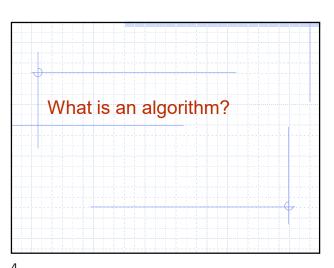
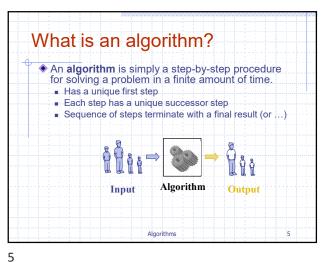


Lecture 1: Theoretical Computer Science or, What problems can computers solve? Locating infinity in the study of algorithms.

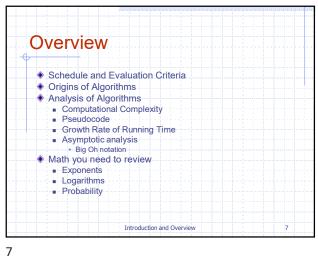


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Wholeness Statement The study of algorithms is a core part of computer science and brings the scientific method to the discipline; it has its theoretical aspects (a systematic expression in mathematics), can be verified experimentally, has a wide range of applications, and has a record of achievements. Science of Consciousness: SCI also has theoretical and experimental aspects, and can be applied and verified universally by anyone. Introduction and Overview

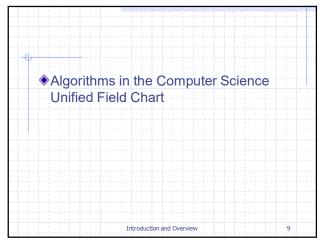
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Schedule CS 435 Algorithms Introduction and Overview 8

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Course Syllabus

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Course Goal The goal of the course is to learn how to design and analyze various algorithms to solve a computational We will achieve this through in-class and homework exercises to help us learn how to break a problem into subtasks, select from a range of possible design strategies, select from a set of abstract data types,
 Then design an algorithmic solution using pseudo code, evaluate the efficiency of our algorithm to justify the selections used in the design of our solution. This goal will also be achieved by studying examples from a range of algorithms, including their design, analysis, implementation, and experimentation. This is a course in problem solving Introduction and Overview

**Course Objectives** Students should be able to: Design an algorithm to solve a computational problem based on one or more of the basic design strategies: exhaustive search, divide-and-conquer, greedy, dynamic programming, memoization, randomization, and/or prune-Explain and use big O notation to specify the asymptotic space and time complexity (upper bounds) of some specific algorithm's, e.g., the computational complexity of the principal algorithms for sorting, searching, selection, and hashing. Create complex algorithms by breaking a problem into subtasks and then using various abstract data structures as building blocks to create efficient solutions. Explain factors other than computational efficiency that influence the choice of adjorithms, such as programming time, simplicity, maintainability, and the use of application-specific patterns in the input data.

Understand the importance of the basic complexity classes P, NP, NP-Hard, and NP-Complete and why certain problems will likely remain intractable unless P=NP. Design solutions to graph problems by incorporating the fundamental graph algorithms, including depth-first and breadth-first search, single-source shortest paths, and minimum spanning tree algorithms. Explain the connection between the Science of Consciousness and Algorithm Analysis and Design. Introduction and Overview

11 12

VALUATION CRITE	
The course grade will be based on tw	o examinations,
several quizzes, lab assignments, cla the Professional Etiquette evaluation	ss participation, ar
weights:	with the following
Class Participation and Attendance	5%
Homework, Labs & Quizzes	10%
Midterm Exam	40%
Final Exam	45%
Attendance at all class sessions inclu	ding labs is require
Attendance at all class sessions inclu Unexcused absences or tardiness will final grade.	l reduce a student'

**APPROXIMATE GRADING SCALE** Percent Grade 97 - 100A+ 90 - 97Α 87 - 90A-B+ 84 - 8776 - 84В 73 - 76B-70 – 73 C+ 62 - 70C 0 - 62NC Introduction and Overview

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COURSE TEXTBOOK

The following textbook is was used as the basis for this course. Reading assignments will be made from this text.

\* Algorithm Design: Foundations, Analysis, and Internet Examples, by M. Goodrich & R. Tamassia, published by Wiley & Sons, 2002.

OTHER REFERENCES

 An Introduction to Algorithms by T.H. Cormen, C.E. Leiserson, R.L. Rivest published by McGraw-Hill (1000 pages, difficult reading but a great reference.)

 The Algorithm Design Manual by Steve S. Skiena published by Springer-Verlag 1998 (500 pages, a unique and excellent book containing an outstanding collection of real-life challenges, a survey of problems, solutions, and heuristics, and references help one find the code one needs.)

 Data Structures, Algorithms, and Applications in Java by Sartaj Sahni published by McGraw-Hill Companion website:
 http://www.mhe.com/engcs/compsci/sahnijava/ (Java code for many algorithms.)

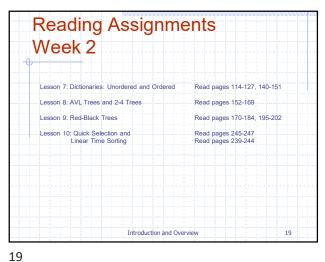
 Foundations of Algorithms, Using Java Pseudocode by Richard Neapolitan and Kumarss Naimipour published by Jones and Bartlett Publishers, 2004 (600 pages, all mathematics is fully explained; clear analysis)

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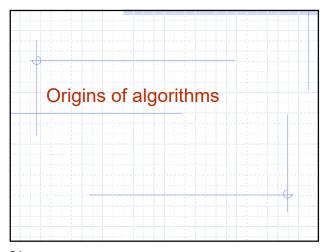
**Daily Schedule** 10am-12:15pm lecture (with a break) 12:15-12:30pm morning meditation Afternoon: 12:30-1:30pm 1:30-2:45pm lecture or homework 2:55-3:20pm group meditation 3:30-4:00pm class as needed Evening: dinner, homework, rest Introduction and Overview 17 Reading Assignments Week 1 Lesson 1a: Overview & Algorithm Analysis Read pages 4-20, 31-33, 42-46 Lesson 1b: Mathematical Review Read pages 21-28 Lesson 2: Stacks, Queues, Vectors, Lists, Read pages 56-74 and Sequences Lesson 3: Amortization and Trees Read pages 34-41, 75-93 Lesson 4: Priority Queues and Sorting Read pages 94-113 Read pages 218-224, Read pages 235-238, 263-267 Lesson 5: Divide-and-Conquer: Merge-Sort and Quick-Sort Lesson 6: Master Method, Sorting Lower Read pages 268-270, Bound Introduction and Overview 18

17 18



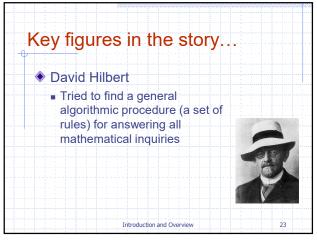
Reading Assignments Weeks 3 and 4 Lesson 11: Greedy Method and Dynamic Programmin Read pages 258-262 Read pages 274, 278-281 Lesson 12: Graphs & Graph Traversal Read pages 288-315 Read pages 340-359 Lesson 13: Weighted Graphs & Shortest Paths Lesson 14: Minimum Spanning Trees Read pages 360-375 Lesson 15: P vs. NP or Is P = NP? Read pages 592-599 Read pages 499-617, Read pages 618-626 Lesson 16: NP-Completeness and Approximation Read pages 316-334 Lesson 17: Directed Graphs Introduction and Overview

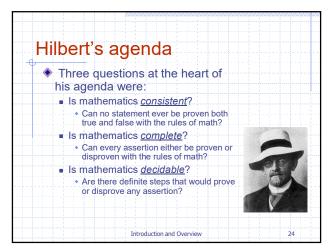
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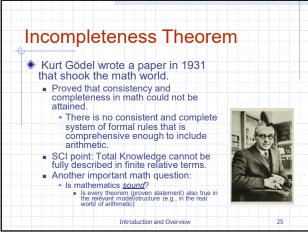


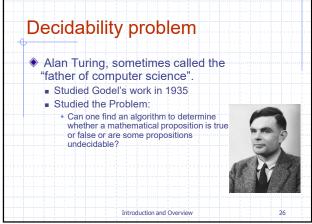
Once upon a time... In 1928 in the world of mathematics There existed the hope that a set of axioms (rules) could be identified that could unlock all the truths of mathematics ■ Properly applied, these rules could be applied to solve/prove the validity of any math problem/proposition ...and the world would be a better place. Introduction and Overview

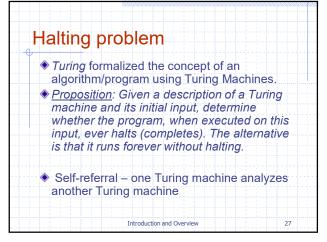
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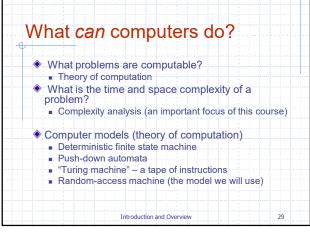






Does this program ever halt? A perfect number is an integer that is the sum of its positive factors (divisors), not including original number: 6 = 1 + 2 + 3 Algorithm FindOddPerfectNumber() Input: none Output: Returns an odd perfect number n := 1sum := 0 while sum ≠ n do n := n + 2sum := 0for fact := 1 to n/2 do if fact is a factor of n then sum := sum + fact return n Introduction and Overview

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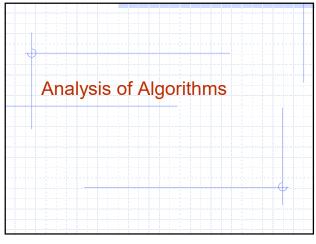


Main Point

1. The Halting Problem as well as other problems are provably non-computable, i.e., undecidable. That is, there cannot exist a universal method (algorithm) that can be used to determine whether every given mathematical proposition is true or false, such as whether or not a given program halts on a specific input. Such an algorithm would be finite but it would have to answer the question for an infinite number of propositions or programs.

Science of Consciousness: Total Knowledge, which is infinite, cannot be fully described in the finite relative. However, as we develop higher consciousness, we can experience and thus verify the existence of Total Knowledge as the unbounded silence at the source of thought; this is the basis of human creativity so we can apply it for the good of everything and everyone.

29 30



Algorithm Analysis

Answers the questions:

Can a problem be solved by algorithm?

Can it be solved efficiently?

Algorithms may look very similar, but be very different

Or

They may look very different, but be equivalent (in running time)

31 32

Computational Complexity

The theoretical study of time and space requirements of algorithms

Time complexity is the amount of work done by an algorithm

Roughly proportional to the critical (inherently important) operations

Running Time (§1.1) Most algorithms transform average case input objects into output objects. The running time of an algorithm typically grows with the input size. Average case time is often difficult to determine. So we usually focus on worst case running time. Easier to analyze Crucial to applications such as games, finance and robotics Introduction and Overview

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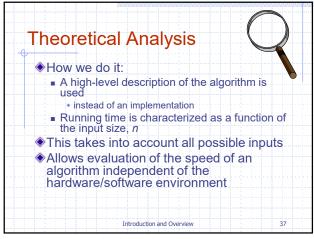
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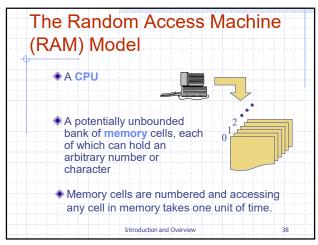
Experimental Studies (§ 1.6) Write a program implementing the algorithm Run the program with inputs of varying size and 5000 composition 4000 Use a method like 3000 System.currentTimeMillis() to 2000 get an accurate measure of the actual running time 1000 Plot the results 50 100 **Input Size** Introduction and Overview

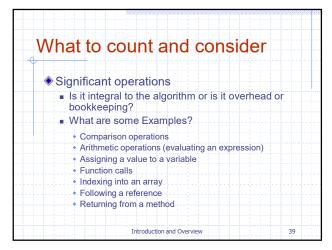
Limitations of Experiments

Requires implementation of the algorithm,
which may be difficult
Results may not be indicative of the running time on other inputs not included in the experiment.
To compare two algorithms,
the same hardware and software environments must be used

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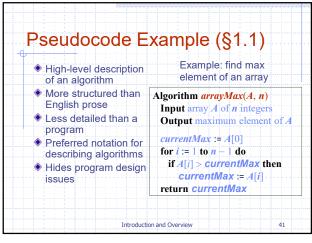




Pseudocode Details Method call Control flow var.method (arg [, arg...]) • if ... then ... [else ...] Return value • while ... do ... return expression do ... while .... Expressions for ... do ... ←or := Assignment Indentation replaces braces (like = in Java) Method declaration Equality testing Algorithm method (arg [, arg...]) (like == in Java) n<sup>2</sup> Superscripts and other mathematical formatting Input ... Output ... Introduction and Overview

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39



Primitive Operations

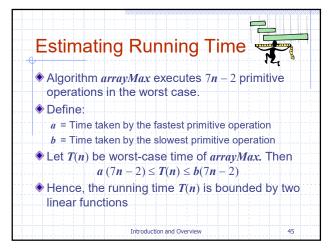
Basic computations performed by an algorithm
Identifiable in pseudocode
Largely independent of a programming language
Exact definition not important
(we will see why later)
Assumed to take a constant amount of time in the RAM model

41 42

## Counting Primitive Operations (§1.1) Inspect the pseudocode to determine the maximum number of primitive operations executed by an algorithm as a function of the input size Algorithm arrayMax(A, n) # operations currentMax := A[0] for i := 1 to n − 1 do if A[i] > currentMax then currentMax := A[i] { increment counter i (add & assign) } return currentMax Total

**Counting Primitive** Operations (§1.1) Inspect the pseudocode to determine the maximum number of primitive operations executed by an algorithm as a function of the input size Algorithm arrayMax(A, n) # operations currentMax := A[0] for i := 1 to n - 1 do 1 + **n** if A[i] > currentMax then 2(n-1)2(n-1)currentMax := A { increment counter i (add & assign) } 2(n-1)return currentMax Total 7n-2Introduction and Overview

43 44



Main Point

2. Complexity analysis determines the resources (time and space) needed by an algorithm so we can compare the relative efficiency of various algorithmic solutions. To design an efficient algorithm, we need to be able to determine its complexity so we can compare any refinements of that algorithm so we know when we have created a better, more efficient solution.

Science of Consciousness: Through regular deep rest (transcending) and dynamic activity we refine our mind and body until our thoughts and actions become most efficient; in the state of enlightenment, the conscious mind operates at the level of pure consciousness, which always operates with maximum efficiency, according to the natural law of least action, so we can spontaneously fulfill our desires and solve even non-computable problems.

45 46

Asymptotic Analysis

Asymptote:

A line whose distance from a given curve approaches zero as they tend to infinity

A term derived from analytic geometry

Originates from the Greek word asumptotos which means not intersecting

Thus an asymptote is a limiting line

Asymptotic:
Relating to or having the nature of an asymptote

Asymptotic analysis in complexity theory:
Describes the upper (or lower) bounds of an algorithm's behavior in terms of its usage of time and space
Used to classify computational problems and algorithms according to their inherent difficulty

We are going to classify algorithms in terms of functions of their input size

Therefore, how can we draw graphs of quadratic or cubic functions so the graphs look and behave like asymptotes (a limiting line)?

Log-Log Graph

A two-dimensional graph that uses logarithmic scales on both the horizontal and vertical axes.

The scaling of the axes is nonlinear

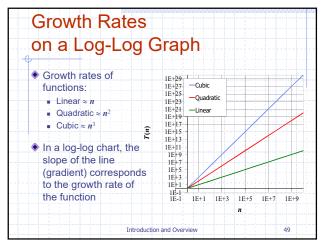
So a function of the form y = ax<sup>b</sup> will appear as a straight line

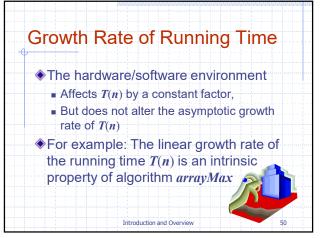
Note that

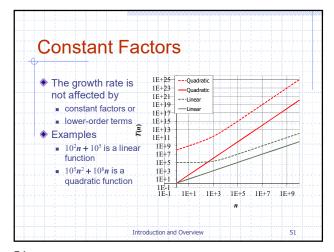
b is the slope of the line (gradient)

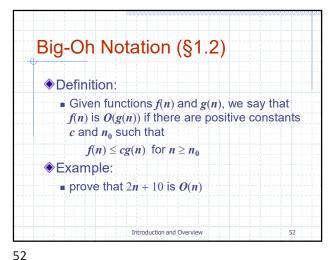
a is the y value when x = 1

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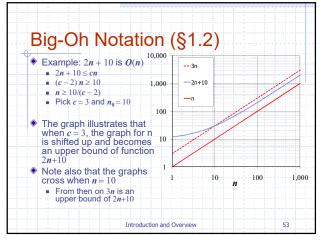


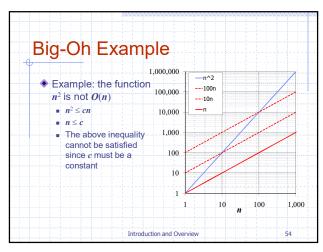




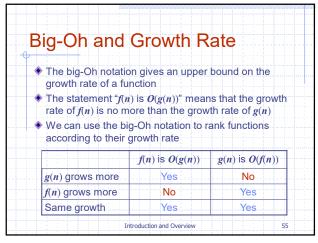


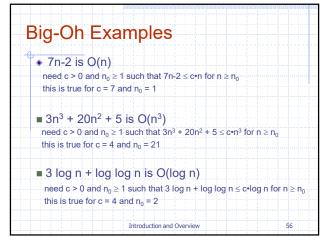
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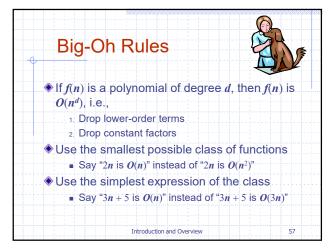




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Asymptotic Algorithm Analysis

The asymptotic analysis of an algorithm determines the running time in big-Oh notation

To perform the asymptotic analysis

We find the worst-case number of primitive operations executed as a function of the input size

We express this function with big-Oh notation

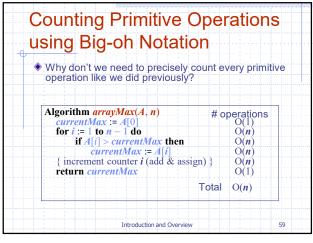
Example:

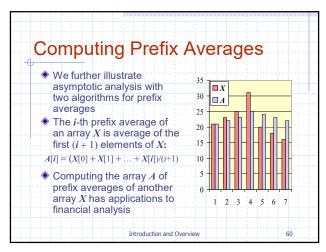
We determine that algorithm arrayMax executes at most 7n-2 primitive operations

We say that algorithm arrayMax "runs in O(n) time"

Since constant factors and lower-order terms are eventually dropped, we can disregard them when counting primitive operations

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59 60

Prefix Averages (Quadratic) The following algorithm computes prefix averages in quadratic time by applying the definition Algorithm *prefixAverages1(X, n)* Input array X of n integers Output array A of prefix averages of XA := new array of n integersn for i := 0 to n - 1 do s := X[0]for j := 1 to i do 1+2+...+(n-1)s := s + X[j]1+2+...+(n-1)A[i] := s / (i + 1)n return 4 1 Introduction and Overview

Arithmetic Progression

◆ The running time of prefixAverages1 is
O(1+2+...+n)

◆ The sum of the first n integers is n(n+1)/2

◆ Thus, algorithm prefixAverages1 runs in O(n²) time

61 62

Prefix Averages (Linear) The following algorithm computes prefix averages in linear time by keeping a running sum Algorithm *prefixAverages2(X, n)* Input array X of n integers Output array A of prefix averages of X#operations A := new array of n integersn for i := 0 to n - 1 do n s := s + X[i]n A[i] := s / (i+1)n return A ◆ Algorithm prefixAverages2 runs in O(n) time Introduction and Overview

Optimality

Can be proven by showing that every possible algorithm has to do at least some number of critical operations to solve the problem
Then prove that a specific algorithm attains this lower bound
Simplicity is an important practical consideration!!

Course motto: consider efficiency, but favor simplicity

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Main Point

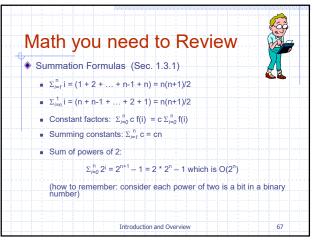
3. An algorithm is "optimal" if its computational complexity is equal to the "maximal lower bound" of all algorithmic solutions to that problem; that is, an algorithm is optimal if it can be proven that no algorithmic solution can do asymptotically better.

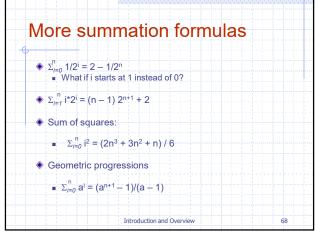
Science of Consciousness: An individual's actions are optimal if they are the most effective and life-supporting. Development of higher states of consciousness results in optimal action because thoughts are performed while established in the silent state of pure consciousness, the source of creativity and intelligence in nature.

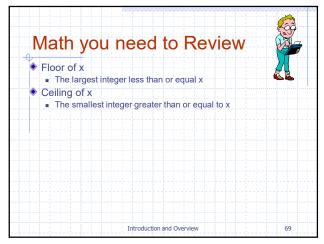
Math you need to Review

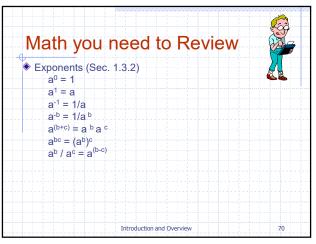
Summations (Sec. 1.3.1)
Logarithms and Exponents (Sec. 1.3.2)
Proof techniques (Sec. 1.3.3)
Basic probability (Sec. 1.3.4)

65 66

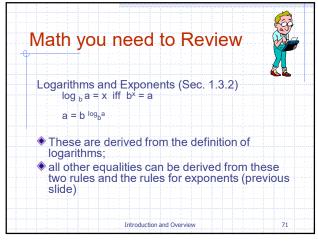


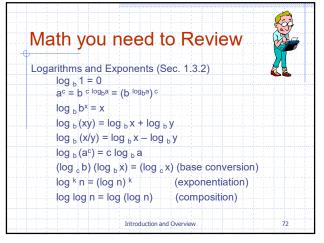




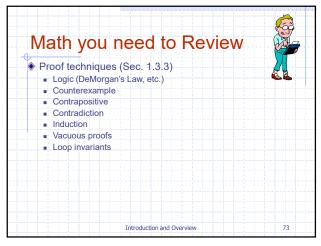


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Math you need to Review

Basic probability (Sec. 1.3.4)

Events
Independent
Mutually independent
Probability space
Random variables (independent)

A function that maps outcomes from some sample space S to real numbers (usually the interval (0, 1) to indicate the probability)

Expected values
Motivation (need to know the likelihood of certain sets of input)
Usually assume all are equally likely
E.g., if N possible sets, then 1/N is the probability

73 74

## Connecting the Parts of Knowledge with the Wholeness of Knowledge 1. An algorithm is like a recipe to solve a computable problem starting with an initial state and terminating in a definite end state. 2. To help develop the most efficient algorithms possible, mathematical techniques have been developed for formally expressing algorithms (pseudocode) so their complexity can be measured through mathematical reasoning and analysis; these results can be further tested empirically.

3. Transcendental Consciousness is the home of all knowledge, the source of thought. The TM technique is like a recipe we can follow to experience the home of all knowledge in our own awareness.

4. Impulses within Transcendental Consciousness: Within this field, the laws of nature continuously calculate and determine all activities and processes in creation.

5. Wholeness moving within itself: In unity consciousness, all expressions are seen to arise from pure simplicity--diversity arises from the unified field of one's own Self.