## BAILKEZ IDLOTHTEZ ONOMOPQON ZYNAPTHSEON

1. Thourantoipeva

Optopos 1.1. Even I CIR avoikto
stavenpa, y: I > C 51 to EI.

It of réjecon diapopionin orco to

arr of ourapaioris u=Ref V=Imf Eiral Magagnyion (185 600 to.

Z'augh Env Trépitrouon jea éou pre

p'(to) = u'(to) + iv'(to).

Or stabobiothes omobeloss ens

hoppins p(t) = u(t)+iv(t) teI (IER avoiked diagram/ca)

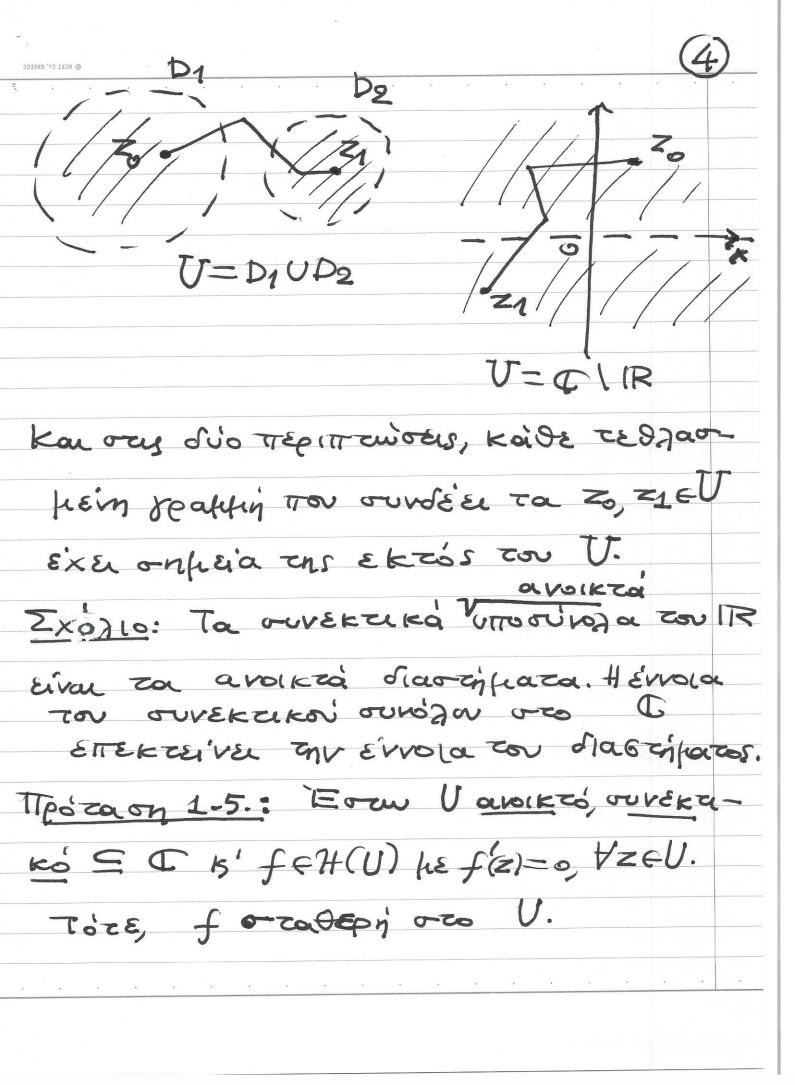
EXOUN O'JES ES LOIDENTES HON E'XONN

OL Trapajujionnes ouvaptions main

OE sias in paral, EKTOS allo To O. Rolle

TT-x.  $\Psi(t)=e^{it}$ ,  $t\in [0,2\pi]$  (2) \$(0) = \$\p(\gamma\text{tr}) = 1 appai \p(\text{t}) = ieit\frac{7}{29} ₩t∈ (0,2π). Maparenenon 1.2. Ear Pet = u(t) + iv(t) teI, suggestioning orco I hexp(t)=0, YtEI, Tôce y= oradepi 6 to I. Thathaci a and the webittemen, u'(t)=v'(t)=0, t∈I → u, vorca dep e's
orco I. πρόταση 1.3. Εστω UST αγοικτό, f:U + to ) o poppen 15' q: I > U scapop.
(I SIR avolked). Total, d [f(p(t))] = f'(p(t))p'(t), te] Even Zo, Z1 E C. To sud. Epinfia ke apxil to Zo 5' Trépas to Z1 Eivan [20,21]={A-t)zo+tz1 { te[0,1]}

4	
	Optopos 1.4. Evan US Carotko.
	To U référan ouvékaro aux tzo, z EU
	F TED ANGEN SCAPIN TEN
	ousse za zo, z <sub>1</sub> .
	TT.X. Za Tropaka'an oringa sivar ovekerka.
	U= C L(-00,0]
	Ta Hagakairon orinda der eivan



## Anodesty:

Loxuplohos: Ear Zo, ZIEU he [zo, Z] CU,

Tote y feivar orantepin oran [zo, z1]

[Trajpace +te (0,1),

 $\frac{d}{dt}\left[f(n-t)z_0+tz_1)\right] =$ 

 $= f'((1-t)z_1+tz_1)\cdot \frac{d}{dt}[(1-t)z_1+tz_1]$ 

= f'((1-t)z+tz1). (z1-z0)=0, apoi

f'=0, 000 U.]

Evru ruiga Zo, ZI EU. Epidoor U

ruvekziko, 7 zedzaopén jeappin TeV
pe kopupés

 $J_0=Z_0, J_1, J_2, \cdots, J_{n-1}, J_n=Z_1(n)$ 

 $Z_0 = J_0$   $J_3$   $Z_1 = J_0$ 

Nojur zou lo xuploqueri, y f sivar o ca depir 6 zo di a o cripica ca [Zo, 71], [J1, J2], ..., [Jn-2, Jn-1],  $[J_{n-1}, Z_{1}].$ Apa,  $f(z_{0}) = f(J_{1}), f(J_{1}) = f(J_{2}), \cdots$  $f(J_{n-2}) = f(J_{n-1}), f(J_{n-1}) = f(z_1)$ => f(20)=f(21), 4 20, 21 EU. Enopeins, foratepi. Σχόλιο: Η συνεκτικότητα του υστην
Τζούταση 1.5 <u>σεν μπορεί να παρ</u>α-- Deredei jevika. TT.x. D1 = {zec | 121<1}, D= {zec | 121>2}, U= DIUDZ. To U sivai avoikes, fin ourskaks.

O suporps on our openion f:U > C he  $f(z) = \begin{cases} 1, & z \in D_1 \\ 0, & z \in D_2 \end{cases}$ ffH(V), f'-0,000 U &'f hy oradepi.

Opiopos 1-6. Tredio oro C, sivar sivar avoikto, ouvektiko oviono EC. Trocaon 1.7: Even UE C TESio 5' feH(U). Loxiour contraparaion: (i) Eav Ref ή Imf σταθερή, τότε f σταθερή. (ii) Eav f = H(V), τότε f σταθερή. (iii) Ear Ifloradepy, zòce foradepy. ATTÓ SEFN: (i) u= Ref v= mf. As unoteoroupe of u = 6 contepy. Total,  $u_{x} = u_{y} = 0$ , or 0 U. And our sikes (C-R) to air vorte  $V_{x} = -u_{y} = 0$ , or 0 U=> f'= ux+ivx=0,000 U (TPOZ.1.5) o catepy. [Opola, av V 6 coldepy.] (ii)  $\overline{f} = u - iv$ , u = Ref, v = lmf(E-R) pa env f: ux=vy uy=-vx E-R 1 (1) 4 F: U=-Vy, uy=Vx.

ETTE con o'ce ux = 1x = 0 >> f = 0,000 U (Teòt. 1-5) f=ocateph.

(iii) Eou If = c= oradepn ∈ [0,+0). · av C=0, zòze f=0,000 U. · E6 eu òze C \( \forall \). Tòze, \( \text{ZFU}, [f(z)|2=c2 ⇒ f(z):f(z)=c2 => f(z) = c2, HZEU > f = H(U) (ii) of GEOGEPH. Arknon 1: Fran UE OTERIO 15feH(U). f = 6 con 0 epn. Amodersy: (i) (ef) =0  $\Rightarrow$  f!ef=0  $\Rightarrow$  f=0,000 U  $\Rightarrow$  f=0tabeen. (ii) 0 s'au g=f2. Tôce, g'=2f.f'=0 Tore, If l= |g| = ICI => If l=VICI  $\Rightarrow |f| = 6 \cos \theta \cos \theta$  (TTP of . 1.7)  $f = 6 \cos \theta \cos \theta$ 

Aorenon 2: Even U ECT TESIO 5'

fige H(U) wore f(z)+g(z) eIR, YZEU. Na s.o. F CER f(z) = C+g(z), YZEV. And sufn: Os'en h=f-g. Tions, & ZEU, f(z)+g(z) = f(z)+g(z)=  $= f(z) + \overline{g(z)} = \overline{f(z)} + g(z)$  $\Rightarrow$   $h(z) = \overline{h(z)}, \forall z \in U \Rightarrow h, \overline{h} \in \mathcal{H}(U)$ TTEST. 1.5 h = c = 6 20 Epy - A729, C = 0 AGENON 3: Form US CITEDIO 5'  $f: U \to \mathbb{C}$  fua ouraigenon work  $f^3 \in \mathcal{H}(U)$ ,  $f^2 \in \mathcal{H}(U)$ . Na σ-0. f = caθερή.

Απόσειξη: f = (f3) 2 = H(V), F6 = (F2)3 ∈ H(U) (treoc.1.7) f = 6 table n. 1928 [fle=[te]= e copeén > |f|= 6000epi ⇒ 171= c >0. Total  $f^3 = G \in C$ ,  $|f^2| = |f|^2 = C^2$   $f^3 = G \in C$ ,  $|f^2| = |f|^2 = C^2$ 

⇒ C1= C2.f(z), \ZEU.

· Av (2 =0, coce f=0, oco U.

· Av (2 70, 20 28 f(z) = 9/(2, 424U.

Apa, f = ocatepi or kabe mepinton.

(+) Eivar  $\int_{-\infty}^{2} = 7 \left( U \right) \sin \left[ \int_{-\infty}^{2} \left[ - \sigma \cos \theta \right] \right]$ 

=> f2 = 6 carepy.

@ NEVI CO CREECE