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0514 O
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Let V, W be finite-dim vector spaces

Let 1: V>W be a linear transformation

dim V= dim (ker 1)+ dim (Im)

Rmk

- (1) If dim(Im(1)) < dim V ⇒ ker = + {0} = 1 is not 1-1
- (Z) 103
- 3 If dim V=dim W, then:
- · 4 is 1-1

· \$ is bijective

3個高局的等等1/金

2.8. Affine Subspaces 2.8.1. Affine Subspaces

Defn (AS)

Let V be a vector space

* 6 6 V & U EV

L'is called an affine subspaces/linear manifold 3 AS可能人是向雪空間 * Note that if Xo & U かのなxo+U か代表后重空間 コト=×0+0(平線)={xotul|u160}5V

Let L= Xo+U be an AS , EB= {b,,...be} be a basis of U dim 1 := dim U Km/

0 5111

1. - Ele AS by line

2. 二新EAS My Plane

3. hyperplane: Rizy 69A5"L", dim L = n-1

2,8,2, Affine Mapping 4: vaw

Defs 在山裡存在一向量中,及一個無性転換更

S.t. \$(k) = a1 + \(\overline{A}(K) \)

RML®每一個 AM 智是編性動音與再估文字移。 2個 AM 完多 still AM

CH3 Analytic Geometry 解析M3 3.1 Norms

Defn' 3.1 (Norm)

主見有- Sp V, A norm on V is a fen

11·11: V→R (11×11 = 向量× b3長度)

s.t. BRER, X, yev:

@ Absolutely homogeneous

12. *11 = 124. 11x11

@ Triangle inequality

O Positive definite IZ

0=×<>0=||×|| 00 0/||×||

Manhattan Norm (One Norm) $\|x\|_{4} := \frac{n}{k!} |x_{i}| \qquad x = \begin{bmatrix} x_{i} \\ x_{i} \end{bmatrix}$

Euclidean Norm (Two Norm)

11×112:=1=1 2 X;2

3,2. Inner Product MAR

3.2.1 Dot Product

(我们年草熟悉69×-4)=<×,4>=×,4>

7,2,2 General Innor Product

bilinear map: -1圈固定不到時是海性

Ω (×, 4) , V *, 4. æ € V , λ, 4 εR

Q(2x+44,2)=252(x/2)+42(4(2))

0514 B

Defn 3.2 Let a: VXV be a bilinear map

0 if Ω (X, Y)= Ω (Y, X) > Ω is symmetric

图附有不是口的的量,自己和自己內較季季20

Def, 3,3

の A is 正年 & symmetric on V ラ A is inner product

油部內華冊任: <水,少>

○ 内集監問: (1,<,,,>)

 $\langle x, y \rangle = [X_1, X_2] \begin{bmatrix} a & c \\ d & b \end{bmatrix} \begin{bmatrix} Y_1 \\ Y_2 \end{bmatrix}$

· AT = A (Symmetric)

· A 15年記

VX GRZ, XTAX DO, XAX-OC) X-D

Let <*, W> = [*] A[4]B

(زطا, نطا> = زنه