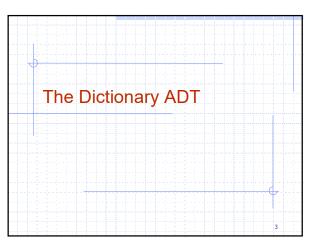


## Wholeness Statement

The Dictionary ADT stores a searchable collection of key-value items that represents either an unordered or an ordered collection. Hashing solves the problem of item-lookup by providing a table whose size is not unreasonably large, yet it can store a large range of keys such that the element associated with each key can be accessed quickly (O(1)). SCI provides systematic techniques for accessing and experiencing total knowledge of the Universe to enhance individual life.



## Two Types of Dictionaries

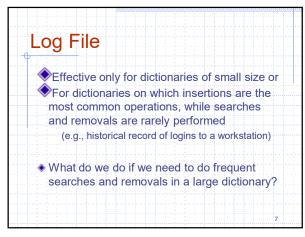
- 1. Unordered (§2.5.1)
- 2. Ordered (§3.1)
- Both use a key to identify a specific element/value
- Stores items, i.e., key-value pairs
- For the sake of generality, multiple items can have the same key

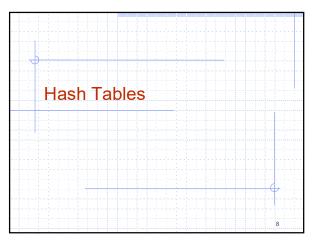
3

**Unordered Dictionary** ADT (§2.5.1) The dictionary ADT models a searchable collection of key-Dictionary ADT methods: findValue(k): if the dictionary has an item with key k, returns its element, else, element items The main operations of a returns the special element dictionary are searching, NO SUCH KEY inserting, and deleting items insertItem(k, o); inserts item Multiple items with the same key (k, o) into the dictionary are allowed removeItem(k): if the Applications: dictionary has an item with key k, removes it from the address book dictionary and returns its credit card authorization element, else returns the special element NO\_SUCH\_KEY mapping host names (e.g. (e.g., 128.148.34.101) size(), isEmpty() keys(), values(), items()

Log Files (§2.5.1) A log file (or audit trail) is a dictionary implemented by means of an unsorted sequence Items are stored in the dictionary in a sequence in arbitrary order Based on doubly-linked lists or a circular array Performance: insertItem takes O(1) time since we can insert the new item at the beginning or at the end of the sequence • find Value and remove tem take O(n) time since in the worst case (the item is not found) we traverse the entire sequence to look for an item with the given key

5 6





Hash Tables and Hash
Functions (§2.5.2)

A hash table for a given key type consists of
Hash function h
Array (called table) of size N

A hash function h maps keys of a given type to integers in a fixed interval [0, N-1]

Example:
h(k) = k mod N
is a hash function for integer keys
The integer h(k) is called the hash value of key k

Goals of Hash Functions

1. Store item (k, o) at index i = h(k) in the table

2. Avoid collisions as much as possible

Collisions occur when two keys hash to the same index i

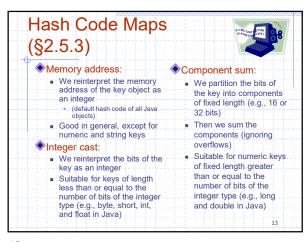
The average performance of hashing depends on how well the hash function distributes the set of keys (i.e., avoids collisions)

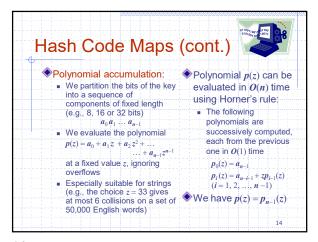
10

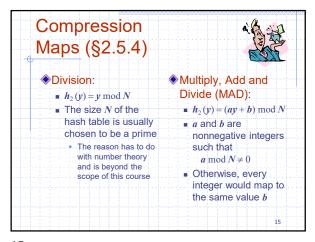
9

Example Design a hash table for a 025-612-0001 dictionary storing items 981-101-0002 (SSN, Name), where SSN (social security number) is a 451-229-0004 nine-digit positive integer Our hash table uses an array of size N = 10,000 and 9998 9999 Ø 200-751-9998 the hash function h(x) =last four digits of x11 Hash Functions (§ 2.5.3) The hash code map A hash function is is applied first, and usually specified as the the compression map composition of two is applied next on the functions: result, i.e., Hash code map:  $\boldsymbol{h}(\boldsymbol{x}) = \boldsymbol{h}_2(\boldsymbol{h}_1(\boldsymbol{x}))$  $h_1$ : keys  $\rightarrow$  integers The goal of the hash function is to Compression map: "disperse" the keys in  $h_2$ : integers  $\rightarrow [0, N-1]$ an apparently random

11 12





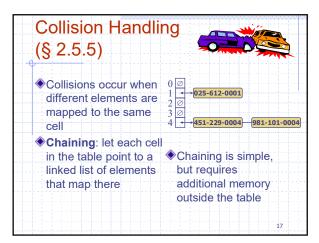


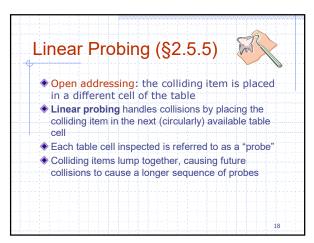
Main Point

1. The hash function solves the problem of fast table-lookup, i.e., it allows the element associated with each key to be accessed quickly (in O(1) time). A hash function is composed of a hash code function and a compression function that transforms (in constant time) each key into a specific location in the table.

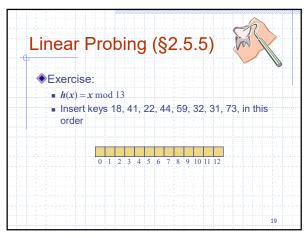
Science of Consciousness: Through a process of self-referral, the unified field transforms itself into all the values of creation without making mistakes.

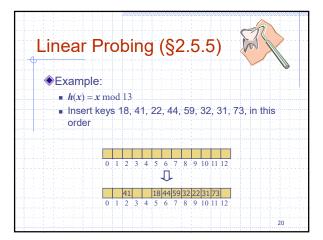
15 16

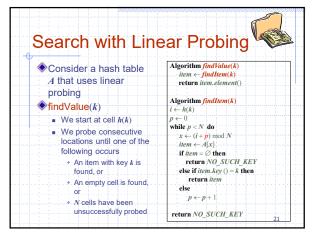


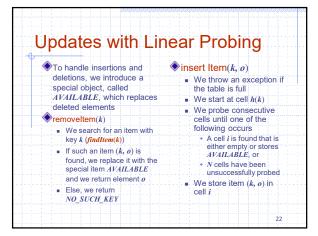


17 18

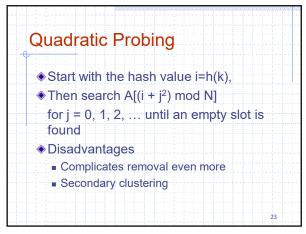


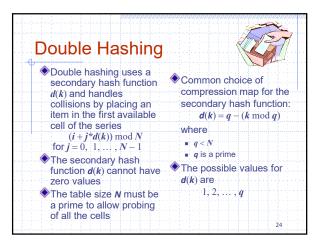




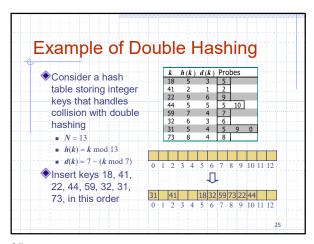


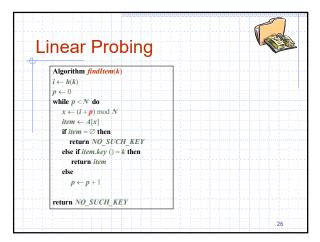
21 22

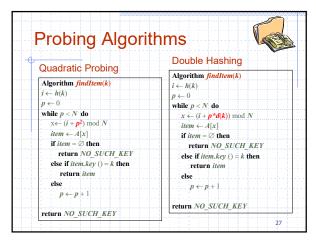




23 24





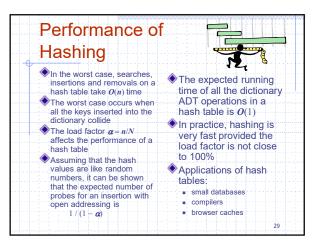


Load Factors and Rehashing

Load factor is n/N where n is the number items in the table and N is the table size

When the load factor goes above .75, the table is resized and the items are rehashed

27 28



Universal Hashing

If allowed to pick the keys to be hashed, then a malicious adversary can choose n keys that all hash to the same slot

Any fixed hash function is vulnerable to this sort of worst-case behavior

The only effective way to improve the situation

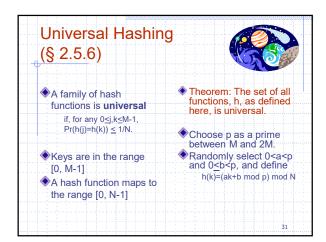
Choose the hash function randomly in a way that is independent of the keys to be stored

This approach is called universal hashing

The hash function is chosen randomly at beginning of execution

Yields good performance no matter what keys are chosen by an adversary

29 30

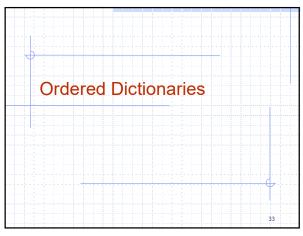


Main Point

2. A hash table is an example of a highly efficient implementation of an unordered Dictionary ADT (its operations have complexity O(1)). However, efficiency is only possible if the issues related to implementation are handled, e.g., resizing, handling collisions.

Science of Consciousness: Access to Pure Consciousness is simple, effortless, easy, and spontaneous through the introduction of the proper techniques.

31 32



Ordered Dictionaries

• Keys are assumed to come from a total order, i.e., the keys can be sorted.
• Constraints of iterator operations:

• keys()

Returns an iterator of the keys in sorted order

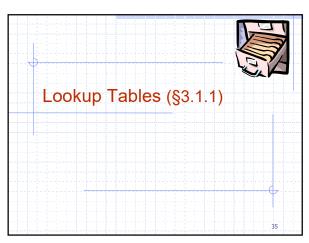
• values()

Returns the element of the items in key-sorted order

• items()

Returns the (k, e) items in sorted order by key (k) of the item

33 34



Lookup Table (§3.1.1)

A dictionary implemented by means of a sorted sequence

• store the items of the dictionary in an array-based sequence, sorted by key

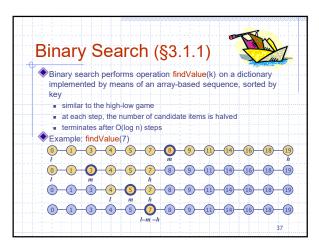
• use an external comparator for the keys

When would a table like this be useful?

• only useful if primarily used for lookup and rarely updated with added items or removals

• when the input to the table is processed or comes in in sorted order

35 36



Binary Search Algorithm

(recursive)

Algorithm BinarySearch(S, k, low, high):
Input: An ordered vector S storing n items, accessed by keys()
Output: An element of S with key k and rank between low & high.

if low > high then
return NO\_SUCH\_KEY
else
mid ← (low + high)/2
if k = key(mid) then
return elem(mid)
else if k < key(mid) then
return BinarySearch(S, k, low, mid-1)
else
return BinarySearch(S, k, mid + 1, high)

37 38

Running Time of Binary Search

Running time proportional to number of recursive calls performed.

Recurrence equation:  $T(n) = \begin{cases} b & \text{if } n = 0 \\ T(n/2) + b & \text{else,} \end{cases}$ Exercise: solve this recurrence equation (use the master method).

Running Time of Binary Search

Recurrence equation:  $T(n) \leq \begin{cases} b & \text{if } n < 2 \\ T(n/2) + b & \text{else,} \end{cases}$ Guess: T(n) is  $O(\log n)$ Assume  $T(n/2) \leq c \log n/2$   $T(n) \leq c \log n/2 + b$   $= c (\log n - \log 2) + b$   $= c (\log n - 1) + b$   $= c \log n - c + b$   $\leq c \log n & \text{for } b \leq c$ 

39 40

Binary Search Algorithm (iterative)
for use in a Lookup Table

Algorithm BinarySearch(S, k):
 Input: An ordered Sequence S storing n items, ordered by keys()
 Output: The rank in S where key k is stored; if not in table, then the rank
 where an item containing k should be inserted.

| low ← 0
| high ← S.size() - 1
| while low < high do
| mid ← (low + high)/2
| item ← S.elemAtRank(mid)
| if item.key() < k then | // only one key comparison per iteration
| low ← mid + 1
| else | // item.key() ≥ k (mid is not eliminated yet)
| high ← mid
| return low // the rank where an item with key k is located or should be
| // inserted because every item at rank < low, the item.key() < k
| 41

findValue using a Binary Search to find an item in a Lookup Table

Algorithm findValue(k):
Input : An ordered (by keys)) Sequence S storing n items is a private internal field inside the Lookup Table

Output: the element associated with k in the sequence of items in S if it is in the table.

rank ← binarySearch(S, k)

if S.size() ≤ rank then return NO\_SUCH\_KEY // handles empty S item ← S.elemAlRank(rank)

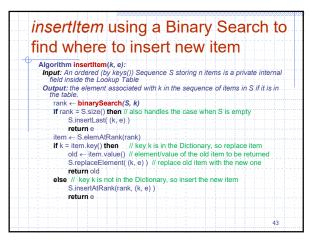
if k = item.key() then

return item.value()

else // key k is not in the Dictionary

return NO\_SUCH\_KEY

41 42



removeItem using Binary Search to find where to remove

Algorithm removeItem(k):
Input: An ordered (by keys()) Sequence S storing n items as a private internal field inside the Lookup Table

Output: the item containing k in the sequence of items in S is removed from the table if it exists.

rank ← binarySearch(S, k)

If S.size() ≤ rank then return No\_SUCH\_KEY // handles empty S item ← S.elemAlRank(rank)

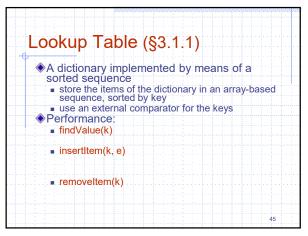
If k = item.key() then // key k is in the Dictionary

old ← item.value() // element of the old item is to be returned S.removeAtRank(rank) // remove old item return old

else // key k is not in the Dictionary

return No\_SUCH\_KEY

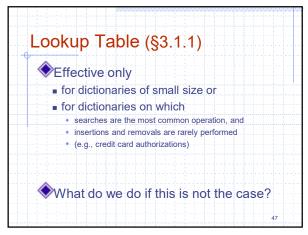
43 44



Lookup Table (§3.1.1)

♠ A dictionary implemented by means of a sorted sequence
■ store the items of the dictionary in an array-based sequence, sorted by key
■ use an external comparator for the keys
♠ Performance:
■ findValue takes O(log n) time, using binary search
■ insertItem takes O(n) time since in the worst case we have to shift n items to make room for the new item
■ removeItem take O(n) time since in the worst case we have to shift n/2 items to compact the items after the removal

45 46



Main Point

3. A lookup table is an example of an ordered Dictionary ADT allowing elements to be efficiently accessed in order by key. When implemented as an ordered sequence, searching for a key is relatively efficient, O(log n), but insertion and deletion are not, O(n).

Science of Consciousness: The unified field of natural law always operates with maximum efficiency.

47 48

## Connecting the Parts of Knowledge with the Wholeness of Knowledge

- A hash table is a very efficient way of implementing an unordered Dictionary ADT; the running time of search, insertion, and deletion is expected O(1) time.
- 2. To achieve efficient behavior of the hash table operations takes a careful choice of table size, load factor, hash function, and handling of collisions.

- 3. Transcendental Consciousness is the silent field of perfect efficiency and frictionless flow for coordinating all activity in the universe.
- 4. Impulses within Transcendental
  Consciousness: The dynamic natural laws
  within this unbounded field create and maintain
  the order and balance in creation, all
  spontaneously without effort.
- 5. Wholeness moving within itself: In Unity Consciousness, the diversity of creation is experienced as waves of intelligence, perfectly efficient fluctuations of one's own self-referral consciousness.

5