

Wholeness Statement

In a weighted graph, the shortest path algorithm finds the path between a given pair of vertices such that the sum of the weights of that path's edges is the minimum. Science of Consciousness:

Natural law always chooses the path of least action, the shortest path to the goal with no wasted effort.

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Outline and Reading

Weighted graphs (§7.1)

Shortest path problem
Shortest path properties
Dijkstra's algorithm (§7.1.1)
Algorithm
Edge relaxation

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Weighted Graphs

In a weighted graph, each edge has an associated numerical value, called the weight of the edge

Edge weights may represent, distances, costs, etc.

Example:

In a flight route graph, the weight of an edge represents the distance in miles between the endpoint airports

SFO

1843

ORD

WIA

ORD

WIA

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Shortest Path Problem

Oriver a weighted graph and two vertices u and v, we want to find a path of minimum total weight between u and v.

Length of a path is the sum of the weights of its edges.

Example:
Shortest path between Providence and Honolulu
Applications
Internet packet routing
Flight reservations
Driving directions

SFO

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ORD

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MIA

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Shortest Path Properties

Property 1:
A subpath of a shortest path is itself a shortest path
Property 2:
There is a tree of shortest paths from a start vertex to all the other vertices
Example:
Tree of shortest paths from Providence

SFO

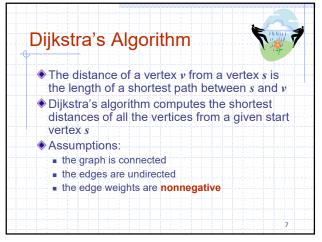
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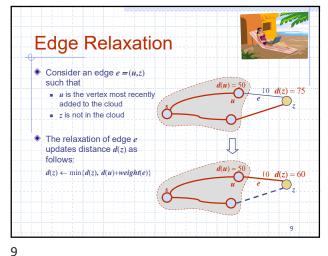
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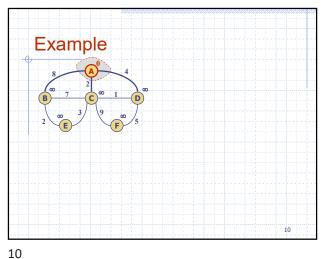
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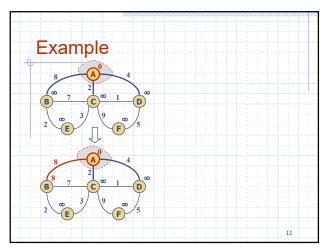


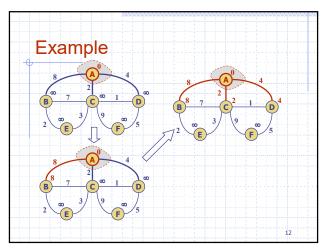
Dijkstra's Algorithm (Informal) lacktriangle We grow a "cloud" of vertices, beginning with s and eventually covering all the vertices We could also grow a tree of shortest paths from s to all other vertices in the graph (we can do this with a small change to our algorithm) • We store with each vertex v a label d(v) represents the distance of ν from s in the subgraph consisting of the cloud and its adjacent vertices At each step ■ We add to the cloud a vertex u outside the cloud
with the smallest distance label, d(u) - d(u) is the shortest distance s from u we will explain why we can't do better ■ Then we update the labels of the vertices adjacent to u

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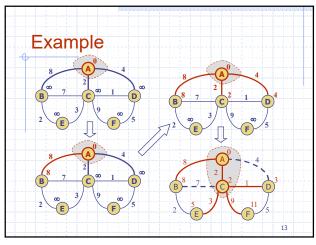


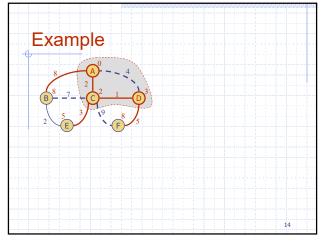




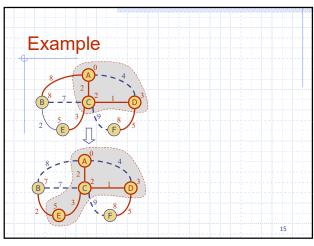


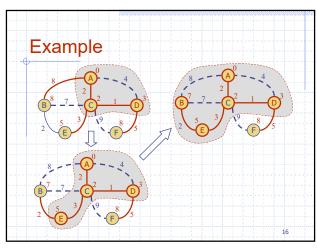
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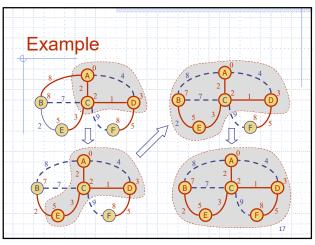


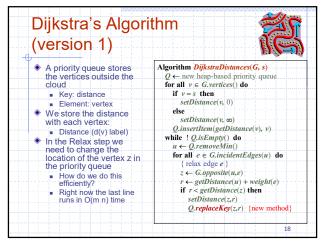
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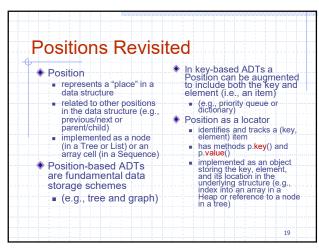


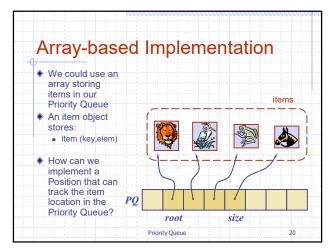
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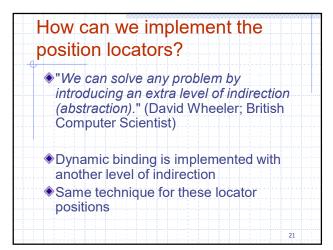


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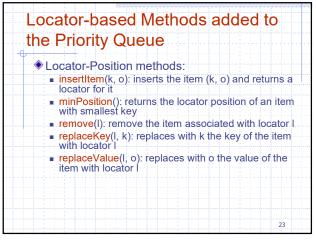


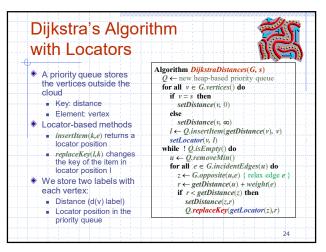
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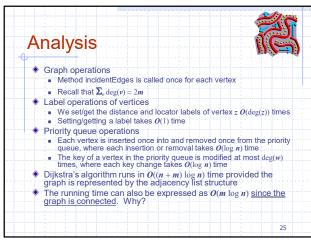
Array-based Implementation We use an array storing locatorpositions in our **Priority Queue** Another level of indirection A position object stores: Item (key,elem) locator / Index positions root size 22 Sequences

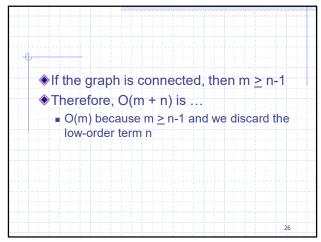
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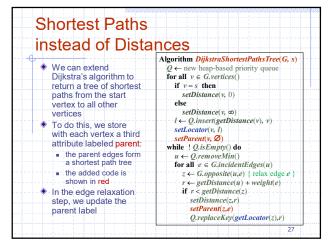


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Why Dijkstra's Algorithm
Works

Dijkstra's algorithm is based on the greedy method. It adds vertices by increasing distance.

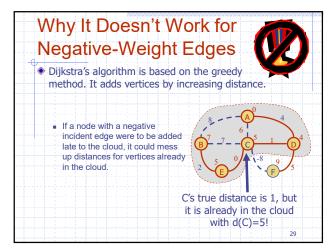
Suppose it didn't find all shortest distances. Let F be the first wrong vertex the algorithm processed.

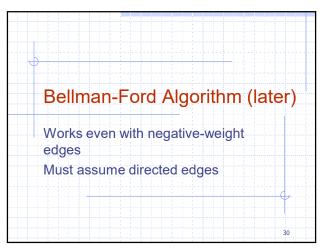
When the previous node, D, on the true shortest path was considered, its distance was correct.

But the edge (D,F) was relaxed at that time!

Thus, as long as d(F)≥d(D), F's distance cannot be wrong. That is, there is no wrong vertex distance.

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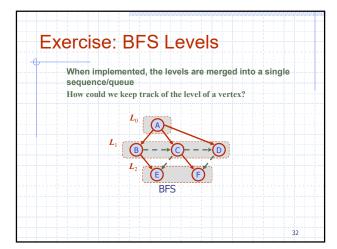




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Main Point

2. By using the adjacency list data structure to represent the graph and a priority queue enhanced with locator positions to store the vertices not yet in the tree, the shortest path algorithm achieves a running time *O(m log n)*. Science of Consciousness: The algorithms of nature are always most efficient for maximum growth and progress.



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BFS Algorithm The BFS algorithm using a single sequence/list/queue Algorithm BFScomponent(G, s) setLabel(s, VISITED) $L \leftarrow$ new empty List L.insertLast(s)Algorithm BFS(G) {top level} Input graph Gwhile ! L.isEmpty() do Output labeling of the edges and partition of the vertices of G for all $u \in G$, vertices() $v \leftarrow L.remove(L.first())$ for all $e \in G.incidentEdges(v)$ do if getLabel(e) = UNEXPLOREDsetLabel(u_UNEXPLORED) w ← opposite(v,e)
if getLabel(w) = UNEXPLORED
setLabel(e, DISCOVERY) for all $e \in G.edges()$ setLabel(e, UNEXPLORED) for all $v \in G.vertices()$ setLabel(w, VISITED) if isNextComponent(G, v) L.insertLast(w) BFScomponent(G, v) setLabel(e, CROSS) Algorithm isNextComponent(G, v) return getLabel(v) = UNEXPLORED 33

Connecting the Parts of Knowledge with the Wholeness of Knowledge

1. Finding the shortest path to some desired goal is a common application problem in systems represented by weighted graphs, such as airline or highway routes.

By systematically extending short paths
using data structures especially suited to
this process, the shortest path algorithm
operates in time O(m log n).

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- 3. Transcendental Consciousness is the silent field of infinite correlation where everything is eternally connected by the shortest path.
- 4. Impulses within Transcendental
 Consciousness: Because the natural laws
 within this unbounded field are infinitely
 correlated (no distance), they can govern all
 the activities of the universe simultaneously.
- Wholeness moving within itself: In Unity Consciousness, the individual experiences the shortest path between one's Self and everything in the universe, a path of zero length.

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