

Final Examination

Notice: Please turn off any types of handheld devices, and leave them far from reach. Use only standalone calculators for calculation if it is needed. The examination takes 110 minutes.
只需繳回答案紙，題目紙請同學保留。

1. (10%) Find the governing differential equation for current i_2 in the circuit shown in Fig. 1.

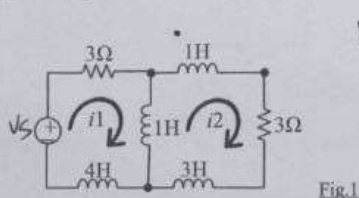


Fig. 1

2. (11%) For the circuit shown in Fig. 2, suppose $R = 0.2\Omega$, $L = 1/12\text{H}$, $C = 0.5\text{F}$, $v(0) = 20\text{V}$, and $i(0) = 11\text{A}$:

- (a) Find the natural response of $v(t)$ for $t > 0$, and determine this circuit as either overdamped, critically damped, or underdamped?
(b) If we want this circuit to be critically damped by changing the value of C and keeping R and L with their original values, please determine the value of C . (取至小數點第三位)

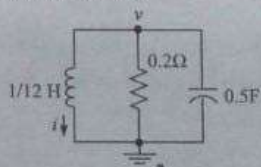


Fig. 2

3. (10%) Find the forced response i_f for the inductor current i in the circuit shown in Fig. 3 when $i_s = 15e^{-6t}\text{A}$. Let $R = 8\Omega$, $L = 10\text{H}$, and $C = 1/40\text{F}$.

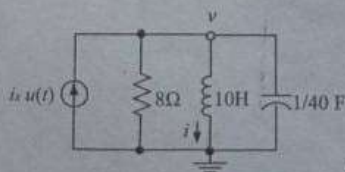


Fig. 3

4. (11%) Determine the voltage $v_o(t)$ while the AC source input in the circuit shown in Fig. 4 is:

$$v_s(t) = 10\cos(1500t + 37^\circ)\text{V}$$

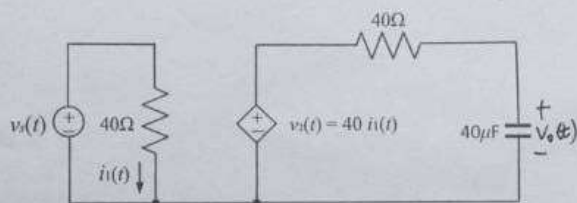


Fig. 4

5. (12%) Determine the output voltage $v_o(t)$ in the circuit shown in Fig. 5, when the AC source input is:

$$v_s(t) = 200\cos(10^4t + 30^\circ)\text{mV}$$

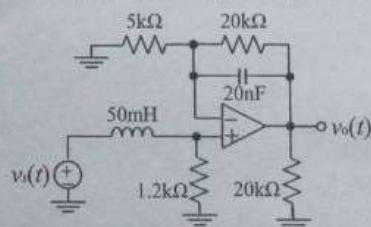


Fig. 5

6. (10%) Find Thévenin equivalent circuit of the AC circuit shown in Fig. 6.

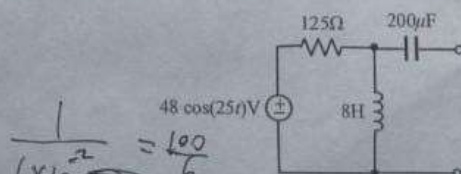


Fig. 6

背面還有題目

Handwritten calculation: $\frac{1}{6 \times 10^{-2}} = \frac{100}{6}$

7. (10%) Determine the voltage $v_o(t)$ across the 9Ω resistor in the circuit shown in Fig. 7.

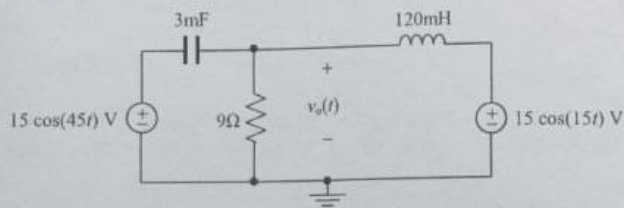


Fig. 7

8. (11%) Determine the network function, $H(\omega) = \frac{V_o(\omega)}{V_s(\omega)}$, of the circuit shown in Fig. 8 while the input voltage is v_s , the output voltage is v_o .

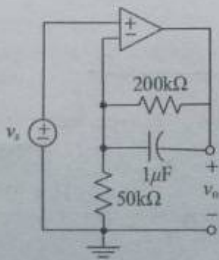


Fig. 8

9. (15%) Find the complete response $v(t)$ for $t > 0$ for the circuit of Fig. 9. Assume the circuit is at steady state at $t = 0^-$.

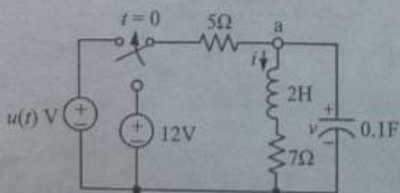


Fig. 9

$t > 0$:

$$\begin{aligned} \frac{V-1}{s} + i + 0.1V(t) &= 0 \rightarrow i(t) = -0.1V(t) - \frac{V-1}{s} \\ V &= 2i(t) + 7i \\ V &= 2(-0.1V'(t) - \frac{V-1}{s}) + 7(-0.1V'(t) - \frac{V-1}{s}) \\ V &= -0.2V''(t) - 0.4V'(t) - 0.7V(t) - \frac{7(V-1)}{s} \\ V &= -0.2V''(t) - 1.1V'(t) - \frac{7}{s}V + \frac{7}{s} \\ 0.2V''(t) + 1.1V'(t) + \frac{7}{s}V &= \frac{7}{s} \\ 0.2s^2 + 1.1s + \frac{7}{s} &= 0 \\ 0.2s & \end{aligned}$$

$$\begin{matrix} 2s & 6 & 8 \\ s & 4 & 3 \end{matrix}$$