

# CSCI 599: Deep Learning and its Applications

## Lecture 4

Spring 2019  
Joseph J. Lim

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## Office Hours

- Instructor OH @ RTH 402
  - Tuesday 2-3:30pm
  - This is NOT for homework related questions.
- TA OH @ SAL 125
  - Monday 5-6pm & Tuesday 12:30-1:30pm
  - Extra OH for assignment due & midterm weeks:  
Monday 4-5pm & Tuesday 11:30-12:30pm

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## Disclaimer

- This course is taught for the 2nd time @ USC. This course is 599, and thus an **experimental** course.
- The syllabus, course policy, and grading details **may change** over the semester (**check website!**)
- If you prefer a well-structured course, this is **NOT** a course for you, and I encourage you to take the course next year.
- But, it will be **fun** and **challenging!**

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# Communication

- Please use **Piazza** for any general communication including questions  
<https://piazza.com/usc/spring2019/csci599/home>
- E-mails will be ignored.
- **Register TODAY. Look for your project team mates!**

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# Assignment 1

- Assignment 1 will be released next week.

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# Important Dates

- Entrance exam: 1/15
- Assignment 1: 2/19
- Midterm: 3/5
- Project meeting with Instructor #1: 3/6 — 3/8
- Assignment 2: 3/26
- Project meeting with Instructor #2: 4/1 — 4/3
- Project meeting with TA: 2 times (arranged later)
- Final presentation: 4/23 5-9:00pm **4 hours**

Subject to change!

# Course Project

Subject to change!

- Computational resource (**be conservative**)  
\$150 Google Cloud credit per student  
\$125 Amazon AWS credit per student
- Tentative Schedule for Project
  - Week 5 (2/5): Course Project Team
  - Week 8 (2/26): Course Project Proposal
  - Week 13 (4/2): Mid-report
  - Week 16 (4/23): **Project Presentation** (5-9pm) + Report

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## Course Project

- Team-based project (4-5 students per team)
- Each team will have at least 1 dedicated TA
  - 2 Mandatory meetings with TA
  - 2 meetings with me
- Create your own problems (extra points)
  - **Talk and discuss** with your TAs and me!
  - In the worst case, we will give a project idea
    - Less fun, Less points!

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## Project Evaluation

- Creativity and difficulty of the problem setup
- Novelty of the approach
- Thoroughness of the experiments
- Quality of student's presentation, report, and meetings with TA/instructor

**Extra credit** for creating your own project (OK to discuss and get help from TAs)

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## Project

- Report: a blog post (rather than a paper format)
- Lots of “what if we fail” questions

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## Team Formation

- Start forming your team NOW!

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## Today's agenda

- Recap: Neural Networks & Loss function
- Optimization
- Convolutional Neural Networks
- Training Neural Networks

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- Recap: Neural Networks & Loss function
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It's matter of one function

$$X \longrightarrow f(X) \longrightarrow Y$$

It's matter of one function

$$X \longrightarrow f(X) \longrightarrow Y$$

Really...?

Let's take a look

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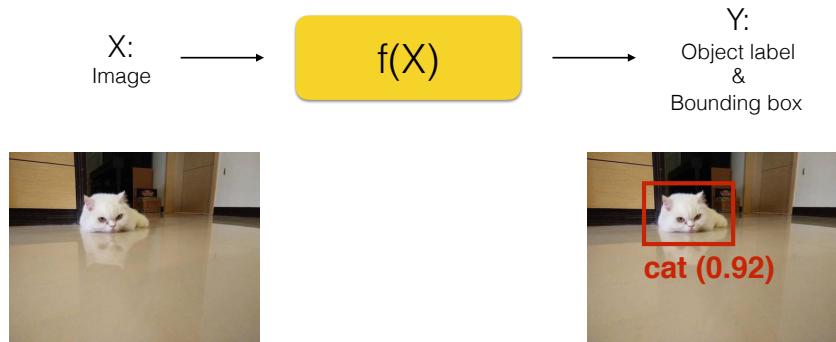
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## Object Detection

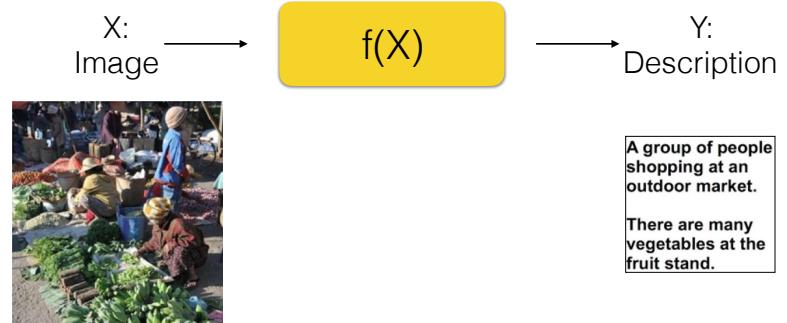


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## It's matter of one function

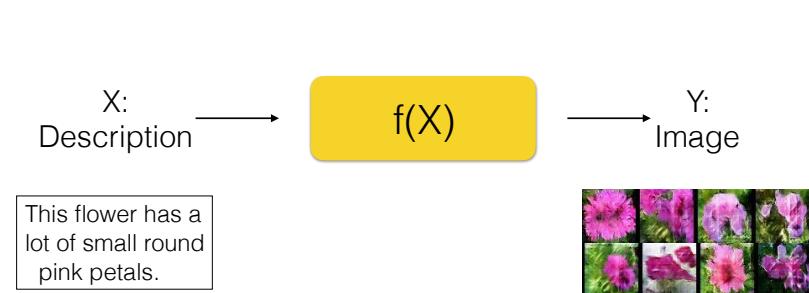


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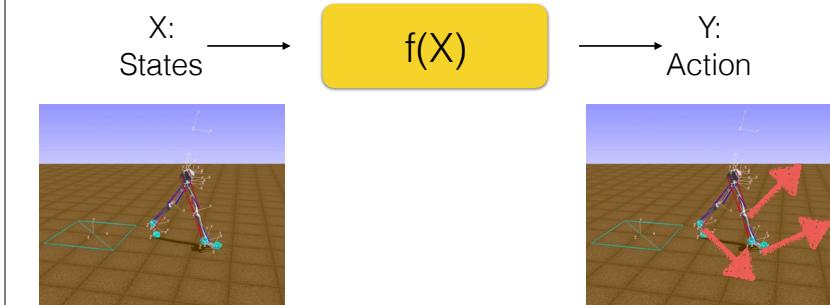


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## Learning to Walk



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## Types of Learning



- Supervised Learning                      desired output (**Y**) in training data
- Unsupervised Learning                  **Y** not in training data
- Weakly / Semi-supervised Learning    some of **Y** in training data
- Reinforcement Learning                 rewards based on a set of actions

Definition from Dhruv Batra's deep learning course (ECE 5604)

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## Our goal is “to approximate”



There may exist an exact function ( $f^*$ ) mapping from  $X$  to  $Y$ .

Our goal is not to find this exact function.

Rather, we are happy as long as  $f(X)$  can **approximate**  $f^*(x)$ .  $f$  does NOT have to be exactly  $f^*$ .

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## Our goal is “to approximate”



For  $f(X)$  to approximate any  $f^*(X)$ ,  $f$  is better to be highly capable.

Deep learning is an effective method for this

- Non-linear (high capacity)
- Hierarchical
- End-to-End learning

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## Recap: Our course



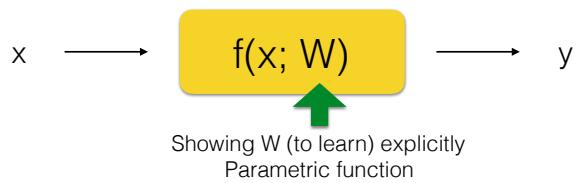
- (1) How do we learn this function (using deep learning)?
- (2) How to formulate a problem into this

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## Loss function & Optimization



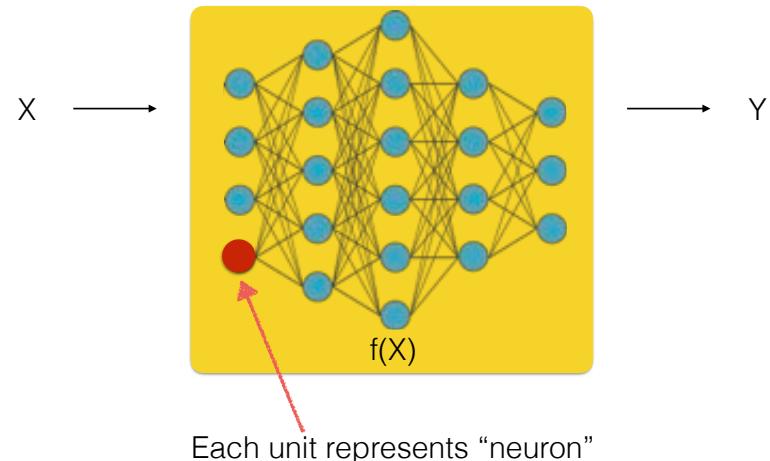
- **Loss function ( $L$ )** measures how well learned  $W$  can map  $X$  to  $Y$  (compared to  $f^*$ ).
- **Optimization** finds the best  $W$  given a loss function  $L$  (i.e. finding  $W$  that minimizes  $L$ ).

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## Neural Networks

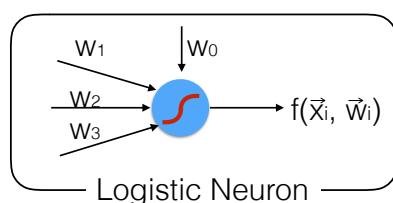
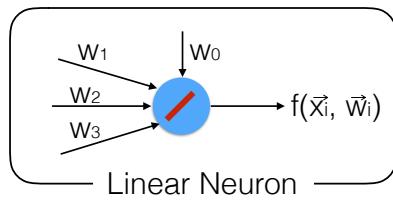
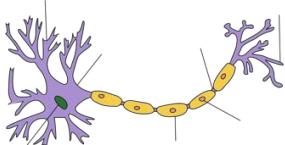


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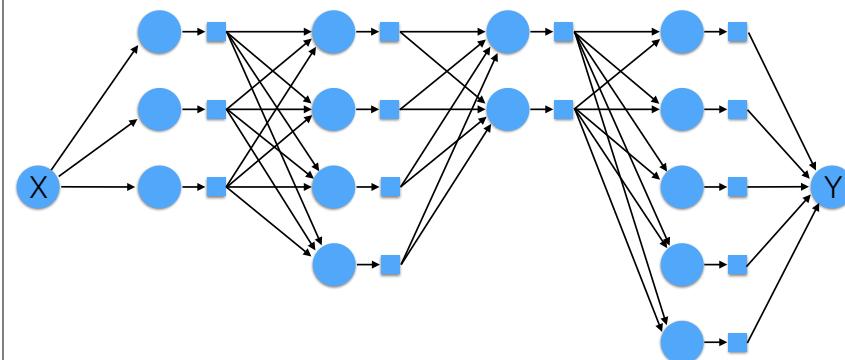
## “Neuron”



More neurons!

Modified from the HKUST slide

## Neural Networks Example

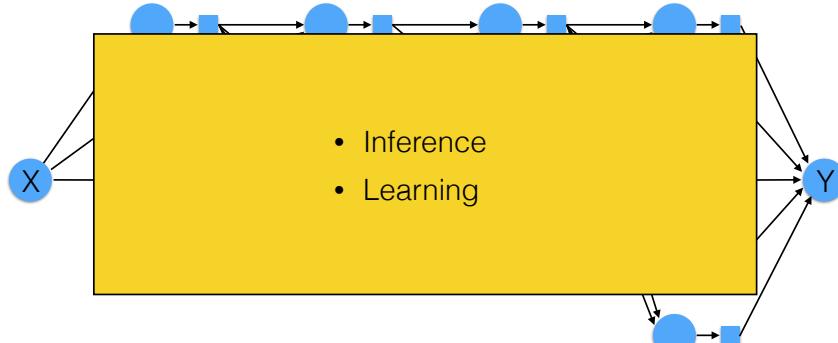


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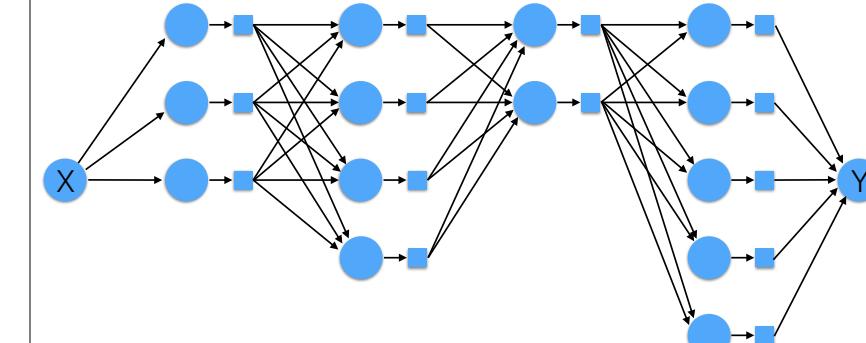


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## Forward propagation

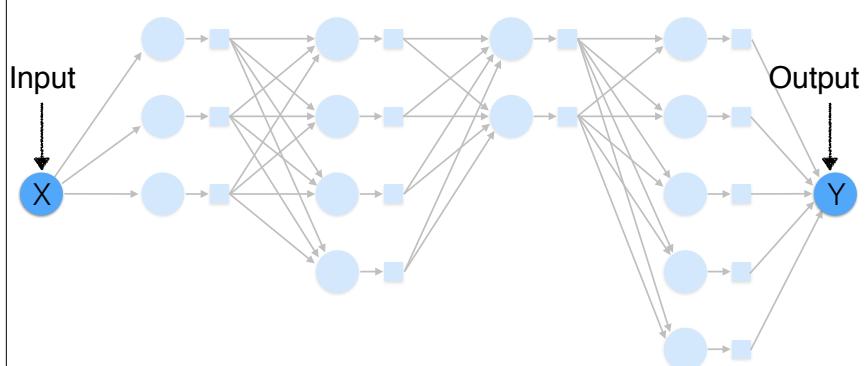


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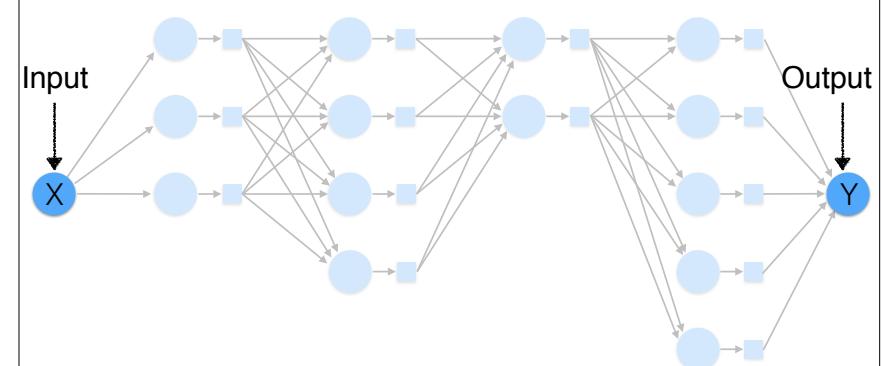


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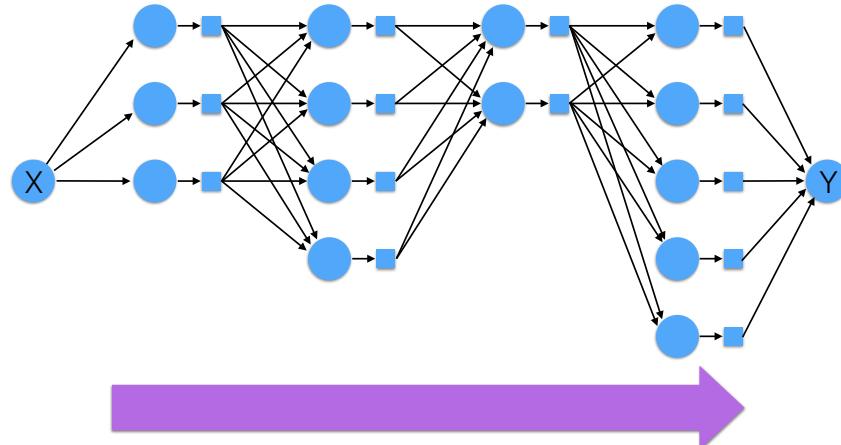


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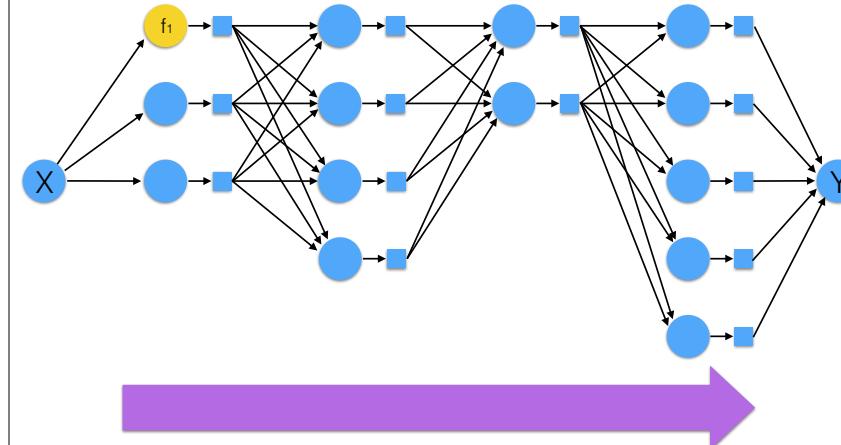


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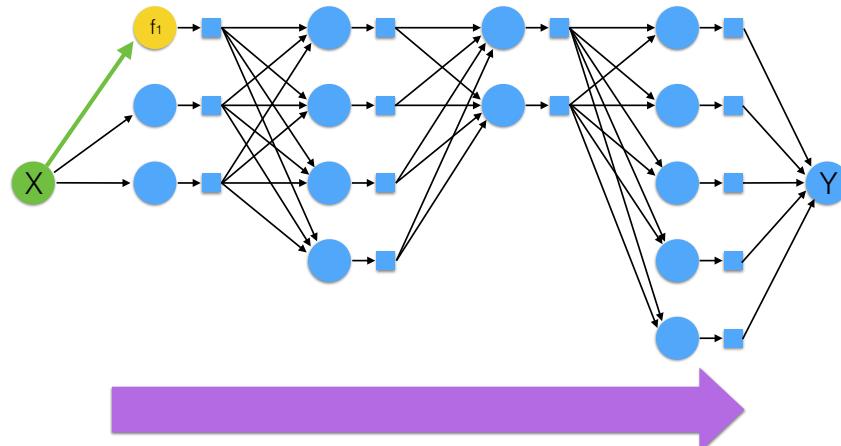


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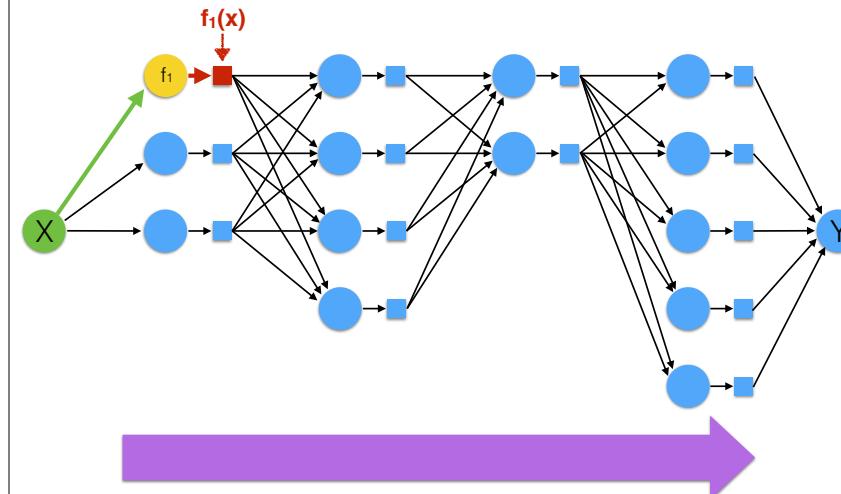


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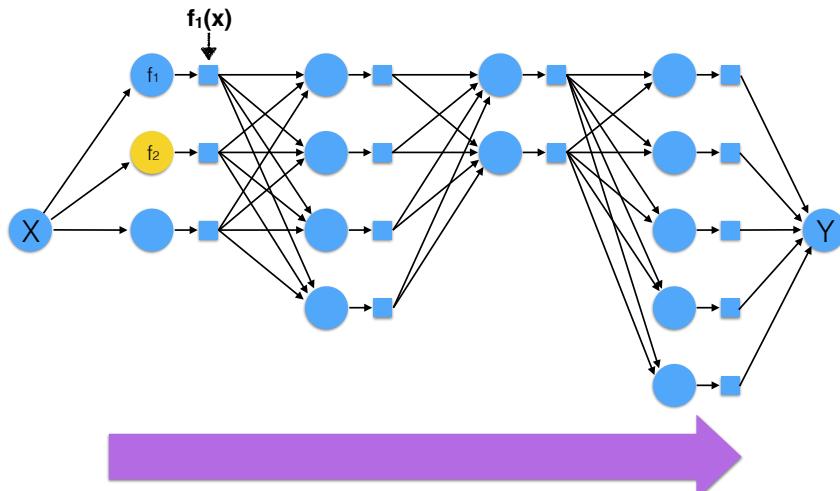


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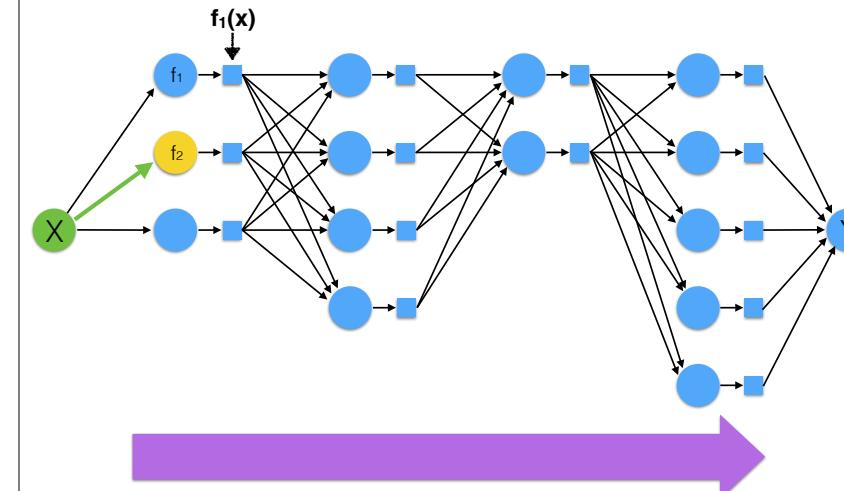


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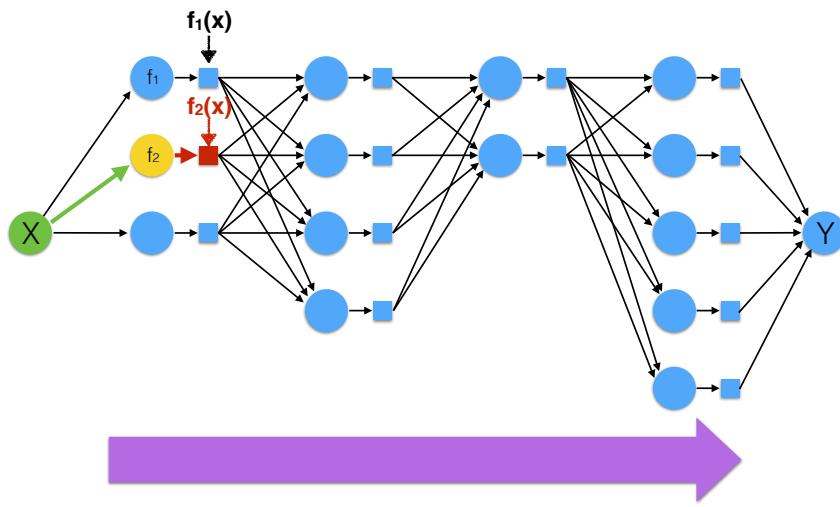


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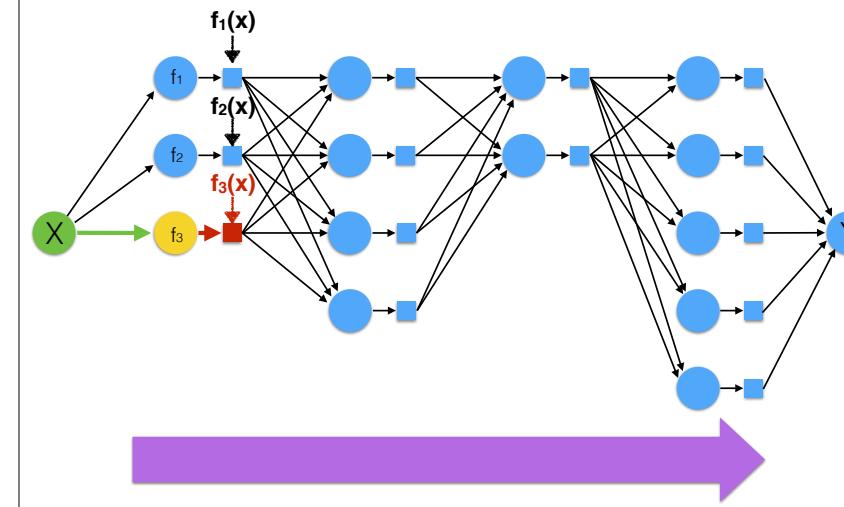


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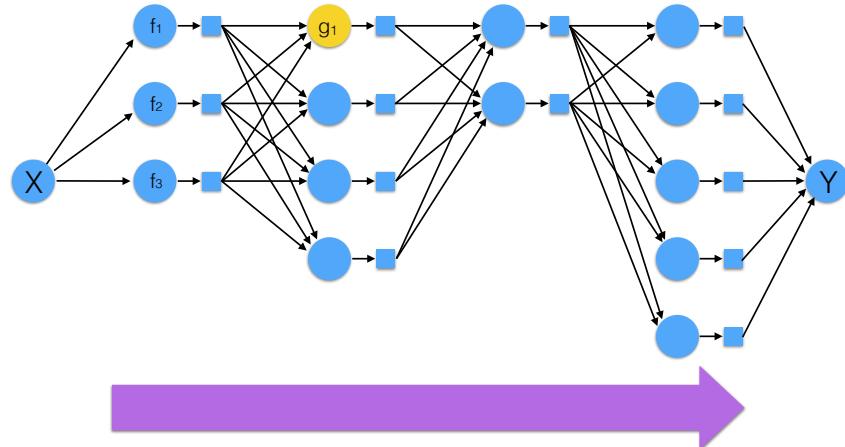


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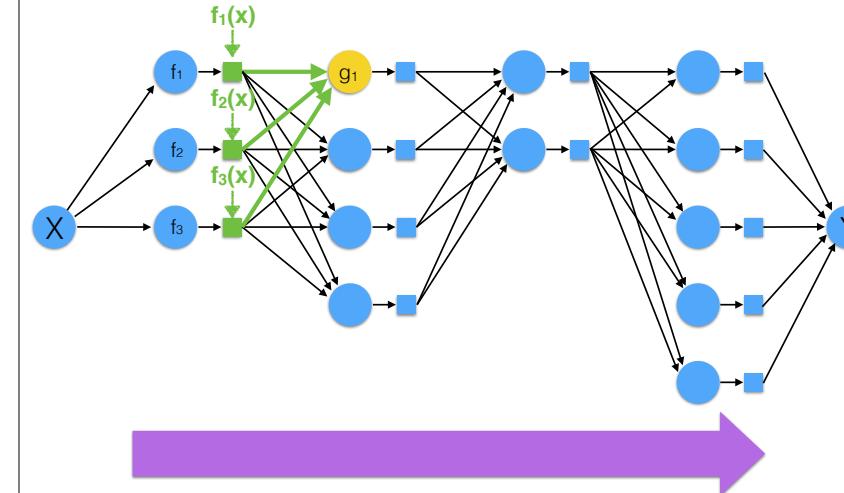


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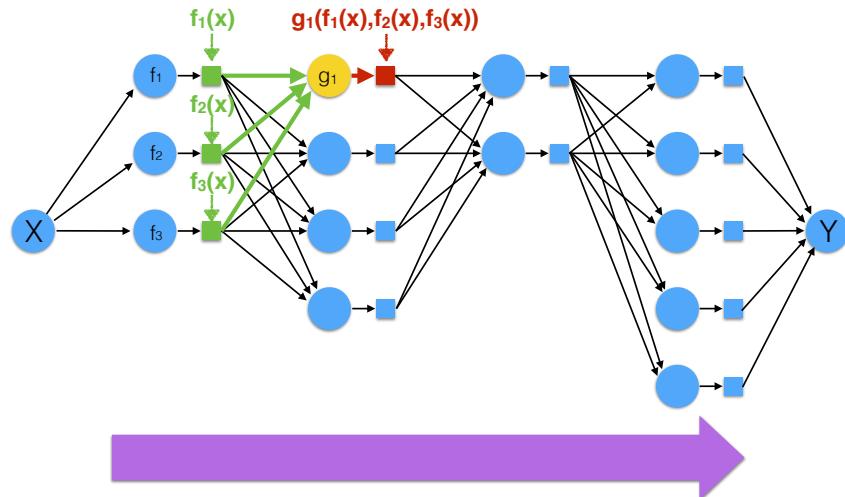


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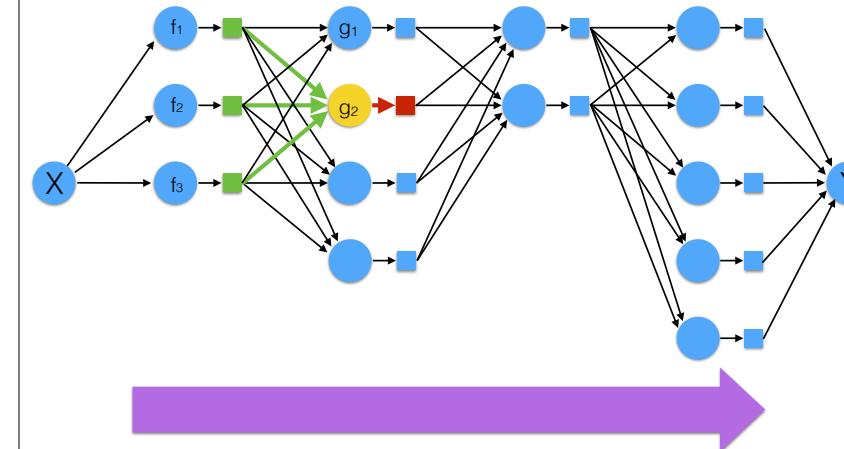


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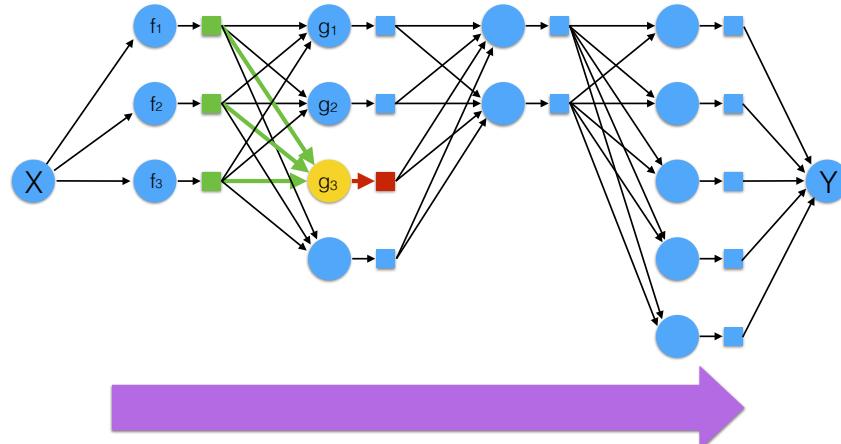


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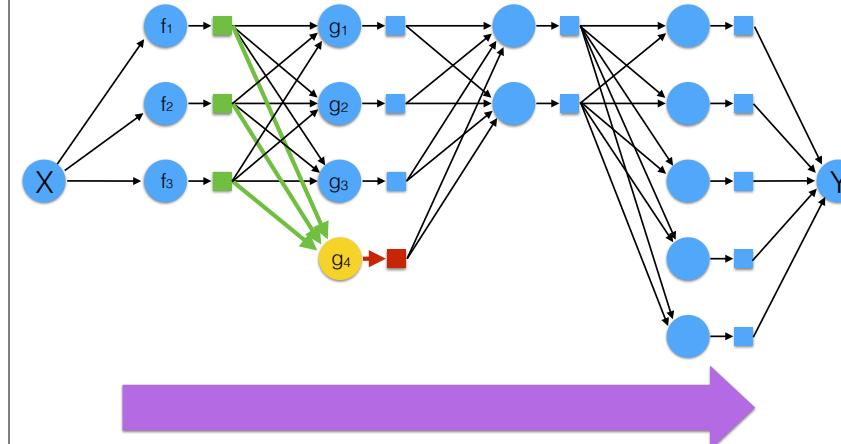


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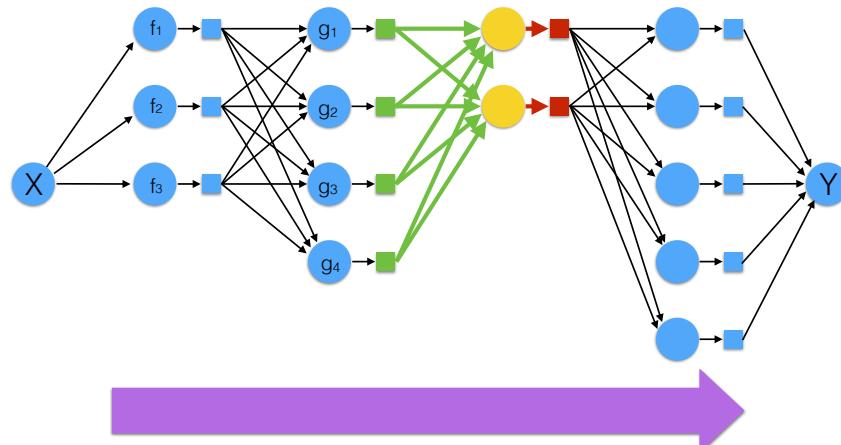


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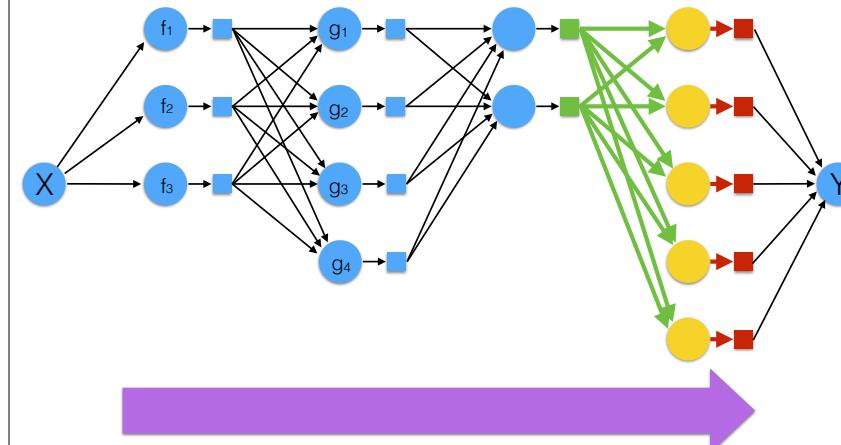


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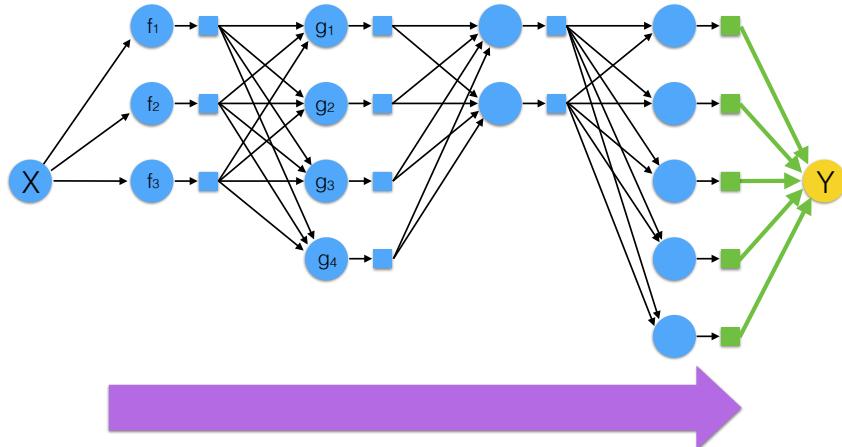


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## Forward propagation

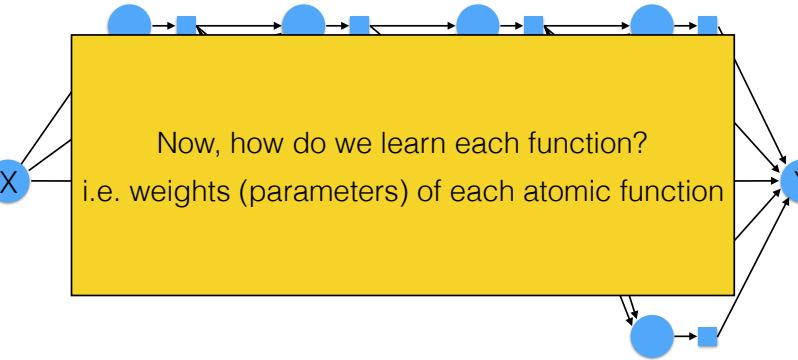


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## Neural Networks Example



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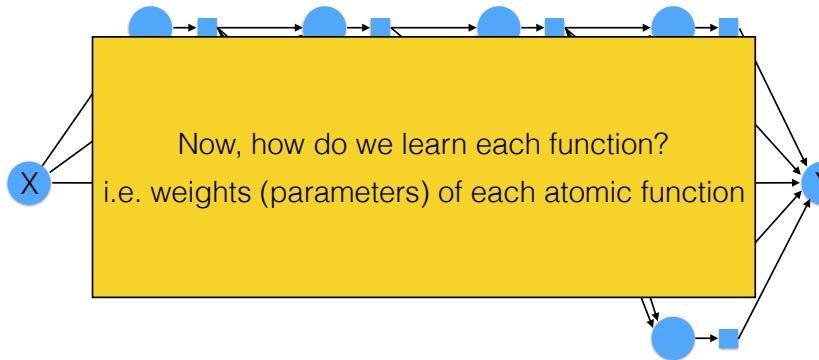
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## Today's agenda

- Recap: Neural Networks & Loss function
- Optimization
- Convolutional Neural Networks
- Training Neural Networks

## Neural Networks Example

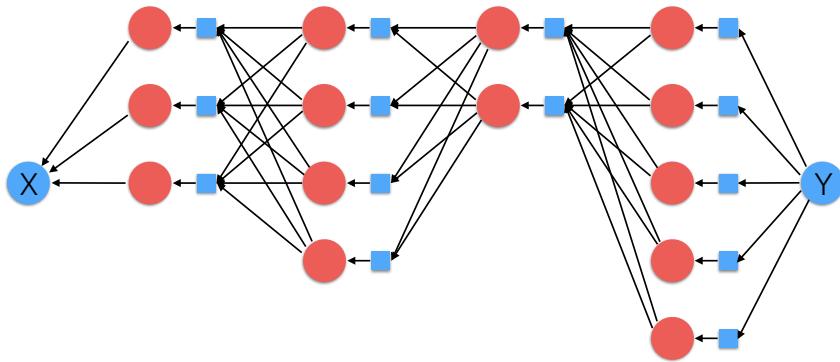


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## Backward propagation



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## Computational Graph

Let's step back.

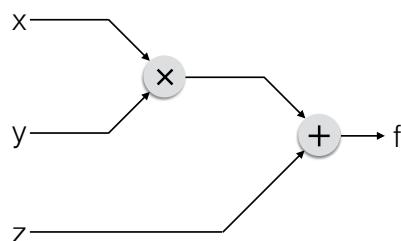
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## Computational Graph

Function:  $f(x, y, z) = x \cdot y + z$



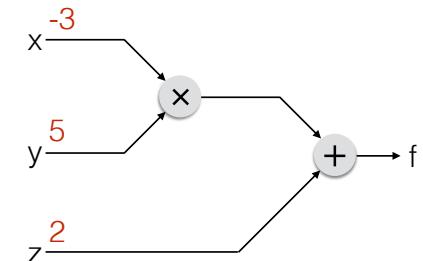
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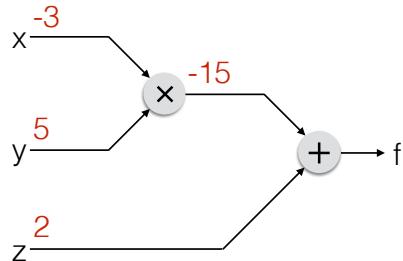
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## Computational Graph

Function:  $f(x, y, z) = x^*y+z$



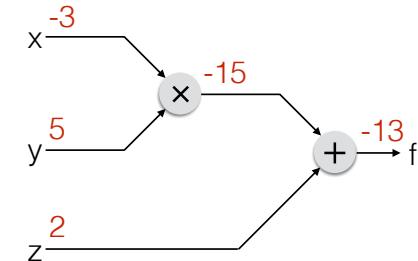
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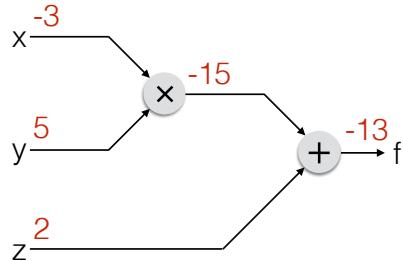
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## Computational Graph

Function:  $f(x, y, z) = x^*y+z$

Backpropagation



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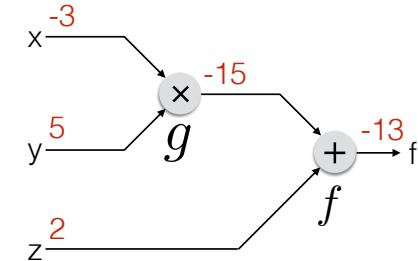
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Function:  $f(x, y, z) = x^*y+z$

Backpropagation

$$g = x \times y$$

$$f = g + z$$



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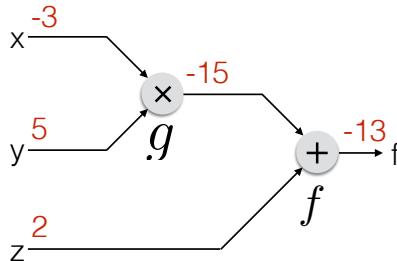
## Computational Graph

Function:  $f(x, y, z) = x^*y+z$

Backpropagation

$$g = x \times y \quad \frac{\partial g}{\partial x} = y \quad \frac{\partial g}{\partial y} = x$$

$$f = g + z \quad \frac{\partial f}{\partial g} = 1 \quad \frac{\partial f}{\partial z} = 1$$



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## Computational Graph

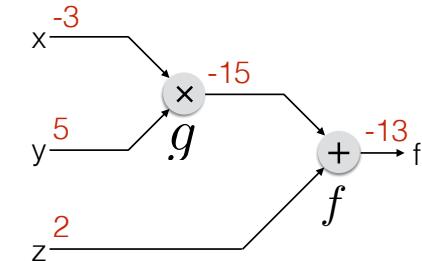
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We want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$



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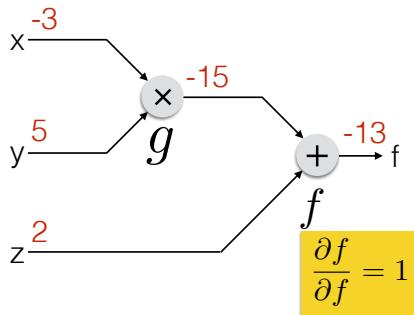
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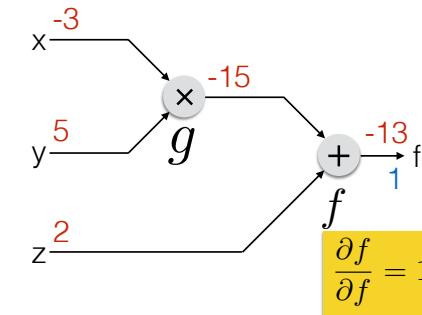
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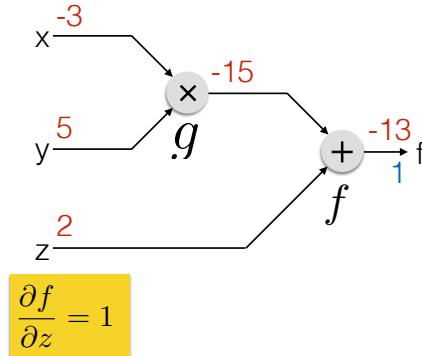
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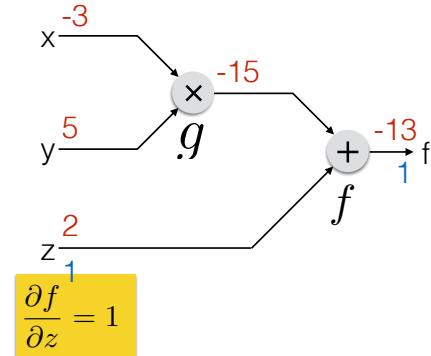
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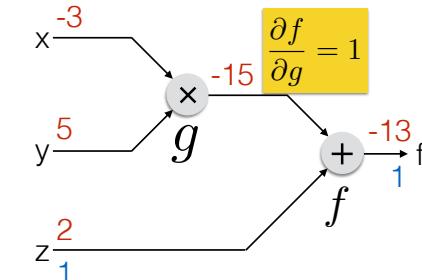
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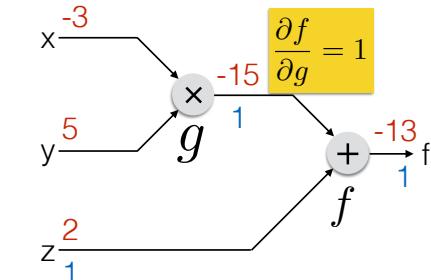
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## Computational Graph

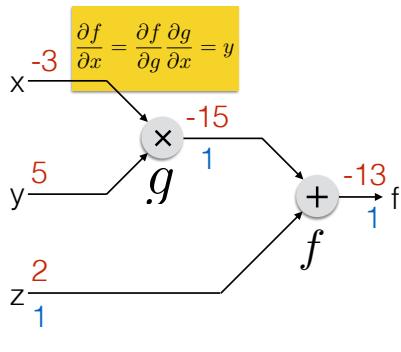
Function:  $f(x, y, z) = x^*y+z$

Backpropagation

$$g = x \times y \quad \frac{\partial g}{\partial x} = y \quad \frac{\partial g}{\partial y} = x$$

$$f = g + z \quad \frac{\partial f}{\partial g} = 1 \quad \frac{\partial f}{\partial z} = 1$$

We want:  $\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}, \frac{\partial f}{\partial z}$



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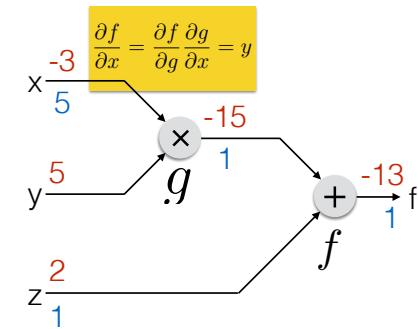
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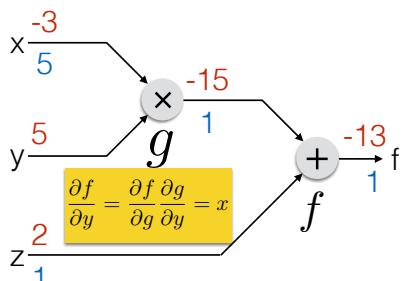
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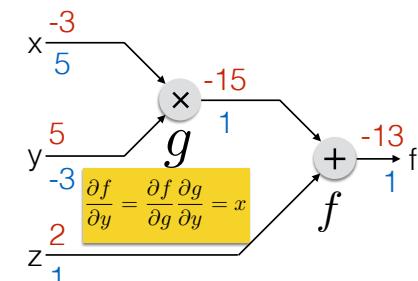
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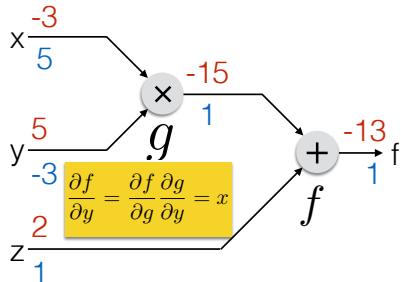
Function:  $f(x, y, z) = x^*y+z$

Backpropagation

$$\frac{\partial f}{\partial x} = 5$$

We get:  $\frac{\partial f}{\partial y} = -3$

$$\frac{\partial f}{\partial z} = 1$$



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## Computational Graph

Note: a local view of it

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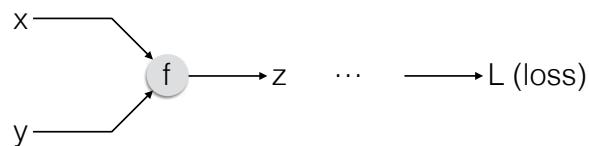
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## Computational Graph

Function:  $f(x, y, z) = x^*y+z$

**A local view** of backpropagation

Forward propagation



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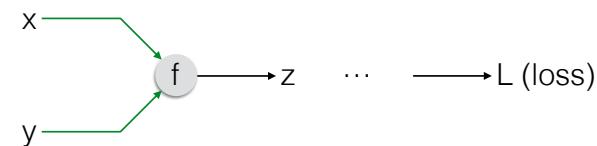
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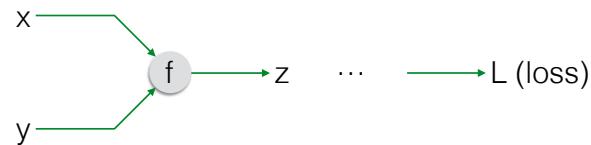
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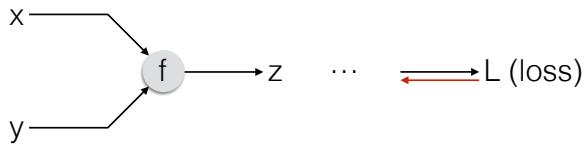
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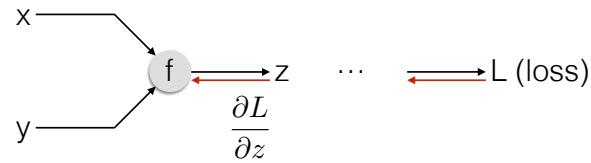
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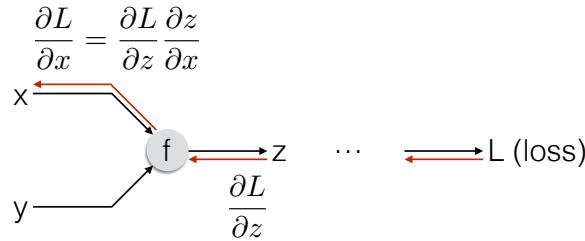
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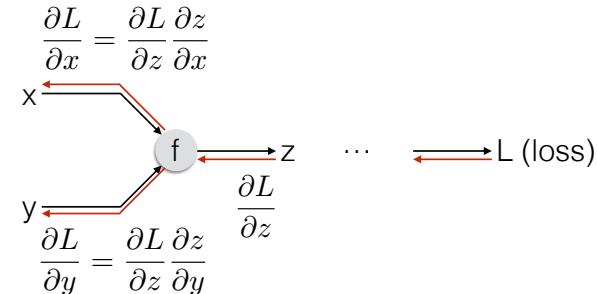
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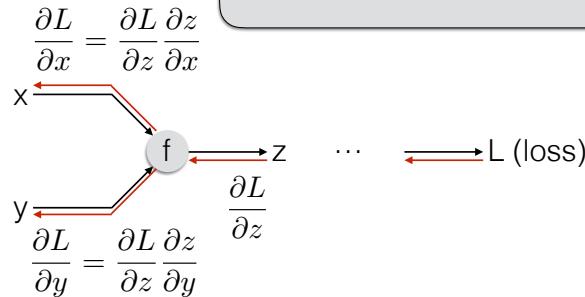
## Computational Graph

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**A local view** of backpropagation

Backpropagation

Requires a function to be differentiable



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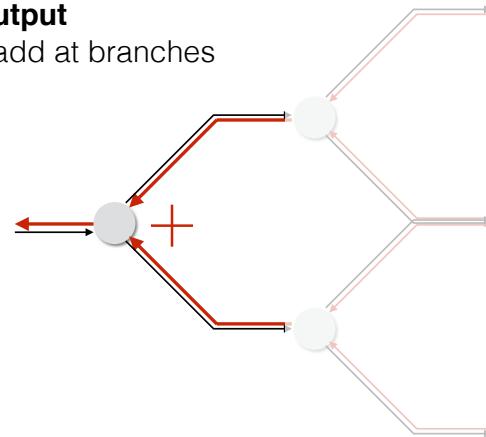
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## Computational Graph

Function:  $f(x, y, z) = x^*y+z$

**Multiple output**

Gradients add at branches



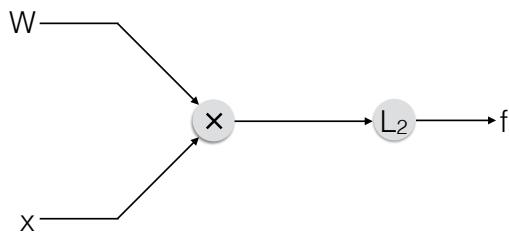
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## Computational Graph

A vectorized example:  $f(x, W) = \|W \cdot x\|^2 = \sum_{i=1}^n (W \cdot x)_i^2$



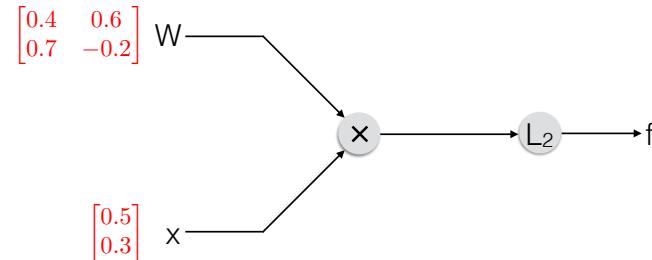
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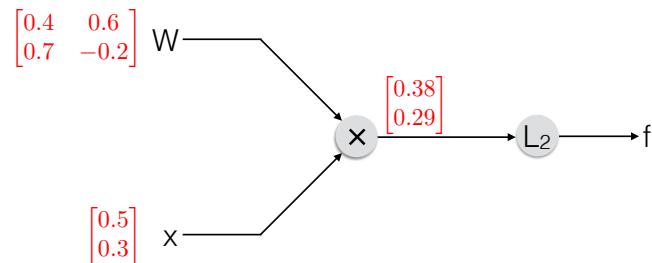
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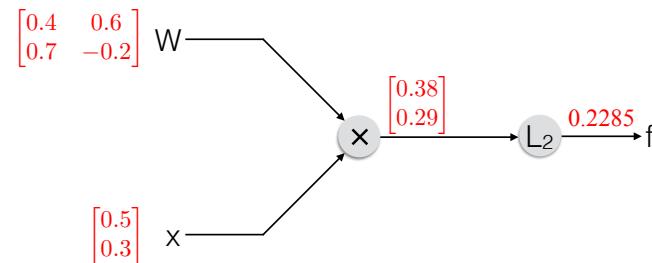
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We want:  $\frac{\partial f}{\partial W_{i,j}}, \frac{\partial f}{\partial x_i}$

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We want:  $\boxed{\frac{\partial f}{\partial W_{i,j}}}, \frac{\partial f}{\partial x_i}$

$$q = W \cdot x = \begin{pmatrix} W_{1,1}x_1 + \dots + W_{1,n}x_n \\ \vdots \\ W_{n,1}x_1 + \dots + W_{n,n}x_n \end{pmatrix}$$

$$f(q) = \|q\|^2 = q_1^2 + \dots + q_n^2$$

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$$\frac{\partial q_k}{\partial W_{i,j}} = 1_{k=i} x_j$$

$$\frac{\partial f}{\partial W_{i,j}} = \sum_k \frac{\partial f}{\partial q_k} \frac{\partial q_k}{\partial W_{i,j}} = \sum_k (2q_k)(1_{k=i} x_j) = 2q_i x_j$$

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$$\frac{\partial f}{\partial x_i} = \sum_k \frac{\partial f}{\partial q_k} \frac{\partial q_k}{\partial x_i} = \sum_k 2q_k W_{k,i}$$

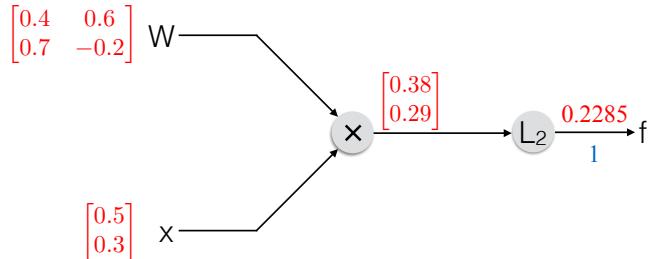
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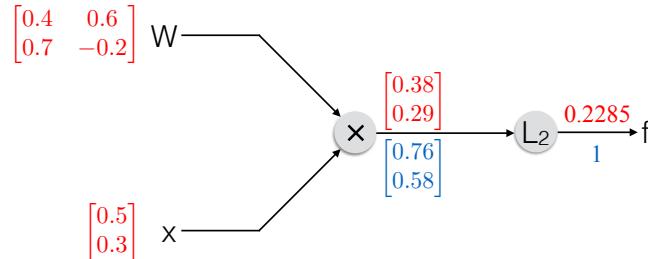
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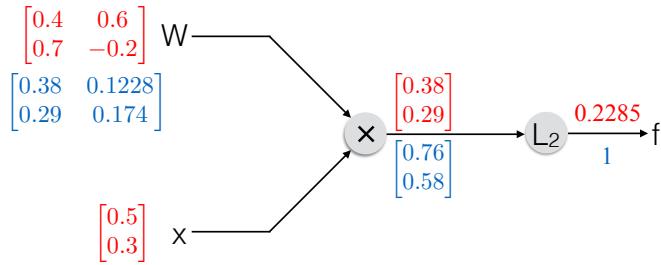
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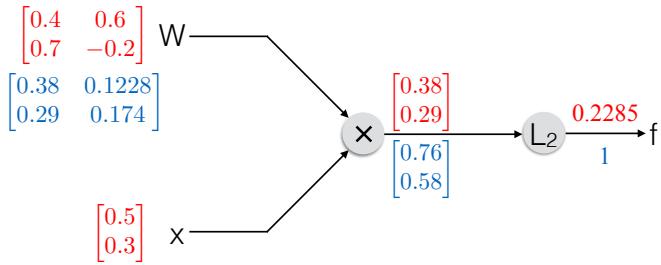
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# Computational Graph

A vectorized example:  $f(x, W) = \|W \cdot x\|^2 = \sum_{i=1}^n (W \cdot x)_i^2$



$$\begin{bmatrix} 0.71 \\ 0.34 \end{bmatrix} \quad \frac{\partial q_k}{\partial x_i} = W_{k,i}$$

$$\frac{\partial f}{\partial x_i} = \Sigma_k \frac{\partial f}{\partial q_k} \frac{\partial q_k}{\partial x_i} = \Sigma_k 2q_k W_{k,i}$$

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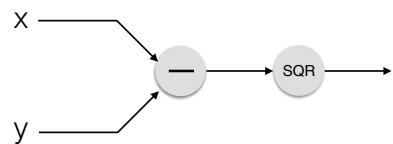
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## Lecture 4

# Layers with Computational Graph

## L2-loss

$$L_2(x, y) = (x - y)^2$$



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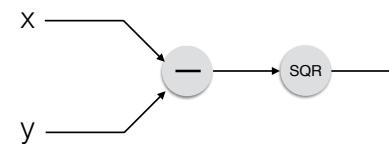
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## Lecture 4

# Layers with Computational Graph

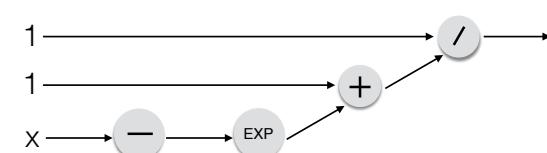
## L2-loss

$$L_2(x, y) = (x - y)^2$$



## Sigmoid

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$



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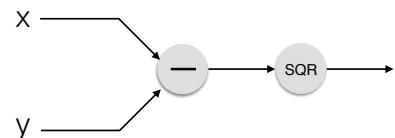
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## Lecture 4

## Layers with Computational Graph

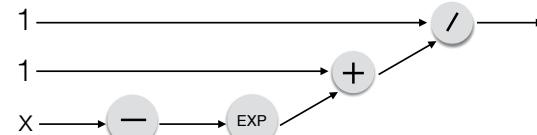
### L2-loss

$$L_2(x, y) = (x - y)^2$$



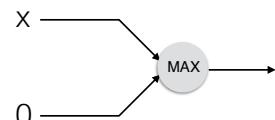
### Sigmoid

$$\text{sigmoid}(x) = \frac{1}{1 + e^{-x}}$$



### ReLU

$$\text{ReLU}(x) = \max(x, 0)$$

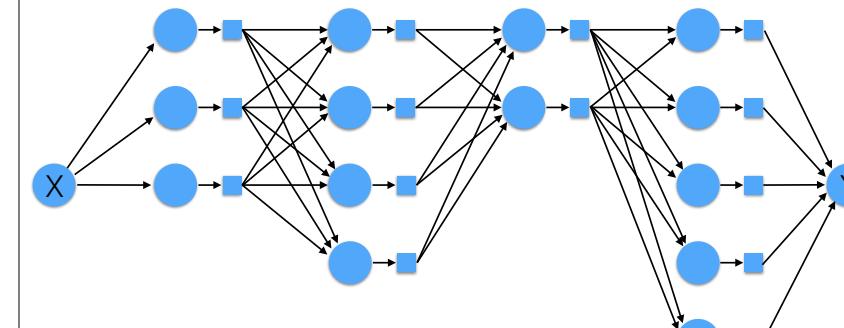


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## Neural Networks Example

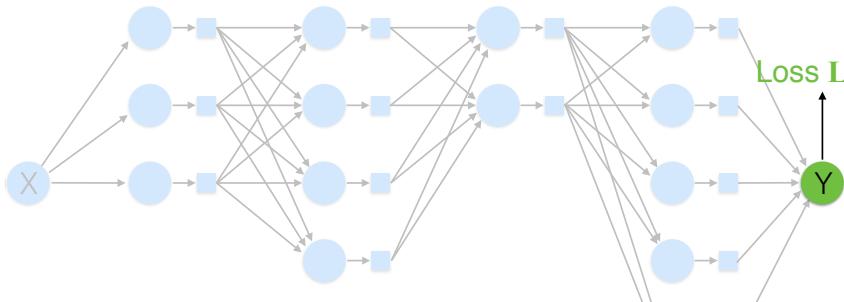


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Lecture 4

## Backward propagation



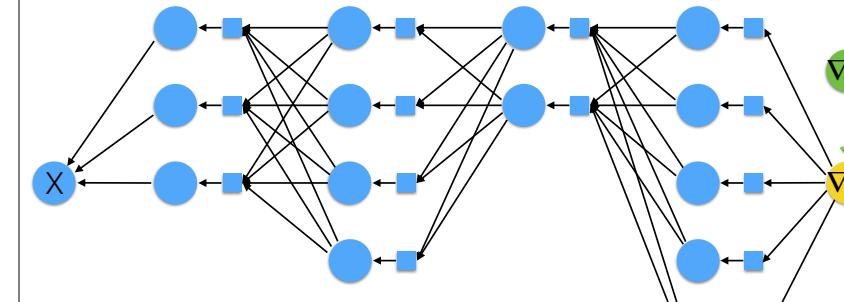
Compute a loss using an estimated  $Y$  and the ground truth  $Y^*$ .  
e.g.,  $L(W) = \| f(X; W) - Y^* \|_2$

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## Backward propagation



Compute gradients of  $Y$  using  $\nabla L$ .

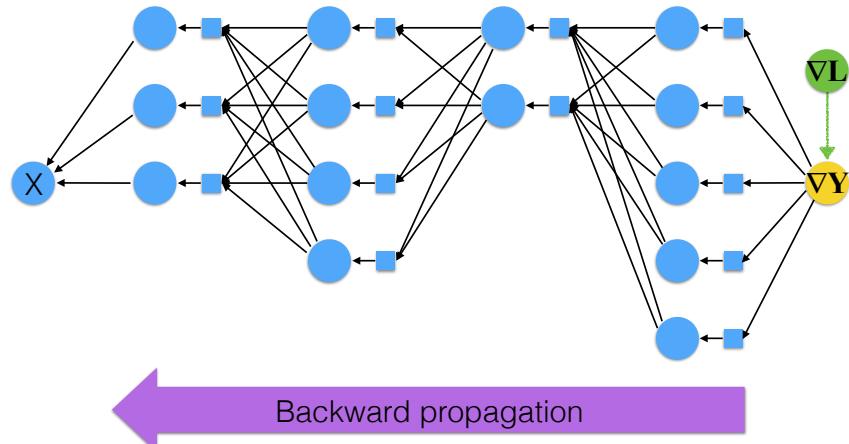
$$\frac{\partial L}{\partial X} = \frac{\partial L}{\partial Y} \cdot \frac{\partial Y}{\partial X}$$

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## Backward propagation

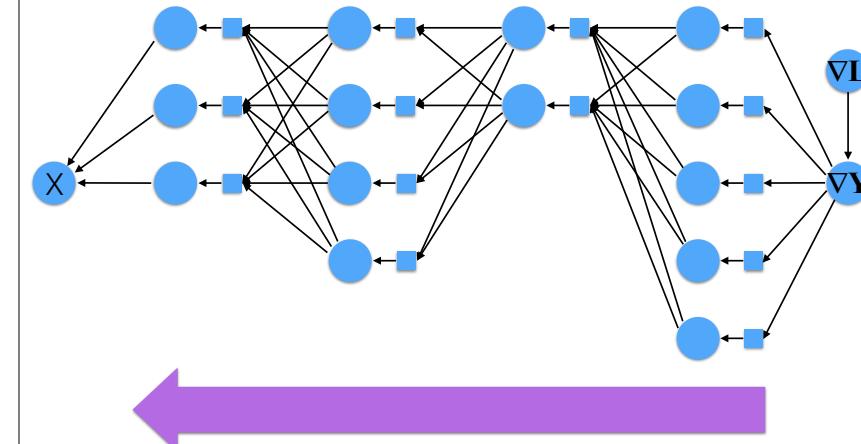


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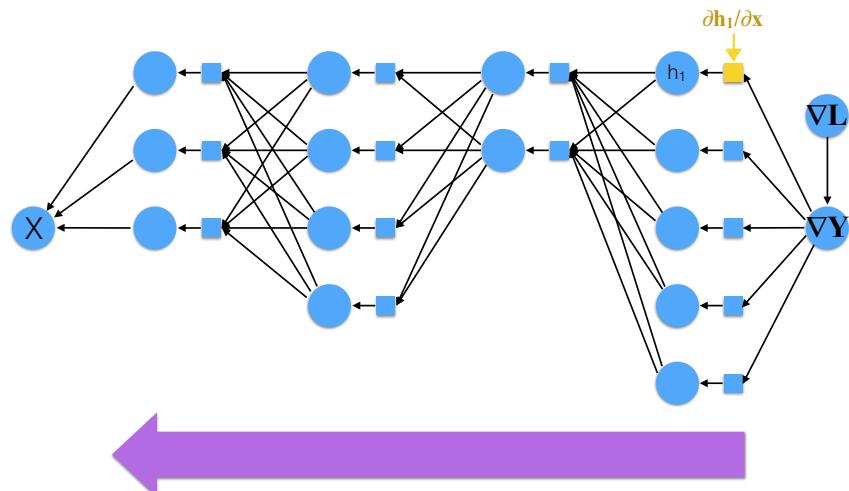


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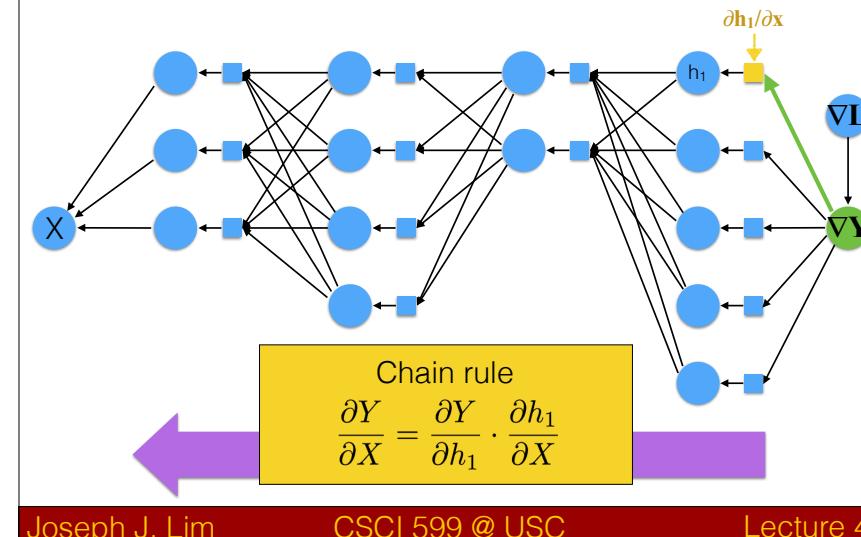


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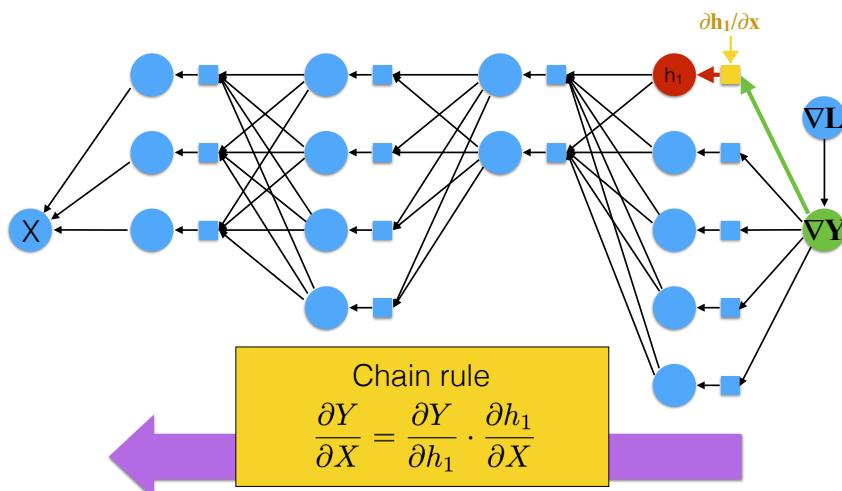


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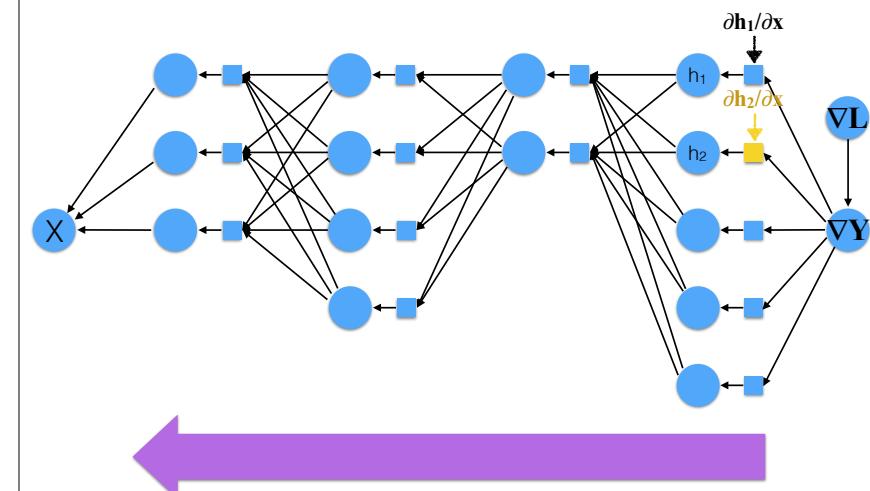


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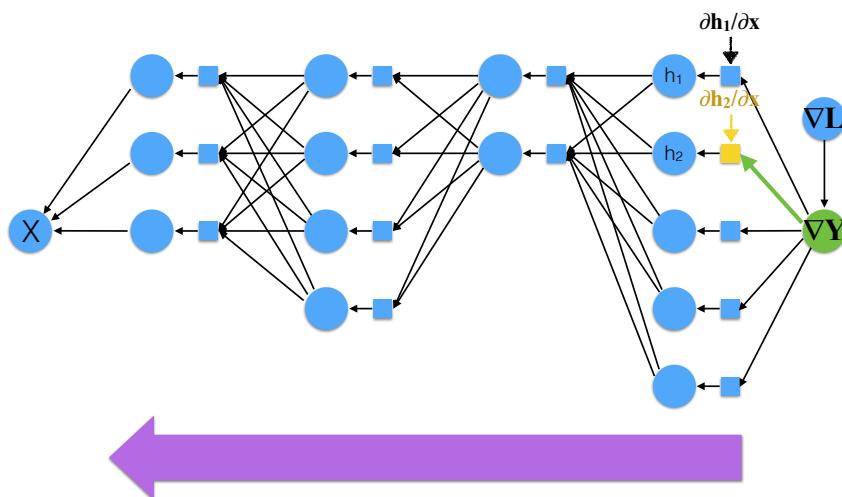


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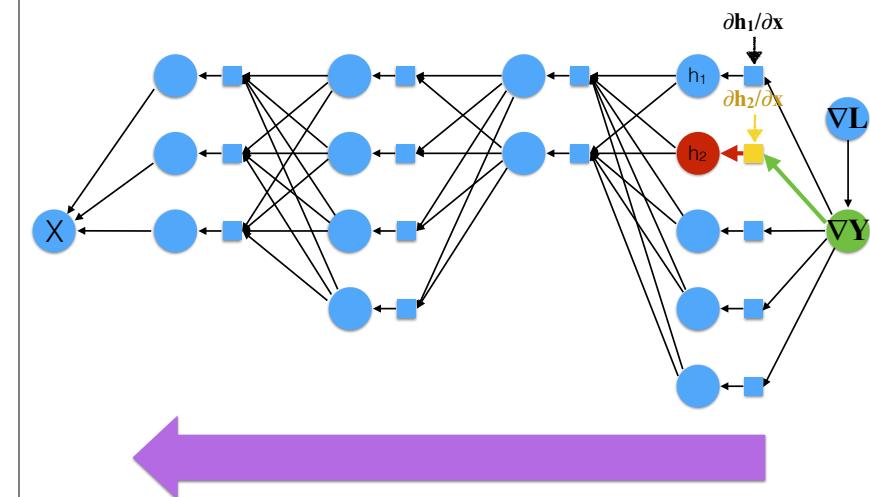


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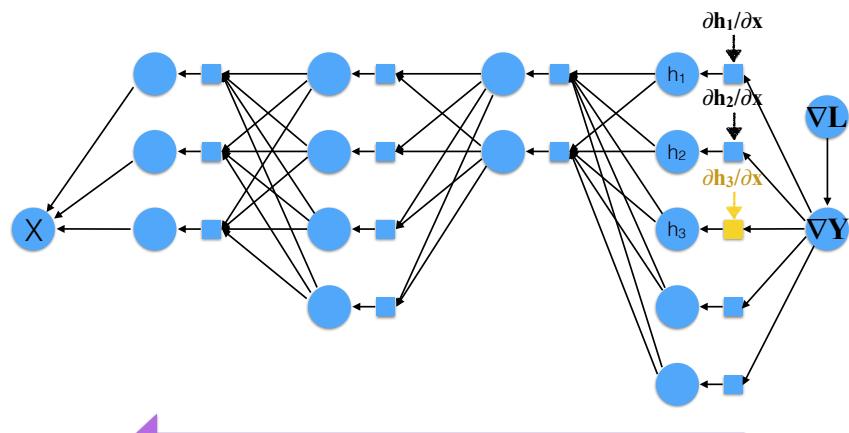


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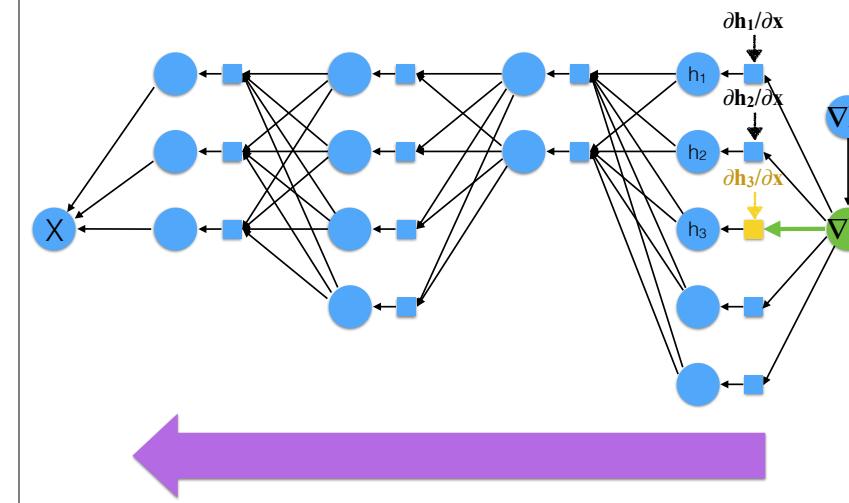


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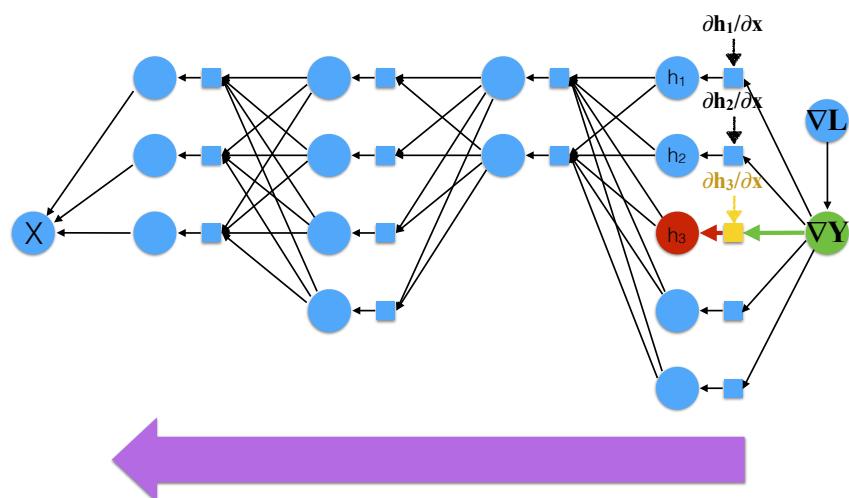


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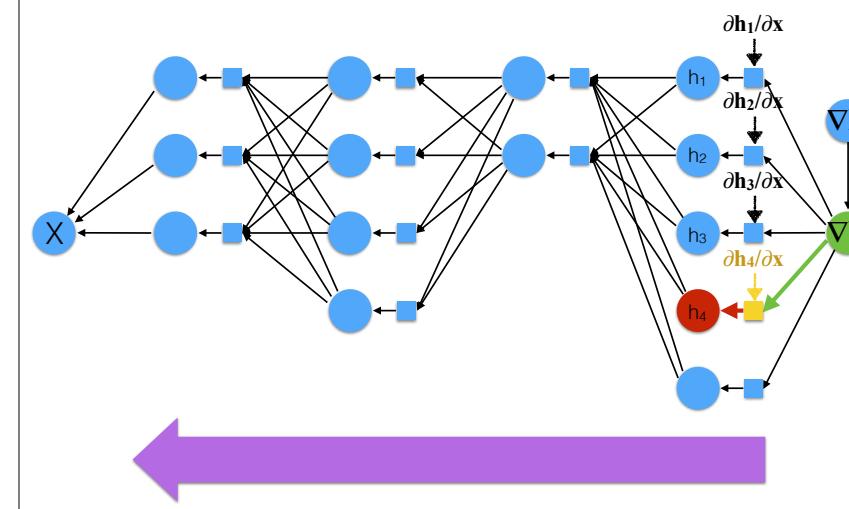


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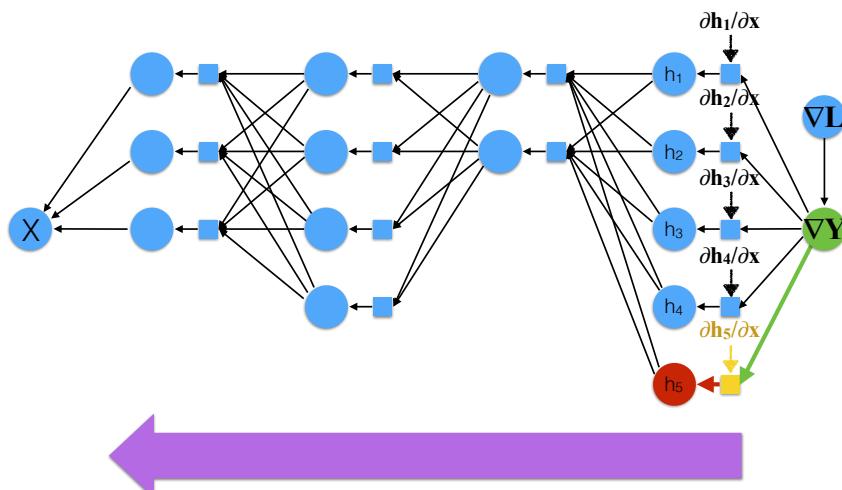


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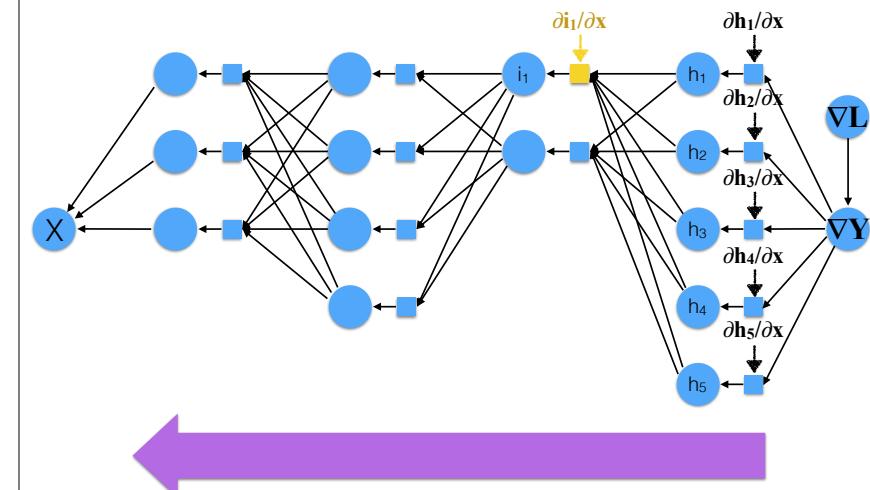


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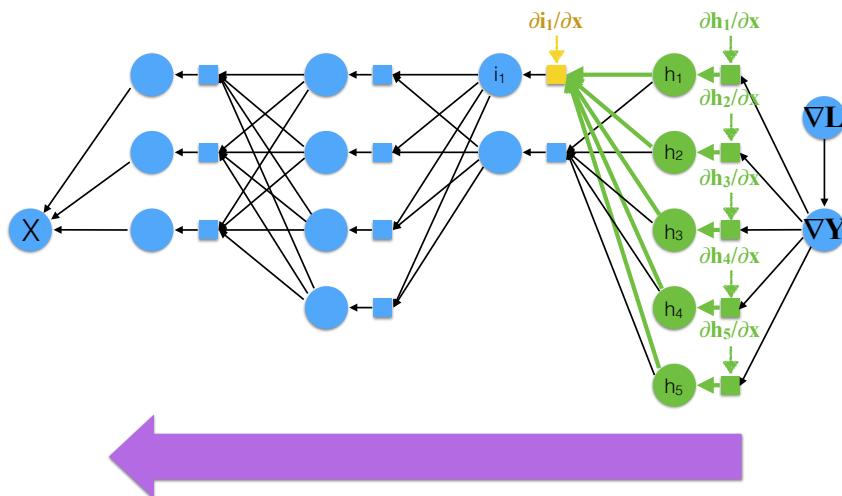


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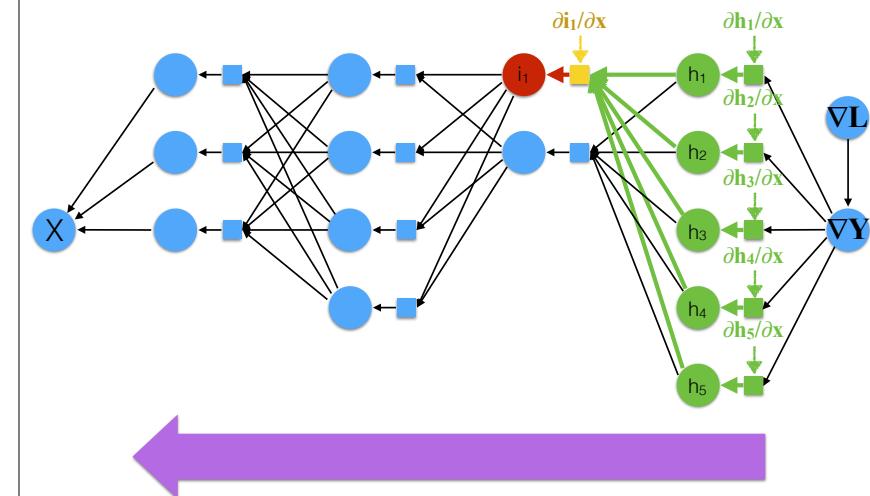


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## Backward propagation

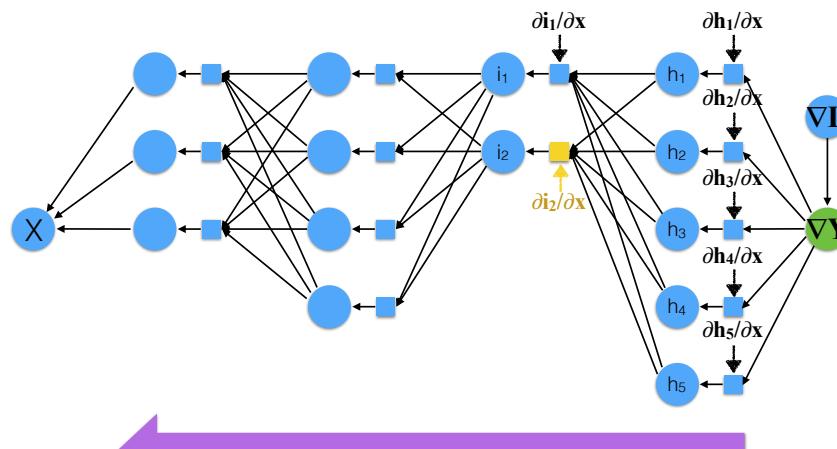


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## Backward propagation

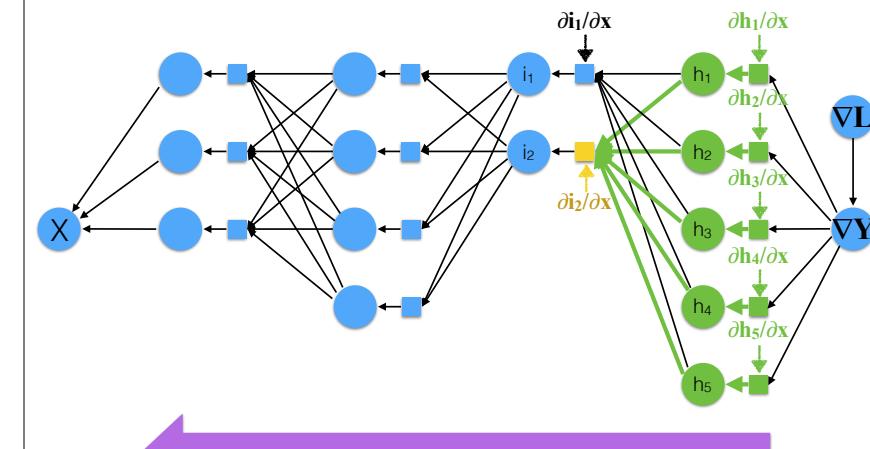


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## Backward propagation

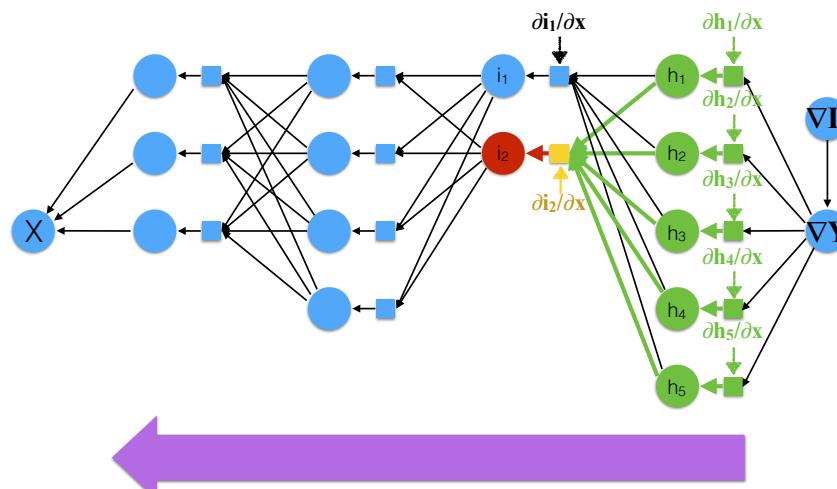


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## Backward propagation

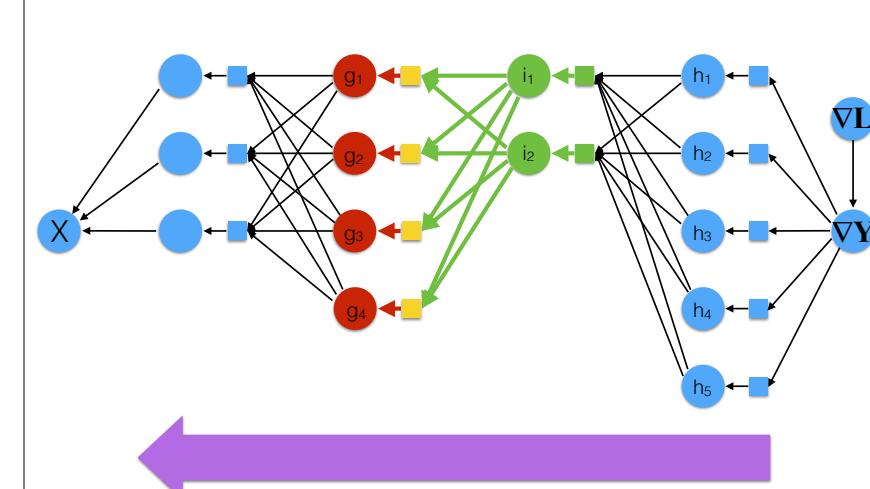


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## Backward propagation

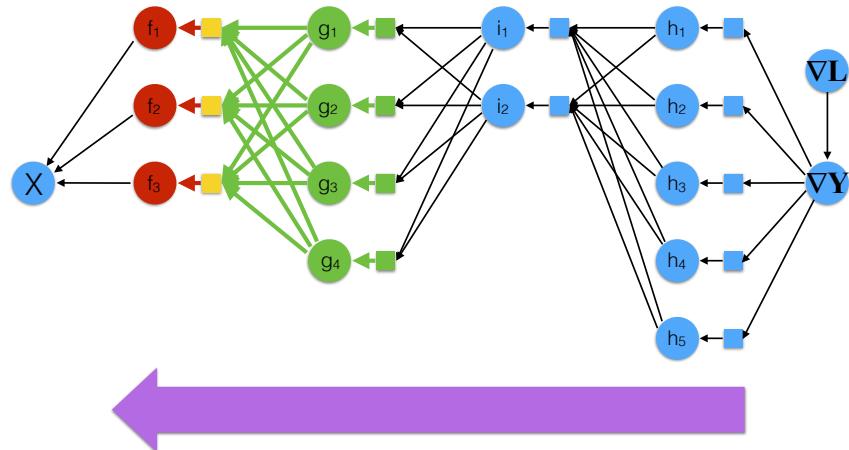


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## Backward propagation

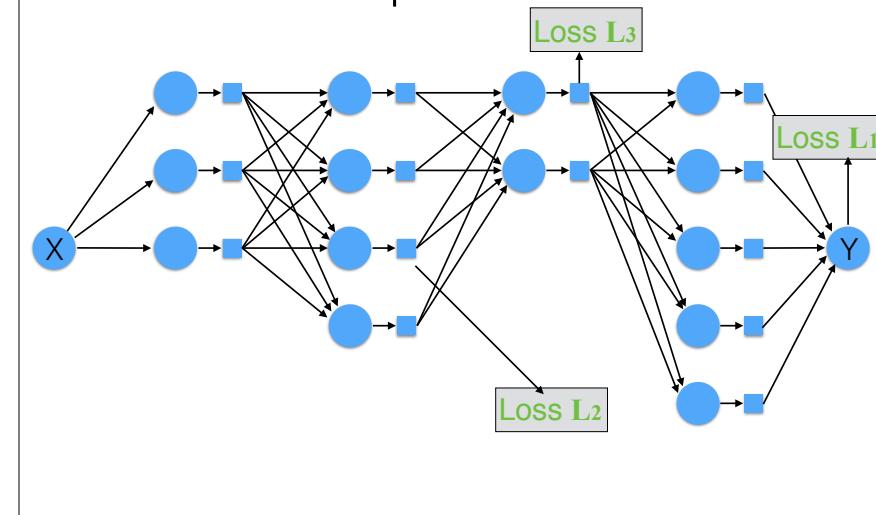


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## Multiple losses

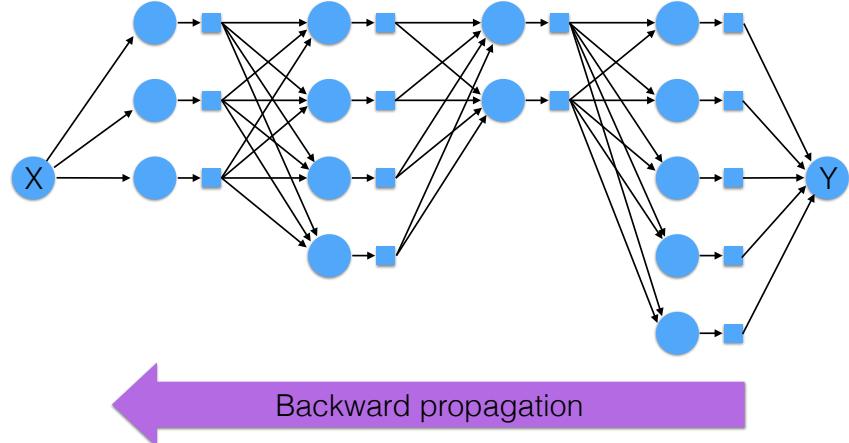


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## Neural Networks Example



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## Summary

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## Summary

- A choice of **loss function** matters.

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## Summary

- A choice of **loss function** matters.
- Neural networks is essentially **wired neurons** (small functions).

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## Summary

- A choice of **loss function** matters.
- Neural networks is essentially **wired neurons** (small functions).
- Weights can be learned using **backward propagation** (e.g. computational graph).

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Break Time

See you in 5 mins!

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## Today's agenda

- Recap: Neural Networks & Loss function
- Optimization
- Convolutional Neural Networks
- Training Neural Networks

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## Different NN models

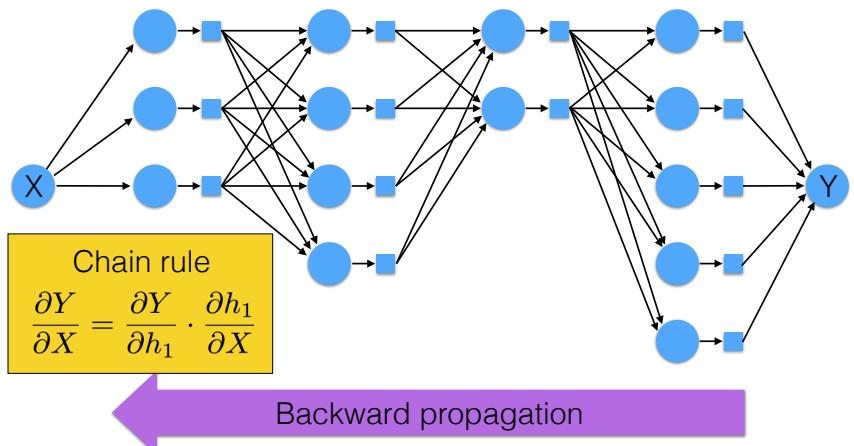
- Feedforward networks (CNNs, ...)
- Recurrent networks (RNNs, ...)
- Memory networks
- ...

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## Recap: Backward Propagation



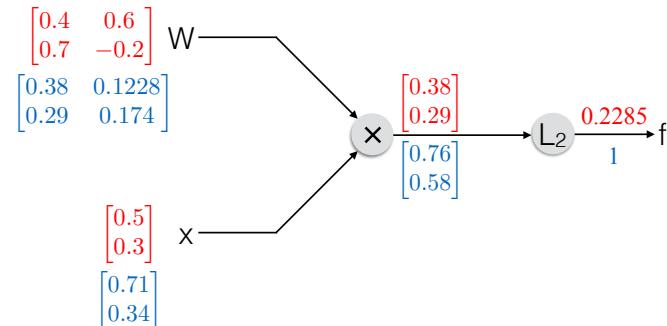
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## Recap: Computational Graph

A vectorized example:  $f(x, W) = \|W \cdot x\|^2 = \sum_{i=1}^n (W \cdot x)_i^2$



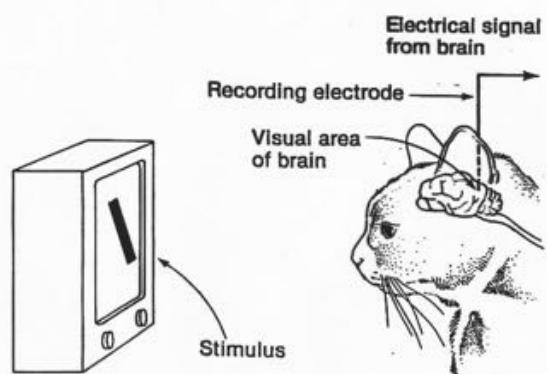
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# History

## Hubel & Wiesel



Understanding how the system constructs complex representation from simple stimulus features.

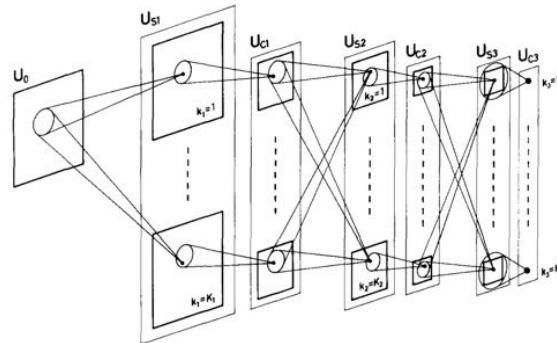
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# History

## Neocognitron



Fukushima, Kunihiko. Neocognitron: A self-organizing neural network model for a mechanism of visual pattern recognition. Competition and cooperation in neural nets 1982.

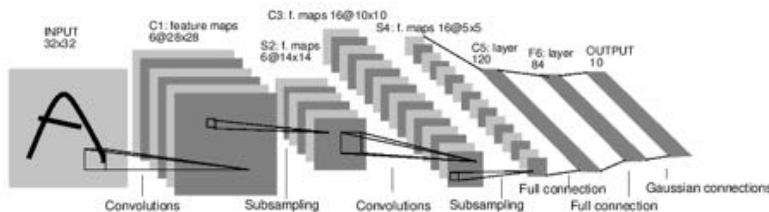
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# History

## LeNet



Y. LeCun, et. al. Handwritten digit recognition with a back-propagation network. NIPS 1989.

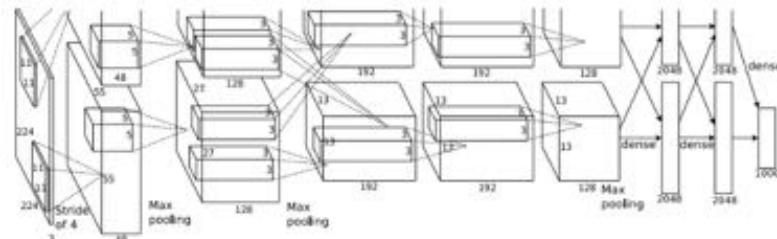
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# History

## AlexNet



A Krizhevsky, et. al. ImageNet Classification with Deep Convolutional Neural Networks. NIPS 2012.

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# History

## VGGNet



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# Convolutional NNs

## Classification



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# Convolutional NNs

## Detection



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[Faster R-CNN: Ren, He, Girshick, Sun 2015]

## Segmentation



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[Farabet et al., 2012]

Slide credit: CS 231N

# Convolutional NNs

## Game AI



[Guo et al. 2014]

Figures copyright Xiaoxiao Guo, Satinder Singh, Honglak Lee, Richard Lewis, and Xiaoshi Wang, 2014. Reproduced with permission.

## Arts



Original Image: Haight-Ashbury, San Francisco, California, USA. CC0 public domain.



Starry Night: Vincent van Gogh, 1889. CC0 public domain.

Gatys et al., "Image Style Transfer using Convolutional Neural Networks", CVPR 2016

Gatys et al., "Controlling Perceptual Factors in Neural Style Transfer", CVPR 2017

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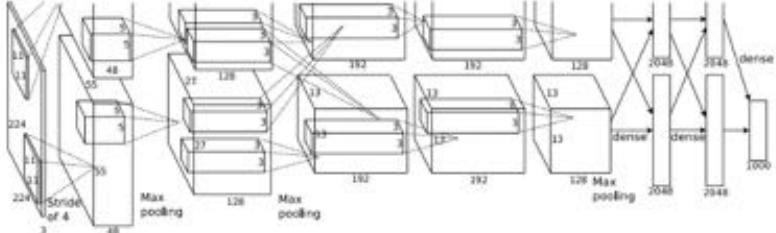
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## AlexNet in details



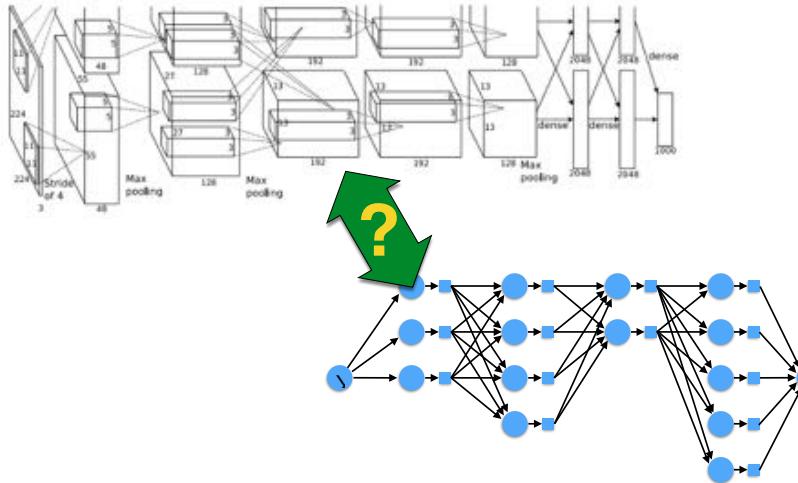
A Krizhevsky, et. al. ImageNet Classification with Deep Convolutional Neural Networks. NIPS 2012.

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## AlexNet in details

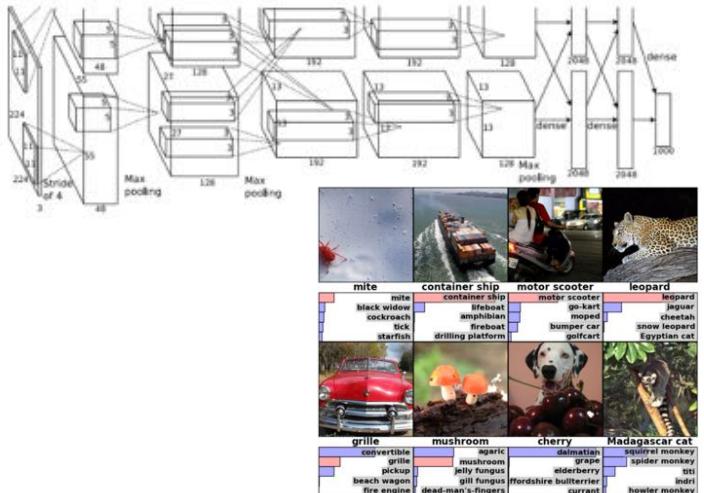


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## AlexNet in details



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## AlexNet in details



Image



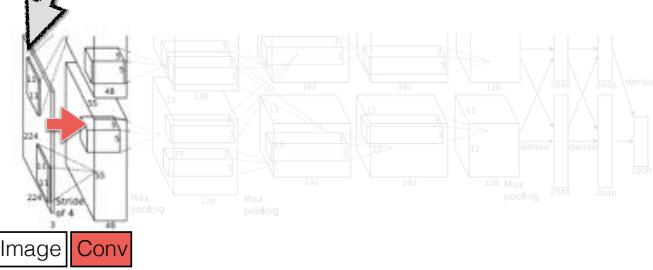
PC: Daniel Yang

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## AlexNet in details

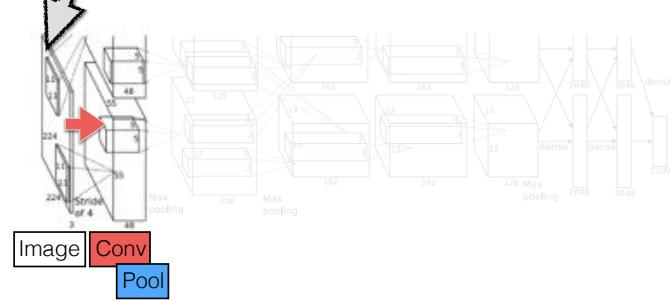


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## AlexNet in details

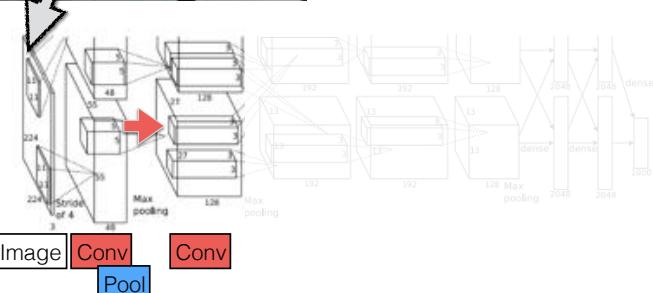


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## AlexNet in details

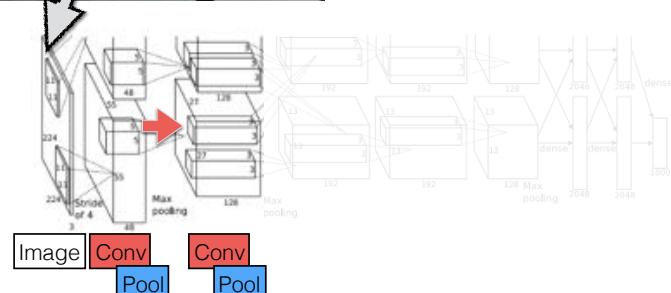


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## AlexNet in details

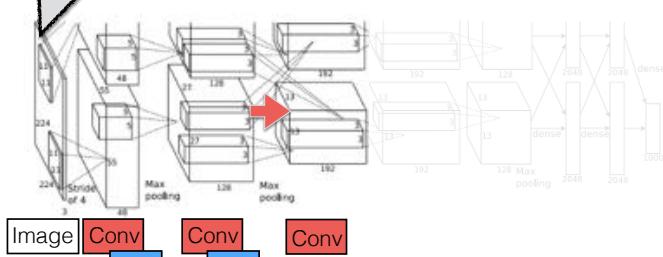


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## AlexNet in details

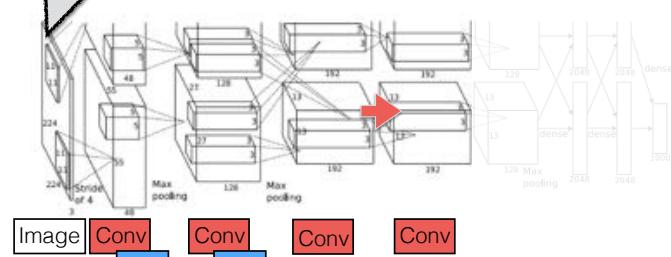


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## AlexNet in details

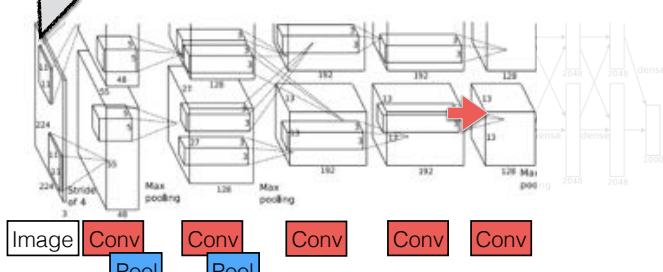


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## AlexNet in details

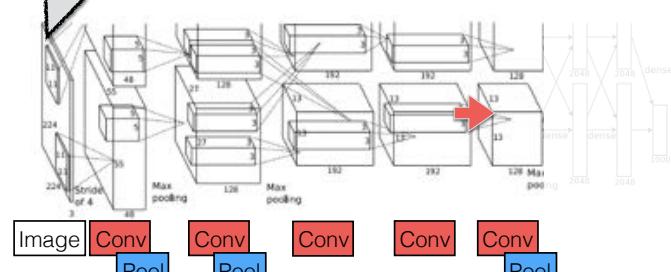


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## AlexNet in details

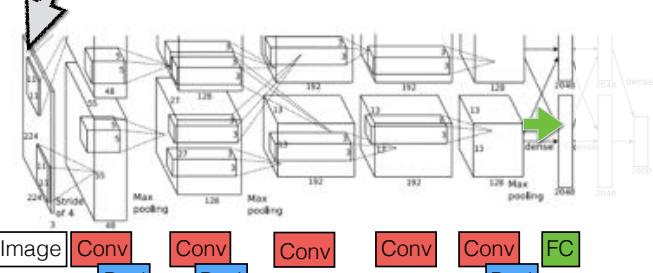


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## AlexNet in details

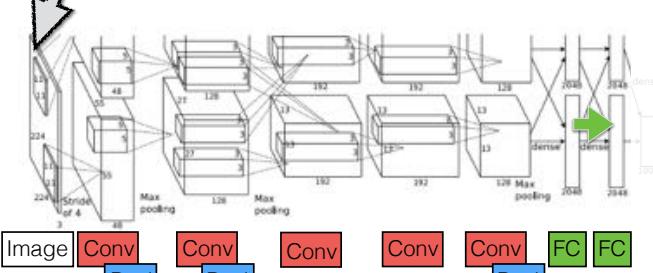


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## AlexNet in details

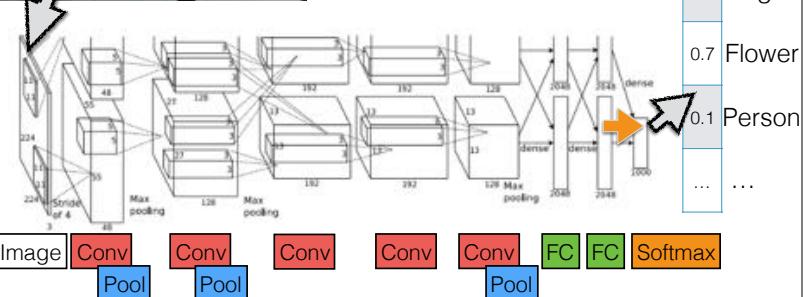


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## AlexNet in details

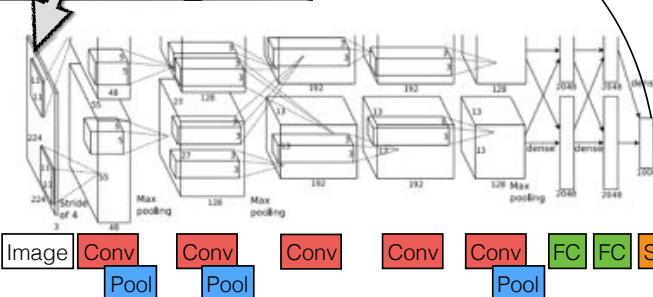


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## AlexNet in details



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## What are these layers?

- Convolutional layer 
- Pool layer 
- Fully connected layer 
- Softmax layer 

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## What are these layers?

- Convolutional layer 
- Pool layer 
- Fully connected layer 
- Softmax layer 

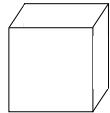
Layer = Function

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## Fully connected layer (FC)



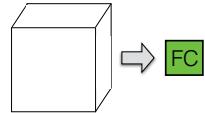
$M \times N \times P$

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## Fully connected layer (FC)



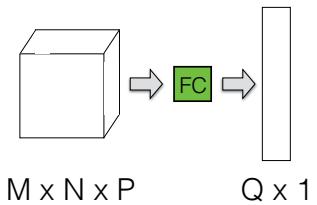
$M \times N \times P$

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## Fully connected layer (FC)

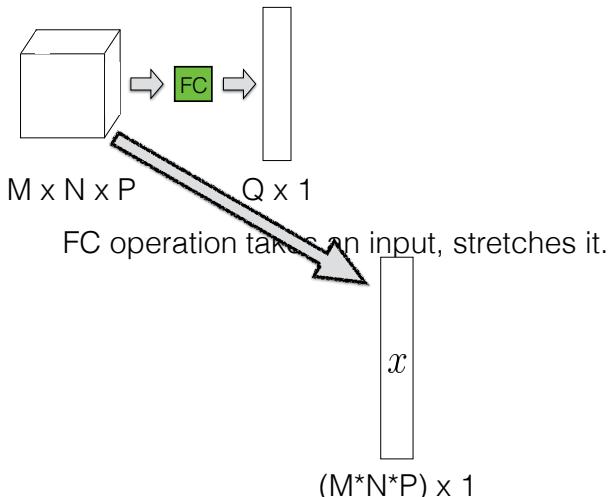


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## Fully connected layer (FC)

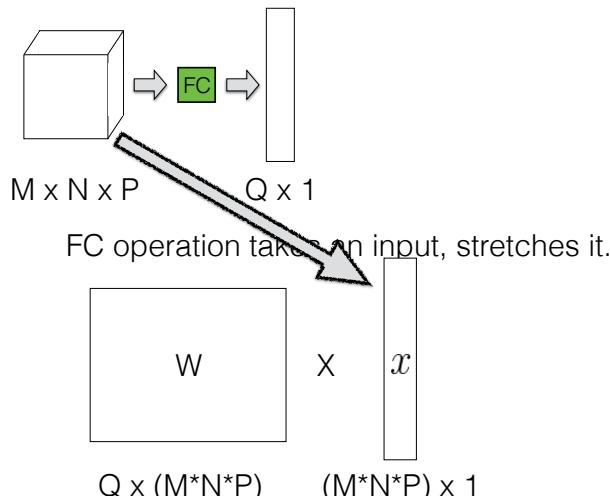


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## Fully connected layer (FC)

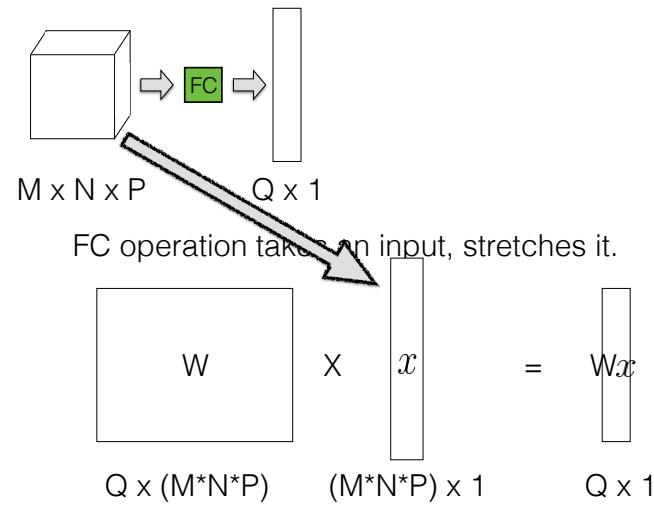


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## Fully connected layer (FC)

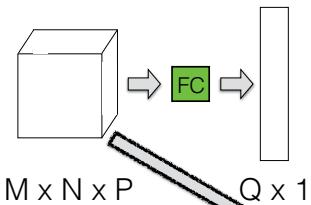


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## Fully connected layer (FC)



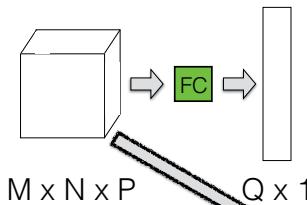
$$\begin{matrix} W \\ \text{Learned} \end{matrix} \quad \times \quad \begin{matrix} x \\ (M^*N^*P) \times 1 \end{matrix} \quad = \quad \begin{matrix} Wx \\ Q \times 1 \end{matrix}$$

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## Fully connected layer (FC)



$$\begin{matrix} W \\ \text{Learned} \end{matrix} \quad \times \quad \begin{matrix} x \\ (M^*N^*P) \times 1 \end{matrix} \quad = \quad \begin{matrix} Wx \\ Q \times 1 \end{matrix}$$

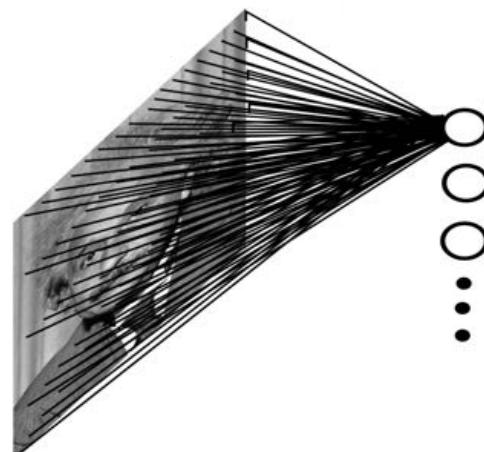
Why is this called FC?

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## Fully connected layer (FC)



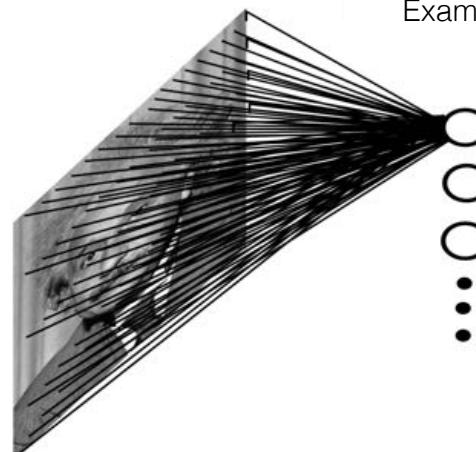
Slide credit: Marc'Aurelio Ranzato

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## Fully connected layer (FC)



Example: 200x200 image

Slide credit: Marc'Aurelio Ranzato

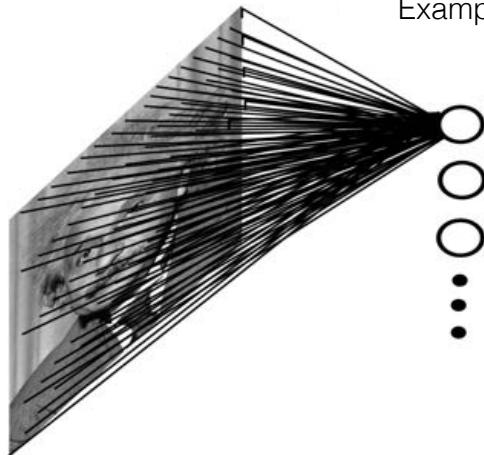
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## Fully connected layer (FC)

Example: 200x200 image  
40k hidden units



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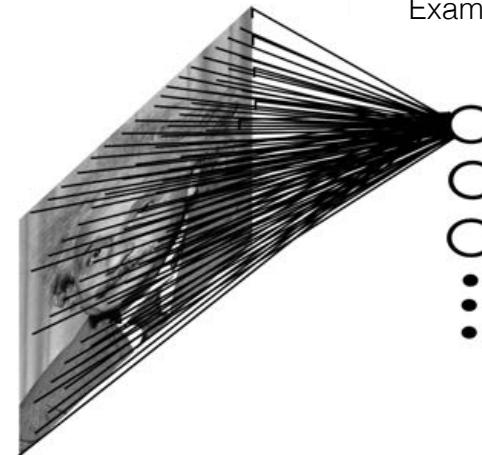
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Slide credit: Marc'Aurelio Ranzato

## Fully connected layer (FC)

Example: 200x200 image  
40k hidden units  
**~2B parameters!!!**

Why?



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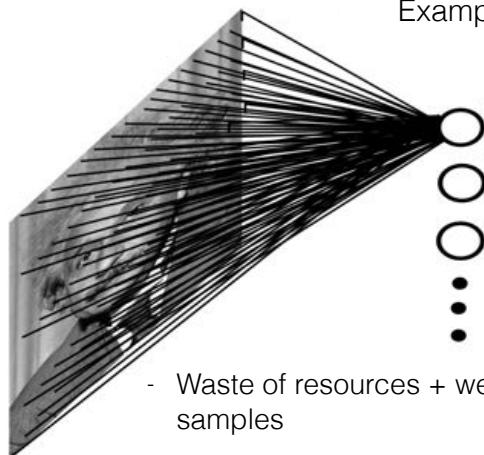
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Slide credit: Marc'Aurelio Ranzato

## Fully connected layer (FC)

Example: 200x200 image  
40k hidden units  
**~2B parameters!!!**



- Waste of resources + we have not enough training samples

Slide credit: Marc'Aurelio Ranzato

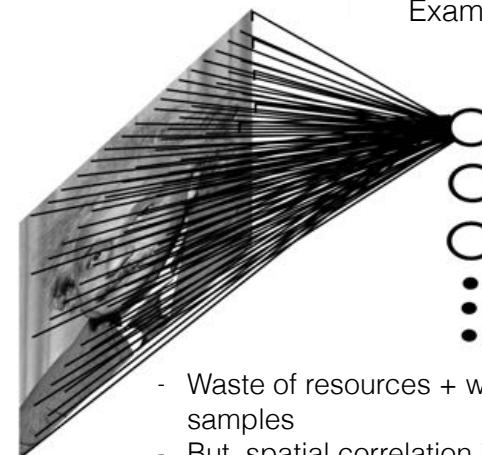
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## Fully connected layer (FC)

Example: 200x200 image  
40k hidden units  
**~2B parameters!!!**



- Waste of resources + we have not enough training samples
- But, spatial correlation is local!

Slide credit: Marc'Aurelio Ranzato

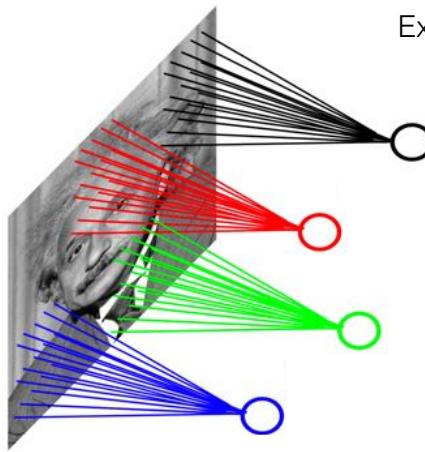
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## Locally connected layer

Example: 200x200 image  
40k hidden units  
Filter size: 10x10



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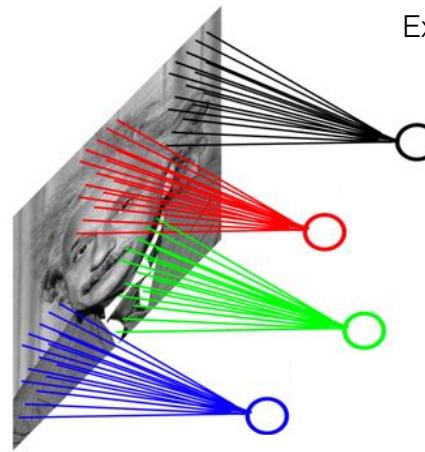
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Slide credit: Marc'Aurelio Ranzato

## Locally connected layer

Example: 200x200 image  
40k hidden units  
Filter size: 10x10  
**4M parameters**



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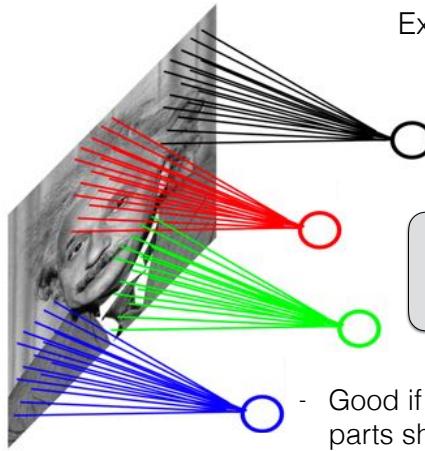
Slide credit: Marc'Aurelio Ranzato

## Locally connected layer

Example: 200x200 image  
40k hidden units  
Filter size: 10x10  
**4M parameters**

What can we do?

- Good if images are registered (i.e. parts show up at the same locations)



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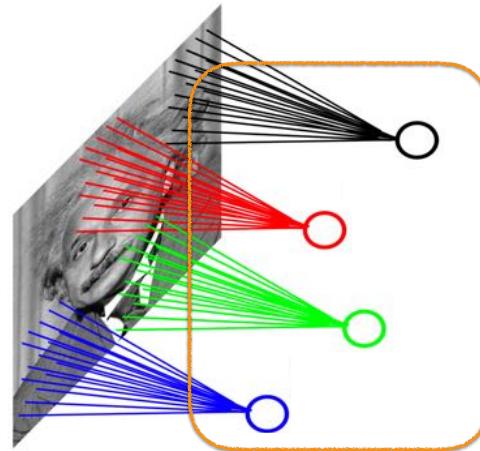
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## Locally connected layer

Share all local weights



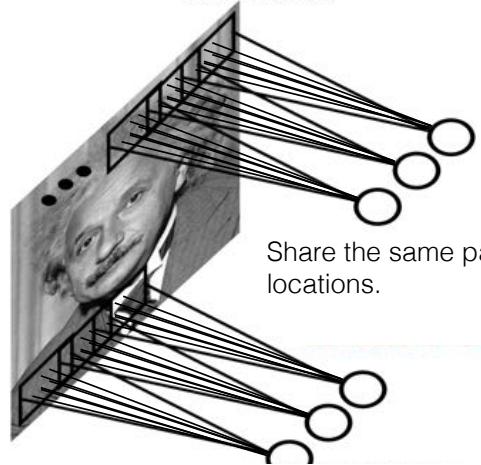
Slide credit: Marc'Aurelio Ranzato

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## Convolutional layer



Share the same parameters across different locations.

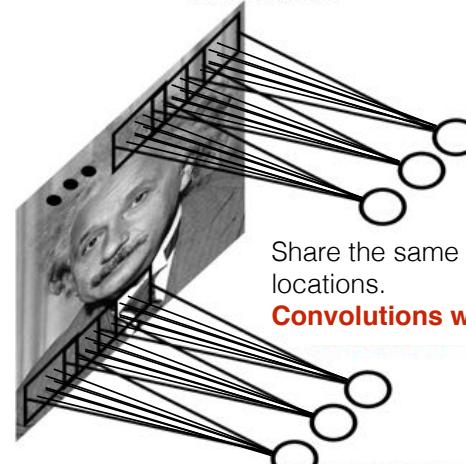
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## Convolutional layer



Share the same parameters across different locations.

**Convolutions with learned kernels (weights)**

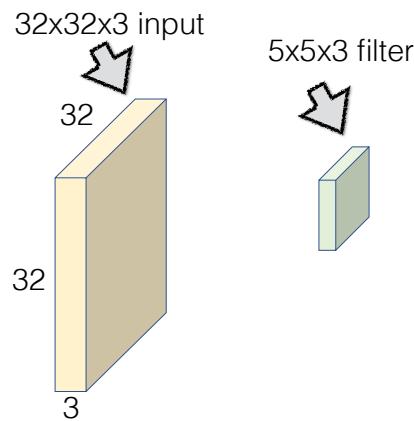
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Slide credit: Marc'Aurelio Ranzato

## Convolutional layer



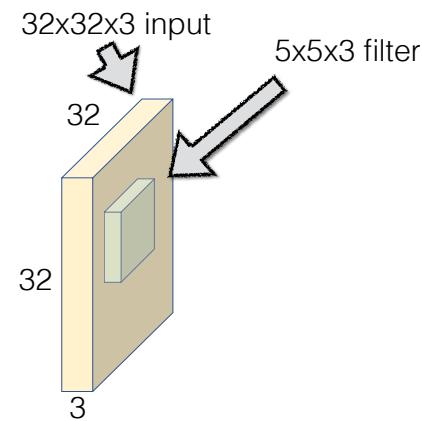
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## Convolutional layer



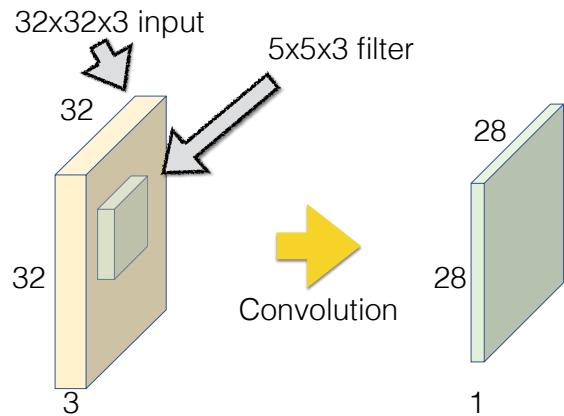
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Slide credit: CS 231N

## Convolutional layer



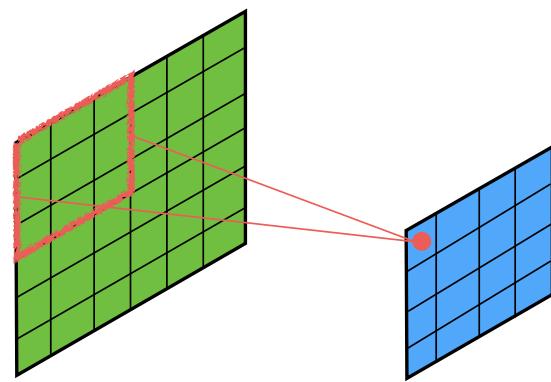
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## Convolution?

## Convolutional layer



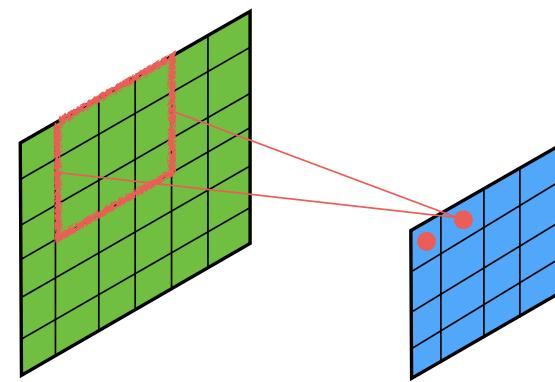
Inspired by Marc'Aurelio Ranzato's slides

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## Convolutional layer



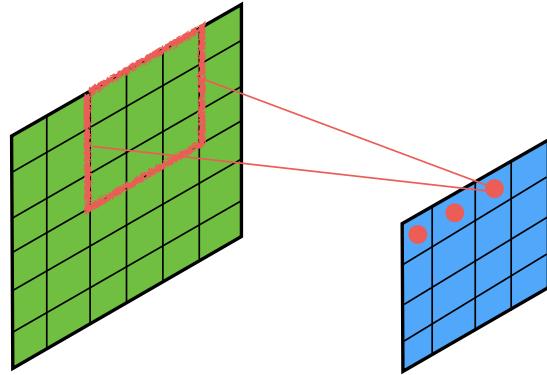
Inspired by Marc'Aurelio Ranzato's slides

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## Convolutional layer



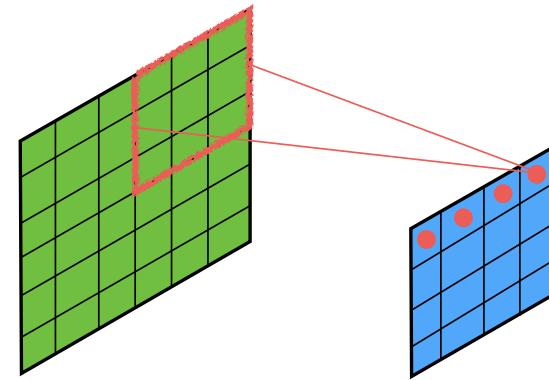
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## Convolutional layer



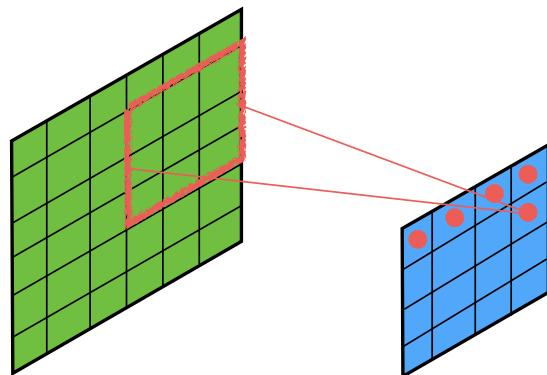
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## Convolutional layer



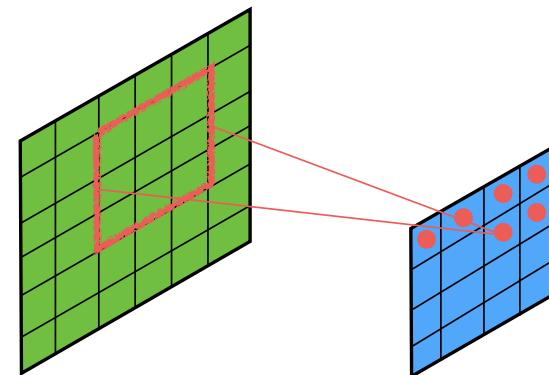
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Inspired by Marc'Aurelio Ranzato's slides

## Convolutional layer



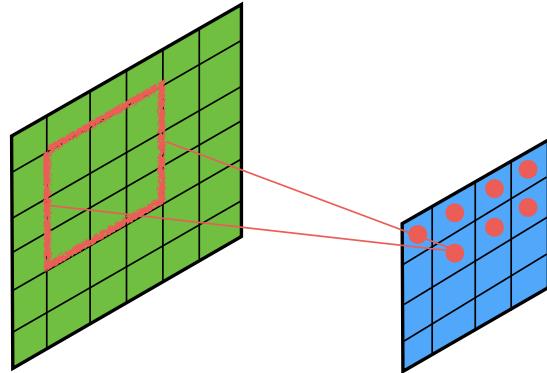
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## Convolutional layer



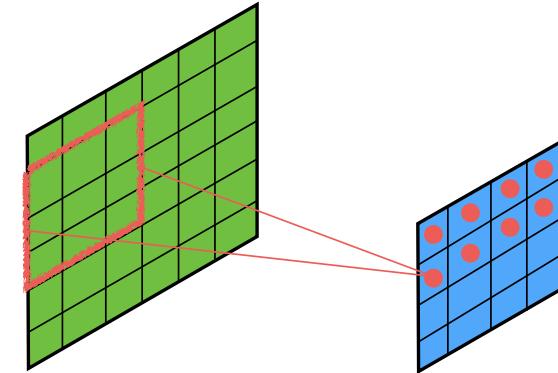
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## Convolutional layer



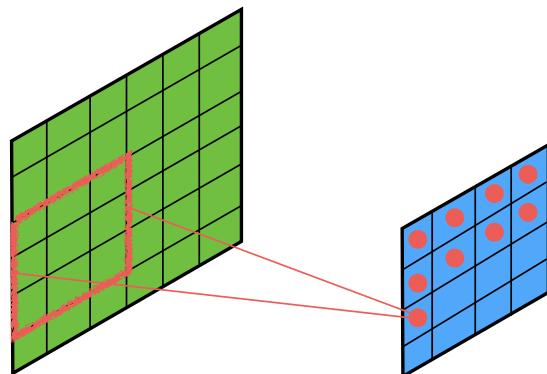
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## Convolutional layer



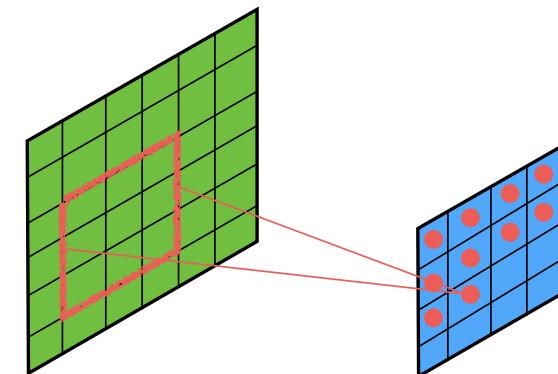
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## Convolutional layer



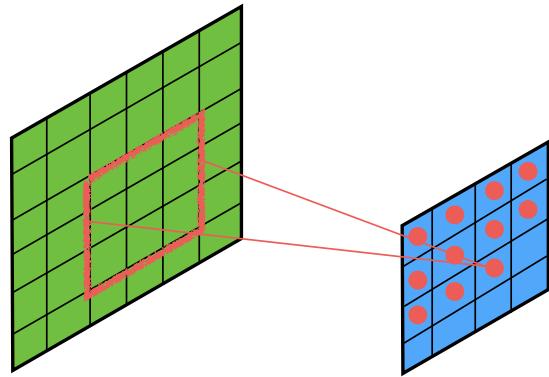
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## Convolutional layer



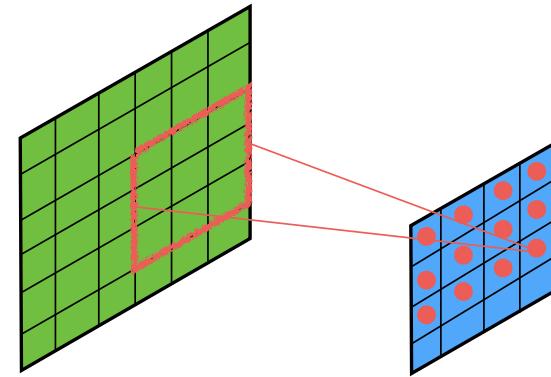
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## Convolutional layer



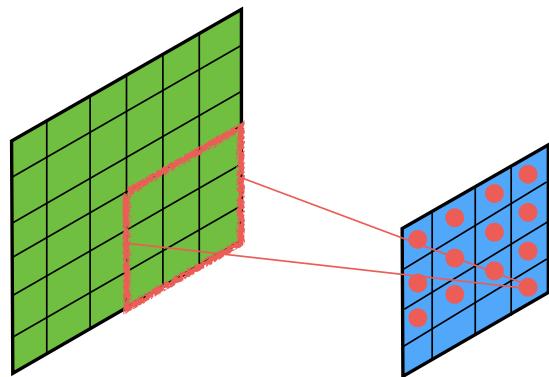
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## Convolutional layer



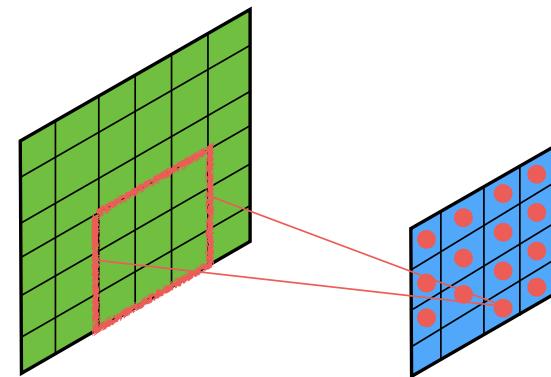
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## Convolutional layer



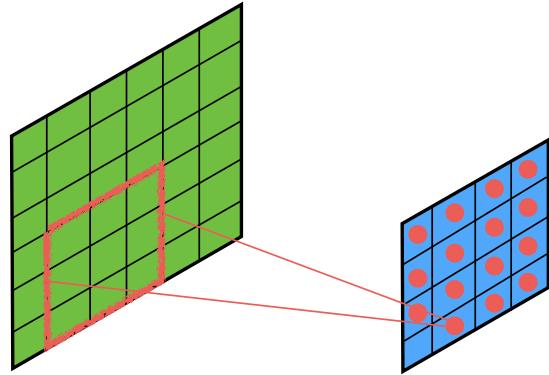
Inspired by Marc'Aurelio Ranzato's slides

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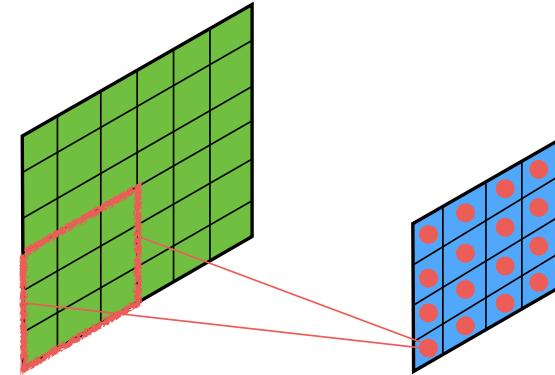
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## Convolutional layer



## Convolutional layer



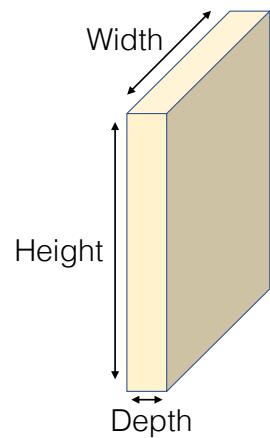
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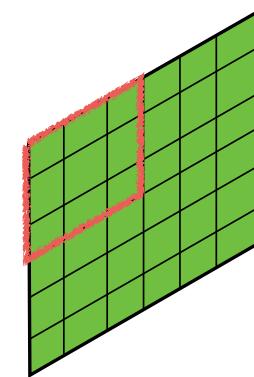
Lecture 4

Inspired by Marc'Aurelio Ranzato's slides

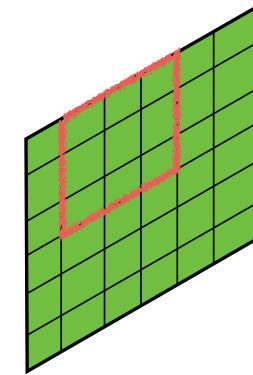
## Terminologies



## Terminologies



Stride 1



Step 2

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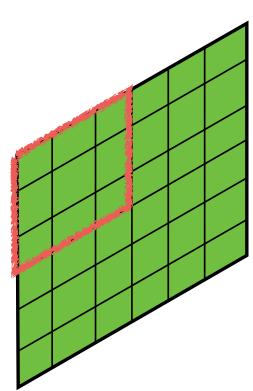
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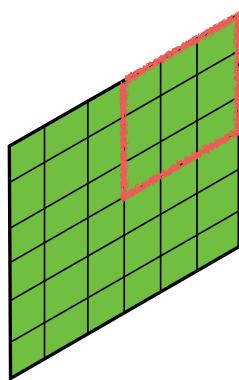
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## Terminologies



Step 1



Stride 3

Step 2

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## Terminologies

a	b	c	d	e
f	g	h	i	j
k	l	m	n	o
p	q	r	s	t
u	v	w	x	y

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## Terminologies

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	a	b	c	d	e	0	0	0
0	0	f	g	h	i	j	0	0	0
0	0	k	l	m	n	o	0	0	0
0	0	p	q	r	s	t	0	0	0
0	0	u	v	w	x	y	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

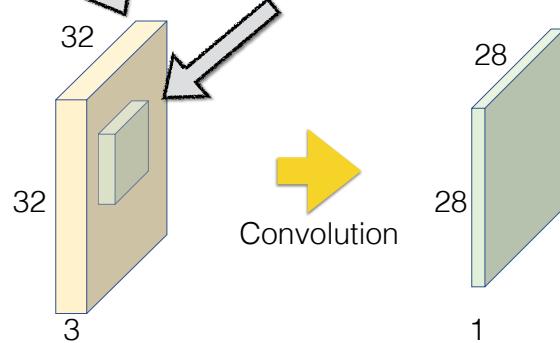
Zero-padding: 2

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## Convolutional layer

32x32x3 input

5x5x3 filter



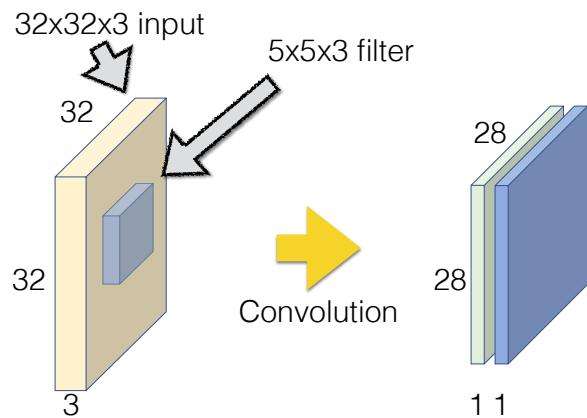
Slide credit: CS 231N

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## Convolutional layer



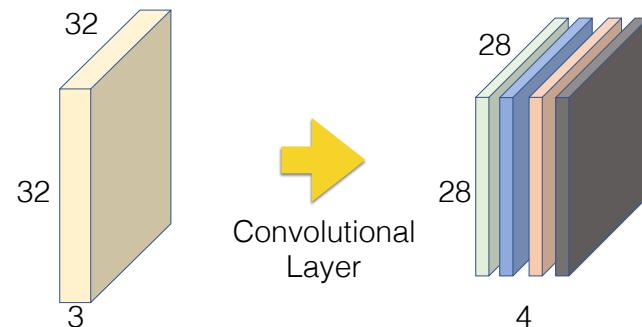
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## Convolutional layer

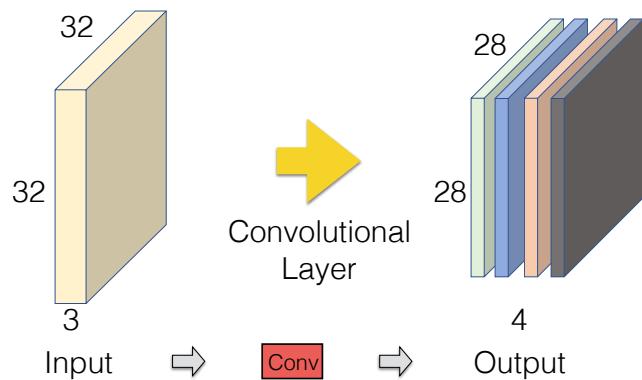
With 4 5x5x3 filters, we will get 4 activation outputs.  
Hence, the final output is 28x28x4.



Slide credit: CS 231N  
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## Convolutional layer

With 4 5x5x3 filters, we will get 4 activation outputs.  
Hence, the final output is 28x28x4.

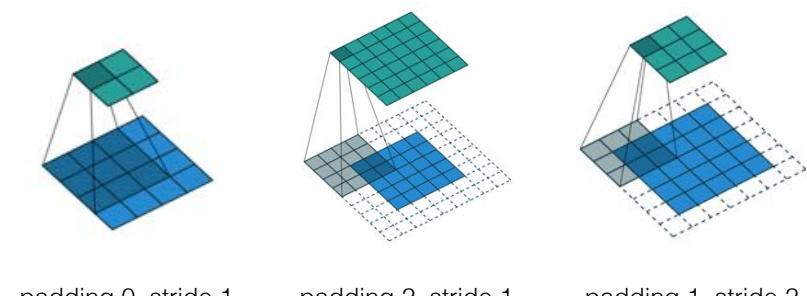


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## Convolutional layer



Note: it can have **depth** (3rd dimension).

Image credit: vdumoulin (github): [https://github.com/vdumoulin/conv\\_arithmetic](https://github.com/vdumoulin/conv_arithmetic)

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# Deconvolutional layer

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# Deconvolutional layer

Warning: this is not about **de**-convolution!

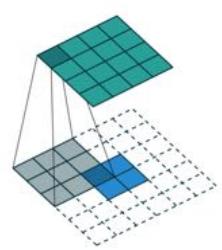
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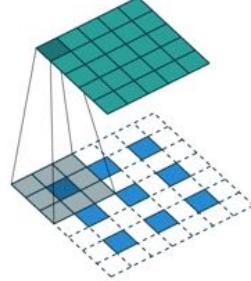
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# Deconvolutional layer

Warning: this is not about **de**-convolution!



padding 0, stride 1



padding 1, stride 1

Why do we need this?

Image credit: vdumoulin (github): [https://github.com/vdumoulin/conv\\_arithmetic](https://github.com/vdumoulin/conv_arithmetic)

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# Fully connected vs Convolutional

- Fully connected layer
- Locally connected layer
- Convolutional layer
- Which layer is the best? Why?

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## What are these layers?

- Convolutional layer
- Pool layer
- Fully connected layer
- Softmax layer

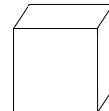


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## Max pooling layer



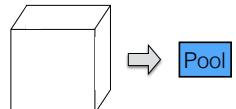
$M \times N \times P$

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## Max pooling layer



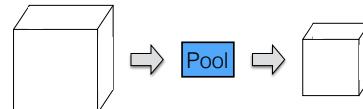
$M \times N \times P$

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## Max pooling layer



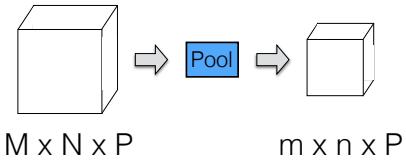
$M \times N \times P$        $m \times n \times P$

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## Max pooling layer



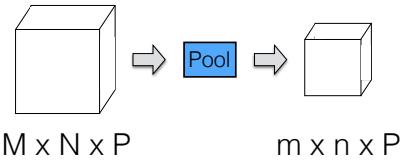
- Shrinks the feature smaller (compact + manageable)

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Slide credit: CS 231N  
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## Max pooling layer



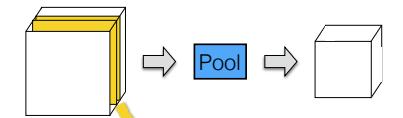
- Shrinks the feature smaller (compact + manageable)
- Each activation map (3rd dim) is handled separately

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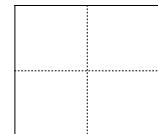
Slide credit: CS 231N  
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## Max pooling layer

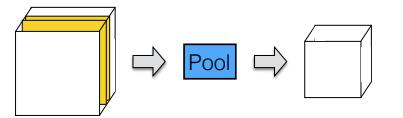


1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2

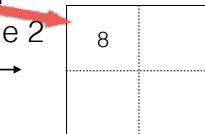


## Max pooling layer



1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2



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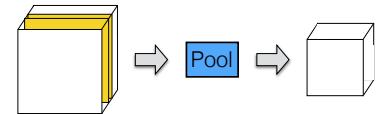
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## Max pooling layer



$M \times N \times P$        $m \times n \times P$

1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2

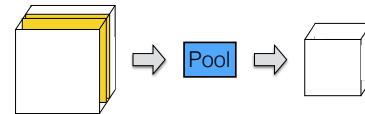
8	7
---	---

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## Max pooling layer



$M \times N \times P$        $m \times n \times P$

1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2

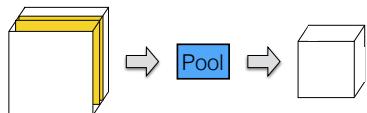
8	7
8	

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## Max pooling layer



$M \times N \times P$        $m \times n \times P$

1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2

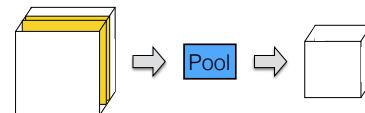
8	7
8	9

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## Max pooling layer



$M \times N \times P$        $m \times n \times P$

1	3	2	7	2
5	1	3	0	5
4	8	5	0	6
3	2	6	0	8
0	7	4	6	9

max pool with  
3x3 filters & stride 2

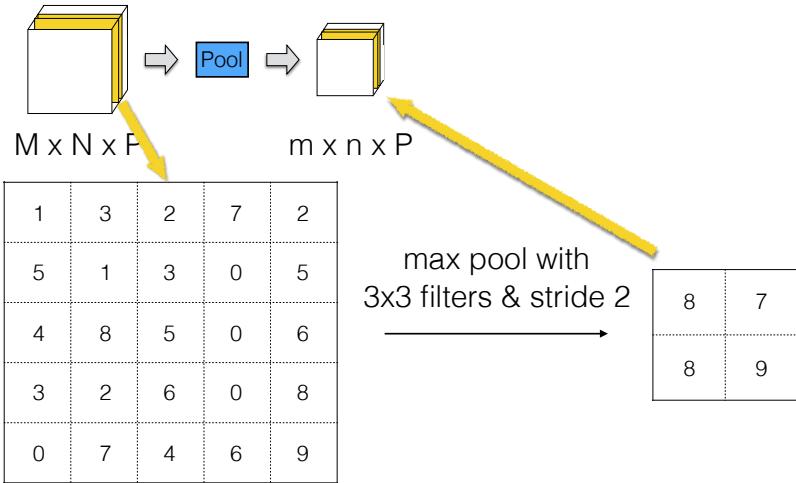
8	7
8	9

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## Max pooling layer



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## Pooling layers

- **Max pooling** (most common)
- Average pooling
- L2-norm pooling
- ...

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## Why pooling layers?

## Why pooling layers?

- Reduces # of parameters in the following layers

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## Why pooling layers?

- Reduces # of parameters in the following layers
  - Hence, less overfitting!

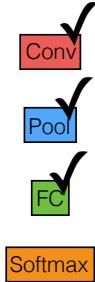
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## What are these layers?

- Convolutional layer
- Pool layer
- Fully connected layer
- Softmax layer



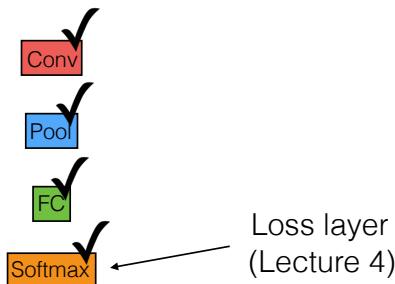
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## What are these layers?

- Convolutional layer
- Pool layer
- Fully connected layer
- Softmax layer



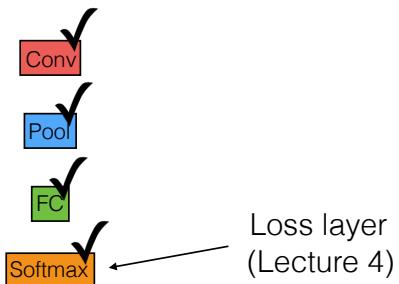
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**All these are linear!!!**

- Convolutional layer
- Pool layer
- Fully connected layer
- Softmax layer

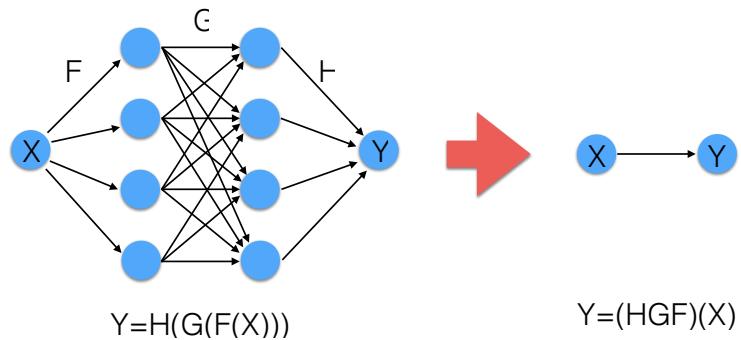


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## Activation functions



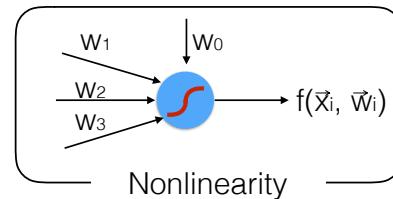
Without nonlinear activation,  
multiple layers are reduced to one matrix multiplication.

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## Activation functions



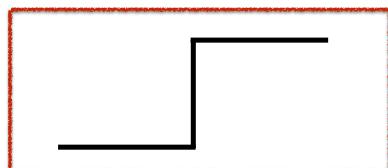
Nonlinearity makes a neural network deeper

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## Step function



- Firing after a threshold
- Is not differentiable
- Cannot apply back-propagation

Anything else we can use?

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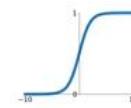
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## Activation functions

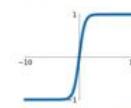
### Sigmoid

$$\sigma(x) = \frac{1}{1+e^{-x}}$$



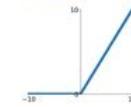
### tanh

$$\tanh(x)$$



### ReLU

$$\max(0, x)$$



### Leaky ReLU

$$\max(0.1x, x)$$



### Maxout

$$\max(w_1^T x + b_1, w_2^T x + b_2)$$

### ELU

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

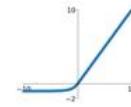


Figure from Stanford cs231n lecture slides

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## Activation functions

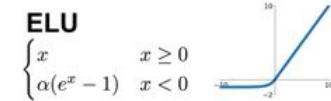
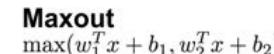
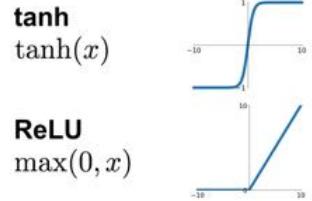
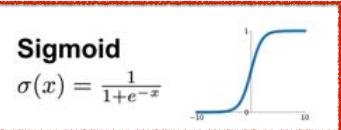


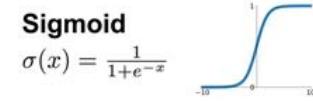
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## Sigmoid



- Similar to step functions, but differentiable
- (-) easily saturated (no gradients)

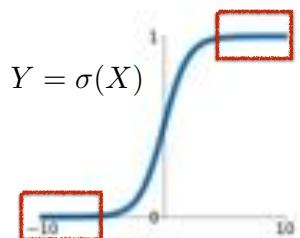
Figure from Stanford cs231n lecture slides

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## Gradient vanishing problem



Chain rule  
$$\frac{\partial Y}{\partial X} = \frac{\partial Y}{\partial \sigma} \cdot \frac{\partial \sigma}{\partial X}$$

is almost 0 for most of X

Thus,  $\frac{\partial Y}{\partial X}$  also goes to 0.

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## Activation functions

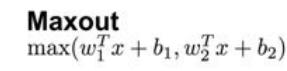
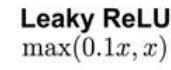
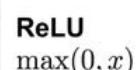
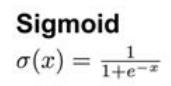


Figure from Stanford cs231n lecture slides

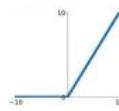
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## ReLU

**ReLU**  
 $\max(0, x)$



- Prevent gradient vanishing when  $x > 0$
- Computationally efficient
- Biologically plausible
- (-) Still loose gradient when  $x < 0$

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## Activation functions

**Sigmoid**

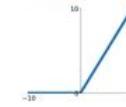
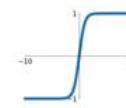
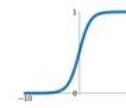
$$\sigma(x) = \frac{1}{1+e^{-x}}$$

**tanh**

$$\tanh(x)$$

**ReLU**

$$\max(0, x)$$



**Leaky ReLU**  
 $\max(0.1x, x)$

**Maxout**  
 $\max(w_1^T x + b_1, w_2^T x + b_2)$

**ELU**

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$



Figure from Stanford cs231n lecture slides

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## Leaky ReLU/ELU

**Leaky ReLU**  
 $\max(\alpha x, x)$



**ELU**

$$\begin{cases} x & x \geq 0 \\ \alpha(e^x - 1) & x < 0 \end{cases}$$

- No gradient vanishing problem
- Can be used instead of ReLU (e.g. Leaky ReLU for deconvolution)

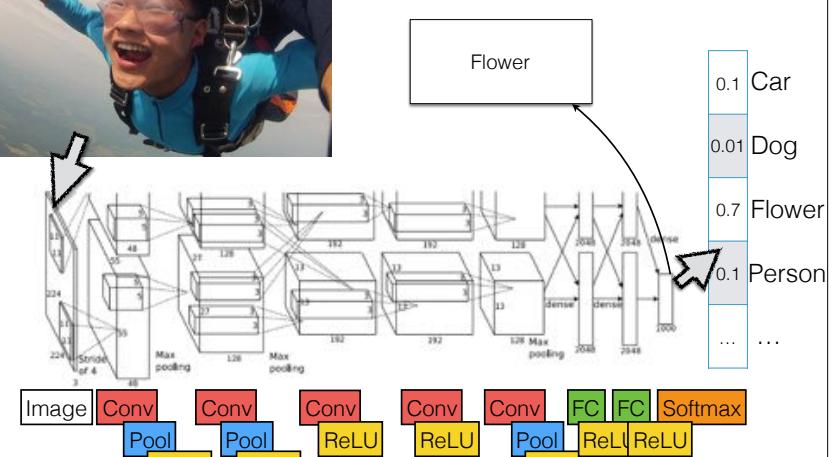
Figure from Stanford cs231n lecture slides

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## AlexNet in details



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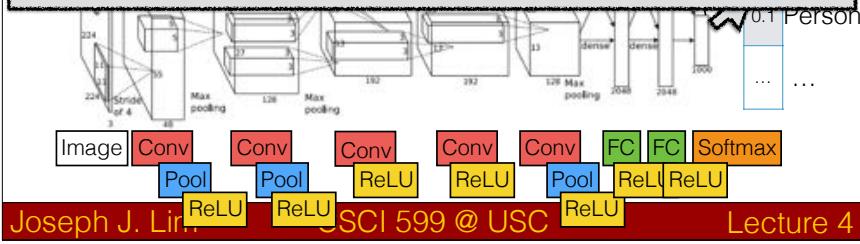
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## AlexNet in details



0.1 Car

Typically omit ReLU for the visualization



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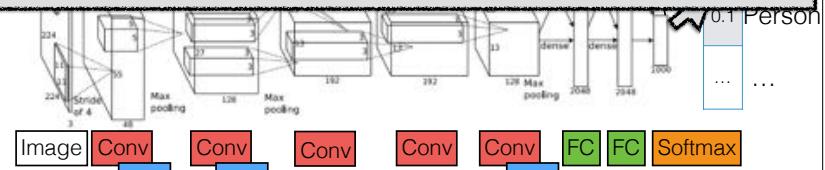
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## AlexNet in details



0.1 Car

Typically omit ReLU for the visualization

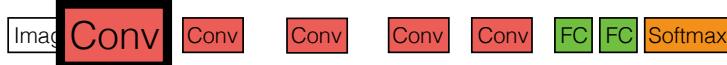


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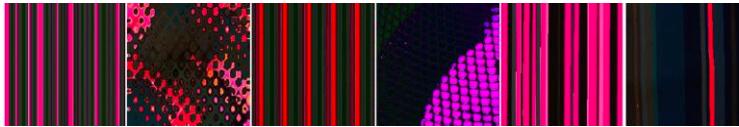
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## What did AlexNet learn?



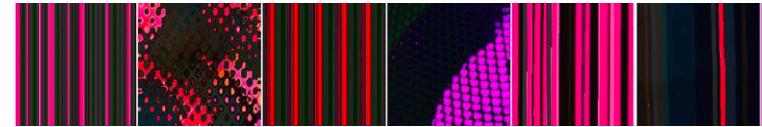
red



## What did AlexNet learn?



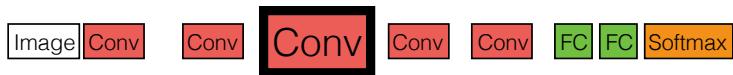
red



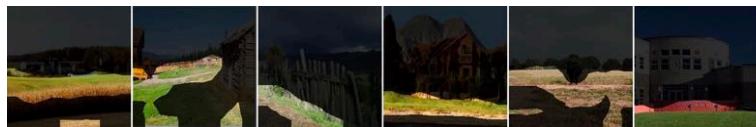
blue



## What did AlexNet learn?



grass



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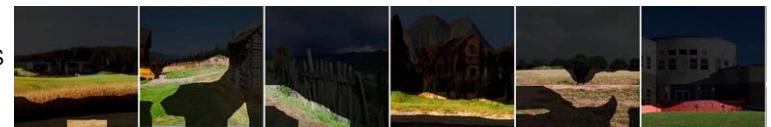
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Bau, Zhou, and et. al. Network Dissection: Quantifying Interpretability of Deep Visual Representations. CVPR 2017.

## What did AlexNet learn?



grass



sky



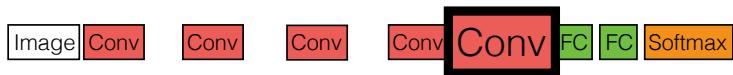
Bau, Zhou, and et. al. Network Dissection: Quantifying Interpretability of Deep Visual Representations. CVPR 2017.

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## What did AlexNet learn?



dog



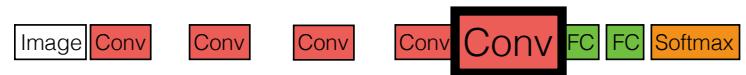
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Bau, Zhou, and et. al. Network Dissection: Quantifying Interpretability of Deep Visual Representations. CVPR 2017.

## What did AlexNet learn?



dog



cat



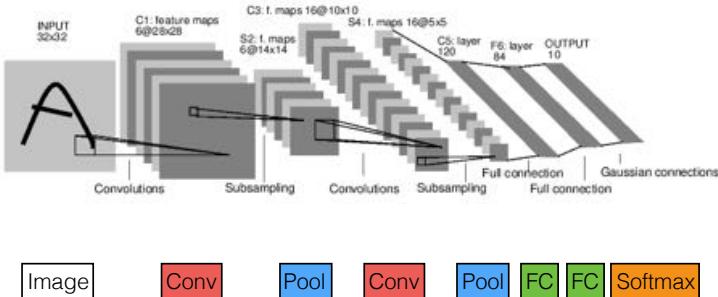
Bau, Zhou, and et. al. Network Dissection: Quantifying Interpretability of Deep Visual Representations. CVPR 2017.

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## CNNs: LeNet



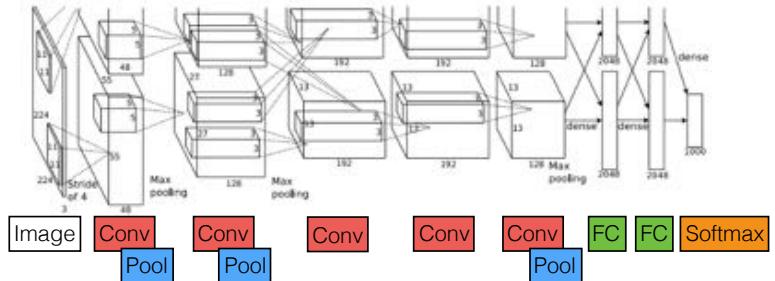
LeCun et. al. Handwritten digit recognition: Applications of neural net chips and automatic learning. IEEE Communication 1989.

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## CNNs: AlexNet



A Krizhevsky, et. al. ImageNet Classification with Deep Convolutional Neural Networks. NIPS 2012.

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## What made AlexNet AlexNet?

- GPU?
- Data?
- ReLU?
- Convolutional?
- Hyperparameter?

## CNNs: VGGNet



Simonyan and Zisserman. Very Deep Convolutional Networks for Large-scale Image Recognition. ICLR 2015.

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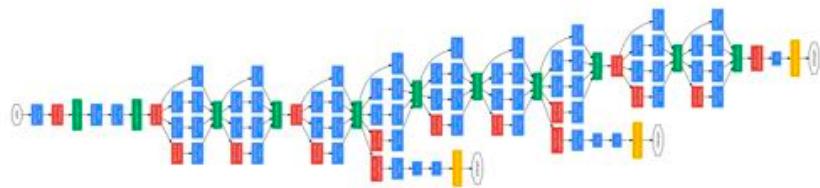
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## CNNs: GoogLeNet



Szegedy, et. al. Going Deeper with Convolution. CVPR 2015.

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## CNNs: ResNet



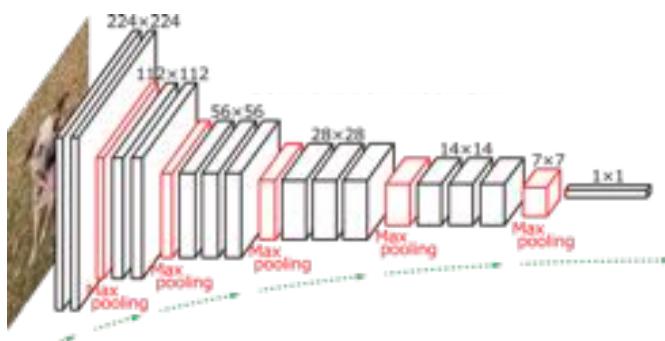
He, et. al. Deep **Residual** Learning for Image Recognition. CVPR 2016.

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## Encoder



Encoding (into a feature / representation)

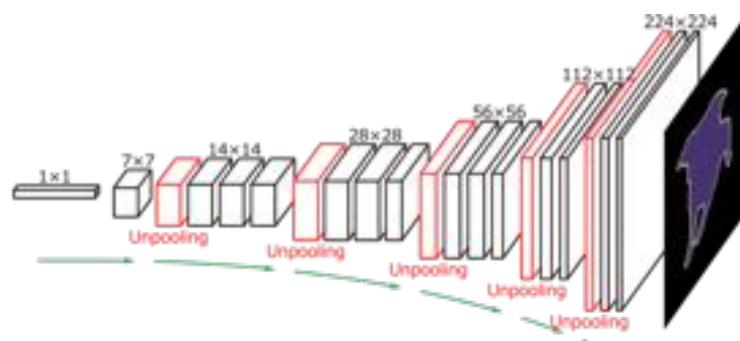
Image credit: Noh, et. al. Learning Deconvolution Network for Semantic Segmentation. ICCV 2015.

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## Decoder



Decoding (from a feature / representation)

Image credit: Noh, et. al. Learning Deconvolution Network for Semantic Segmentation. ICCV 2015.

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Congratulations!

All basic vocabs are covered.