

Attempt to answer these questions (when asked for examples use different examples from the ones given in class):

a- Given 100 cans of coke, 50 cans of sprite, 20 cans of Dr.Pepper, and 10 cans of mountain dew. Given a can what will your best guess be?

$$\text{Sum} = 100 + 50 + 20 + 10 = 180$$

$$P(\text{Coke}) = 100/180 = 10/18$$

$$P(\text{Sprite}) = 50/180 = 5/18$$

$$P(\text{Dr.Pepper}) = 20/180 = 2/18$$

$$P(\text{Mountain Drew}) = 10/180 = 1/18$$

So: **Given a can, the best guess will be Coke.**

b- Given 80 soft-cover books, 50 hard-cover books, 20 magazines, and 30 comics. Knowing that soft-cover books range from 100-500 pages, hard-cover books range from 200-600 pages, magazines range from 30-120 pages, comics range from 20- 100 pages. Given an item with 50 pages, what would your best guess be?

$$\text{Sum} = 80 + 50 + 20 + 30 = 180$$

$$P(\text{Soft-cover books}) = 80/180 = 8/18$$

$$P(\text{Hard-cover books}) = 50/180 = 5/18$$

$$P(\text{Magazines}) = 20/180 = 2/18$$

$$P(\text{Comics}) = 30/180 = 3/18$$

$$P(50 \text{ pages} \mid \text{Soft-cover books}) = 0 \text{ (out of page ranges 100-500)}$$

$$P(50 \text{ pages} \mid \text{Hard-cover books}) = 0 \text{ (out of page ranges 200-600)}$$

$$P(50 \text{ pages} \mid \text{Magazines}) = 1/(210-30+1) = 1/91$$

$$P(50 \text{ pages} \mid \text{Comics}) = 1/(100-20+1) = 1/81$$

We have: $P(A | B) = (P(A)/P(B)) * P(B | A)$,

and $P(50 \text{ pages}) = 1$

so:

$P(\text{Soft-cover books} | 50 \text{ pages})$

$= (P(\text{Soft-cover books}) / P(50 \text{ pages})) * P(50 \text{ pages} | \text{Soft-cover books})$

$= 0$

$P(\text{Hard-cover books} | 50 \text{ pages})$

$= (P(\text{Hard-cover books}) / P(50 \text{ pages})) * P(50 \text{ pages} | \text{Hard -cover books})$

$= 0$

$P(\text{Magazines} | 50 \text{ pages})$

$= (P(\text{Magazines}) / P(50 \text{ pages})) * P(50 \text{ pages} | \text{Magazines})$

$= P(\text{Magazines}) * P(50 \text{ pages} | \text{Magazines}) = (2/18) * (1/91) = 0.001221$

$P(\text{Comics} | 50 \text{ pages})$

$= (P(\text{Comics}) / P(50 \text{ pages})) * P(50 \text{ pages} | \text{Comics})$

$= P(\text{Comics}) * P(50 \text{ pages} | \text{Comics}) = (3/18) * (1/91) = 0.001831$

The best guess will be Comics.

c- Given 10 soft-cover books, 40 hard-cover books, 20 magazines, and 30 comics. Knowing that soft-cover books have 200 pages, hard-cover books range from 300 pages, magazines range from 60 pages, comics range from 50 pages. What are the expected pages if you pick a random item?

$$\text{Sum} = 10 + 40 + 20 + 30 = 100$$

$$P(\text{Soft-cover books}) = 10/100 = 1/10 = 0.1$$

$$P(\text{Hard-cover books}) = 40/100 = 4/10 = 0.4$$

$$P(\text{Magazines}) = 20/100 = 2/10 = 0.2$$

$$P(\text{Comics}) = 30/100 = 3/10 = 0.3$$

$$\mathbf{E(\text{pages}) = 200*0.1 + 300*0.4 + 60*0.2 + 50*0.3 = 20 + 120 + 12 + 15 = 167}$$

d- For problem c (above) what is the standard deviation?

$$E(\text{pages}^2) = 200*200*0.1 + 300*300*0.4 + 60*60*0.2 + 50*50*0.3 = 41470$$

$$\text{Variance} = E(\text{pages}^2) - E(\text{pages})^2 = 41470 - 167*167 = 13581$$

$$\mathbf{\text{Standard deviation} = \text{Sqrt}(\text{variance}) = \text{Sqrt}(13581) = 116.5375}$$