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#include <iostream>
#include <cassert>

using namespace std;

template<class T>
class Queue{
public:
    Queue(int aSize):mSize(aSize),mHead(0),mTail(0){mStorage=new T[mSize];}
    ~Queue(){delete[] mStorage;}
    void Push(T aValue)
    {
        if (mTail==mSize) mTail=0;//make circular
        mStorage[mTail]=aValue;
        mTail+=1;
    }
    T Pop()
    {
        assert(mTail!=mHead);
        T value=mStorage[mHead];
        mHead+=1;
        if (mHead==mSize) mHead=0;//make circular
        return value;
    }
private:
    int mSize;
    int mHead;//points to current head element
    int mTail;//points to element after last inserted (first free element)
    T* mStorage;
};

class Node{
public:
    Node(int aKey):mKey(aKey),mpLeft(0),mpRight(0){}
    Node* Clone(){return new Node(mKey);}
public:
    int mKey;
    Node* mpLeft;
    Node* mpRight;
};

class Tree{
public:
    Tree();
    ~Tree();
    Tree(const Tree& aTreeToCopy);
    Tree& operator=(const Tree& aTreeToCopy);

    int Size()const;
    void Input(const int aValue);
    void Output(ostream& out)const;
    void OutputPostOrder(ostream& out)const;
    bool operator==(const Tree& aT)const;
private:
    void mCopyConstructor(Node* apNodeCurrent, Node* apNodeToCopy);
    void mDestructor(Node* apNode);
    int mSize(Node* apNode)const;

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void mOutputPostOrder(Node* apNode, ostream& out) const;
bool mTestForEquality(const Node* apNodeX, const Node* apNodeY) const;
private:
    Node* mpRoot;
};

Tree::Tree(): mpRoot(0) {}

Tree::Tree(const Tree& aTreeToCopy)
{
    *this = aTreeToCopy;
}

Tree& Tree::operator=(const Tree& aTreeToCopy)
{
    if (aTreeToCopy.mpRoot != 0)
    {
        mpRoot = aTreeToCopy.mpRoot->Clone();
        mCopyConstructor(mpRoot, aTreeToCopy.mpRoot);
    }
    else {}
    return *this;
}

void Tree::mCopyConstructor(Node* apNodeCurrent, Node* apNodeToCopy)
{
    if (apNodeToCopy->mpLeft != 0)
    {
        apNodeCurrent->mpLeft = apNodeToCopy->mpLeft->Clone();
        mCopyConstructor(apNodeCurrent->mpLeft, apNodeToCopy->mpLeft);
    }
    if (apNodeToCopy->mpRight != 0)
    {
        apNodeCurrent->mpRight = apNodeToCopy->mpRight->Clone();
        mCopyConstructor(apNodeCurrent->mpRight, apNodeToCopy->mpRight);
    }
}

Tree::~~Tree()
{
    mDestructor(mpRoot);
}

void Tree::mDestructor(Node* apNode)
{
    if (apNode != 0)
    {
        mDestructor(apNode->mpLeft);
        mDestructor(apNode->mpRight);
        delete apNode;
    }
}

int Tree::Size() const
{
    return mSize(mpRoot);
}
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int Tree::mSize(Node* apNode) const
{
    if (apNode==0) return 0;
    return 1+mSize(apNode->mpLeft)+mSize(apNode->mpRight);
}

void Tree::Input(const int aValue)
{
    int size=Size();
    if (size==0) mpRoot=new Node(aValue);
    else {
        Queue<Node*> local_queue(2*size);
        Node* cursor=mpRoot;
        //iterate until we find a node with either a left or right null child
        while (cursor->mpLeft!=0 && cursor->mpRight!=0)
        {
            local_queue.Push(cursor->mpLeft);
            local_queue.Push(cursor->mpRight);
            cursor=local_queue.Pop();
        }
        //insert substituting null child
        if (cursor->mpLeft==0) cursor->mpLeft=new Node(aValue);
        else cursor->mpRight=new Node(aValue);
    }
}

void Tree::Output(ostream& out) const
{
    Queue<Node*> local_queue(2*Size());
    Node* cursor=mpRoot;
    while (cursor!=0)
    {
        out<<cursor->mKey<<" ";
        local_queue.Push(cursor->mpLeft);
        local_queue.Push(cursor->mpRight);
        cursor=local_queue.Pop();
    }
}

void Tree::OutputPostOrder(ostream& out) const
{
    mOutputPostOrder(mpRoot,out);
}

void Tree::mOutputPostOrder(Node* apNode, ostream& out) const
{
    if (apNode!=0)
    {
        mOutputPostOrder(apNode->mpLeft, out);
        mOutputPostOrder(apNode->mpRight, out);
        out<<apNode->mKey<<" ";
    }
}

bool Tree::operator==(const Tree& aT) const
{

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    return mTestForEquality(mpRoot,aT.mpRoot);
}

bool Tree::mTestForEquality(const Node* apNodeX, const Node* apNodeY)const
{
    if (apNodeX==0 && apNodeY!=0) return false;
    else if (apNodeX!=0 && apNodeY==0) return false;
    else if (apNodeX==0 && apNodeY==0) return true;
    else return apNodeX->mKey==apNodeY->mKey && mTestForEquality(apNodeX->mpLeft,apNodeY->
mpLeft) && mTestForEquality(apNodeX->mpRight,apNodeY->mpRight);
}

ostream& operator<<(ostream& out, const Tree& aTree)
{
    aTree.Output(out);
    return out;
}

int main(){

    const int DIM=10;

    Tree tx;
    for (int i=0;i<DIM;i++)
        tx.Input(i);
    cout<<tx<<endl;
    tx.OutputPostOrder(cout);
    cout<<endl;

    Tree ty;
    ty=tx;
    cout<<ty<<endl;

    Tree tz;
    for (int i=9;i>=0;i--)
        tz.Input(i);
    cout<<tz<<endl;

    cout<<"I due alberi ["<<tx<<"] e ["<<ty<<"] sono ...";
    if (tx==ty) cout<<"uguali"<<endl;
    else cout<<"diversi"<<endl;

    cout<<"I due alberi ["<<tx<<"] e ["<<tz<<"] sono ...";
    if (tx==tz) cout<<"uguali"<<endl;
    else cout<<"diversi"<<endl;

    return 0;
}
```