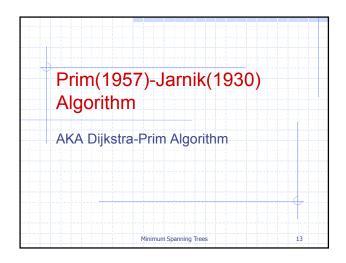
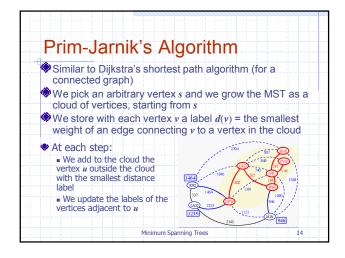
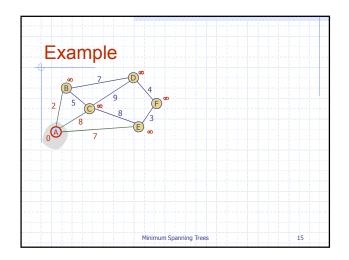


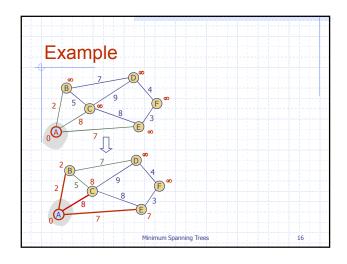
Generic MST Algorithm Algorithm GenericMST(G) T ← a tree with all vertices in G, but no edges while T does not form a spanning tree do (u, v) ← a safe edge of G T ← (u, v) ∪ T return T A safe edge is one that when added to T forms a subgraph of a MST

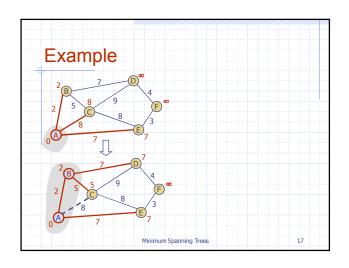
Main Point 1. A minimum spanning tree algorithm gradually grows a (sub-solution) tree by adding a "safe edge" that connects a vertex in the tree to a vertex not yet in the tree. The nature of life is to grow and progress to the state of enlightenment, fulfillment.

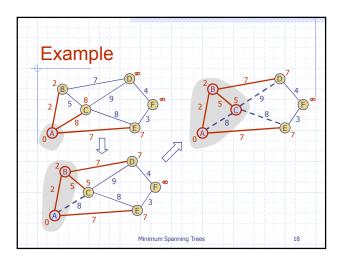


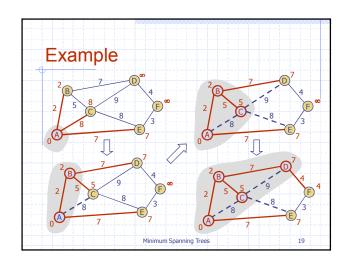


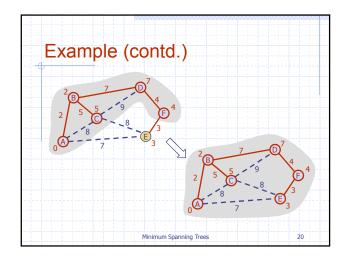


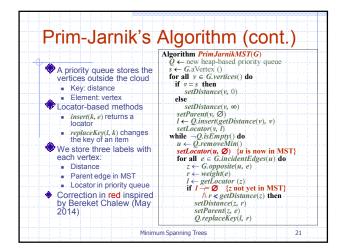


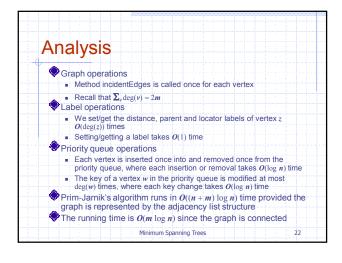




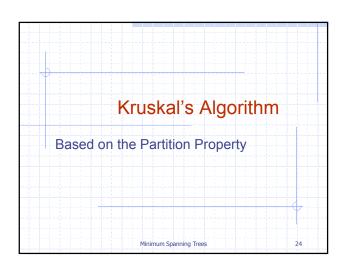


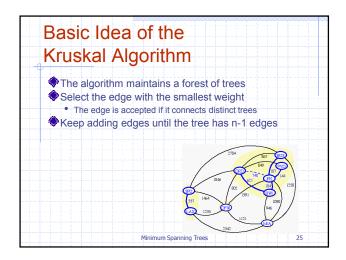


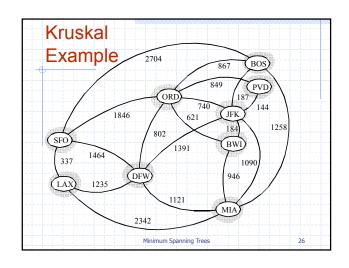


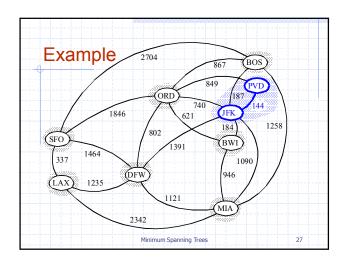


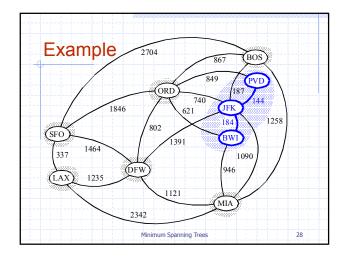
Main Point 2. A defining feature of the Minimum Spanning Tree (and shortest path) greedy algorithms is that once a vertex becomes in-tree (or "inside the cloud"), the resulting subtree is optimal and nothing can change this state. A defining feature of enlightenment is that once this state is reached, one's consciousness is optimal and nothing can change this state. Minimum Spanning Trees 23

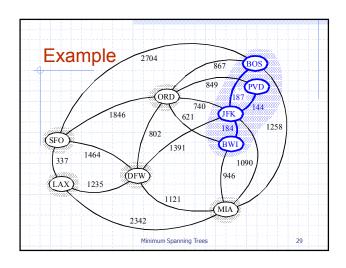


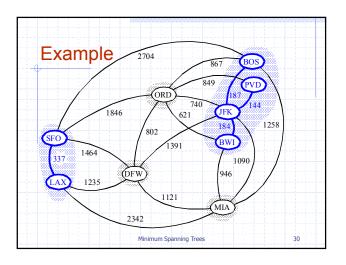


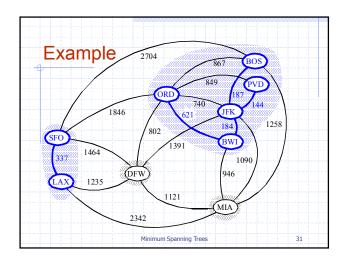


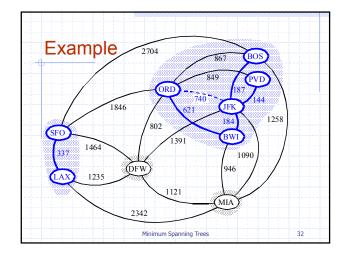


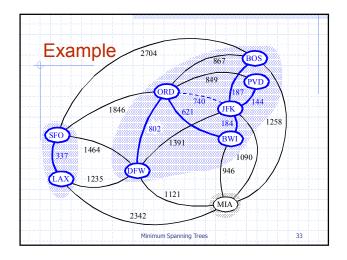


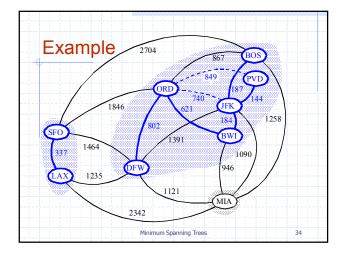


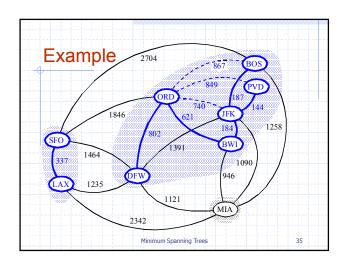


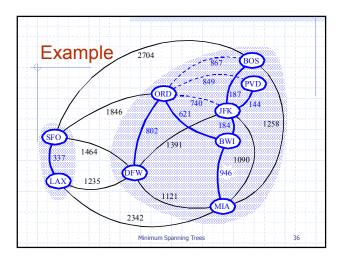


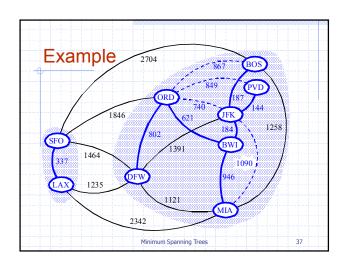


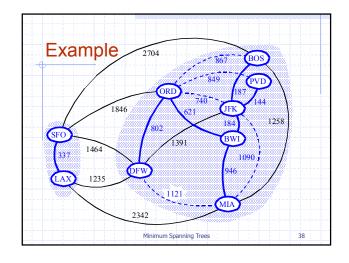


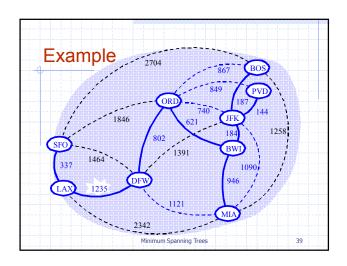


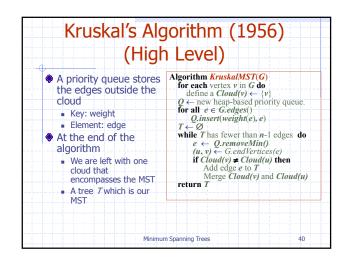


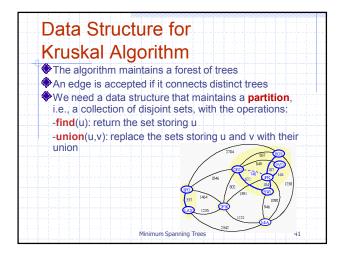


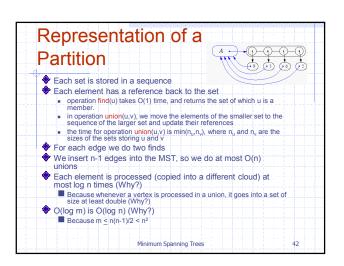


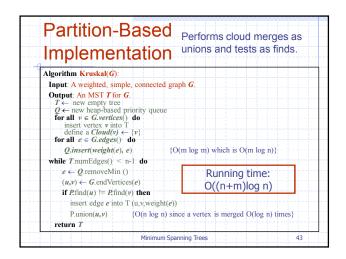


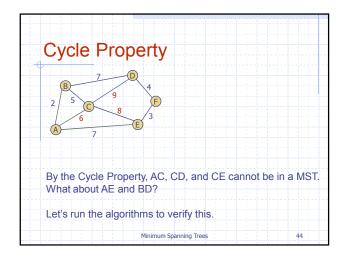


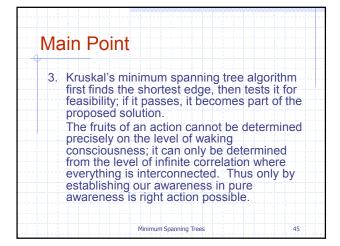


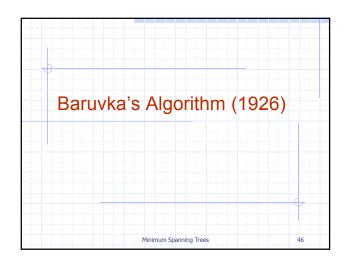


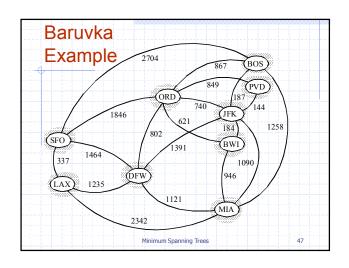


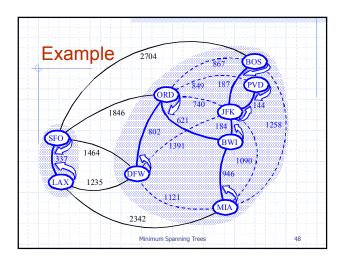


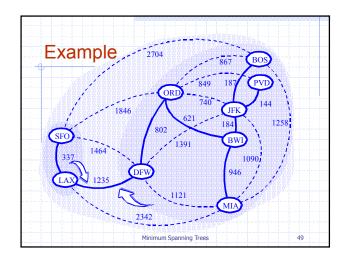


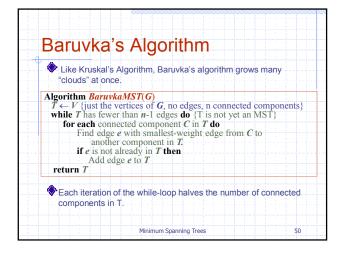












Baruvka's Algorithm
(more details)

Algorithm BaruvkaMST(G)
for each e ∈ G.edges() do {label edges NOT_IN_MST}
setMSTLabel(e, NOT_IN_MST) {no edges in MST}
numEdges ← 0
while numEdges < n-1 do
labelVerticesOfEachComponent(G) {BFS}
insertSmallest-WeightEdgeOutOfComponents(G)
return G

Required functionality

Does not use a priority queue or locators!
Does not use union-find data structures!
Maintains a forest T subject to edge insertion
Can be supported in O(1) time using labels on edges in MST
Step 1: Mark vertices with number of the component to which they belong
Traverse forest T to identify connected components
O(1) time to label each vertex
Requires extra instance variable for each vertex
Takes O(n) time using a DFS or a BFS each time through the while-loop
Step 2: Find a smallest-weight edge in E incident on each cluster/component C (insert into MST)
Scan adjacency lists of each vertex in each C to find minimum
Takes O(m) each time through the for-loop

Analysis of Baruvka's Algorithm

While-loop: each iteration (at worst) halves the number of connected components in T

Thus executed log n times
Identifying connected components (in for-loop)

Vertices are labelled with component name

DFS or BFS of T runs in O(n) time

Find smallest edge incident on each component C

Scan adjacency lists of vertices in G

O(m) time

The running time is O(m log n).

After labeling each vertex with its component number (Hw13) Algorithm DFS(G)
Input graph G
Output the edges of G are labeled as
discovery edges and back edges Algorithm DFS(G, v) setLabel(v, VISITED) startVertexVisit(v) for all $e \in G.incidentEdges(v)$ if getLabel(e) = UNEXPLOREDinitResult()
for all u ∈ G vertices()
setLabel(u, UNEXPLORED)
for all e ∈ G edges()
setLabel(e, UNEXPLORED) $w \leftarrow opposite(v,e)$ edgeVisit(v, e, w)if getLabel(w) = UNEXPLOREDsetLabel(e, DISCOVERY) for all v ∈ G.vertices()
if getLabel(v) = UNEXPLORED
preComponentVisit(v)
DFS(G, v)
postComponentVisit(v) preDiscoveryTraversal(v, e, w)
DFS(G, w) postDiscoveryTraversal(v, e, w) setLabel(e, BACK) backTraversal(v, e, w) finishVertexVisit(v) HW14: Insert into T the smallest-weight edge going out from each component

Lower Bound on MST Computation

- ◆There are <u>randomized</u> algorithms that compute MST's in expected <u>linear</u> time
- Linear time seems to be the lower bound
- Unknown whether there is a deterministic algorithm that runs in linear time (open question)

Minimum Spanning Trees

Main Point

 The "greedy" algorithms used by MST and shortest path only work for problems where localized attention can produce a globally optimal solution.

An enlightened person maintains unbounded awareness along with localized awareness. The behavior of such a person is globally optimal for any problem.

Minimum Spanning Trees

ng Trees 5

Connecting the Parts of Knowledge with the Wholeness of Knowledge

- Finding the minimum spanning tree can be done by an exhaustive search of all possible spanning trees, then choosing the one with minimum weight.
- To devise a greedy strategy, we identify a set of candidate choices, determine a selection procedure, and consider whether there is a feasibility problem. Then we have to prove that the strategy works.

Minimum Spanning Trees

 Transcendental Consciousness is the home of all the laws of nature, the source of all algorithms.

 Impulses within Transcendental Consciousness: The natural laws within this unbounded field are the algorithms of nature governing all the activities of the universe.

 Wholeness moving within itself: In Unity Consciousness, we perceive the spanning tree of natural law and appreciate the unity of all creation.

Minimum Spanning Trees

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