

Wholeness Statement

Knowledge of data structures allows us to pick the most appropriate data structure for any computer task, thereby maximizing efficiency. Science of Consciousness: Pure knowledge has infinite organizing power, and administers the whole universe with minimum effort.

Stacks, Queues, Vectors, & Lists

Τ

What is a type?

♦ x - y

• z.foo()

Stacks, Queues, Vectors, & Lists

Algorithms and Data Structures

- Closely linked
 - Algorithm (operation)
 - a step by step procedure for performing and completing some task in a finite amount of time
 - Data structure
 - an efficient way of organizing data for storage and access by an algorithm
- An ADT provides services to other algorithms
 E.g., operations (algorithms) are embedded in the data structure (ADT)

Stacks, Queues, Vectors, & Lists 4

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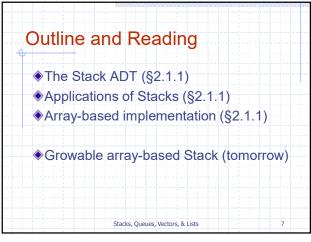
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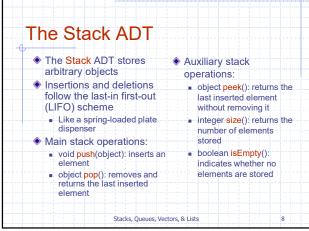
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Abstract Data Types (ADTs) An ADT is an Today we are going to look at abstraction of a data several examples: structure Stack Queue An ADT specifies: Data stored Vector List Operations on the Sequence Error conditions associated with operations Stacks, Queues, Vectors, & Lists

Stacks





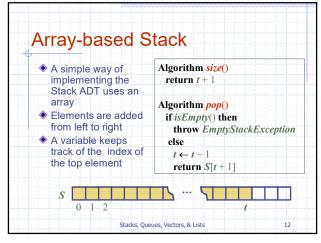
Exceptions Operations on the Operations pop and ADT may cause an top cannot be error condition, called performed if the stack an exception is empty Attempting a pop or Exceptions are said to top on an empty stack be "thrown" when an causes an operation cannot be EmptyStackException executed to be thrown Stacks, Queues, Vectors, & Lists

Applications of Stacks

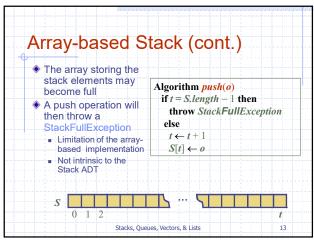
Direct applications
Page-visited history in a Web browser
Undo sequence in a text editor
Chain of method calls in the Java Virtual Machine
Evaluate an expression
Indirect applications
Auxiliary data structure for algorithms
Component of other data structures

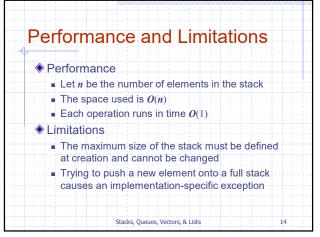
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Runtime Stack in the JVM main() { The Java Virtual Machine int i = 5(JVM) keeps track of the chain of active methods with a stack foo(i); PC = 1 When a method is called, the m = 6JVM pushes onto the stack a frame containing foo(int j) { Local variables and return value int k: PC = 3Program counter, keeping track of the statement being executed k = j+1;k = 6bar(k); j = 5 When a method ends, its frame is popped from the stack and control is passed to the method on top of the stack bar(int m) { These are called stack frames or activation records Stacks, Queues, Vectors, & Lists



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Main Point

1. Stacks are data structures that allow very specific and orderly insertion, access, and removal of their individual elements, i.e., only the top element can be inserted, accessed, or removed.

Science of Consciousness: The infinite dynamism of the unified field is responsible for the orderly changes that occur continuously throughout creation.

Queues

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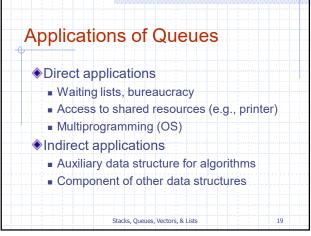
Outline and Reading

The Queue ADT (§2.1.2)
Implementation with a circular array (§2.1.2)
Queue interface in Java

Growable array-based queue (tomorrow)

The Queue ADT ◆ The Queue ADT stores arbitrary
◆ Auxiliary queue objects operations: Insertions and deletions follow object front(): returns the the first-in first-out (FIFO) element at the front without removing it Insertions are at the rear of the integer size(): returns the number of elements stored queue and removals are at the boolean isEmpty(): front of the queue indicates whether no Main queue operations: elements are stored void enqueue(object): inserts an Exceptions element at the end of the queue Attempting the execution of object dequeue(): removes and dequeue or front on an returns the element at the front empty queue throws an of the queue Stacks, Queues, Vectors, & Lists

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Queue ADT Implementation

Can be based on either an array or a linked list
Linked List
Implementation is straightforward
Array
Need to maintain pointers to index of front and rear elements
Need to wrap around to the front after repeated enqueue and dequeue operations
May have to enlarge the array

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Array-based Queue

◆ Use an array of size N in a circular fashion

◆ Two variables keep track of the front and rear

f index of the front element
r index immediately past the rear element

◆ Array location r is kept empty

normal configuration

Q

1 1 2 f r

wrapped-around configuration

Q

0 1 2 r f

Stacks, Queues, Vectors, & Lists

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Queue Operations

We use the modulo operator (remainder of division)

Algorithm size() return (N+r-f) mod N
Algorithm isEmpty() return (f=r)

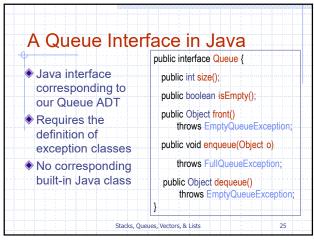
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Queue Operations (cont.) Algorithm enqueue(o) Operation enqueue if size() = N - 1 then throws an exception if the array is full throw FullQueueException This exception is implementation- $Q[r] \leftarrow o$ dependent (N=17) $r \leftarrow (r+1) \bmod N$ Q Q0 1 2 Stacks, Queues, Vectors, & Lists

Queue Operations (cont.) Algorithm dequeue() Operation dequeue if isEmpty() then throws an exception if the queue is empty throw EmptyQueueException This exception is else specified in the $o \leftarrow Q[f]$ queue ADT $f \leftarrow (f+1) \mod N$ return o Q 0.1.2.fQ0 - 1 - 2 - rStacks, Queues, Vectors, & Lists

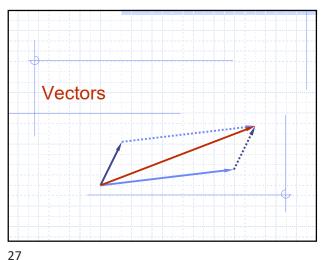
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Main Point 2. The Queue ADT is a special ADT that supports orderly insertion, access, and removal. Queues achieve their efficiency and effectiveness by concentrating on a single point of insertion (end) and a single point of removal and access (front). Science of Consciousness: Similarly, nature is orderly, e.g., an apple seed when planted properly will yield only an apple tree. Stacks, Queues, Vectors, & Lists

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Outline and Reading ◆The Vector ADT (§2.2.1) ◆Array-based implementation (§2.2.1) Stacks, Queues, Vectors, & Lists

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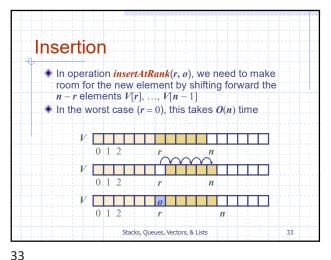
The Vector ADT A Vector stores a sequence of elements Element access is based on the concept of Rank Rank is the number of elements that precede an element in the sequence ◆An element can be accessed, inserted, or removed by specifying its rank An exception is thrown if an incorrect rank is specified (e.g., a negative rank) Stacks, Queues, Vectors, & Lists

Main Vector operations: object elemAtRank(r): • returns the element at rank r without removing it object replaceAtRank(r, o): • replace the element at rank r with o and return the old element void insertAtRank(r, o): ■ insert a new element o to have rank r object removeAtRank(r): removes and returns the element at rank r Additional operations size() and isEmpty() Stacks, Queues, Vectors, & Lists

Applications of Vectors Direct applications Sorted collection of objects (elementary database) Indirect applications Auxiliary data structure for algorithms Component of other data structures Stacks, Queues, Vectors, & Lists

Array-based Vector Use an array V of size N A variable n keeps track of the size of the vector (number of elements stored) ◆ Operation *elemAtRank*(*r*) is implemented in *O*(1) time by returning V[r]Stacks, Queues, Vectors, & Lists 32

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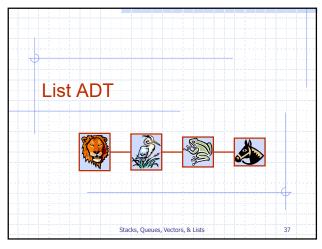
Deletion ♦ In operation removeAtRank(r), we need to fill the hole left by the removed element by shifting backward the n - r - 1 elements V[r + 1], ..., V[n - 1]• In the worst case (r = 0), this takes O(n) time 0 1 2 V Stacks, Queues, Vectors, & Lists

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Performance In the array based implementation of a Vector • The space used by the data structure is O(n)size, isEmpty, elemAtRank and replaceAtRank run in **0**(1) time ■ insertAtRank and removeAtRank run in O(n) time If we use the array in a circular fashion, insertAtRank(0) and removeAtRank(0) run in **0**(1) time ♦ In an *insertAtRank* operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one Stacks, Queues, Vectors, & Lists

Main Point 3. Rank is the number of elements that precede an element in a linear sequence; this is a very simple idea, yet is the powerful basis of the random access operations of the Vector ADT. Science of Consciousness: Pure consciousness is the simplest state of awareness, yet is the source of all activity in the universe. Stacks, Queues, Vectors, & Lists 36

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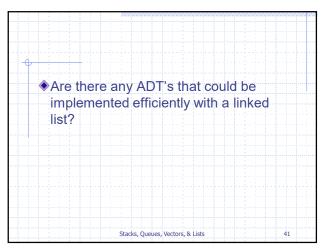
Outline and Reading

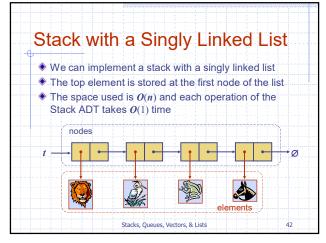
Singly linked list
Position ADT and List ADT (§2.2.2)
Doubly linked list (§ 2.2.2)

Linked List

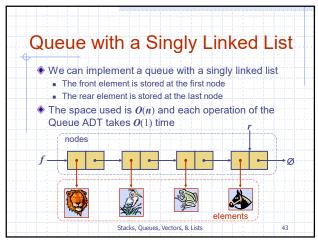
Motivation:

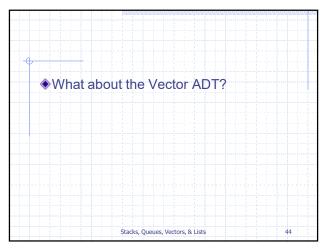
need to handle varying amounts of data
eliminate the need to resize the array
grows and shrinks exactly when necessary
efficient handling of insertion or removal from the middle of the data structure
random access is often unnecessary
Built-in list data structures
Lisp, Scheme, ML, Haskell





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★ Elements are accessed by Position
 ♦ Position is an ADT that models a particular place or location in a data structure
 ♦ We will use this abstraction in several data structures (today in the List ADT)
 ♦ We can think of List ADT as being like a Java Interface that is implemented in different ways

Position ADT

The Position ADT models the notion of place within a data structure where a single object is stored

It gives a unified view of diverse ways of storing data, such as

a cell of an array

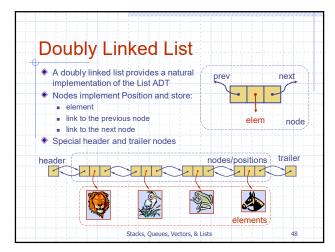
a node of a linked list or tree

Just one method:

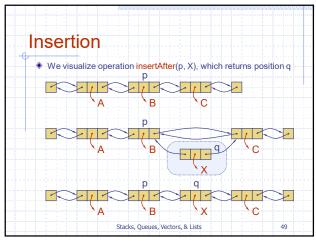
object element(): returns the element stored at the position

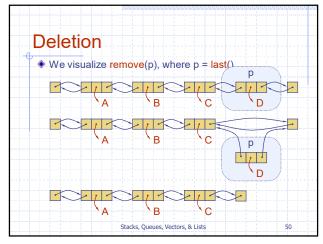
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List ADT The List ADT models a Accessor methods: sequence of positions first(), last() storing arbitrary objects before(p), after(p) It establishes a Update methods: before/after relation replaceElement(p, e), between positions swapElements(p, q) insertBefore(p, e), Generic methods: insertAfter(p, e), size(), isEmpty() insertFirst(e), Query methods: insertLast(e) isFirst(p), isLast(p) remove(p) Stacks, Queues, Vectors, & Lists



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Performance of Linked List implementation of List ADT Generic methods: Update methods: size(), isEmpty() replaceElement(p, e), swapElements(p, q) Query methods: insertBefore(p, e), isFirst(p), isLast(p) insertAfter(p, e) Accessor methods: insertFirst(e), first(), last() insertLast(e) before(p), after(p) remove(p) Stacks, Queues, Vectors, & Lists

Performance

In the implementation of the List ADT by means of a doubly linked list

The space used by a list with *n* elements is *O(n)*The space used by each position of the list is *O(1)*All the operations of the List ADT run in *O(1)* time

Operation element() of the Position ADT runs in *O(1)* time

Stacks, Queues, Vectors, & Lists

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Exercise on List Generic methods: Generic methods:

integer size()

boolean isEmpty()

objectiterator elements()

Accessor methods:

position first()

position last()

position last()

position after(p)

Query methods:

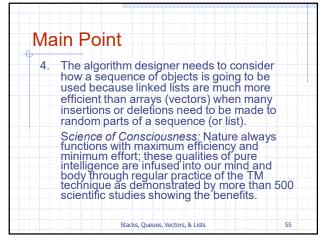
boolean isErist(p)

boolean isLast(p)

Uddate methods: Exercise: Write a method to calculate the sum of the integers in a list of integers Only use the methods in the list to the left. Algorithm sum(L) Update methods: swapElements(p, q)
 object replaceElement(p, o)
 insertFirst(o) Input L is a list of integers Output sum of these integers insertLast(o) insertBefore(p, o) insertAfter(p , o) remove(p)



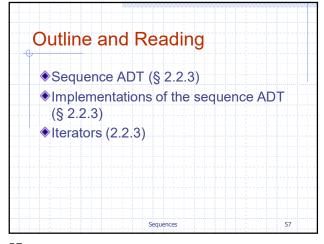
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Sequence ADT

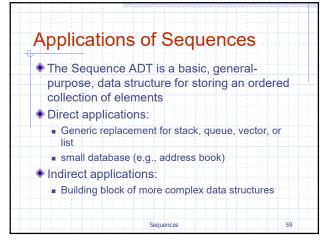
Sequence Sequence 56

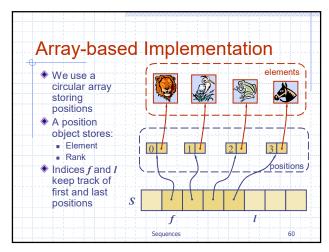
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Sequence ADT The Sequence ADT is the List-based methods: union of the Vector and first(), last(), List ADTs before(p), after(p), Elements accessed by replaceElement(p, o), swapElements(p, q), Rank, or Position insertBefore(p, o), insertAfter(p, o), Generic methods: insertFirst(o). size(), isEmpty() insertLast(o), Vector-based methods: remove(p) elemAtRank(r), Bridge methods: replaceAtRank(r, o), insertAtRank(r, o), atRank(r), rankOf(p) removeAtRank(r) Sequences

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We use the modulo operator (similar to remainder of division	Algorithm index2rank(index) return (N + index - f) mod N	
of natural numbers) Used to convert between rank and index in O(1) time	Algorithm rank2index(rank) return (f + rank) mod N	
Q	1 16	

Sequence Implementations

Operation Array List
size, isEmpty
atRank(r), elemAtRank(r)
replaceAtRank(r, o)
insertAtRank(r, o), removeAtRank(r, o)

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Sequence Implementations

Operation | Array List |
size, isEmpty | 1 | 1 |
atRank(r), elemAtRank(r) | 1 | r |
replaceAtRank(r, o) | 1 | r |
insertAtRank(r, o), removeAtRank(r) | n | r |

Operation	Array List
rankOf(p)	
first(), last()	
before(p), after(p)	
replaceElement(p, o), swa	apElements(p, q)
insertFirst(o), insertLast(o)
insertAfter(p, o), insertBef	fore(p, o)
remove(p)	

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Sequence Implementations Operation Array List rankOf(p) n first(), last() 4 before(p), after(p) 1 replaceElement(p, o), swapElements(p, q) insertFirst(o), insertLast(o) insertAfter(p, o), insertBefore(p, o) 1 n remove(p) 65 Exercise

Generic methods:

integer size()

boolean isEmpty()

cocurs at the middle of S

Accessor methods:

position first()

position last()

position after(p)

Query methods:

boolean isFirst(p)

boolean isFirst(p)

boolean isFirst(p)

cocurs and after ein S

cocurs

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List-Based vs. A Sequence		
Algorithm findMiddle(S) if S.isEmpty() then return null p := S.first() q := S.last() while p ≠ q ∧ S.after(p) ≠ q do q := S.before(q) p := S.after(p) return p	List-Based 1 1 1 1 1 1 n n 1	Array-Based 1 1 1 1 1 n n 1
Algorithm removeMiddle(S) p := findMiddle(S) if p = null then throw NoMidExcptn e := p.element() S.remove(p) return e	n 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	1 1 1

Array-Based Sequence Version Algorithm findMiddle(S) List Array if S.isEmpty() then throw NoMidExcptn mid := (S.size() - 1) / 2p := S.atRank(mid) Algorithm removeMiddle(S) p := findMiddle(S) e := p.element() S.remove(p) 1 n return e Stacks, Queues, Vectors, & Lists

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Iterators An iterator abstracts the An iterator is typically process of scanning through associated with another data a collection of elements structure Methods of the ObjectIterator We can augment the Stack, Queue, Vector, List and boolean hasNext() Sequence ADTs with method: object next() ObjectIterator elements() reset() Two notions of iterator: Extends the concept of Position by adding a traversal snapshot: freezes the contents of the data structure capability at a given time Implementation with an array or singly linked list dynamic: follows changes to the data structure Sequences

Main Point

5. The Sequence ADT captures the abstract notion of a mathematical sequence; it specifies the operations that any list or vector should support. The specifications of the Sequence ADT can be satisfied based on different implementation strategies with different concrete implementations.

Likewise, pure awareness is an abstraction of individual awareness; each individual provides a specific, concrete realization of unbounded, unmoving pure awareness.

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Connecting the Parts of Knowledge
with the Wholeness of Knowledge

1. The Sequence ADT may be used as
an all-purpose class for storing
collections of objects with only
sequential access to its elements.

2. The underlying implementation of an
ADT determines its efficiency
depending on how that data structure
is going to be used in practice.

3. Transcendental Consciousness is the unbounded, silent field of pure order and efficiency.

4. Impulses within Transcendental Consciousness: Within this field, the laws of nature continuously organize and govern all activities and processes in creation.

5. Wholeness moving within itself: In Unity Consciousness, when the home of all knowledge has become fully integrated in all phases of life, life is spontaneously lived in accord with natural law for maximum achievement with minimum effort.

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