The following are to be written up and turned in separately from the rest of the homework.

1. Using the DFS Template Method Pattern algorithm given in the lecture notes, override the appropriate methods so this algorithm computes the connected components of a graph ***G***. Your method should return a sequence of vertices, 1 representative from each connected component.

2. a. Modify the breadth-first search algorithm so it can be used as a Template Method Pattern.
   b. Override the appropriate methods so that given two vertices of ***G***, your BFS finds a path in ***G*** between them with the minimum number of edges, or report that no such path exists.
   c. Override the appropriate methods so your solution finds a simple cycle in a graph ***G***. You as the algorithm designer are to decide what to return from your method.
   d. Can the template version of DFS be used to find the path between two vertices with the minimum number of edges? Briefly explain why or why not.

3. Modify Dijkstra's shortest path algorithm so it can be used as a Template Method Pattern. Then override the appropriate methods so it returns the shortest path between two vertices.

4. Based on either the DFS or the BFS template method algorithms, write the overriding methods so that all nodes in each connected component of a graph G are labeled with a sequence number, i.e., each vertex in a component would be labeled with the same number. For example, each node in the first connected component would be labeled with a 1, each node in the second connected component would be labeled with a 2, etc.