

Wholeness Statement

Graphs have many useful applications in different areas of computer science. However, to be useful we have to be able to traverse them. There are two primary ways that graphs are systematically explored, either using depth-first or breadth-first search. Science of Consciousness: The TM technique provides a simple, effortless way to systematically explore the different levels of the conscious mind until the process of thinking is transcended and unbounded silence is experienced; contacting this field of wholeness of individual and cosmic intelligence benefits individual and society.

Depth-First Search

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Graphs
Outline and Reading

Graphs
Definition
Applications
Terminology
Properties
ADT
Data structures for graphs
Edge list structure
Adjacency list structure
Adjacency matrix structure

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Depth-First Search
Outline and Reading

Definitions
Subgraph
Connectivity
Spanning trees and forests
Depth-first search
Example
Algorithm
Properties

Analysis

Applications of DFS

Path findingCycle finding

Graph

A graph is a pair (V, E), where

Vis a set of nodes, called vertices

E is a collection of pairs of vertices, called edges

Vertices and edges are positions and store elements

Example:

A vertex represents an airport and stores the three-letter airport code

An edge represents a flight route between two airports and stores the mileage of the route

SFO

BA3

ORD

BA9

PVD

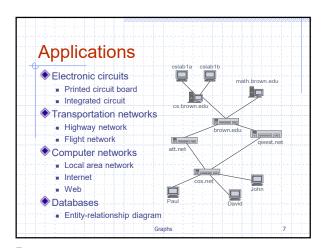
Graphs

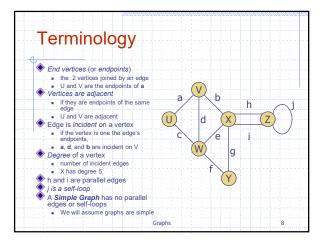
Graphs

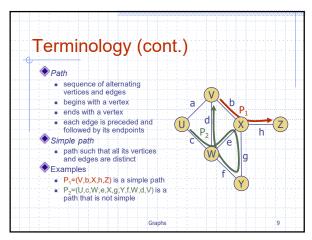
Edge Types Directed edge ordered pair of vertices (u,v) first vertex u is the origin (PVD) AA 1206 ■ second vertex v is the destination e.g., a flight Undirected edge 849 unordered pair of vertices (u,v) miles e.g., a flight route Directed graph all the edges are directed e.g., flight network Undirected graph all the edges are undirected e.g., route network

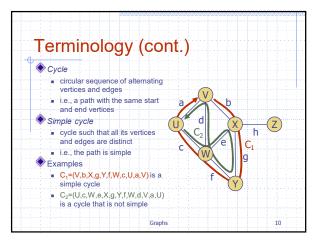
Denth-First Search

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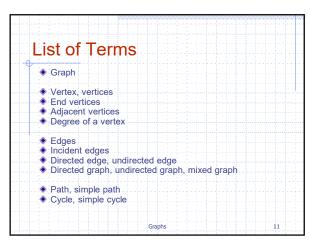








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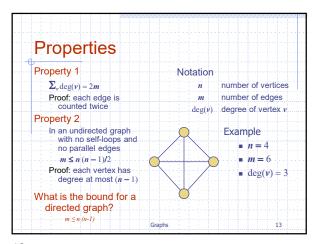
Main Point

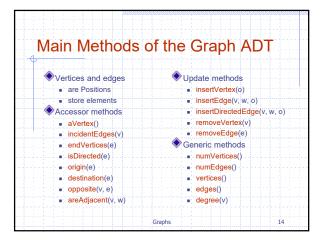
1. A path in a graph is a sequence of alternating vertices and edges, starting with a vertex and ending with a vertex.

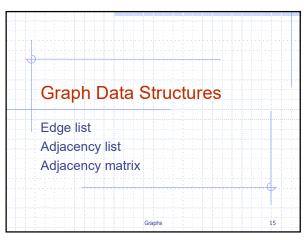
A path is simple if all its vertices and edges are distinct.

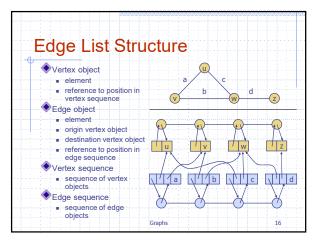
Science of Consciousness: The path to enlightenment is simple: regular practice of the TM technique and a balanced daily routine to stabilize the gains during meditation.

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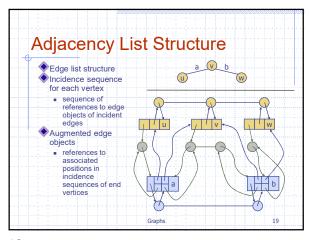


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		ormance	
 n vertices, m edges no parallel edges no self-loops 	Edge List	Adjacency List	Adjacenc Matrix
♦ Bounds are "big-Oh" Space			
incidentEdges(v)			
areAdjacent(v, w)			
insertVertex(o)			
insertEdge(v, w, o)			
removeVertex(v)			
removeEdge(e)			

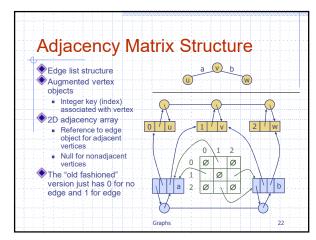
	1 0110	ormance	
 n vertices, m edges no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacenc Matrix
Space Space	n+m		
incidentEdges(v)	m		
areAdjacent(v, w)	m		
insertVertex(o)	1		
insertEdge(v, w, o)	1		
removeVertex(v)	m		
removeEdge(e)	1		

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 		ormance	
 n vertices, m edges no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacenc Matrix
Space	n+m		
incidentEdges(v)	m		
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insertVertex(o)	1		
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removeVertex(v)	m		
removeEdge(e)	1		

Asymptotic Performance			
Asymptotic	Per	iormance	
 n vertices, m edges no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacenc Matrix
Space	n + m	n+m	
incidentEdges(v)	m	deg(v)	
areAdjacent(v, w)	m	$\min(\deg(v), \deg(w))$	
insertVertex(o)	1	1	
insertEdge(v, w, o)	1	1	
removeVertex(v)	m	deg(v)	
removeEdge(e)	1		



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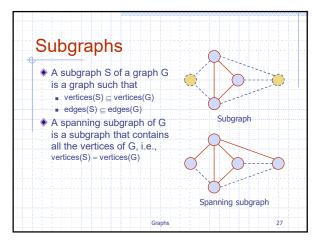
Asymptotic	Per	formance	
• n vertices, m edges • no parallel edges • no self-loops • Bounds are "big-Oh"	Edge List	Adjacency List	Adjacenc Matrix
Space	n + m	n+m	
incidentEdges(v)	m	deg(v)	
areAdjacent(v, w)	m	min(deg(v), deg(w))	
insertVertex(o)	1	1	
insertEdge(v, w, o)	1	1	
removeVertex(v)	m	deg(v)	
removeEdge(e)	1		

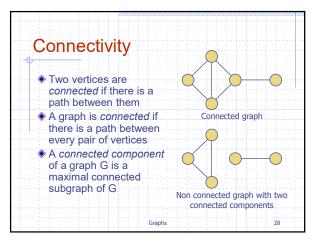
	. 0	formance	
 n vertices, m edges no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacenc Matrix
Space	n + m	n + m	n ²
incidentEdges(v)	m	deg(v)	n
areAdjacent(v, w)	m	min(deg(v), deg(w))	1
insertVertex(o)	1	1	n ²
insertEdge(v, w, o)	1	1	1
removeVertex(v)	m	$\deg(v)$	n ²
removeEdge(e)	1	1	1

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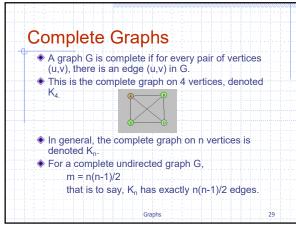
• n vertices, m edges			111 1 1 1 1 1
 no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacency Matrix
aVertex()			
edges()			
vertices()			
endVertices(e)			
opposite(v, e)			
degree(v)	m	1	n
numEdges()			

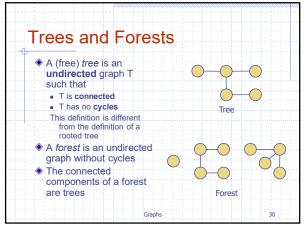
	<u></u>		
 n vertices, m edges no parallel edges no self-loops Bounds are "big-Oh" 	Edge List	Adjacency List	Adjacenc Matrix
aVertex()	1	1	1
edges()	m	m	m
vertices()	n	i n	n
endVertices(e)	1-1-	1	-11
opposite(v, e)	1	1	1
degree(v)	m	- 1	n
numEdges()	i	1	1



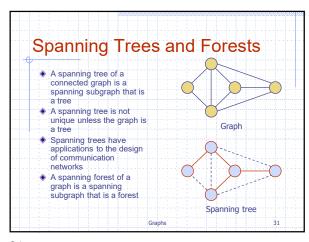


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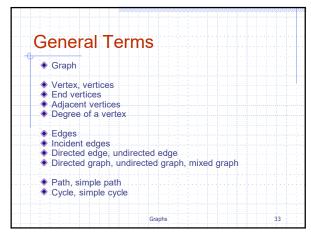


Main Point

2. A spanning tree connects all vertices of a graph without any cycles. A spanning forest is a subgraph in which each connected component is a spanning tree of the vertices in that component.

Science of Consciousness: The pure field of consciousness connects everything in creation and governs everything through laws (algorithms). Contact with pure consciousness brings out the qualities of this field into our mind and body for the benefit of everyone.

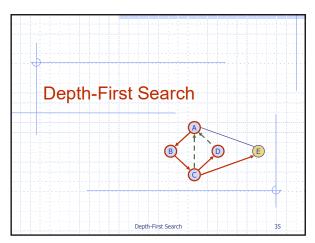
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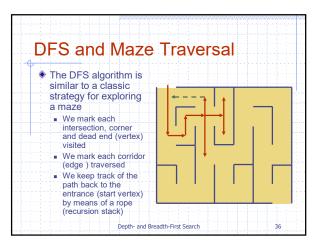


Subgraphs &
Connected Components

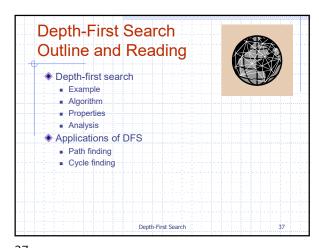
Subgraph
Connectivity
Connected Vertices
Connected Graph
Connected Component
Complete Component
Foree
Spanning Tree and Spanning Forest

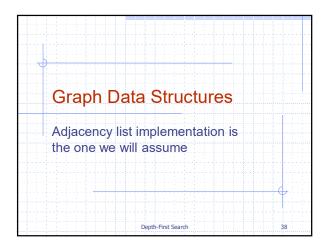
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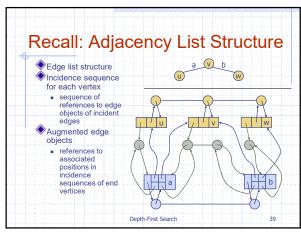


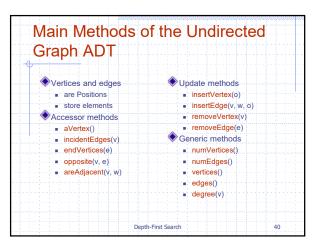


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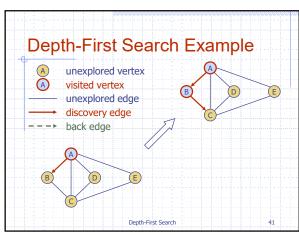


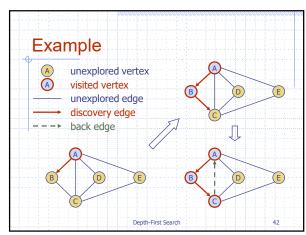




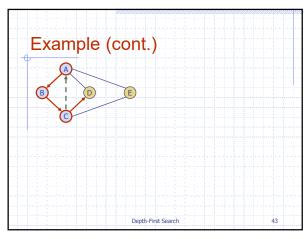


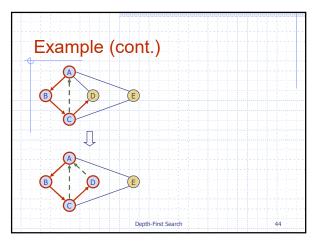
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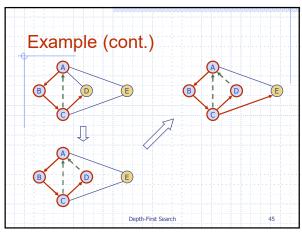


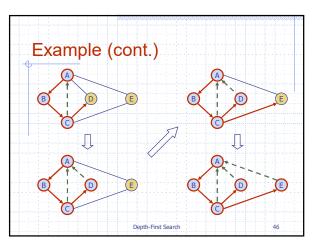


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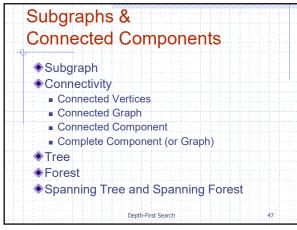


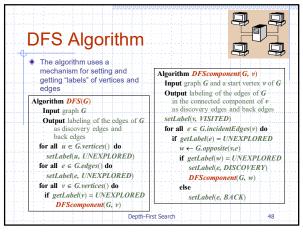




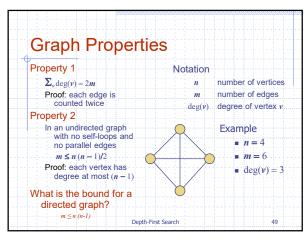


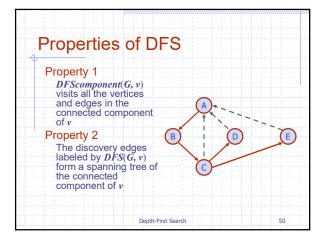
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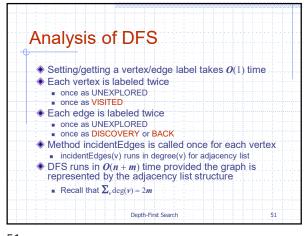




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Depth-First Search

Depth-first search (DFS) is a general technique for traversing a graph

A DFS traversal of a graph G

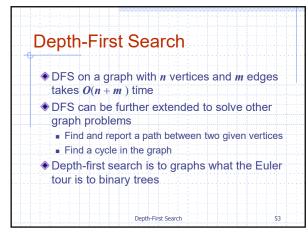
Visits all the vertices and edges of G

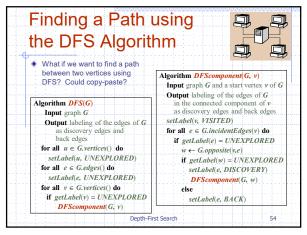
Determines whether G is connected

Computes the connected components of G

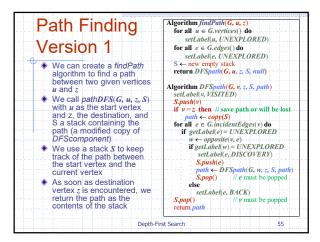
Computes a spanning forest of G

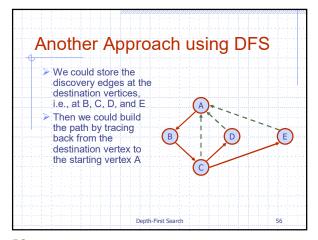
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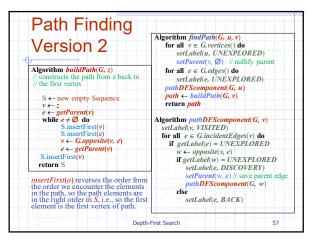


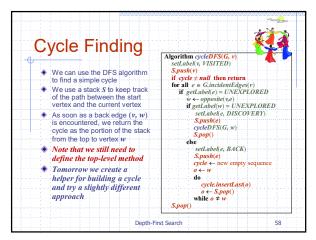


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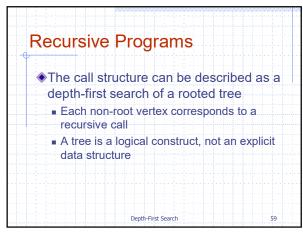








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Main Point

3. During dept-first search of a graph, each path is followed until the end is reached, then it backs up to branch out and explore new edges; all adjacent vertices are visited before backtracking.

Science of Consciousness: The mind is naturally seeking fields of greater happiness. The TM technique uses the nature of the mind to immediately and effortlessly take the mind to the deepest levels where true happiness and fulfillment can be gained.

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Connecting the Parts of Knowledge with the Wholeness of Knowledge

- The edges of a graph connect vertices. Thus connectivity of graphs and connected components are important concepts in graph theory.
- 2. Paths, cycles, spanning trees, and components are important ways that connected vertices can be viewed. Different graph traversal algorithms systematically compute these ways that vertices can be connected as the basis of specific applications. DFS is a particularly effective way to traverse a graph, compute connected components, find paths, cycles and spanning trees.

Depth-First Search

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- Transcendental Consciousness is the underlying basis and connects everything in creation.
- 4. Impulses within Transcendental
 Consciousness: The dynamic natural laws
 within this unbounded field govern all
 activities and evolution of the universe.
- 5. Wholeness moving within itself: In Unity Consciousness, one experiences that the self-referral activity of the unified field gives rise to the whole of the universe.

Denth-First Search