

# Finding Correlated Pairs

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October 26, 2020

## 1 Input

The input is a list of 256-bit vectors, one per line, from stdin. Each vector is divided into four 64-bit parts; each part is store as a signed 64-bit integer. For example, the line

```
2948679682100370091 -6730236453359443949 9154238340659291137 2505149300205180166
```

gives the bit vector (here I am breaking into 4 lines for readability; the bits give a single total vector):

```
001010001110101111010000100011000101000000000010001101010101011
1010001010011001011001011001101010011111001000000010000000010011
0111111100001010011000110100010100000100010000100010010000000001
0010001011000100000101000000010000000100000011000101010100000110
```

The very first line from stdin is an integer that represents the number of vectors that follow.

### 1.1 How Vectors Were Generated

Each bit of every vector is a 1 with probability  $1/3$ , and a 0 with probability  $2/3$ . These choices are made independently.

The correlated vector (we'll call it  $v_c$  for simplicity) is *Pearson-correlated* with another vector  $v$ . For each digit in  $v_c$ , with probability  $7/8$  we set it equal to the corresponding digit in  $v$ . With probability  $1/8$ , the digit is set randomly—1 with probability  $1/3$ , and 0 with probability  $2/3$ . The Pearson-correlated vectors are much more likely to have a large number of 1s in common than two random vectors.

## 2 Correlation

We define the *similarity* of two vectors to be the number of 1s they have in common. We also call them *correlated*.

We guarantee that in each input instance, there is a single pair with similarity at least 70.

As an example, the following two vectors have similarity 93. If we find these two inputs in a file, we can safely output them as the correct answer.

```
-4545410128706124432 423485083363186329 28290711320299080 -1687296419800652167
-4256053852647568032 428569225130022555 28290711253190152 -1687296419734591911
```

## 3 Expected Output

The expected output on CodeJudge is the two indices of the correlated vectors on one line, with the lower index first.