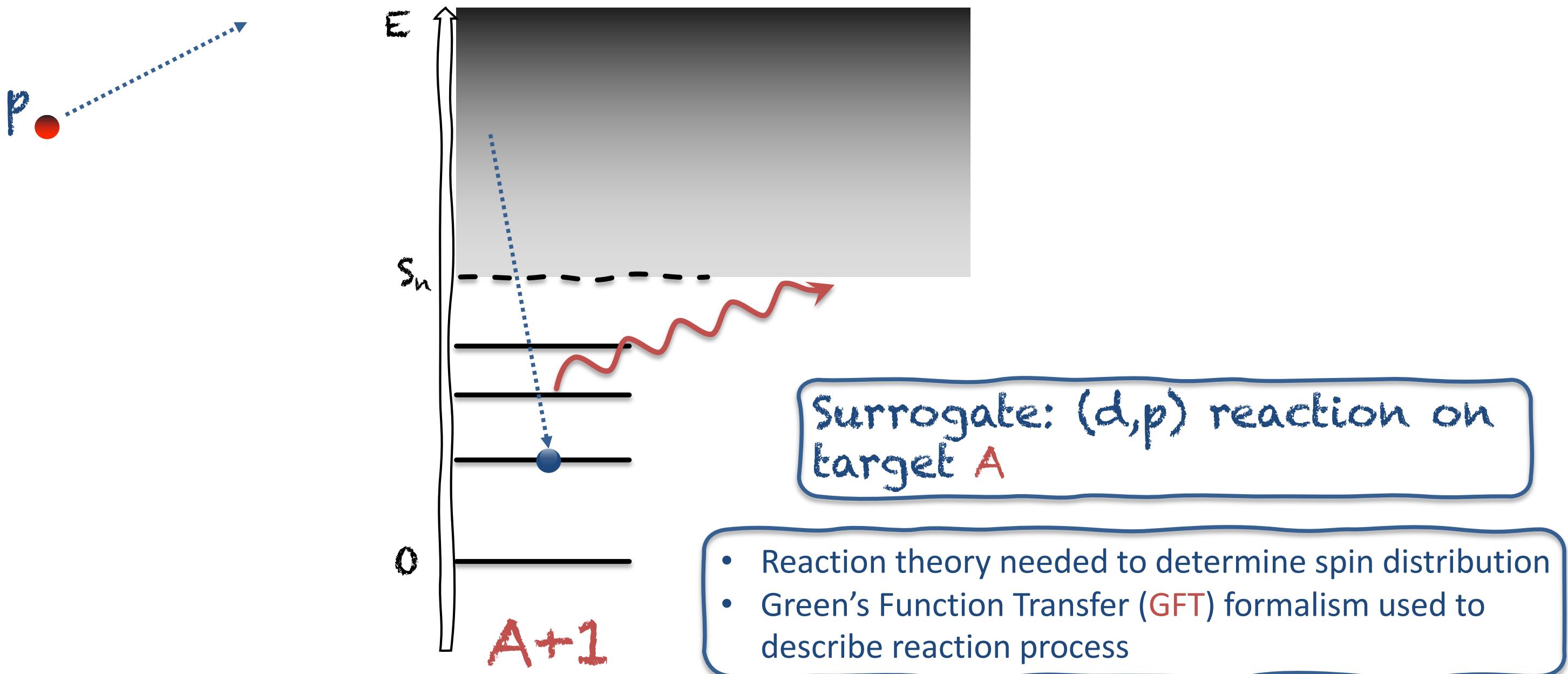
# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(\text{n},\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(\text{d,p}\gamma){}^{A+1}\text{X}$



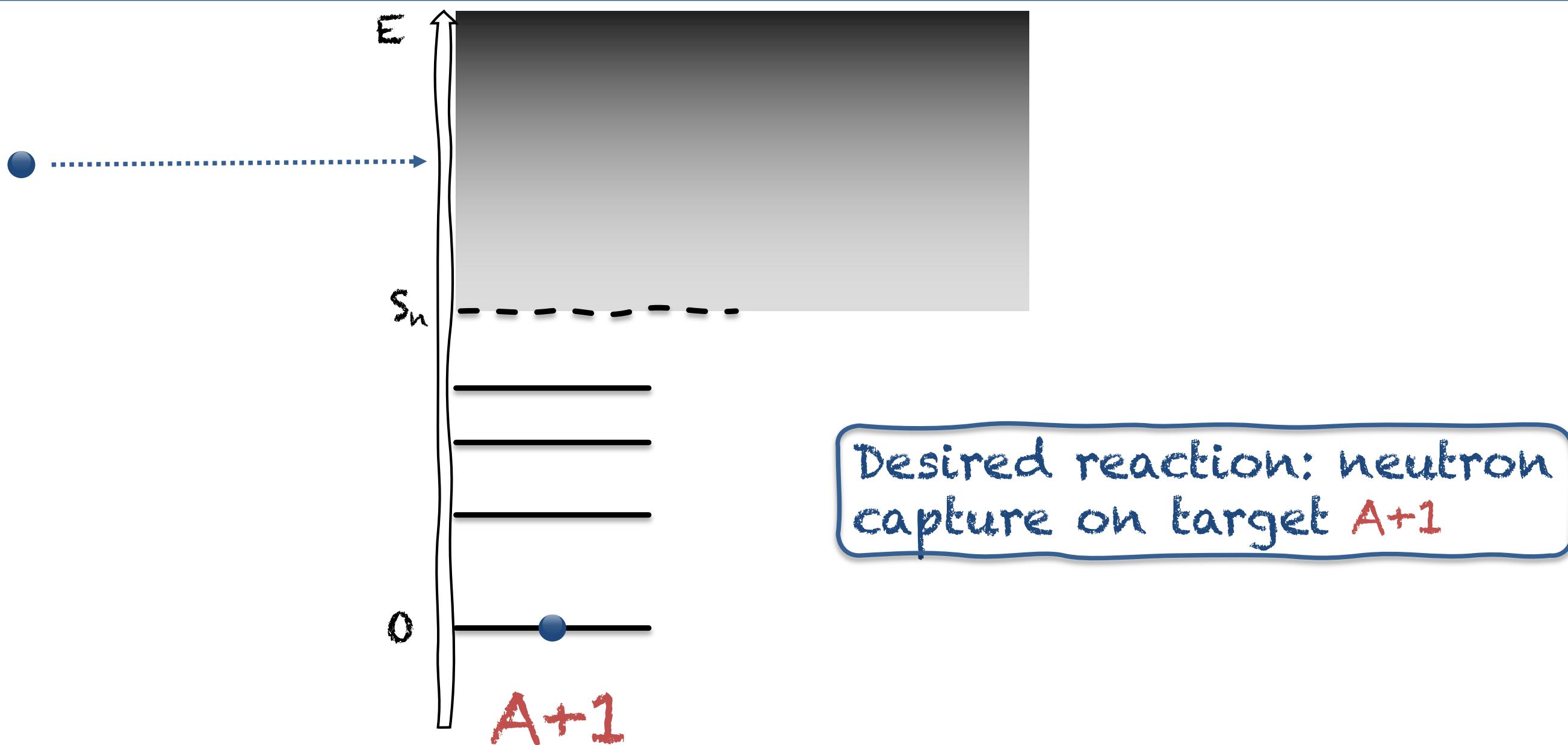
# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(\text{n},\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(\text{d,p}){}^{A+1}\text{X}$



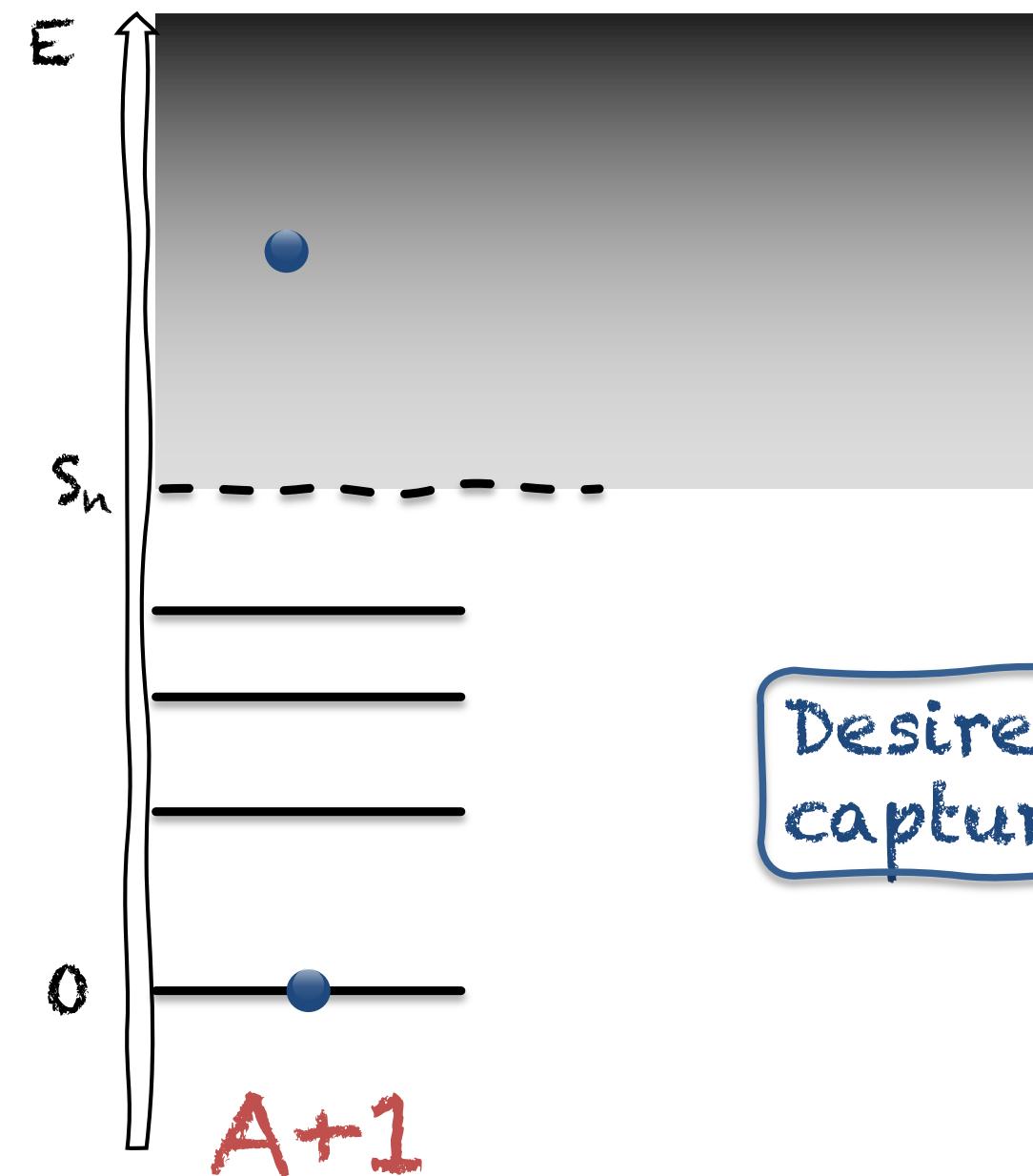
# Using the Surrogate Reaction Method (SRM) to infer ${}^A\text{X}(n,\gamma){}^{A+1}\text{X}$ from ${}^A\text{X}(d,p\gamma){}^{A+1}\text{X}$



## Using the SRM to infer ${}^{A+1}X(n,\gamma){}^{A+2}X$ from ${}^AX(t,p\gamma){}^{A+2}X$

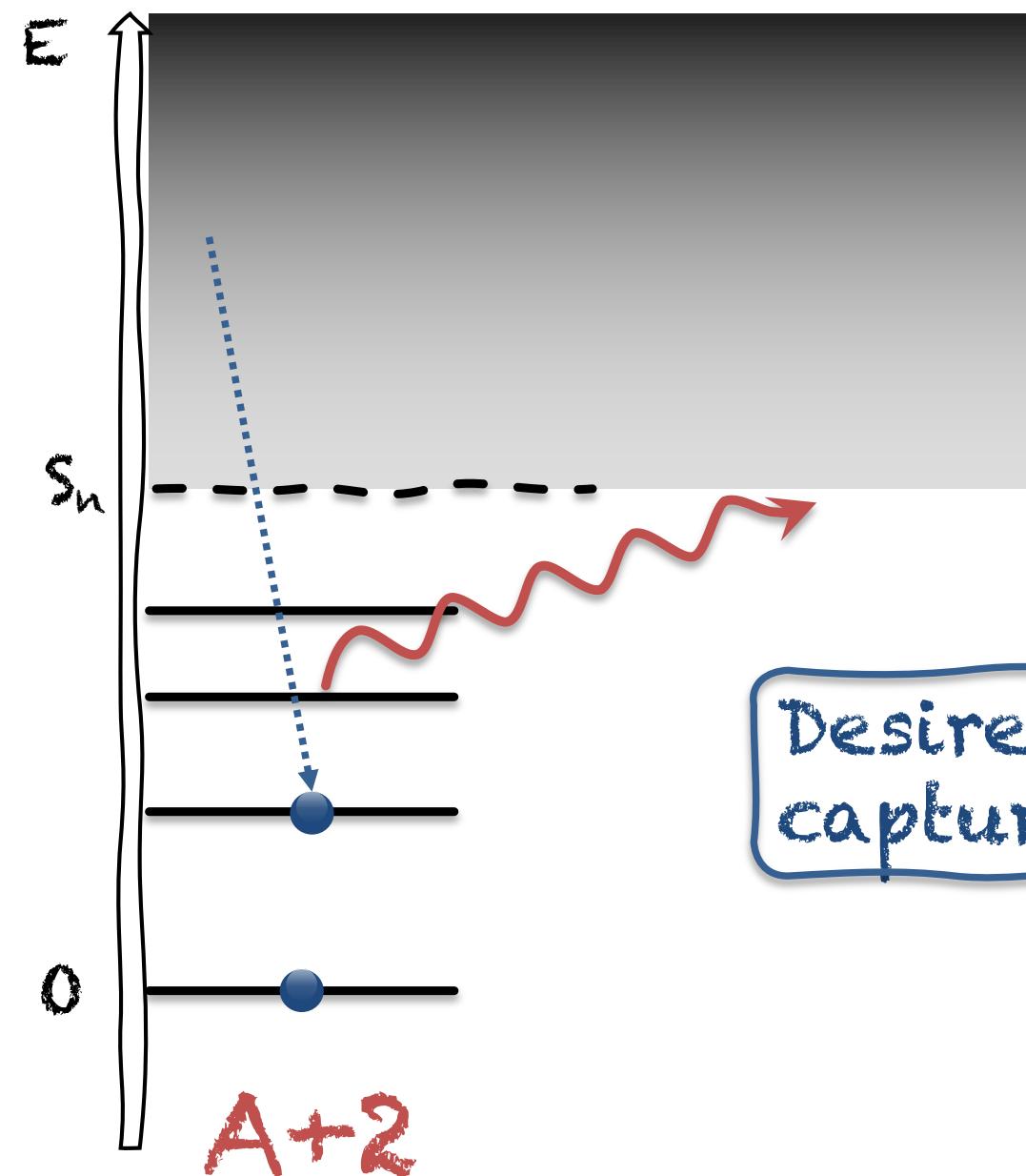


## Using the SRM to infer ${}^{A+1}X(n,\gamma){}^{A+2}X$ from ${}^AX(t,p\gamma){}^{A+2}X$



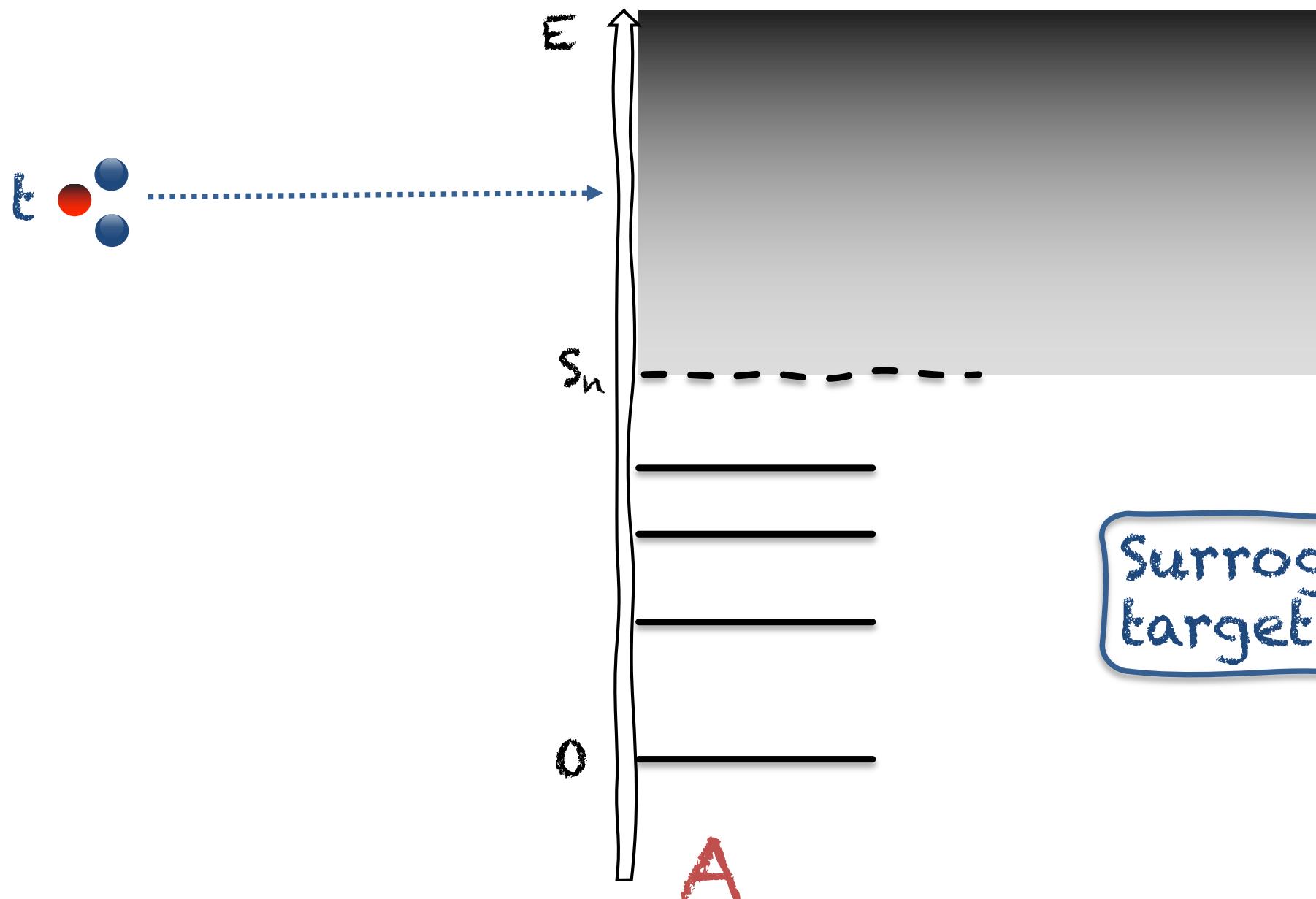
Desired reaction: neutron capture on target  $A+1$

## Using the SRM to infer ${}^{A+1}X(n,\gamma){}^{A+2}X$ from ${}^AX(t,p\gamma){}^{A+2}X$



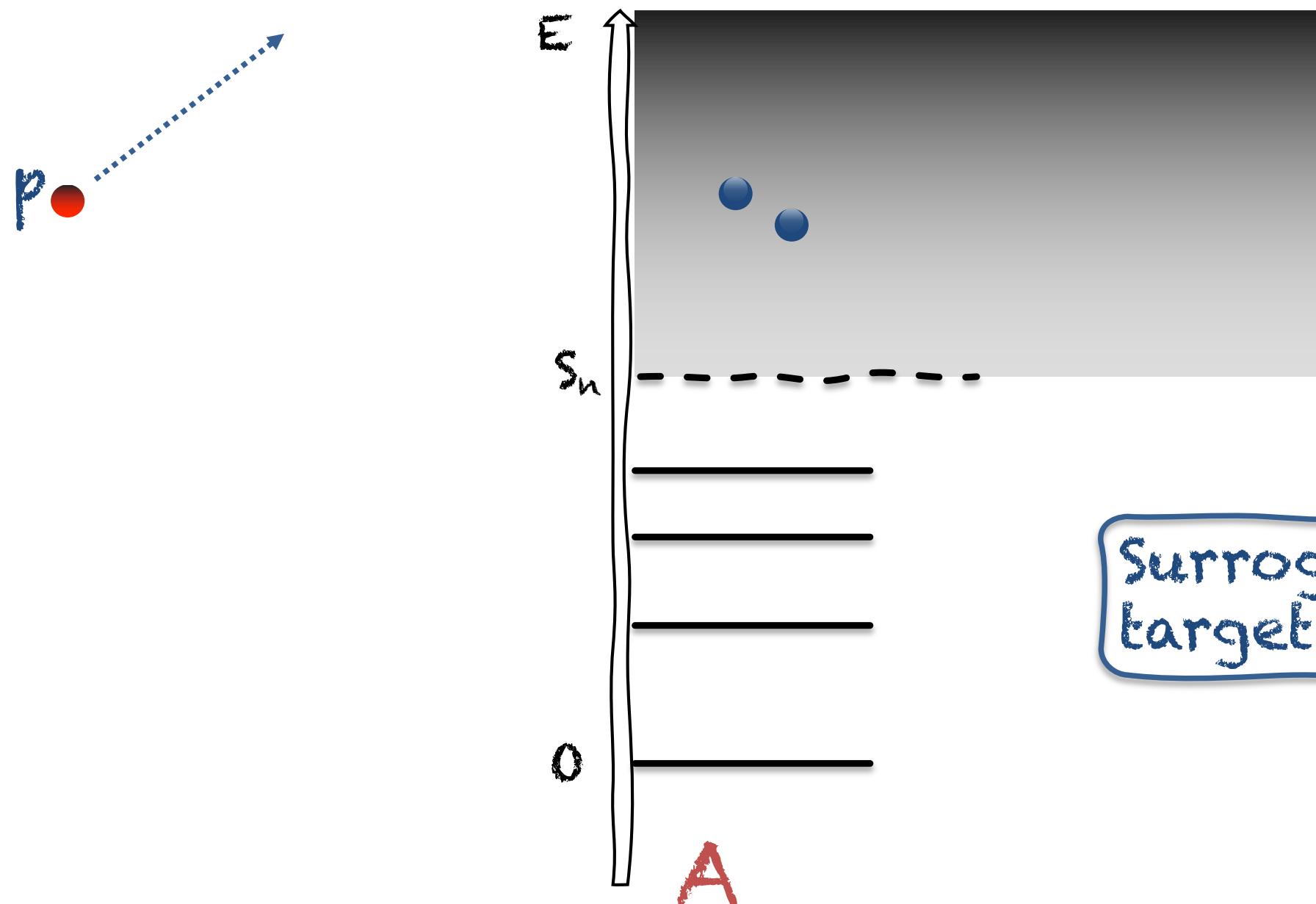
Desired reaction: neutron capture on target  $A+1$

## Using the SRM to infer $^{A+1}X(n,\gamma)^{A+2}X$ from $^AX(t,p\gamma)^{A+2}X$



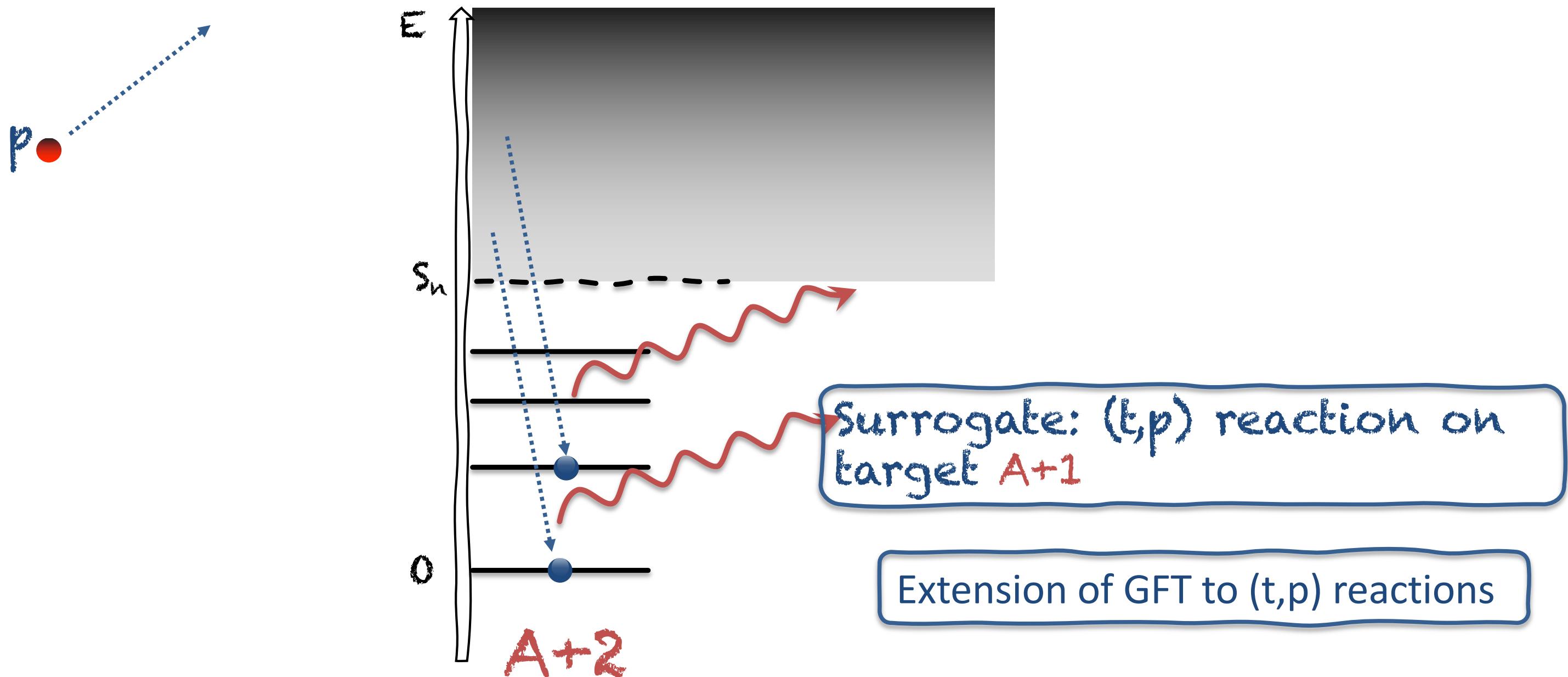
Surrogate:  $(t,p)$  reaction on target  $A+1$

## Using the SRM to infer $^{A+1}X(n,\gamma)^{A+2}X$ from $^AX(t,p\gamma)^{A+2}X$



Surrogate:  $(t,p)$  reaction on target  $A+1$

# Using the SRM to infer $^{A+1}X(n,\gamma)^{A+2}X$ from $^AX(t,p\gamma)^{A+2}X$



# Conclusions

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- Pairing correlations leading to particle-number symmetry breaking are ubiquitous in Fermionic systems.
- In nuclei, (t,p) reactions are the specific probe of pairing correlations.
- Some interesting applications:
  - population of the GPV
  - population of the PDR ( ${}^9\text{Li}(t,p){}^{11}\text{Li}$ (PDR) @ ISOLDE)
  - surrogate reactions

---

## Collaborators:

- E. Vigezzi (INFN, Milano)
- F. Barranco (University of Seville)
- Y. Ayyad (IGFAE, USC)

# Thank you!

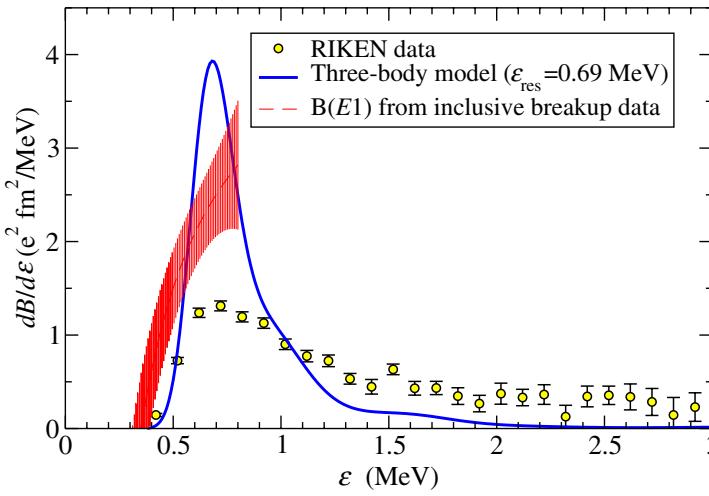


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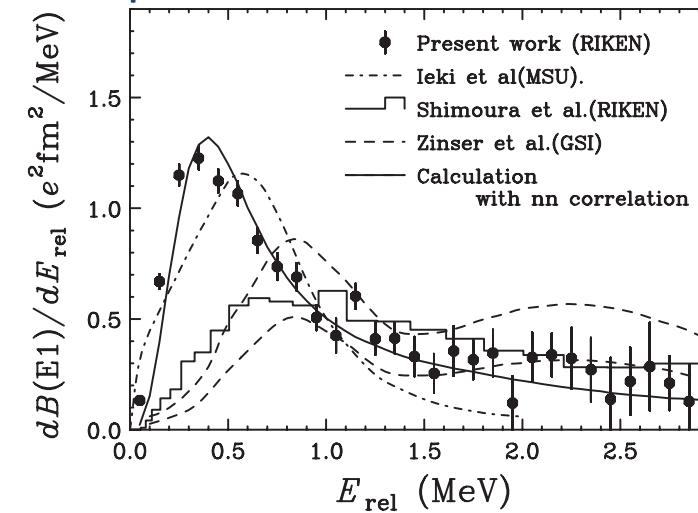
# **BACKUP SLIDES**

# Is there a pygmy resonance in $^{11}\text{Li}$ ? What's its structure?

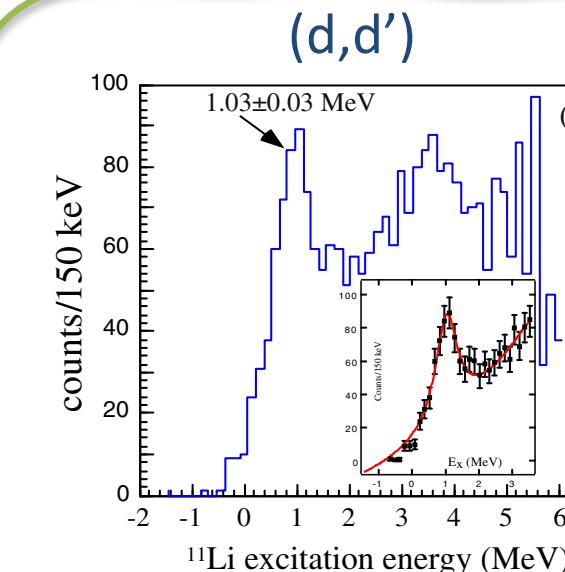
## Coulomb breakup



Fernández *et al.* PRL **110**, 142701 (2013)



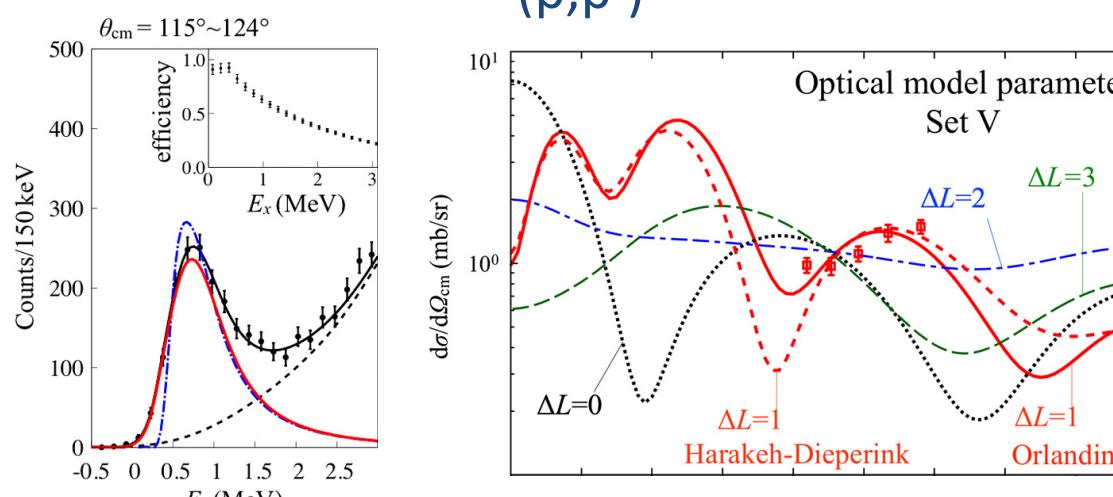
Nakamura *et al.* PRL **96**, 252502 (2006)



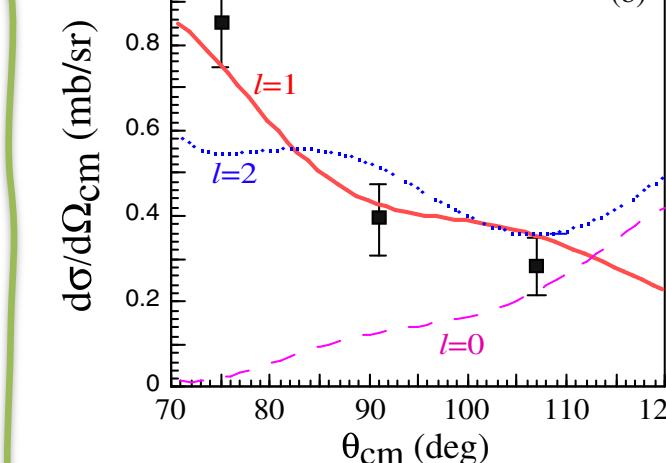
some questions to address:

- How do we characterize the PDR?
- Is it distinct from the GDR?
- How does it compare with theory?

## (p,p')



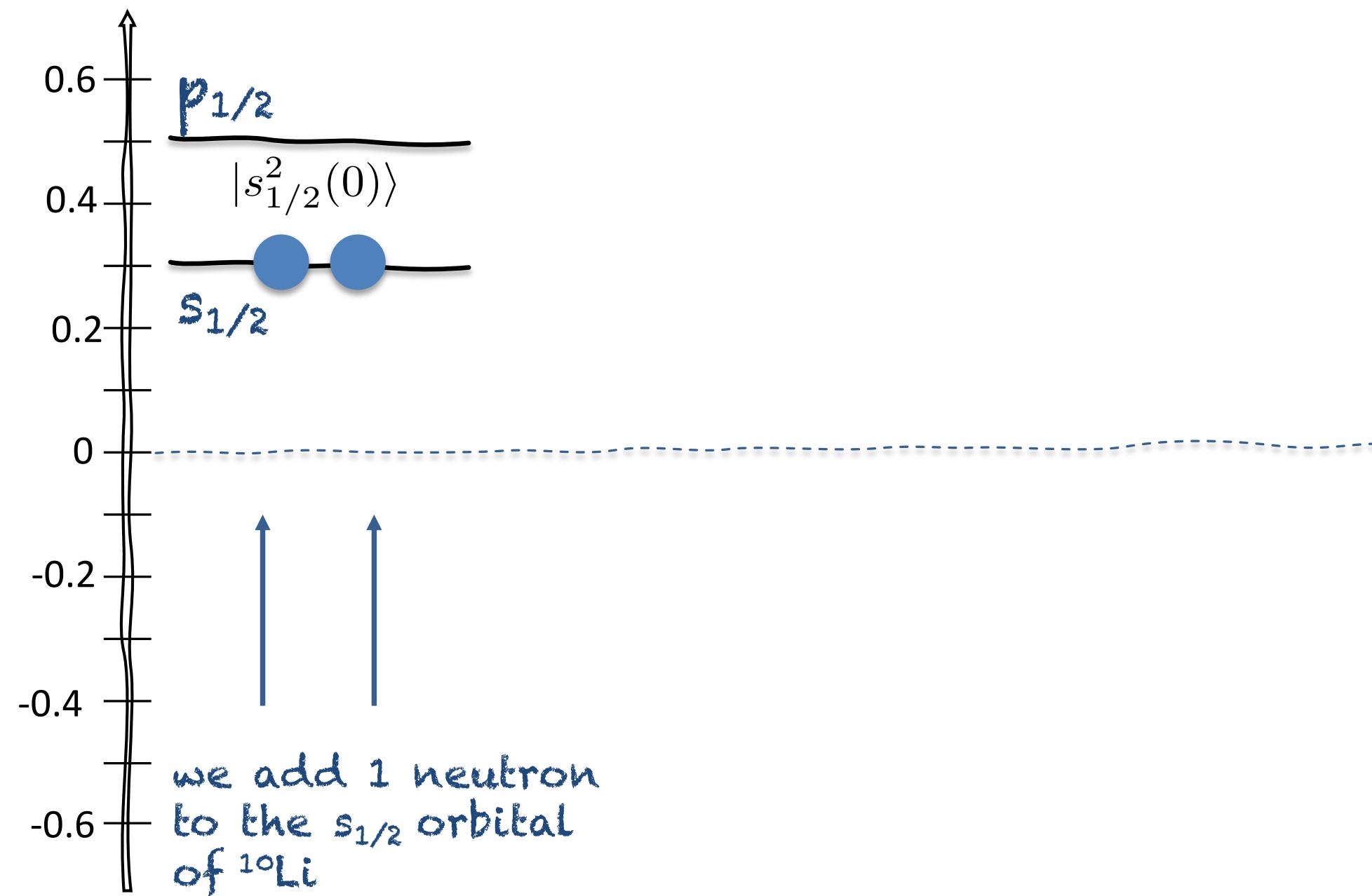
J. Tanaka *et al.* / Physics Letters B 774 (2017) 268–272



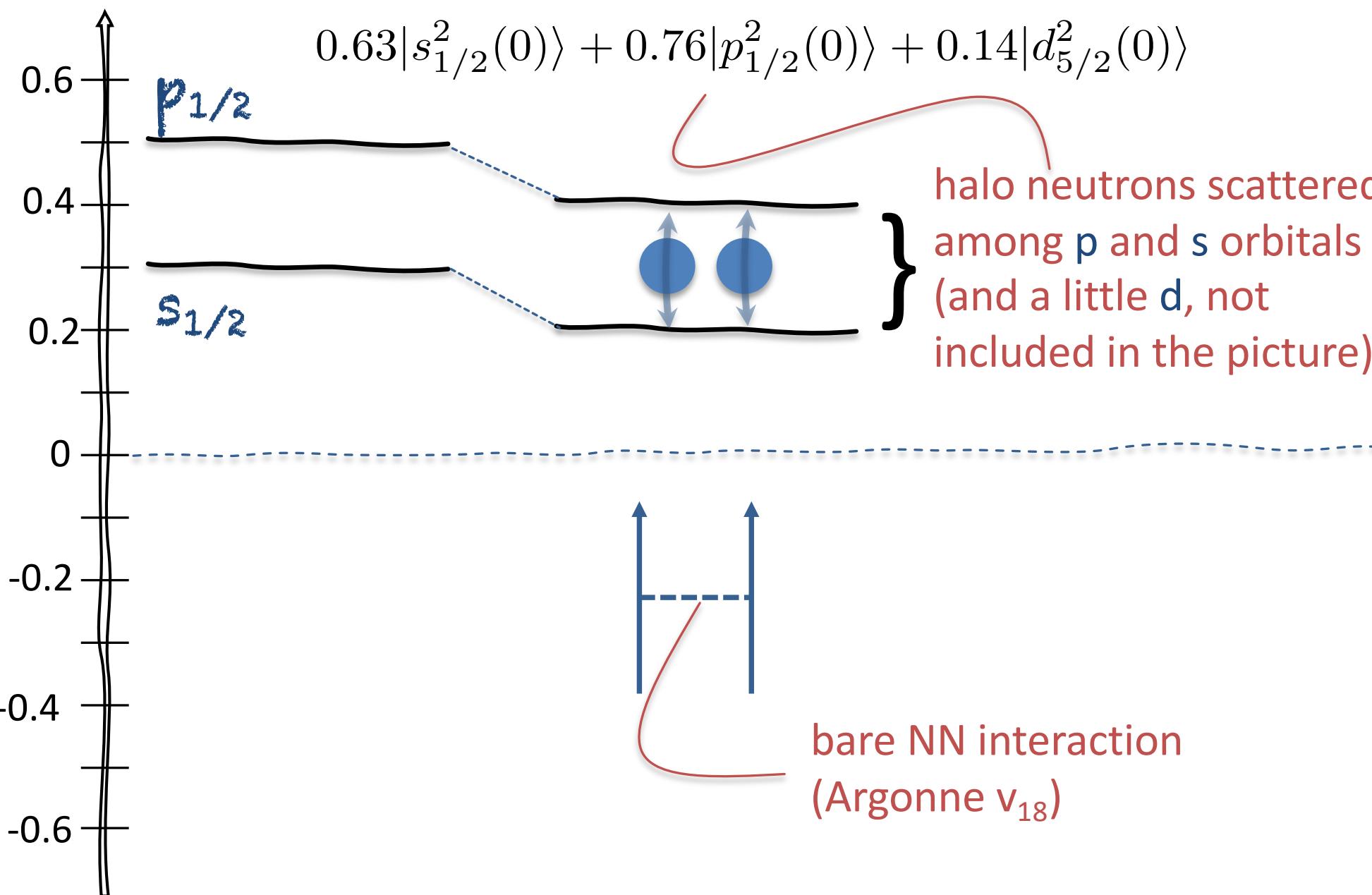
Kanungo *et al.* PRL **114**, 192502 (2015)

# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure

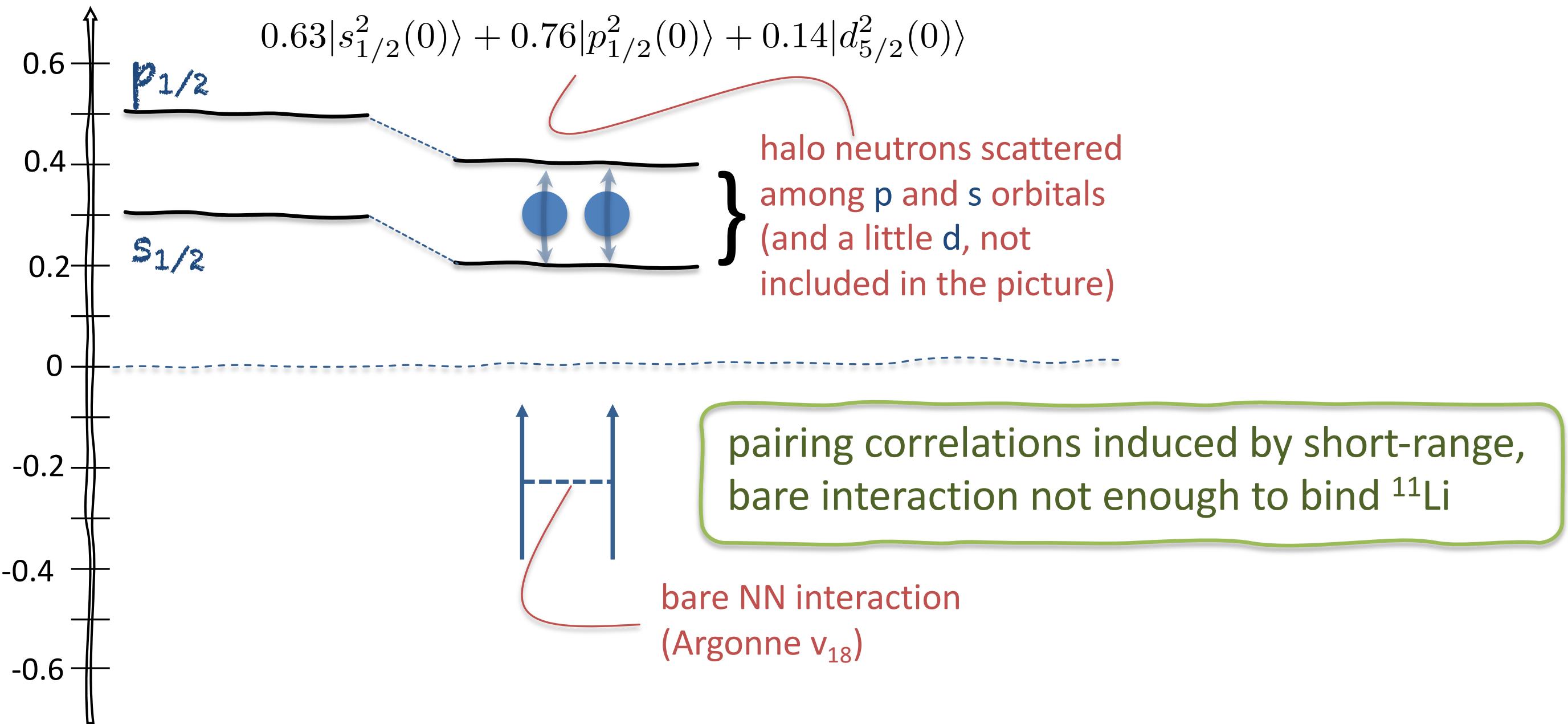
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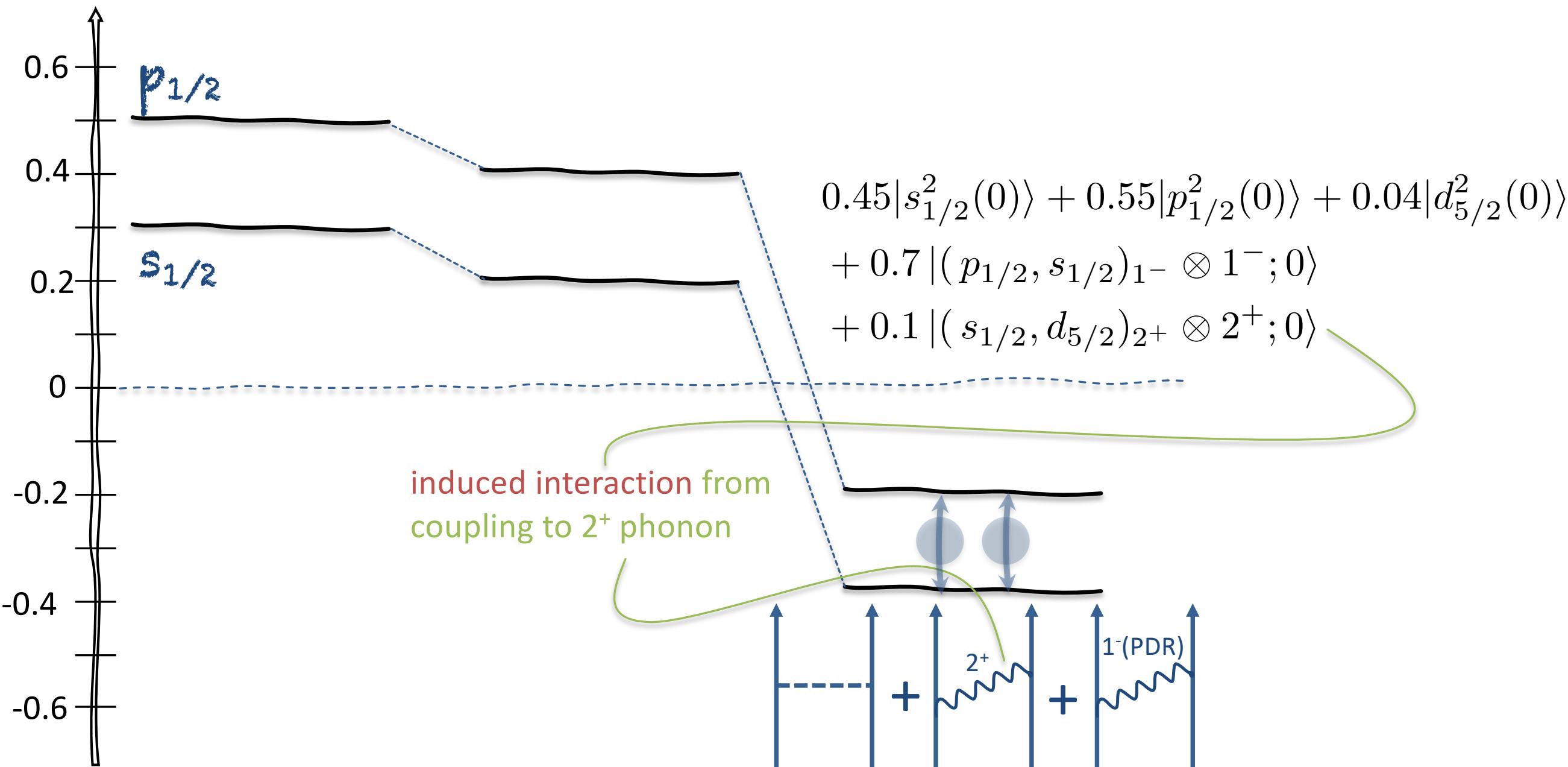
# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure



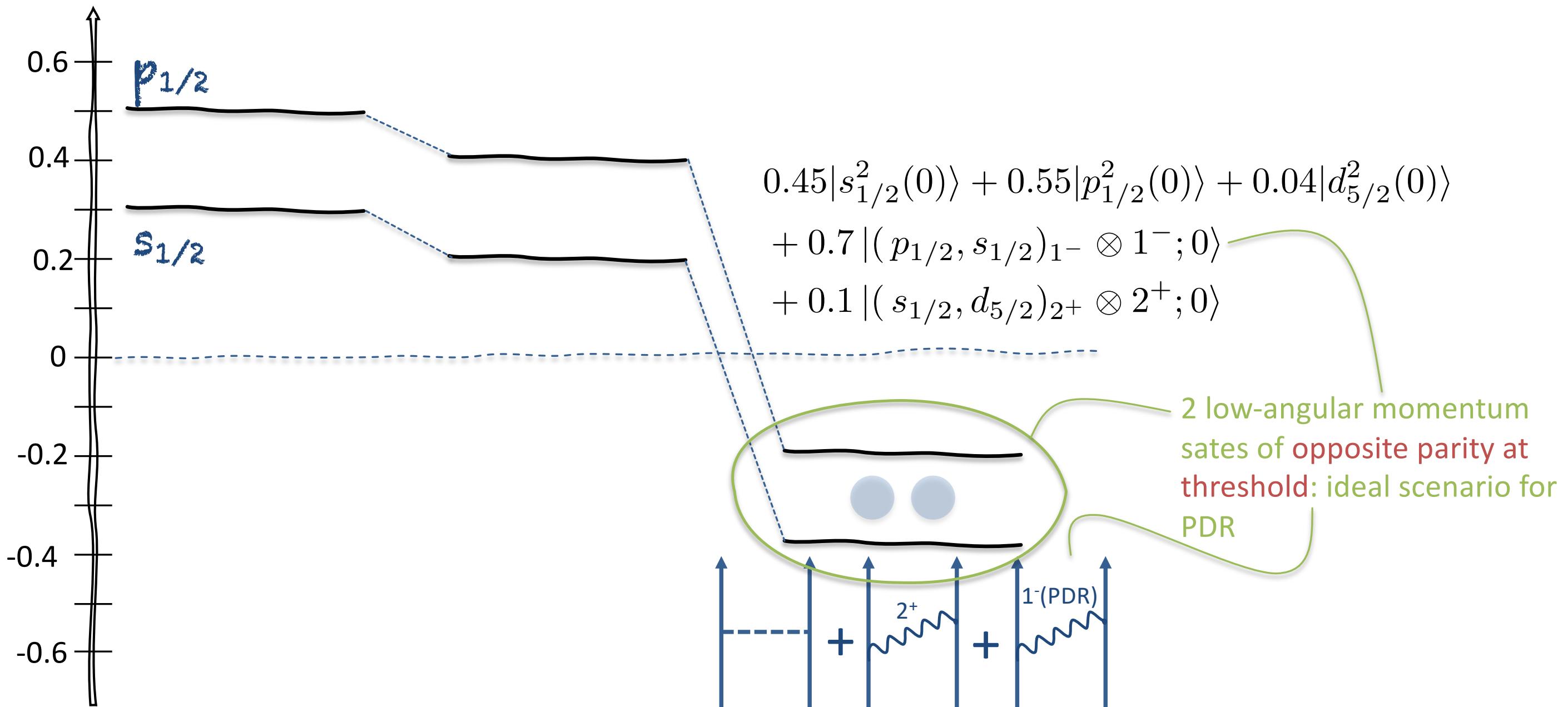
# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure



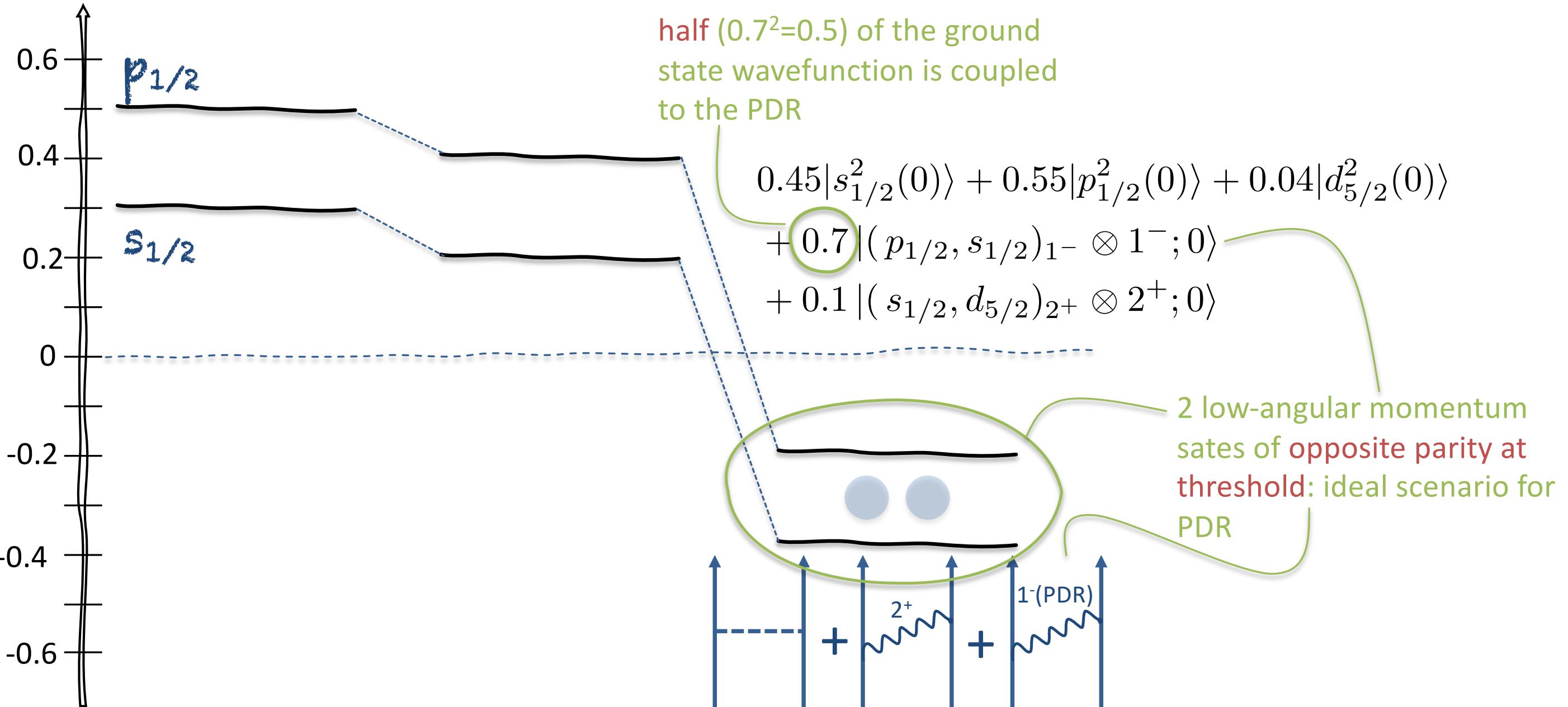
# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure



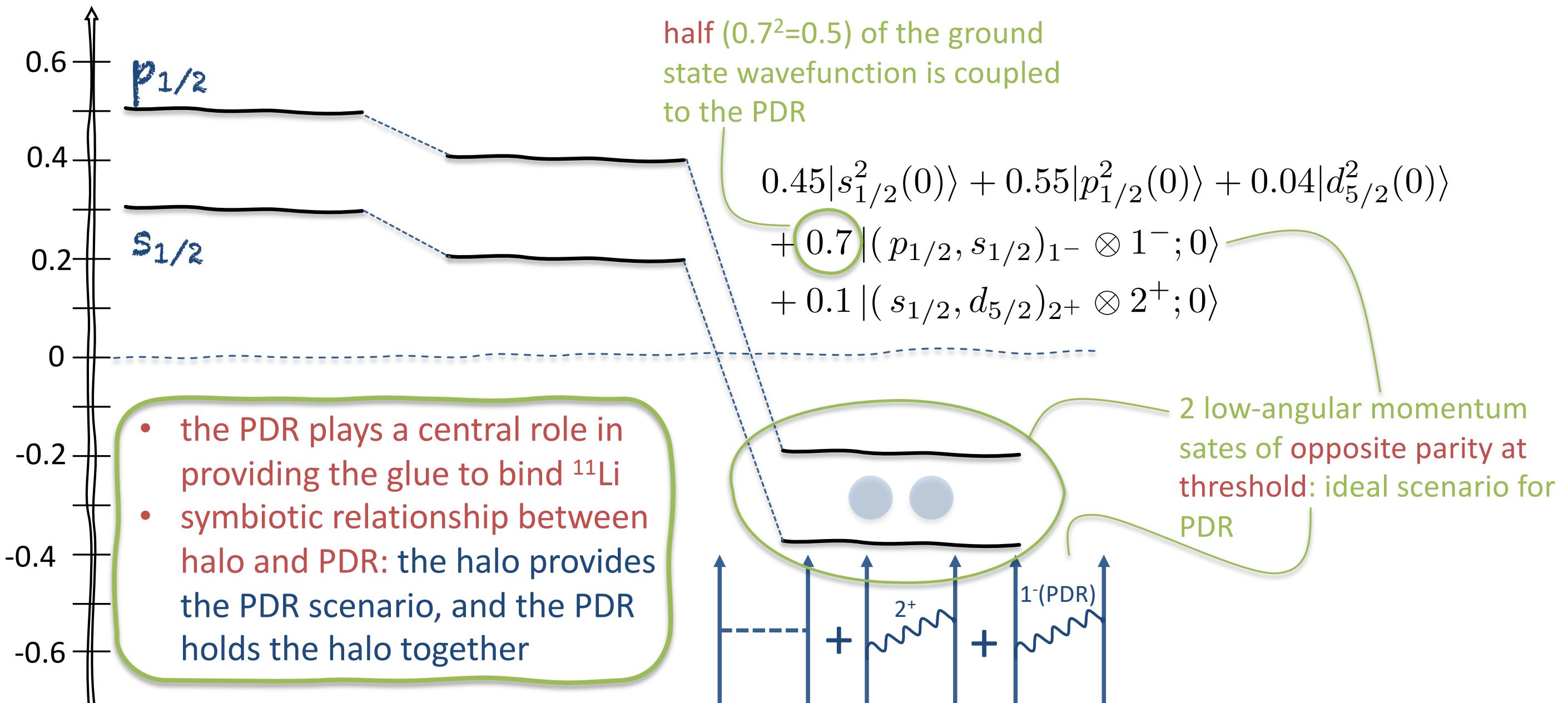
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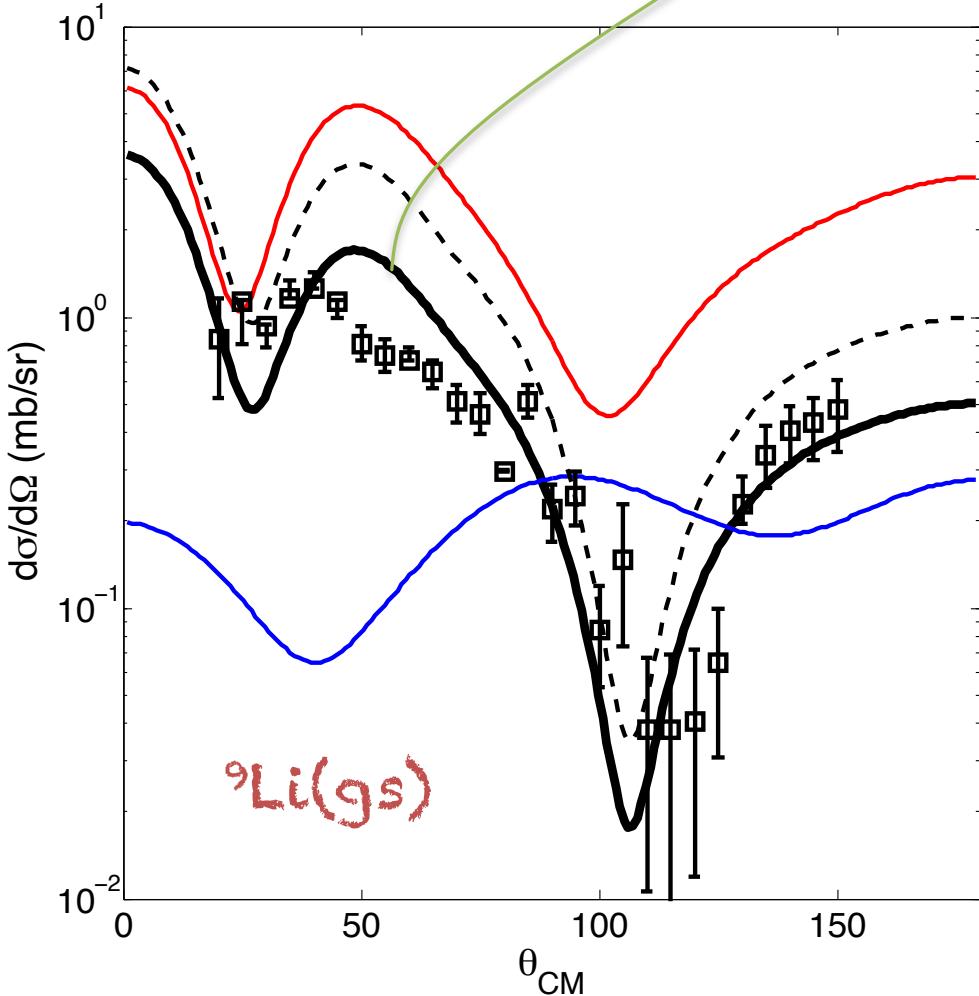


# Nuclear field theory (NFT) highlights the role of the PDR in $^{11}\text{Li}$ structure



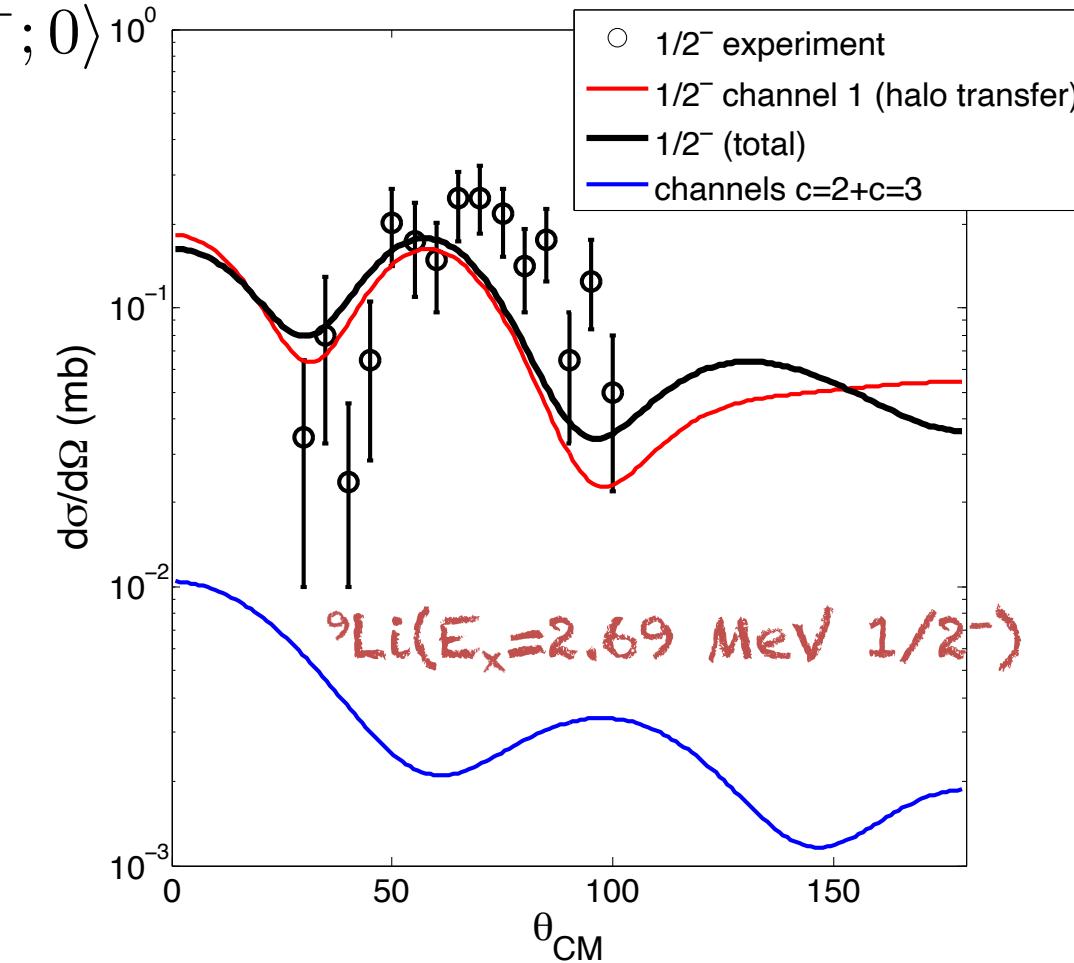
# theory confirmed by $^{11}\text{Li}(\text{p},\text{t})^9\text{Li}(\text{gs}; E_x=2.69 \text{ MeV } 1/2^-)$

GP, Barranco, Vigezzi, Broglia  
PRL **105** 172502 (2010)



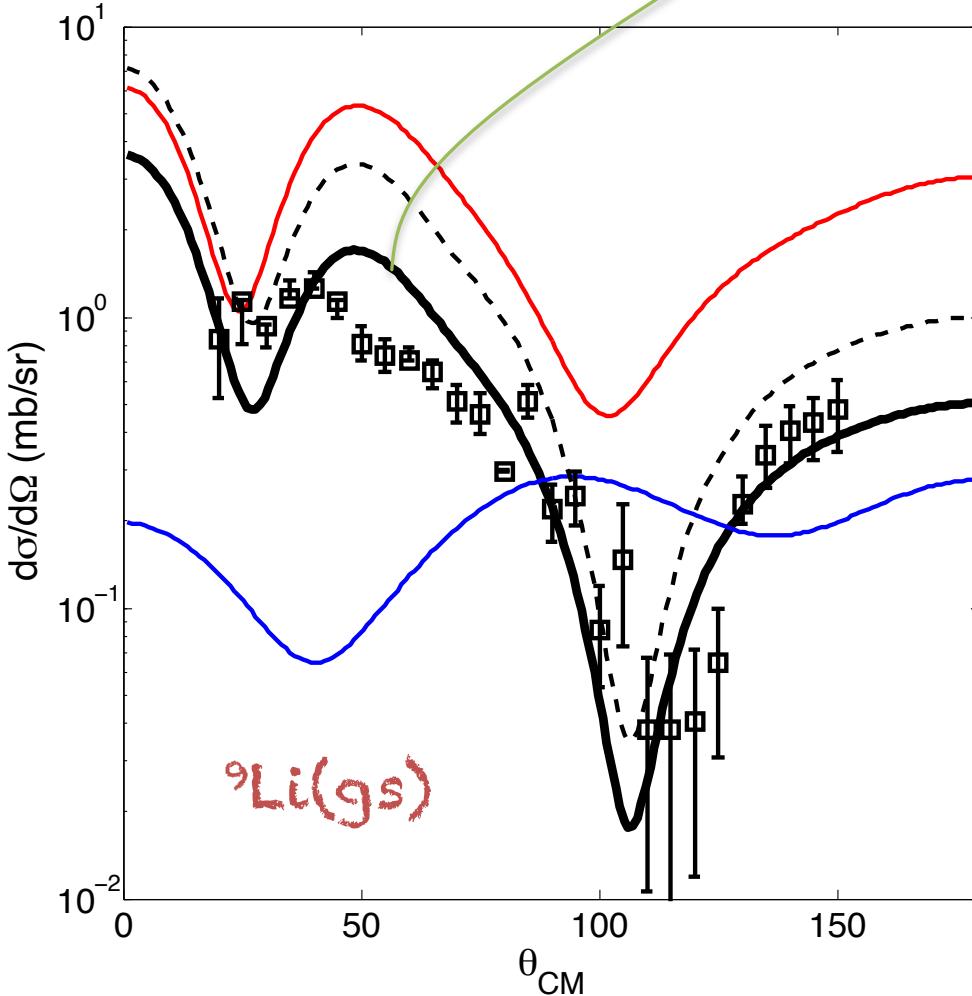
$$0.45|s_{1/2}^2(0)\rangle + 0.55|p_{1/2}^2(0)\rangle + 0.04|d_{5/2}^2(0)\rangle \\ + 0.7|(p_{1/2}, s_{1/2})_{1-} \otimes 1^-; 0\rangle \\ + 0.1|(s_{1/2}, d_{5/2})_{2+} \otimes 2^+; 0\rangle^{10^0}$$

reaction calculation in 2-order DWBA, dominated by successive transfer of the 2 neutrons (E. Vigezzi talk yesterday)

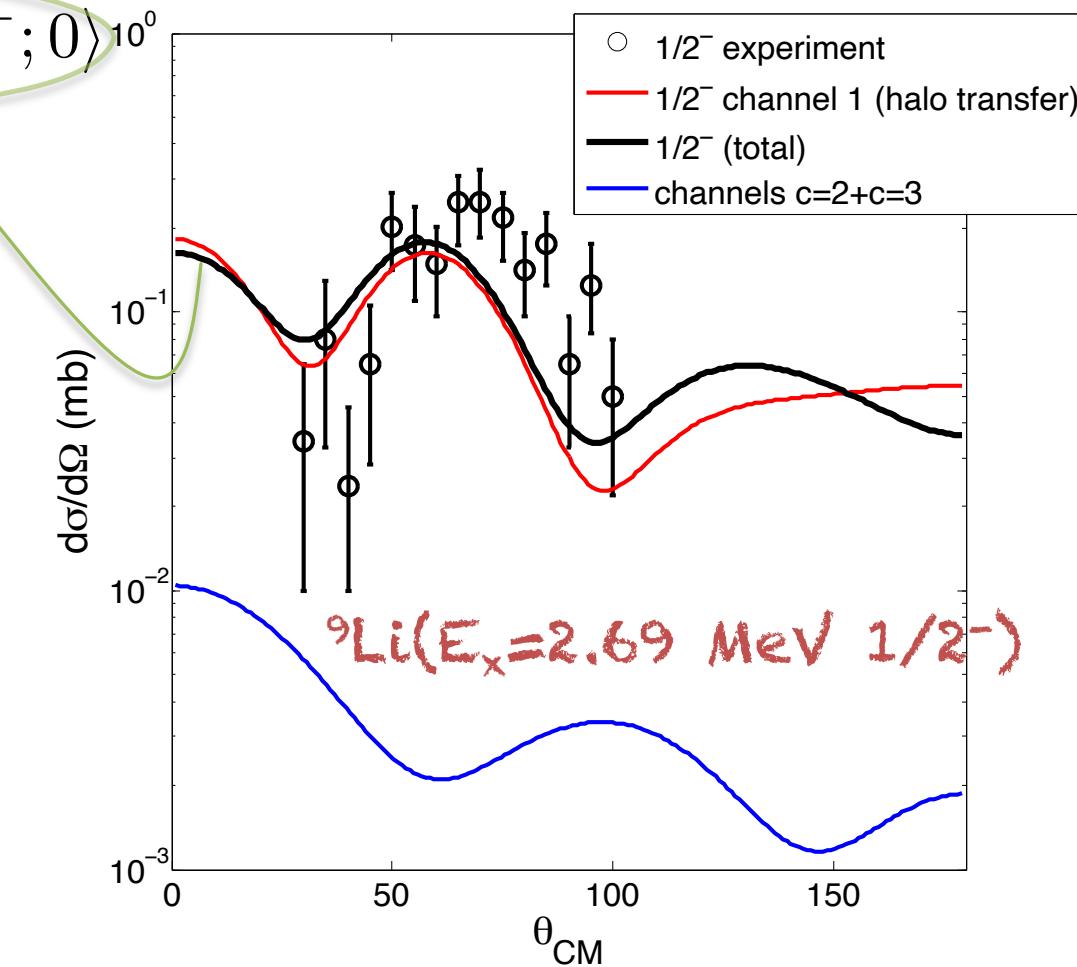


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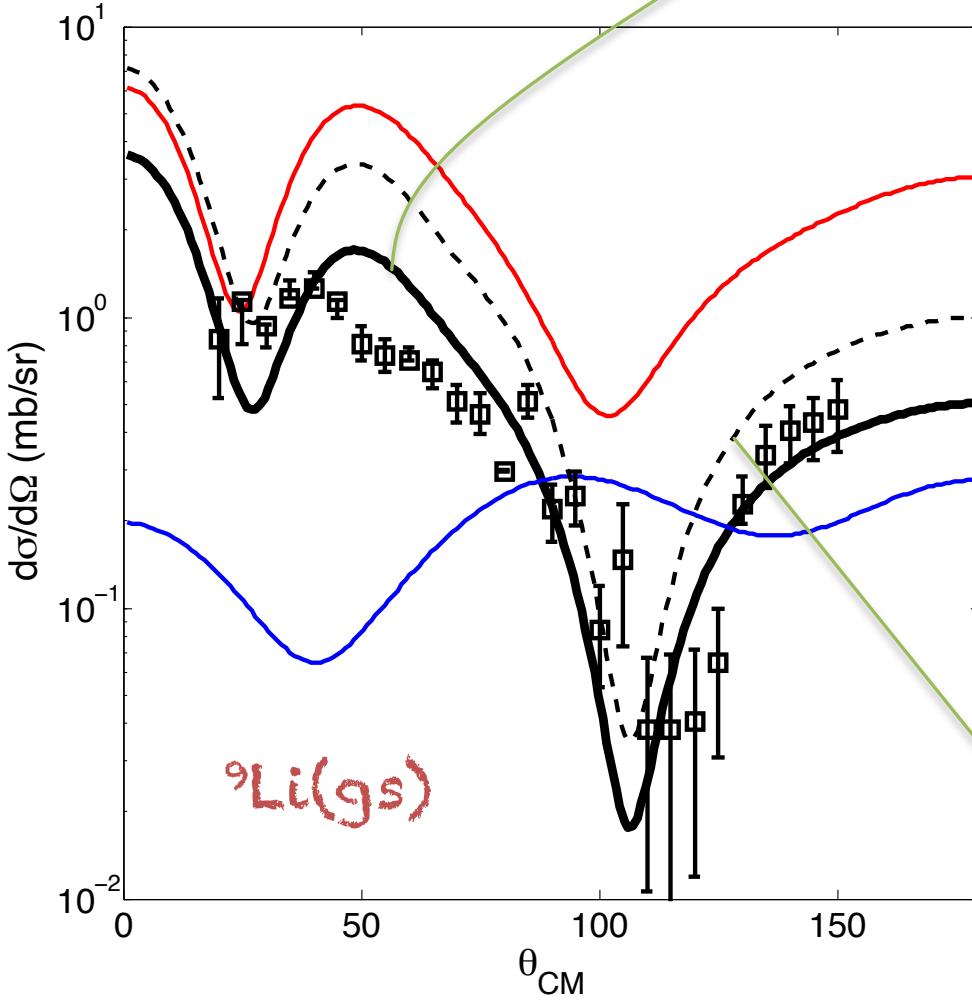


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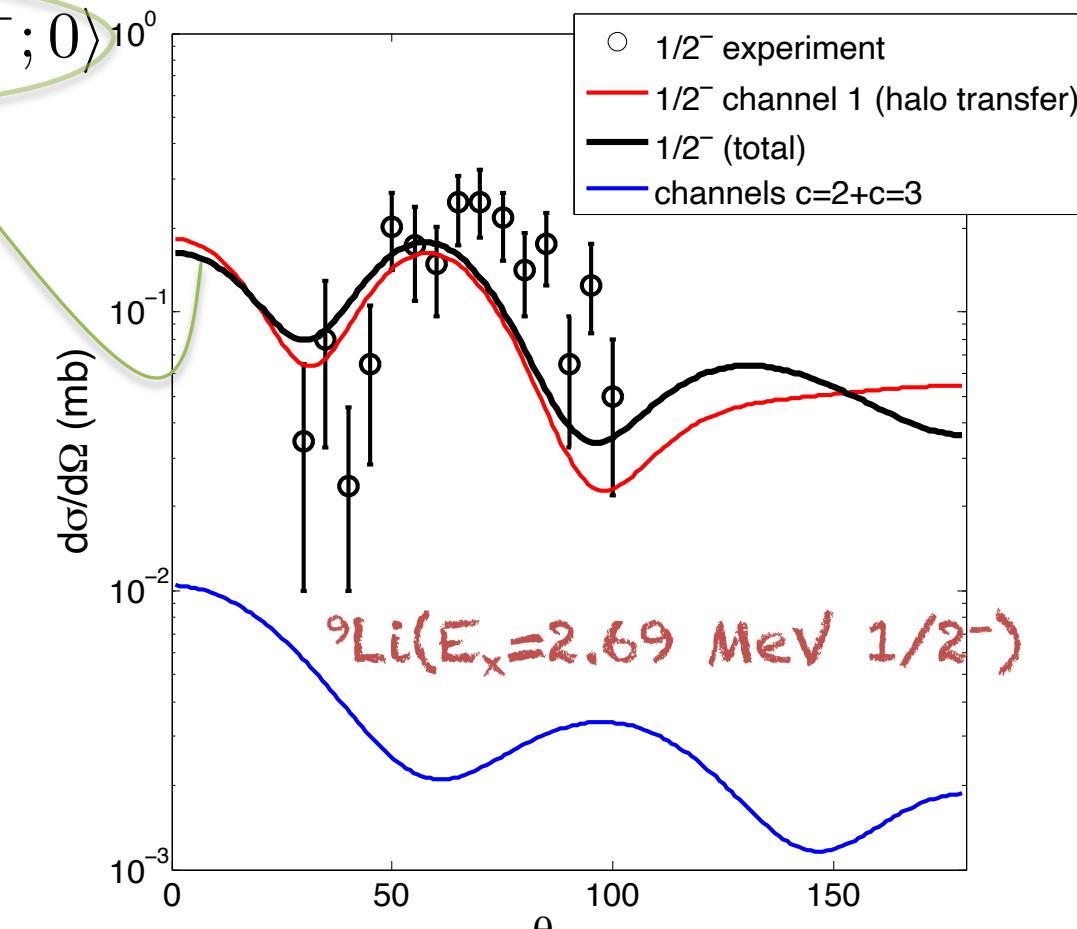


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GP, Barranco, Vigezzi, Broglia  
PRL **105** 172502 (2010)

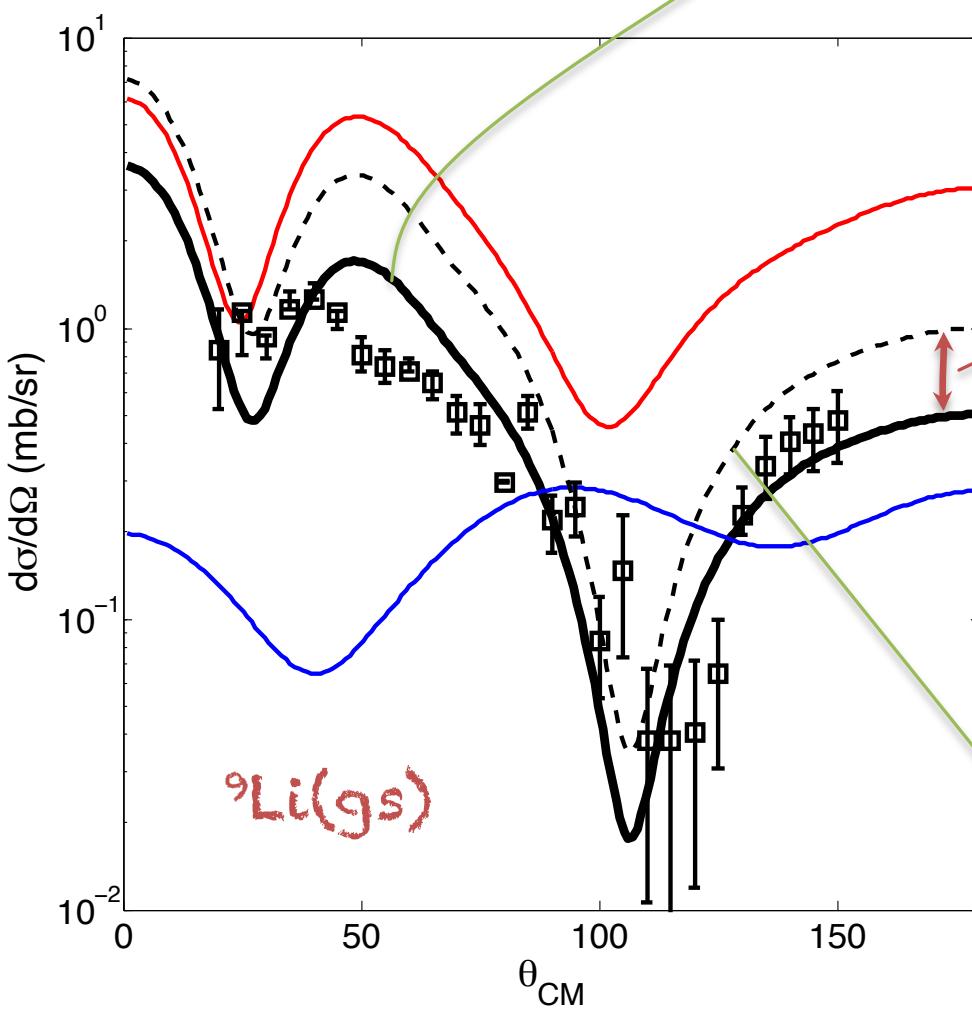


$$\begin{aligned}
 & 0.45|s_{1/2}^2(0)\rangle + 0.55|p_{1/2}^2(0)\rangle + 0.04|d_{5/2}^2(0)\rangle \\
 & + 0.7|(p_{1/2}, s_{1/2})_{1-} \otimes 1^-; 0\rangle \\
 & + 0.1|(s_{1/2}, d_{5/2})_{2+} \otimes 2^+; 0\rangle^{10^0} \\
 & 0.63|s_{1/2}^2(0)\rangle + 0.76|p_{1/2}^2(0)\rangle + 0.14|d_{1/2}^2(0)\rangle
 \end{aligned}$$



# theory confirmed by $^{11}\text{Li}(\text{p},\text{t})^9\text{Li}(\text{gs}; E_x=2.69 \text{ MeV } 1/2^-)$

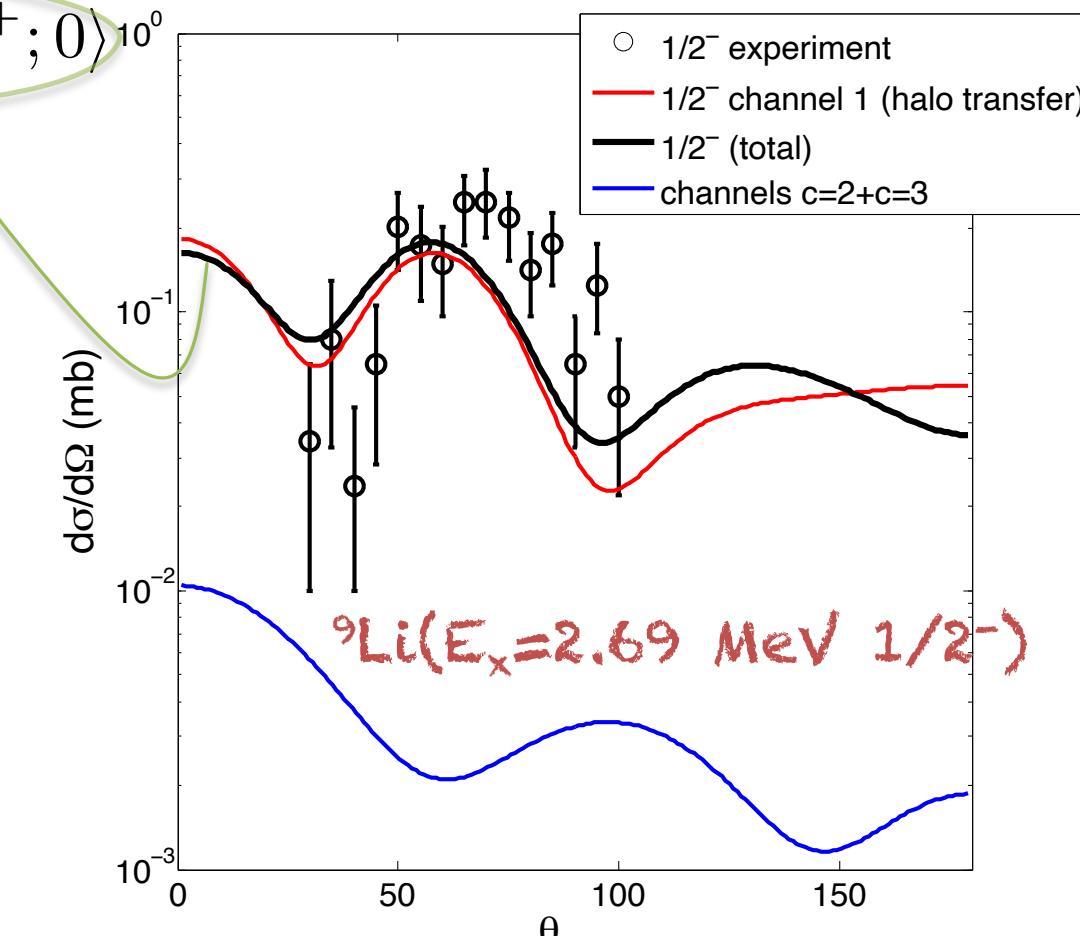
GP, Barranco, Vigezzi, Broglia  
PRL 105 172502 (2010)



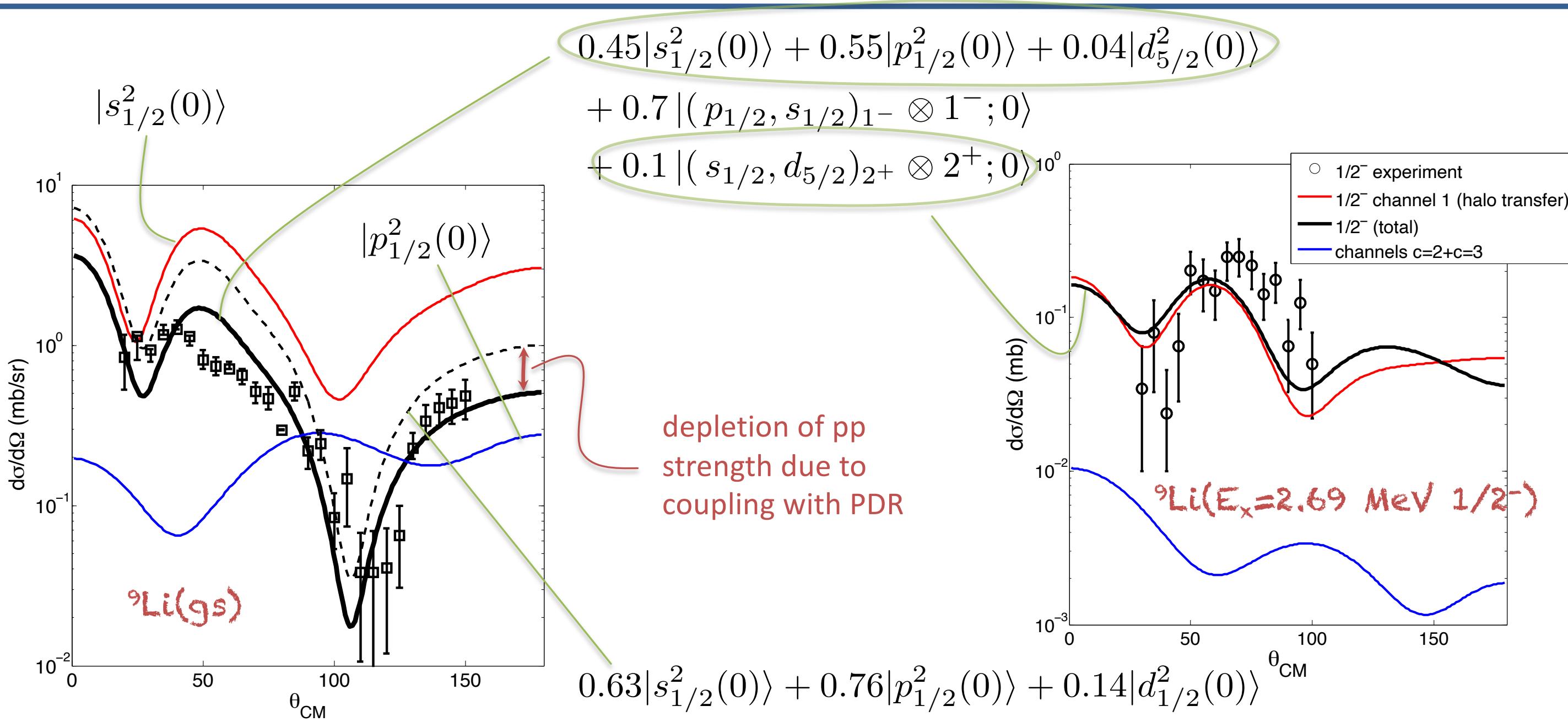
$$0.45|s_{1/2}^2(0)\rangle + 0.55|p_{1/2}^2(0)\rangle + 0.04|d_{5/2}^2(0)\rangle \\ + 0.7 |(p_{1/2}, s_{1/2})_{1-} \otimes 1^-; 0\rangle \\ + 0.1 |(s_{1/2}, d_{5/2})_{2+} \otimes 2^+; 0\rangle^{10^0}$$

depletion of pp strength due to coupling with PDR

$$0.63|s_{1/2}^2(0)\rangle + 0.76|p_{1/2}^2(0)\rangle + 0.14|d_{1/2}^2(0)\rangle$$



# theory confirmed by $^{11}\text{Li}(\text{p},\text{t})^9\text{Li}(\text{gs}; E_x=2.69 \text{ MeV } 1/2^-)$



# we compute the $^{11}\text{Li}$ PDR structure in RPA

3 representative low-lying dipole RPA peaks

E=0.65 MeV				E=1.21 MeV				E=2 MeV						
	<i>i</i>	<i>j</i>	X <sub>ij</sub>		<i>i</i>	<i>j</i>	X <sub>ij</sub>		<i>i</i>	<i>j</i>	X <sub>ij</sub>	Y <sub>ij</sub>		
ν	2s <sub>1/2</sub>	1p <sub>1/2</sub>	-0.780	0.078	ν	2s <sub>1/2</sub>	1p <sub>1/2</sub>	-0.119	0.048	ν	3s <sub>1/2</sub>	1p <sub>1/2</sub>	-0.118	0.040
ν	3s <sub>1/2</sub>	1p <sub>1/2</sub>	0.479	0.108	ν	3s <sub>1/2</sub>	1p <sub>1/2</sub>	-0.748	0.074	ν	4s <sub>1/2</sub>	1p <sub>1/2</sub>	-0.821	0.046
ν	4s <sub>1/2</sub>	1p <sub>1/2</sub>	0.220	0.106	ν	4s <sub>1/2</sub>	1p <sub>1/2</sub>	0.410	0.080	ν	5s <sub>1/2</sub>	1p <sub>1/2</sub>	0.250	0.046
ν	5s <sub>1/2</sub>	1p <sub>1/2</sub>	0.144	0.093	ν	5s <sub>1/2</sub>	1p <sub>1/2</sub>	0.181	0.075	ν	6s <sub>1/2</sub>	1p <sub>1/2</sub>	0.116	0.043
ν	6s <sub>1/2</sub>	1p <sub>1/2</sub>	0.106	0.080	ν	6s <sub>1/2</sub>	1p <sub>1/2</sub>	0.117	0.067	ν	1p <sub>3/2</sub>	4d <sub>5/2</sub>	0.144	0.081
ν	1p <sub>3/2</sub>	4d <sub>5/2</sub>	0.166	0.139	ν	1p <sub>3/2</sub>	4d <sub>5/2</sub>	0.170	0.121	ν	1p <sub>3/2</sub>	5d <sub>5/2</sub>	0.201	0.125
ν	1p <sub>3/2</sub>	5d <sub>5/2</sub>	0.241	0.208	ν	1p <sub>3/2</sub>	5d <sub>5/2</sub>	0.243	0.183	ν	1p <sub>3/2</sub>	6d <sub>5/2</sub>	0.201	0.135
ν	1p <sub>3/2</sub>	6d <sub>5/2</sub>	0.250	0.221	ν	1p <sub>3/2</sub>	6d <sub>5/2</sub>	0.249	0.196	ν	1p <sub>3/2</sub>	7d <sub>5/2</sub>	0.156	0.112
ν	1p <sub>3/2</sub>	7d <sub>5/2</sub>	0.199	0.180	ν	1p <sub>3/2</sub>	7d <sub>5/2</sub>	0.196	0.161	ν	1p <sub>3/2</sub>	8d <sub>5/2</sub>	0.113	0.085
ν	1p <sub>3/2</sub>	8d <sub>5/2</sub>	0.148	0.135	ν	1p <sub>3/2</sub>	8d <sub>5/2</sub>	0.144	0.122	ν	1p <sub>1/2</sub>	9d <sub>3/2</sub>	-0.126	0.014
ν	1p <sub>3/2</sub>	9d <sub>5/2</sub>	0.110	0.102	ν	1p <sub>3/2</sub>	9d <sub>5/2</sub>	0.107	0.093	ν	1p <sub>1/2</sub>	10d <sub>3/2</sub>	0.187	0.026
ν	1p <sub>1/2</sub>	4d <sub>3/2</sub>	0.103	0.075	ν	1p <sub>1/2</sub>	2d <sub>3/2</sub>	0.168	0.024	ν	1p <sub>1/2</sub>	11d <sub>3/2</sub>	0.121	0.040
ν	1p <sub>1/2</sub>	5d <sub>3/2</sub>	0.119	0.095	ν	1p <sub>1/2</sub>	3d <sub>3/2</sub>	0.114	0.043	ν	1p <sub>1/2</sub>	12d <sub>3/2</sub>	0.113	0.053
ν	1p <sub>1/2</sub>	6d <sub>3/2</sub>	0.128	0.108	ν	1p <sub>1/2</sub>	4d <sub>3/2</sub>	0.117	0.063	ν	1p <sub>1/2</sub>	13d <sub>3/2</sub>	0.111	0.064
ν	1p <sub>1/2</sub>	7d <sub>3/2</sub>	0.128	0.112	ν	1p <sub>1/2</sub>	5d <sub>3/2</sub>	0.126	0.081	ν	1p <sub>1/2</sub>	14d <sub>3/2</sub>	0.104	0.068
ν	1p <sub>1/2</sub>	8d <sub>3/2</sub>	0.117	0.106	ν	1p <sub>1/2</sub>	6d <sub>3/2</sub>	0.131	0.094	π	1p <sub>3/2</sub>	1d <sub>5/2</sub>	0.245	0.210
π	2s <sub>1/2</sub>	1p <sub>3/2</sub>	-0.136	-0.131	ν	1p <sub>1/2</sub>	7d <sub>3/2</sub>	0.128	0.099					
π	1p <sub>3/2</sub>	1d <sub>5/2</sub>	0.337	0.322	ν	1p <sub>1/2</sub>	8d <sub>3/2</sub>	0.116	0.094	π	2s <sub>1/2</sub>	1p <sub>3/2</sub>	-0.130	-0.12
					π	2s <sub>1/2</sub>	1p <sub>3/2</sub>	-0.130	-0.12	π	1p <sub>3/2</sub>	1d <sub>5/2</sub>	0.322	0.294

IOP Publishing

Phys. Scr. 94 (2019) 114002 (18pp)

Physica Scripta

<https://doi.org/10.1088/1402-4896/ab2431>

## Pygmy resonances: what's in a name?

R A Broglia<sup>1,2,7</sup>, F Barranco<sup>3</sup>, A Idini<sup>4</sup> , G Potel<sup>5</sup>  and E Vigezzi<sup>6</sup>

# we compute the $^{11}\text{Li}$ PDR structure in RPA

3 representative low-lying dipole RPA peaks

E=0.65 MeV		E=1.21 MeV		E=2 MeV							
i	j	X <sub>ij</sub>	Y <sub>ij</sub>	i	j	X <sub>ij</sub>	Y <sub>ij</sub>	i	j	X <sub>ij</sub>	Y <sub>ij</sub>
$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.780	0.078	$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.119	0.048	$\nu$	$3s_{1/2}$
$\nu$	$3s_{1/2}$	$1p_{1/2}$	0.479	0.108	$\nu$	$3s_{1/2}$	$1p_{1/2}$	-0.748	0.074	$\nu$	$4s_{1/2}$
$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.220	0.106	$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.410	0.080	$\nu$	$5s_{1/2}$
$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.144	0.093	$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.181	0.075	$\nu$	$6s_{1/2}$
$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.106	0.080	$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.117	0.067	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.166	0.139	$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.170	0.121	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.241	0.208	$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.243	0.183	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.250	0.221	$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.249	0.196	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$7d_{5/2}$	0.199	0.180	$\nu$	$1p_{3/2}$	$7d_{5/2}$	0.196	0.161	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$8d_{5/2}$	0.148	0.135	$\nu$	$1p_{3/2}$	$8d_{5/2}$	0.144	0.122	$\nu$	$1p_{1/2}$
$\nu$	$1p_{3/2}$	$9d_{5/2}$	0.110	0.102	$\nu$	$1p_{3/2}$	$9d_{5/2}$	0.107	0.093	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$4d_{3/2}$	0.103	0.075	$\nu$	$1p_{1/2}$	$2d_{3/2}$	0.168	0.024	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$5d_{3/2}$	0.119	0.095	$\nu$	$1p_{1/2}$	$3d_{3/2}$	0.114	0.043	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$6d_{3/2}$	0.128	0.108	$\nu$	$1p_{1/2}$	$4d_{3/2}$	0.117	0.063	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$7d_{3/2}$	0.128	0.112	$\nu$	$1p_{1/2}$	$5d_{3/2}$	0.126	0.081	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$8d_{3/2}$	0.117	0.106	$\nu$	$1p_{1/2}$	$6d_{3/2}$	0.131	0.094	$\pi$	$1p_{3/2}$
$\pi$	$2s_{1/2}$	$1p_{3/2}$	-0.136	-0.131	$\nu$	$1p_{1/2}$	$7d_{3/2}$	0.128	0.099		
$\pi$	$1p_{3/2}$	$1d_{5/2}$	0.337	0.322	$\nu$	$1p_{1/2}$	$8d_{3/2}$	0.116	0.094	$\pi$	$2s_{1/2}$
					$\pi$	$2s_{1/2}$	$1p_{3/2}$	-0.130	-0.12	$\pi$	$1p_{3/2}$
					$\pi$	$1p_{3/2}$	$1d_{5/2}$	0.322	0.294		

IOP Publishing

Phys. Scr. 94 (2019) 114002 (18pp)

Physica Scripta

<https://doi.org/10.1088/1402-4896/ab2431>

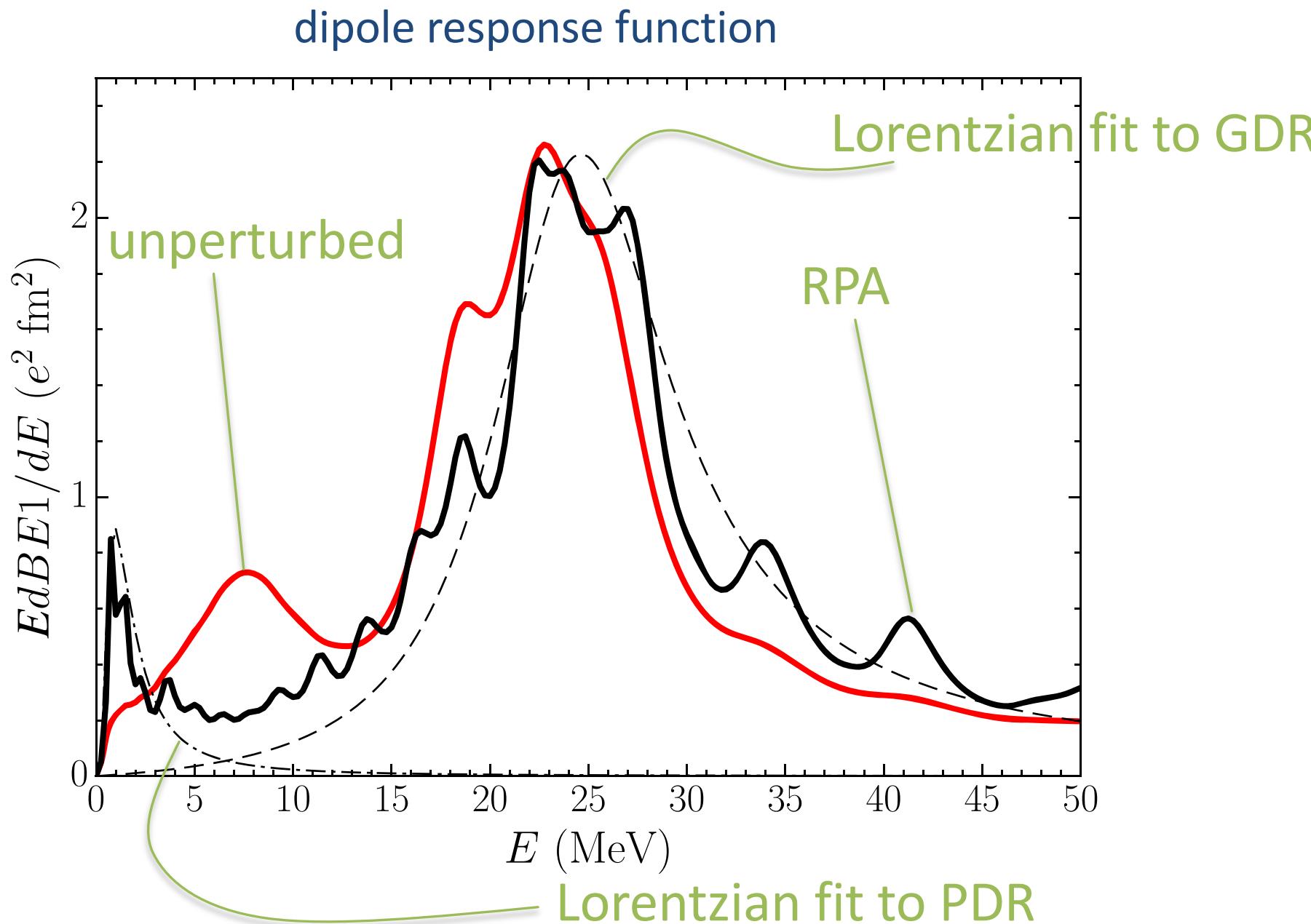
## Pygmy resonances: what's in a name?

R A Broglia<sup>1,2,7</sup>, F Barranco<sup>3</sup>, A Idini<sup>4</sup>, G Potel<sup>5</sup> and E Vigezzi<sup>6</sup>

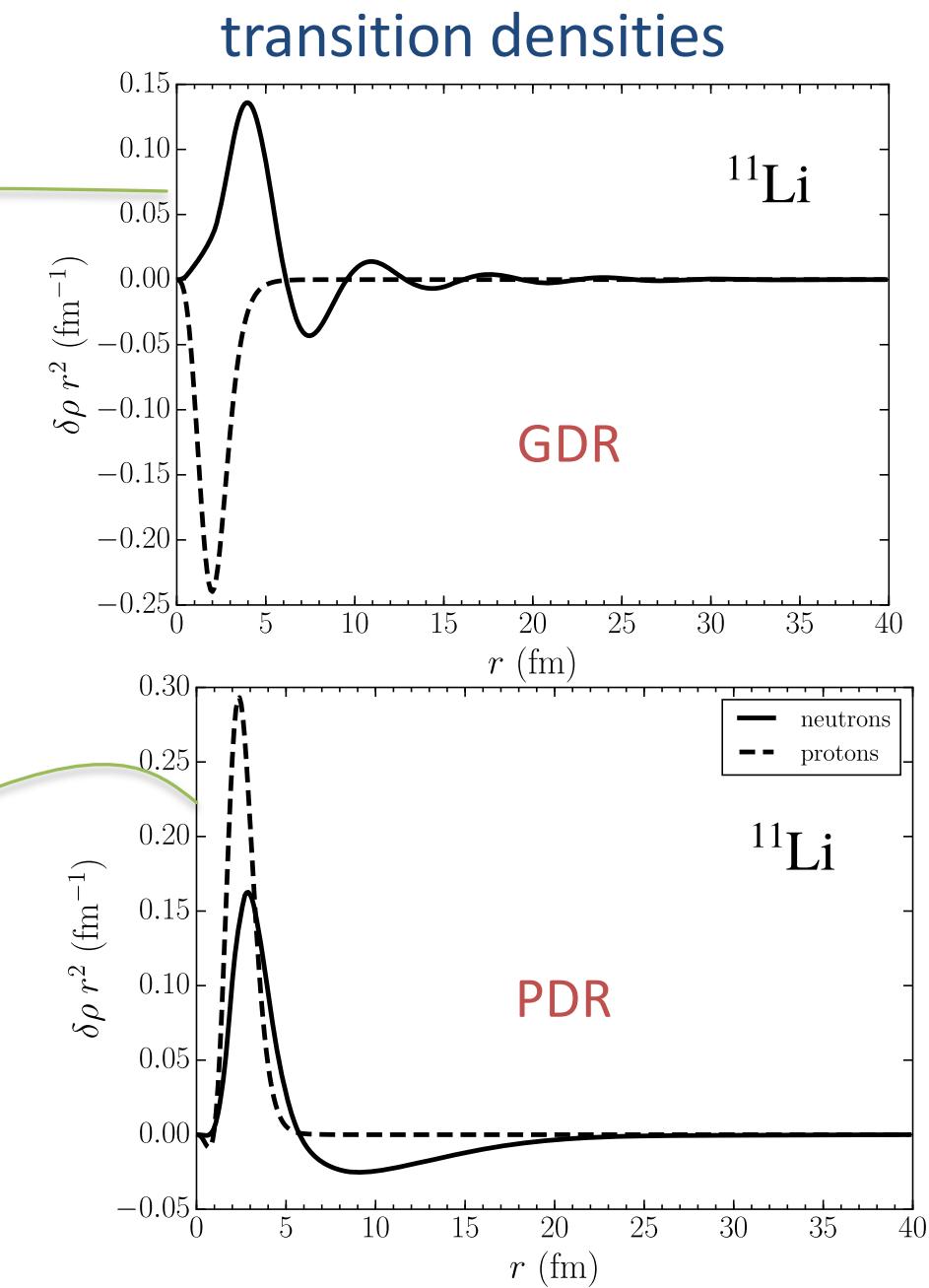
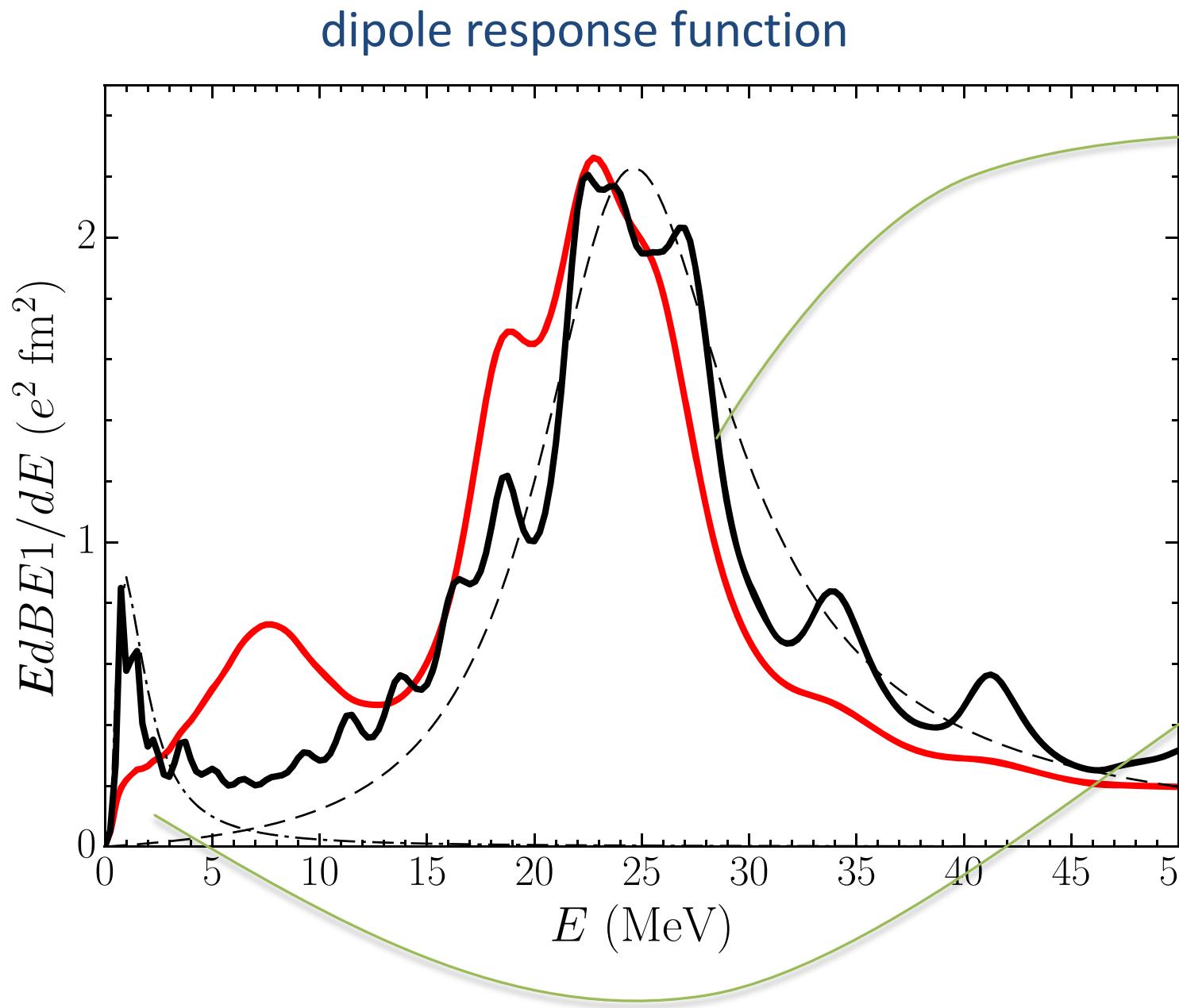
largest components are  
2-quasiparticle neutron  
halo ( $s_{1/2} p_{1/2}$ )<sub>1-</sub> states

the PDR exhausts about 8% of the EWSR

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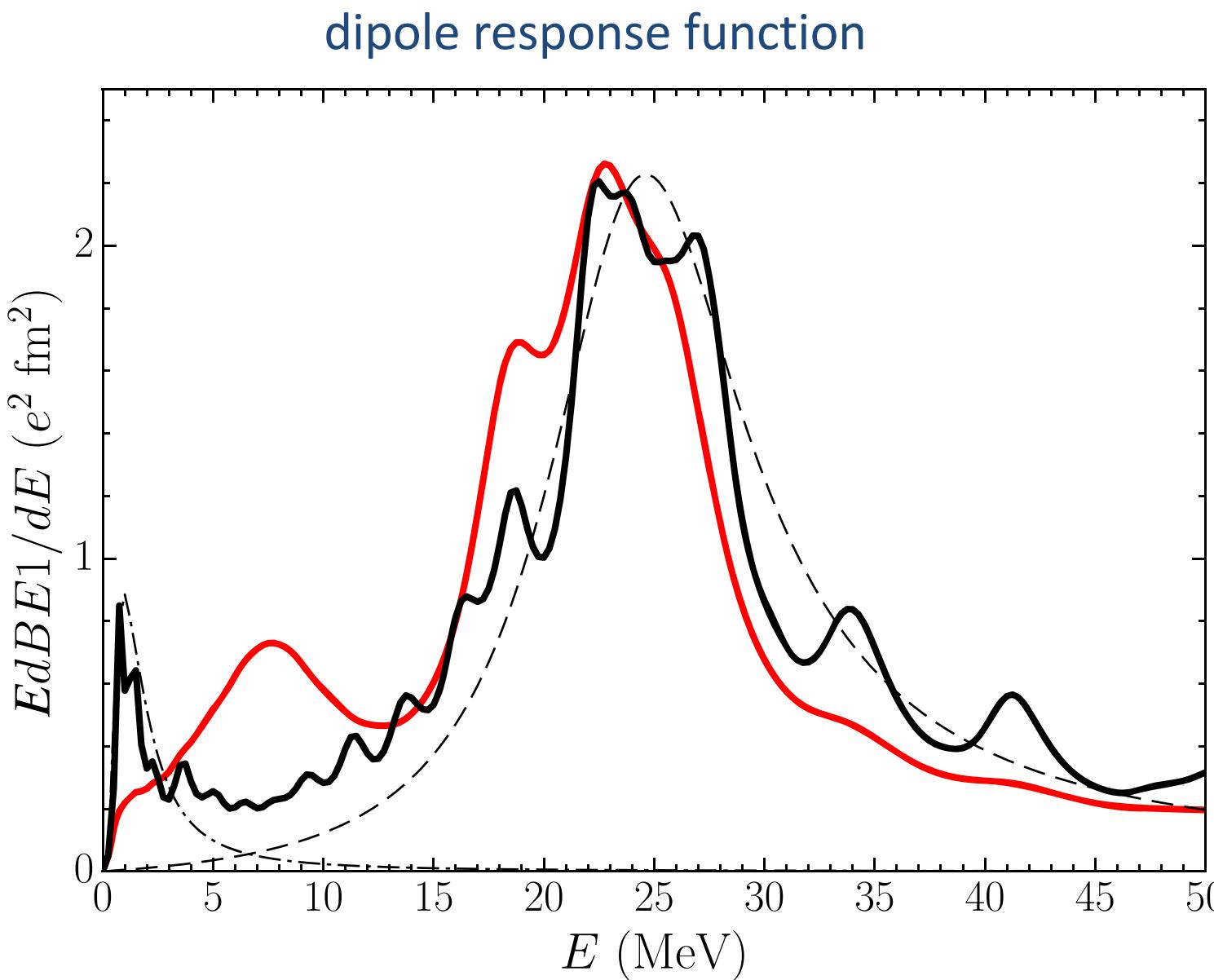


the PDR exhausts about 8% of the EWSR



# the PDR exhausts about 8% of the EWSR

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experiment approved at **FRI**B to probe  
the whole **dipole response** with  $(p, p')$ .  
Spokepersons: Ayyad, Zamora

# Conclusions

- the PDR plays an important role in the structure of the exotic two-neutron halo nucleus  $^{11}\text{Li}$ : **halo-PDR symbiotic nature**
- our calculations point to a strong ***pp*** component of the PDR, as opposed to the more ***ph*** nature of the GDR

talks by Vandebrouck,  
Spieker, Weinert,  
Khumalo



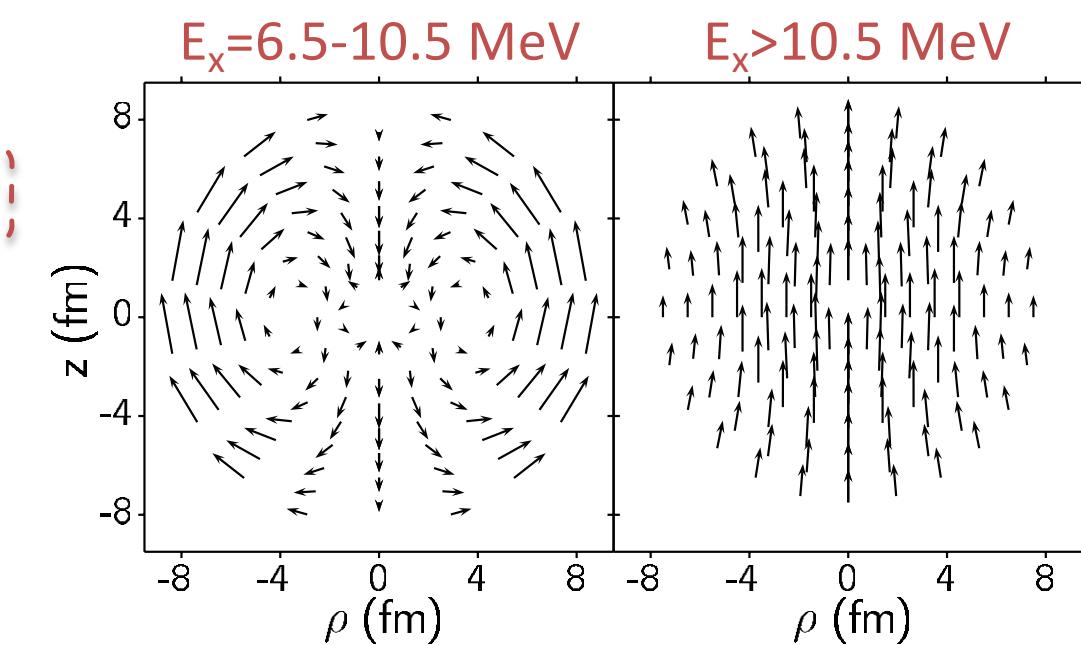
- PDR of  $^{11}\text{Li}$  as a **vortical** excitation of the halo. Extrapolable to **neutron skins**?
- Approved experiments:  $^{11}\text{Li}(\text{p},\text{p}')^{11}\text{Li}^*$  @ **FRIB**, and  $^9\text{Li}(\text{t},\text{p})^{11}\text{Li}(\text{PDR})$  @ **ISOLDE**
- along with  $(\text{d},\text{p})$  and  $(\text{n},\text{n}')$ ,  $(\text{t},\text{p})$  to join the ranks of **novel probes to the PDR**
- personal wish:  $(\text{t},\text{p})$  measurements on nuclei with **neutron skin**. Maybe with new **FSU triton beam**?

# we compute the $^{11}\text{Li}$ PDR structure and the $^9\text{Li} (t,p)^{11}\text{Li}$ (PDR) cross section

3 representative low-lying dipole RPA peaks

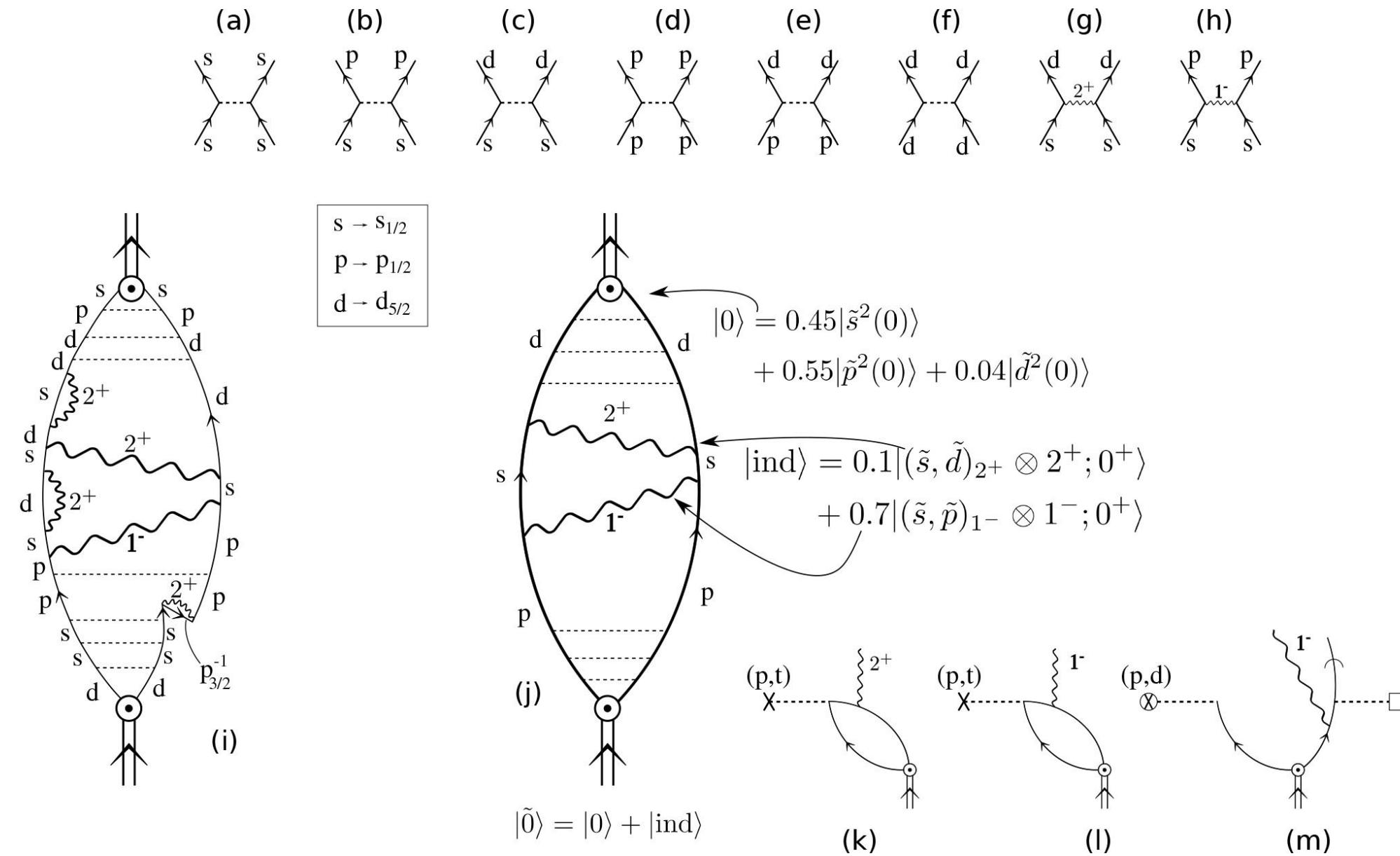
		E=0.65 MeV		E=1.21 MeV		E=2 MeV					
i	j	X <sub>ij</sub>	Y <sub>ij</sub>	i	j	X <sub>ij</sub>	Y <sub>ij</sub>	i	j	X <sub>ij</sub>	Y <sub>ij</sub>
$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.780	0.078	$\nu$	$2s_{1/2}$	$1p_{1/2}$	-0.119	0.048	$\nu$	$3s_{1/2}$
$\nu$	$3s_{1/2}$	$1p_{1/2}$	0.479	0.108	$\nu$	$3s_{1/2}$	$1p_{1/2}$	-0.748	0.074	$\nu$	$4s_{1/2}$
$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.220	0.106	$\nu$	$4s_{1/2}$	$1p_{1/2}$	0.410	0.080	$\nu$	$5s_{1/2}$
$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.144	0.093	$\nu$	$5s_{1/2}$	$1p_{1/2}$	0.181	0.075	$\nu$	$6s_{1/2}$
$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.106	0.080	$\nu$	$6s_{1/2}$	$1p_{1/2}$	0.117	0.067	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.166	0.139	$\nu$	$1p_{3/2}$	$4d_{5/2}$	0.170	0.121	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.241	0.208	$\nu$	$1p_{3/2}$	$5d_{5/2}$	0.243	0.183	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.250	0.221	$\nu$	$1p_{3/2}$	$6d_{5/2}$	0.249	0.196	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$7d_{5/2}$	0.199	0.180	$\nu$	$1p_{3/2}$	$7d_{5/2}$	0.196	0.161	$\nu$	$1p_{3/2}$
$\nu$	$1p_{3/2}$	$8d_{5/2}$	0.148	0.135	$\nu$	$1p_{3/2}$	$8d_{5/2}$	0.144	0.122	$\nu$	$1p_{1/2}$
$\nu$	$1p_{3/2}$	$9d_{5/2}$	0.110	0.102	$\nu$	$1p_{3/2}$	$9d_{5/2}$	0.107	0.093	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$4d_{3/2}$	0.103	0.075	$\nu$	$1p_{1/2}$	$2d_{3/2}$	0.168	0.024	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$5d_{3/2}$	0.119	0.095	$\nu$	$1p_{1/2}$	$3d_{3/2}$	0.114	0.043	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$6d_{3/2}$	0.128	0.108	$\nu$	$1p_{1/2}$	$4d_{3/2}$	0.117	0.063	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$7d_{3/2}$	0.128	0.112	$\nu$	$1p_{1/2}$	$5d_{3/2}$	0.126	0.081	$\nu$	$1p_{1/2}$
$\nu$	$1p_{1/2}$	$8d_{3/2}$	0.117	0.106	$\nu$	$1p_{1/2}$	$6d_{3/2}$	0.131	0.094	$\pi$	$1p_{3/2}$
$\pi$	$2s_{1/2}$	$1p_{3/2}$	-0.136	-0.131	$\nu$	$1p_{1/2}$	$7d_{3/2}$	0.128	0.099	$\pi$	$1p_{3/2}$
$\pi$	$1p_{3/2}$	$1d_{5/2}$	0.337	0.322	$\nu$	$1p_{1/2}$	$8d_{3/2}$	0.116	0.094	$\pi$	$2s_{1/2}$
					$\pi$	$2s_{1/2}$	$1p_{3/2}$	-0.130	-0.12	$\pi$	$1p_{3/2}$
					$\pi$	$1p_{3/2}$	$1d_{5/2}$	0.322	0.294		

velocity field of  $^{208}\text{Pb}$  dipole states



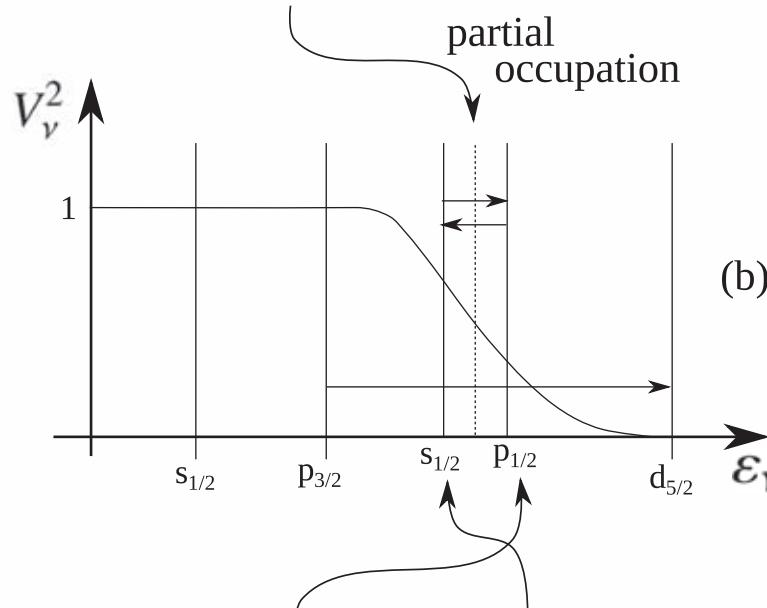
Ryezayeva et al. PRL 89 (2002) 272502

# Ground state of $^{11}\text{Li}$



# Low-lying dipole strength

$$|0\rangle_\nu = |0\rangle + 0.7|(p_{1/2}, s_{1/2})_{1^-} \otimes 1^-; 0\rangle + 0.1|(s_{1/2}, d_{5/2})_{2^+} \otimes 2^+; 0\rangle$$



$$|0\rangle = 0.55|p_{1/2}^2\rangle + 0.45|s_{1/2}^2\rangle + 0.04|d_{5/2}^2\rangle$$

$$|1^-, \text{pygmy}\rangle = \alpha \Gamma_{\text{pygmy}}^\dagger |\text{halo}\rangle + \beta \Gamma_{\text{GDR}}^\dagger |\text{core}\rangle$$

(a)

$\alpha^2 \gg \beta^2$

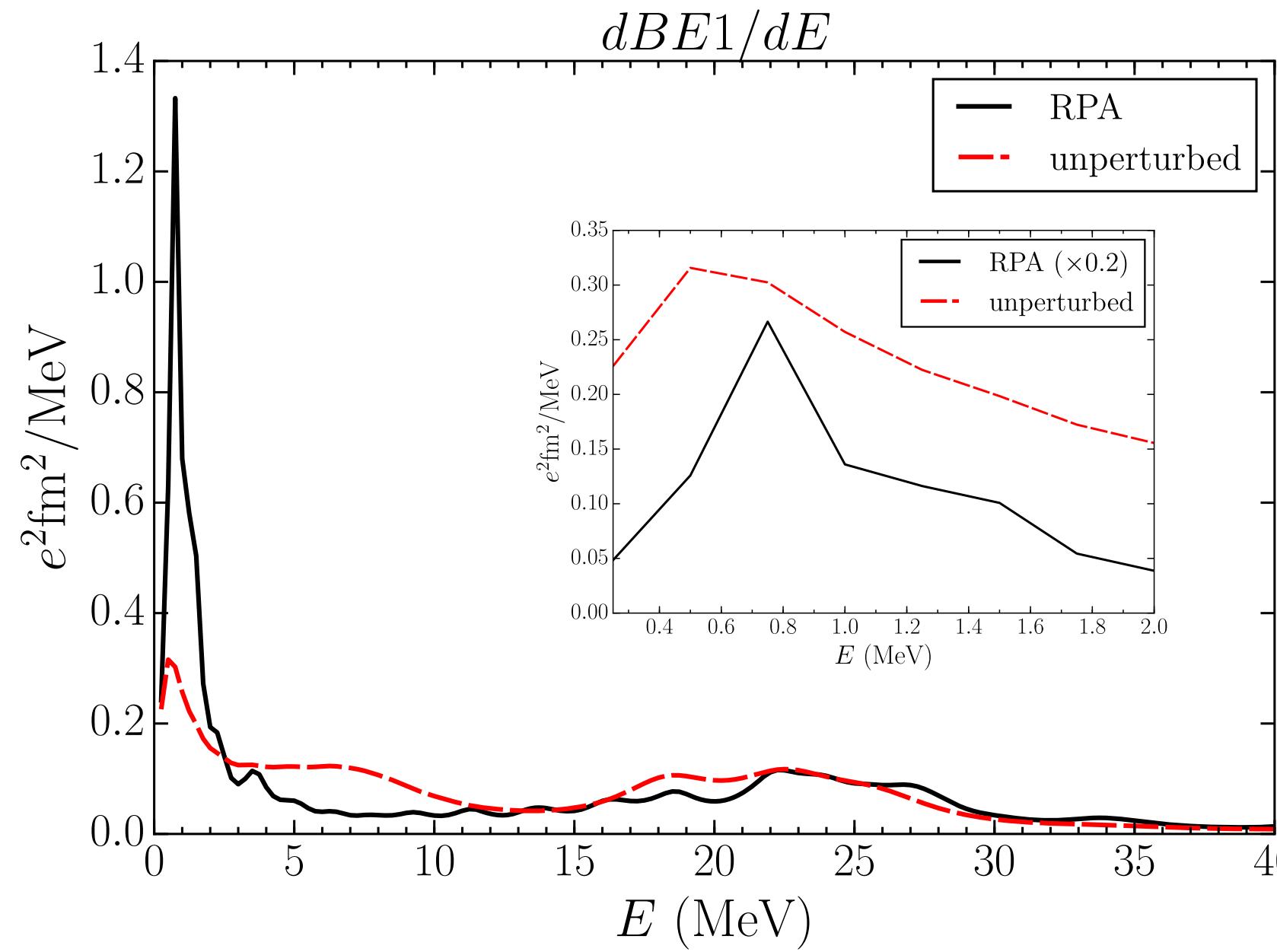
	$1p_{1/2}^{-1} 2s_{1/2}$	$1p_{1/2}^{-1} 3s_{1/2}$	$1p_{1/2}^{-1} 4s_{1/2}$	$1p_{1/2}^{-1} 1d_{3/2}$	$1p_{3/2}^{-1} 4d_{5/2}$	$1p_{3/2}^{-1} 5d_{5/2}$	$1p_{3/2}^{-1} 6d_{5/2}$
X	-0.780	0.479	0.220	0.103	0.166	0.241	0.250
Y	0.078	0.108	0.106	0.075	0.139	0.208	0.221

8% EWSR

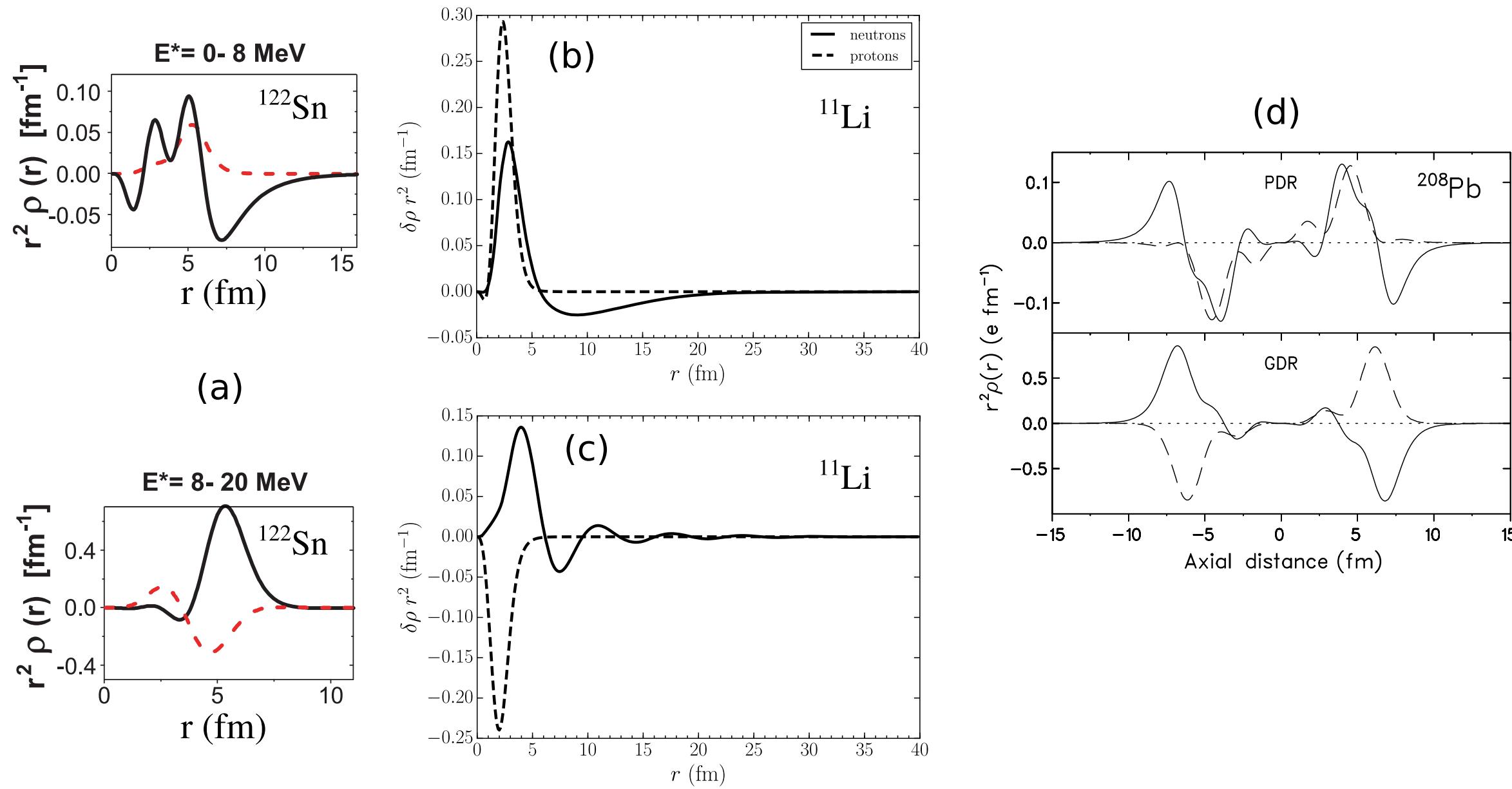
$E_{1^-} \approx 0.7 \text{ MeV}$

# Full dipole strength

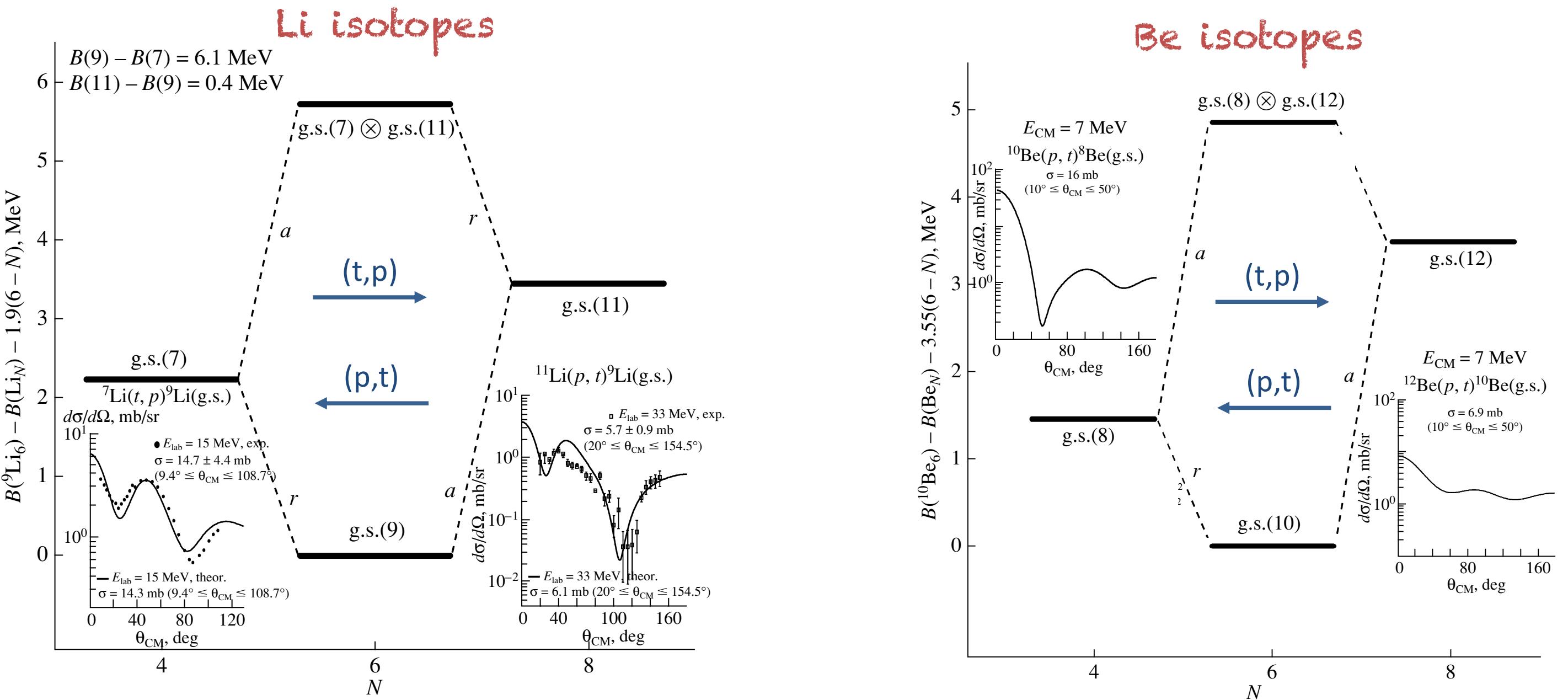
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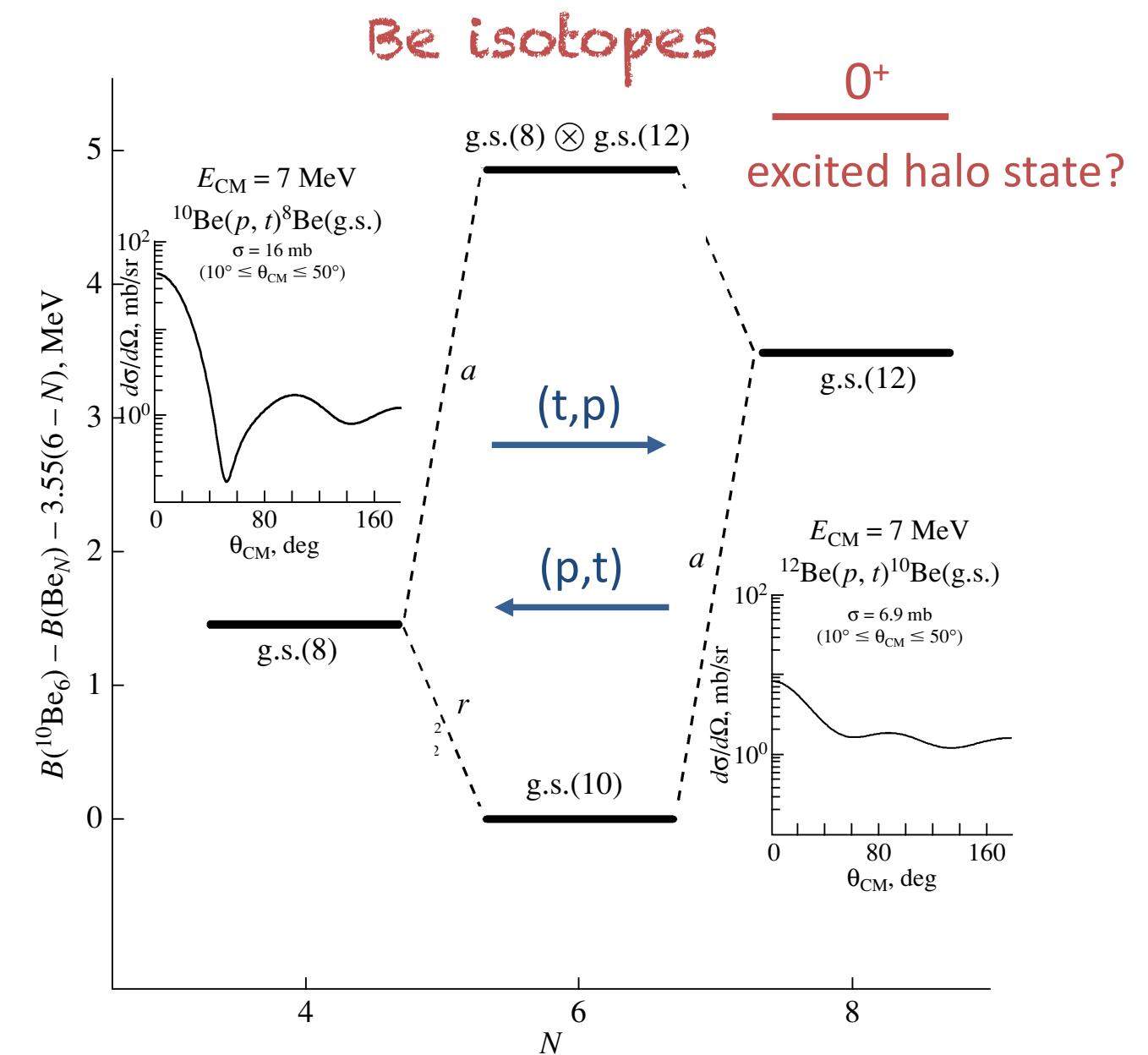
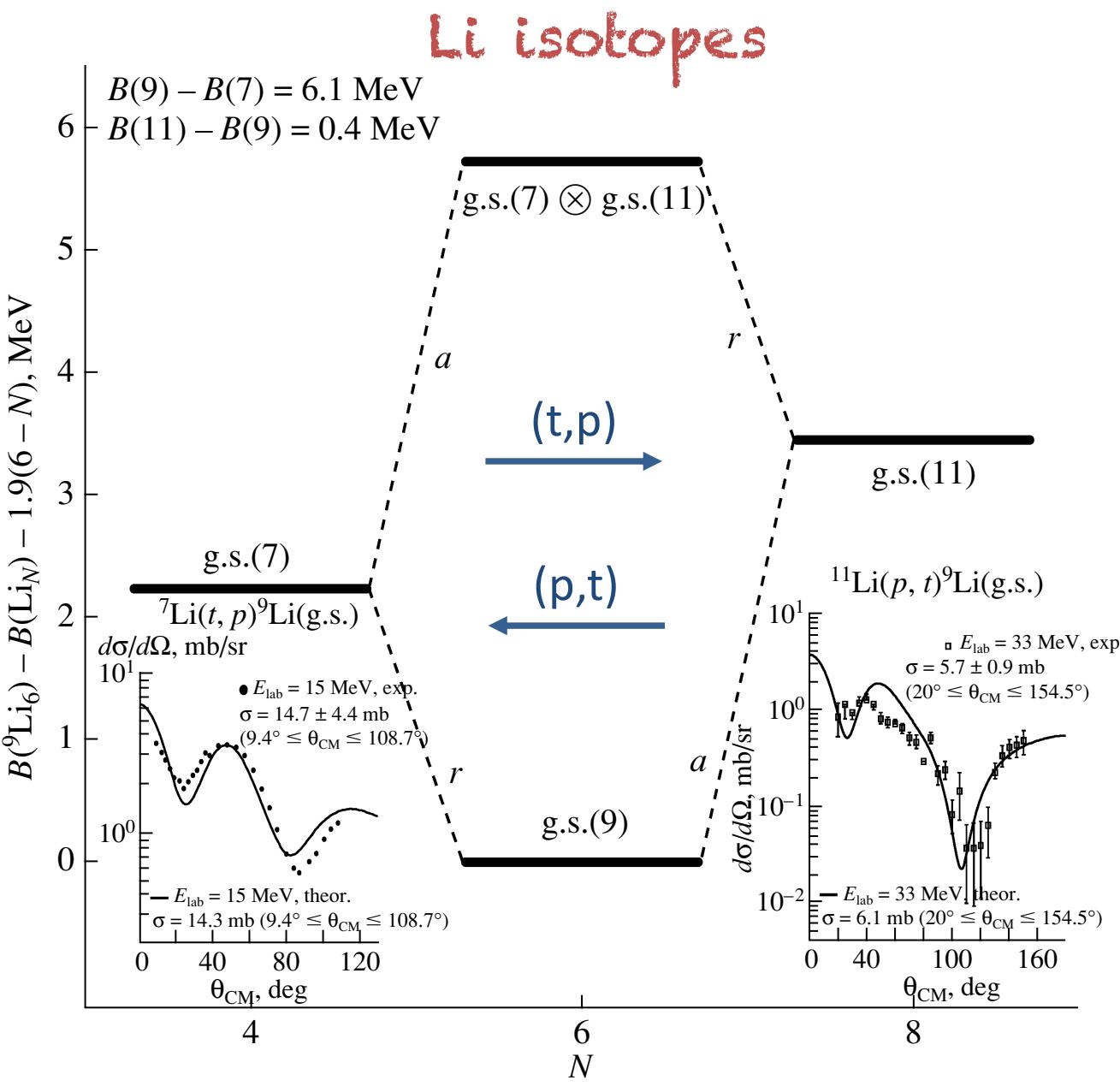
# Transition densities



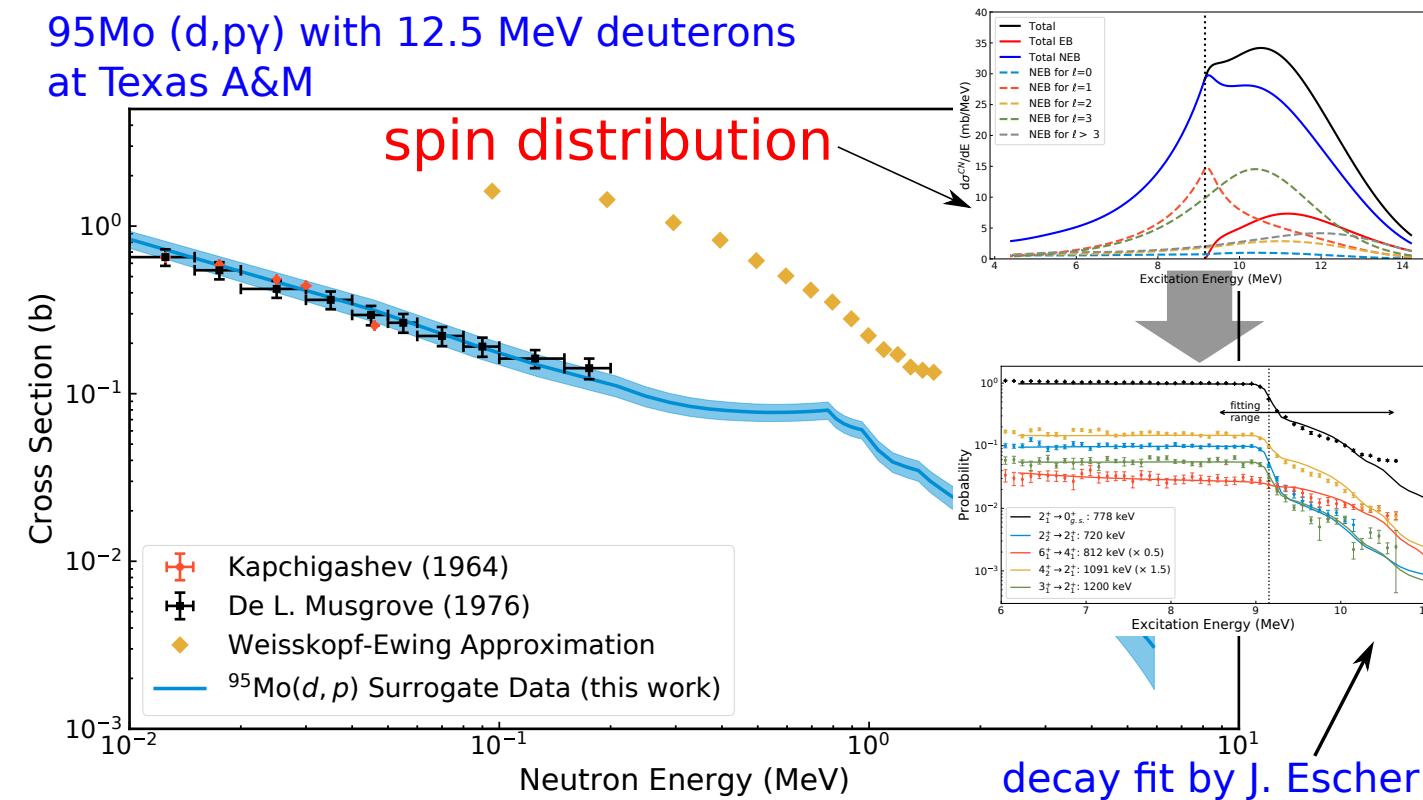
# Excited halo state in $^{12}\text{Be}$ ( $0^+_2$ )



# Excited halo state in $^{12}\text{Be}$ ( $0^+_2$ )



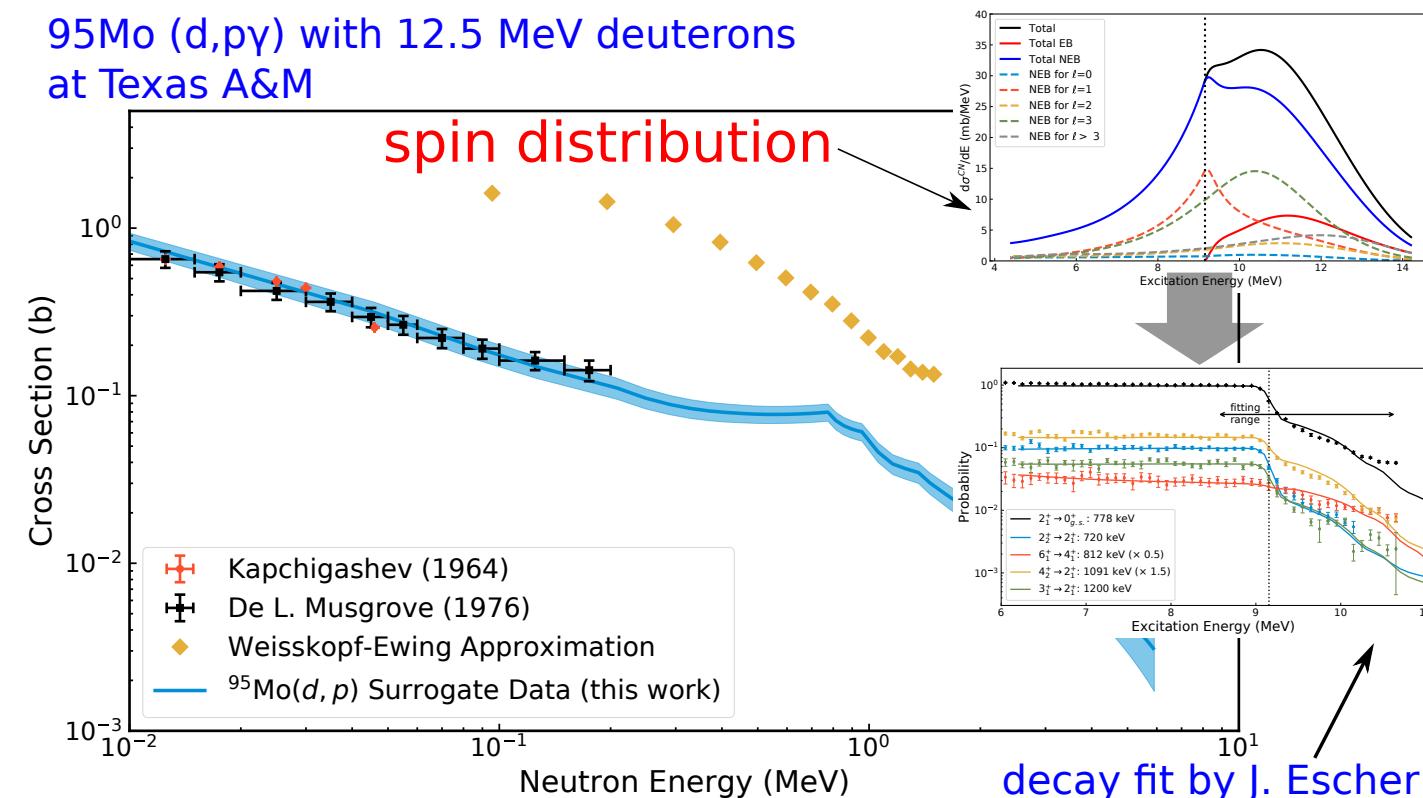
# An opportunity to thoroughly benchmark the SRM with $^{95}\text{Mo}(n,\gamma)$



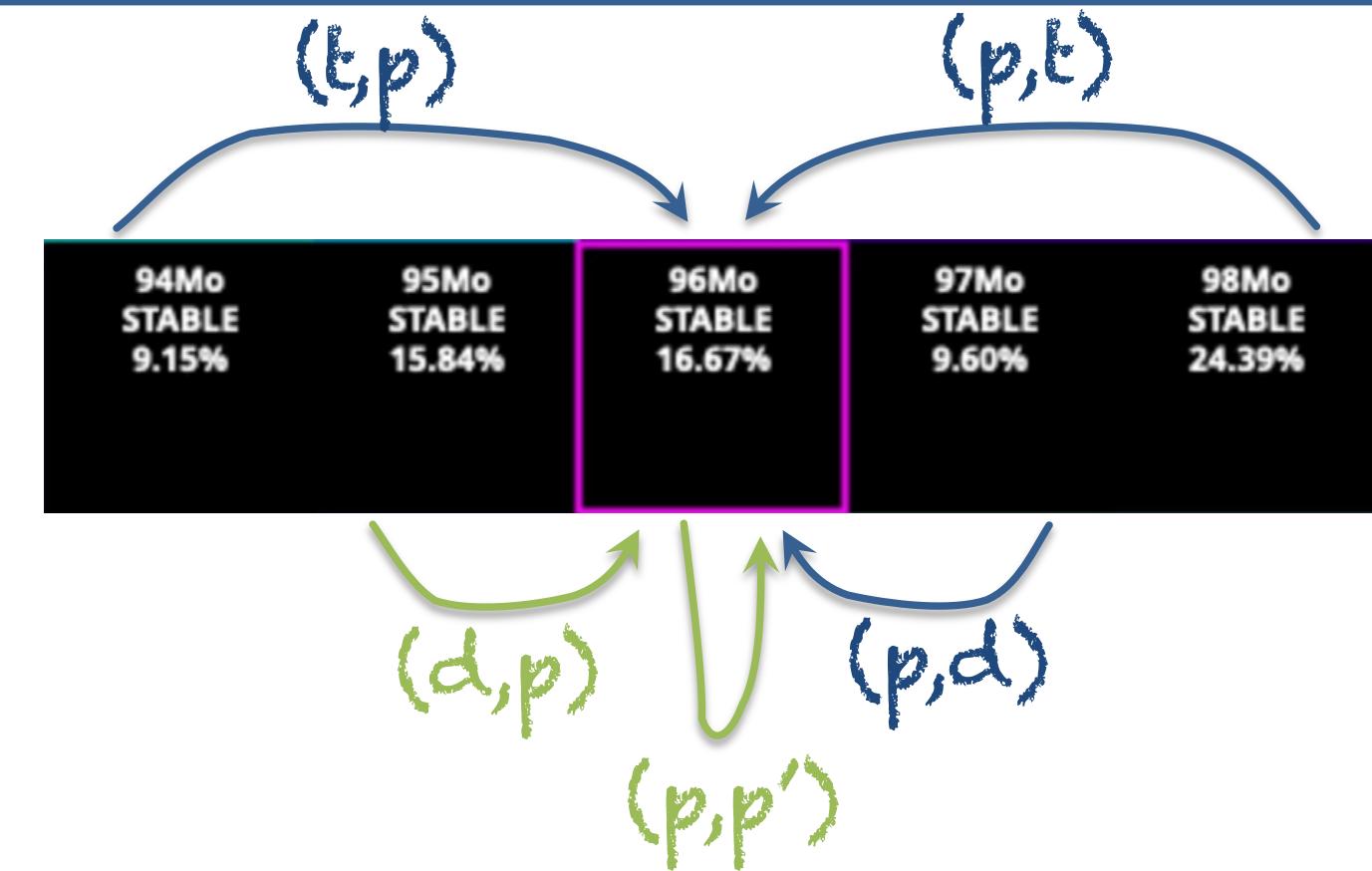
Ratkiewicz, Cizewski, Escher, GP, et al. Phys. Rev. Lett. 122052502 (2019)

- Excellent agreement with  $(n, \gamma)$  data.
  - The fitted Hauser-Feshbach decay is used to infer  $(n, \gamma)$  rates.
- 
- No previous knowledge of  $D_0$ , and/or  $\langle \Gamma_\gamma \rangle$  is needed.
  - No need for separate determination of NLD and  $\gamma$ SF.

# An opportunity to thoroughly benchmark the SRM with $^{95}\text{Mo}(n,\gamma)$

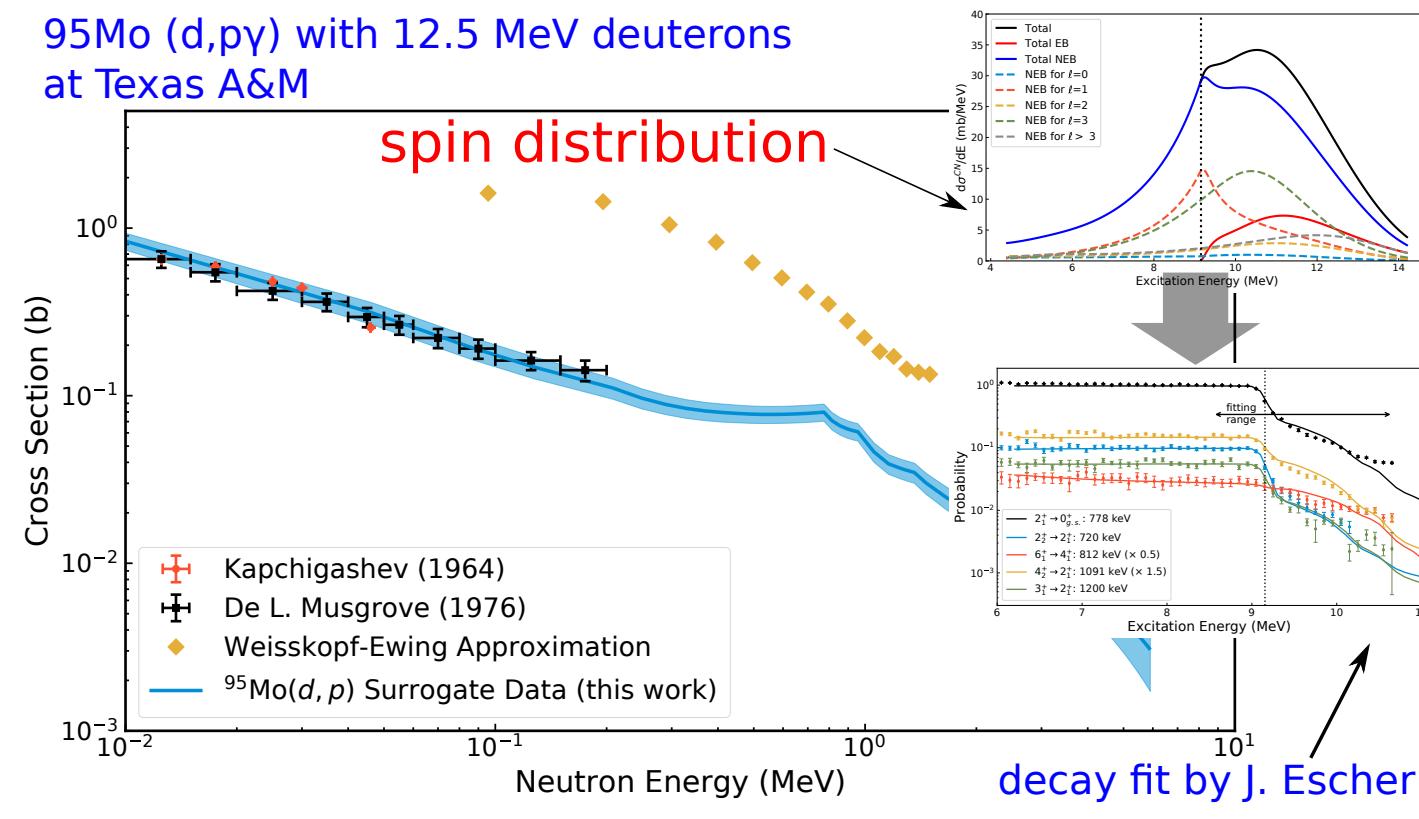


Ratkiewicz, Cizewski, Escher, GP, et al. Phys. Rev. Lett. 122052502 (2019)



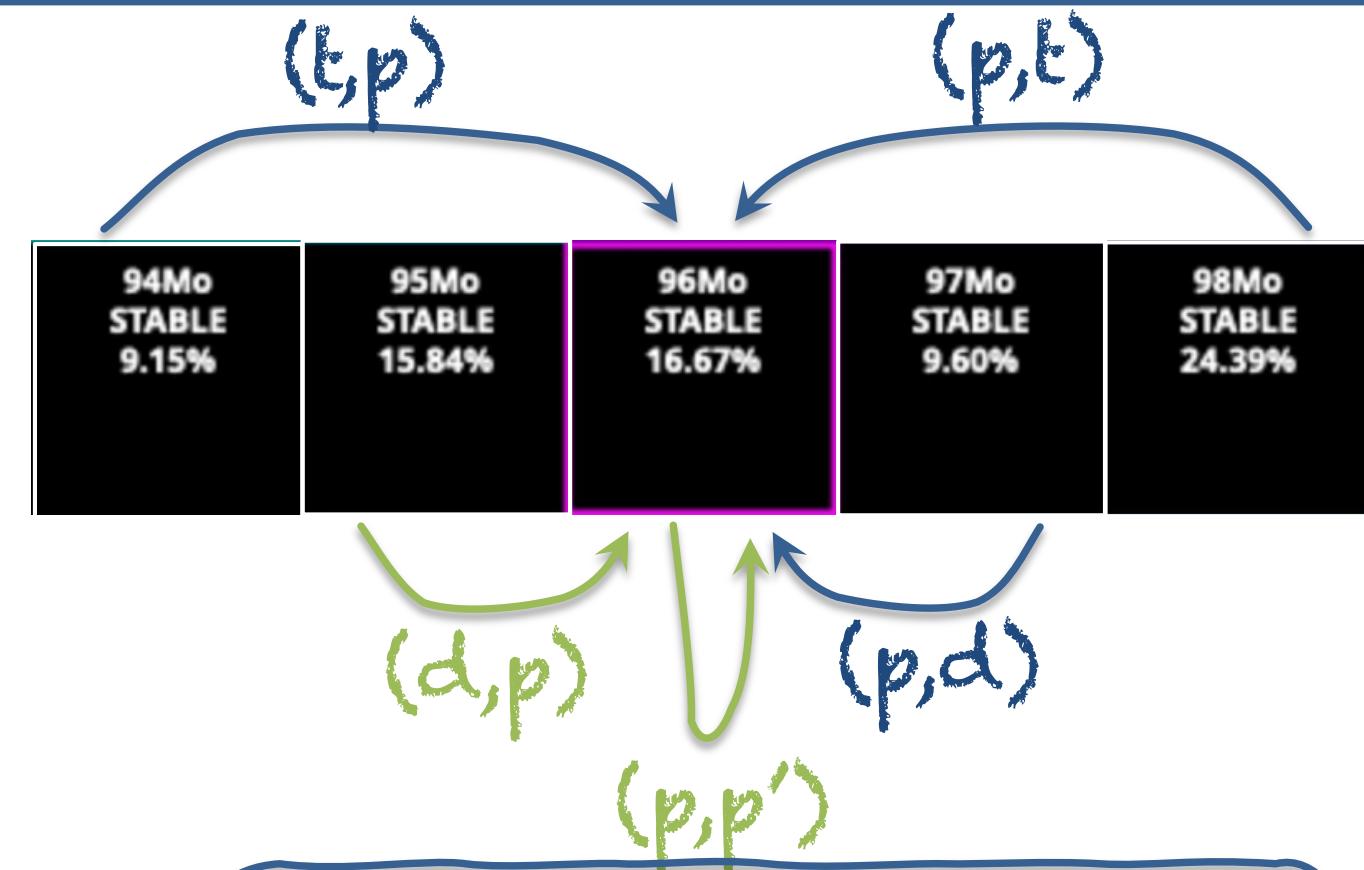
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- $^{94-98}\text{Mo}$  are all stable
- $^{95}\text{Mo}(n,\gamma)$  is known
- $^{95}\text{Mo}(\text{d},\text{p}\gamma)$  and  $^{95}\text{Mo}(\text{p},\text{p}'\gamma)$  have been measured
- Opportunity to benchmark many SRM techniques (A. McIntosh talk)