Convolutional Neural Networks with Template-Based Data Augmentation for Functional Lung Imaging Segmentation

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Rationale and Objectives: We propose an automated segmentation pipeline based on deep learning for ventilation-based quantification which improves on previously proposed methods in terms of computational efficiency while maintaining accuracy and robustness. The large data requirements for the proposed framework is made possible by a novel template-based data augmentation strategy.

Materials and Methods: Convolutional neural network (i.e., U-net) models were generated using a custom multilabel Dice metric loss function and a novel template-based data augmentation strategy. Development and processing utilized *ANTsRNet*—a growing open-source repository of well-known deep learning architectures first introduced here which interfaces with the Advanced Normalization Tools (ANTs) package and the R statistical project. Training (including template generation and data augmentation) employed 500 images. Evaluation was performed on the remaining 1?? images through comparison with a previously reported automated segmentation algorithm based on Gaussian mixture modelling with Markov Random field (MRF) spatial priors.

Results:

Conclusions: The proposed deep learning framework yielded comparable results as the MRF-based algorithm. Such an approach reduces computational time without sacrificing accuracy.

Key Words: Advanced Normalization Tools, ANTsRNet, hyperpolarized gas imaging, neural networks, U-net

INTRODUCTION

Probing lung function under a variety of conditions and/or pathologies has been significantly facilitated by the use of hyperpolarized gas imaging and corresponding quantitative image analysis methodologies. Such developments have provided direction and opportunity for current and future research trends [1]. Computational techniques targeting these imaging technologies permit quantification of spatial ventilation with potential for increased reproducibility, resolution, and robustness over traditional spirometry and radiological readings [2, 3].

One of the most frequently used image-based biomarkers for the study of pulmonary development and disease is based on the quantification of regions of limited ventilation, also known as *ventilation defects* [4]. These features have been shown to be particularly salient in a clinical context, for example ventilation defect volume to total lung volume ratio has been shown to outperform other image-based features in discriminating asthmatics vs. non-asthmatics [5]. Ventilation defects have also demonstrated discriminative capabilities in chronic obstructive pulmonary disease (COPD) [6]. These findings, along with related research, has motivated the development of multiple automated (and semi-automated) segmentation algorithms which have been proposed in the literature [7–11] and are currently used in a variety of clinical research investigations (e.g., [12]).

Despite the enormous methodological progress with existing quantification strategies, recent developments in maching learning (specifically "deep learning" [13]) have generated new possibilities for quantification with improved capabilities in terms of accuracy, robustness, and computational efficiency. The outgrowth of research, in conjunction with advances in computational hardware, has resulted in significant developments in various image research areas including classification, segmentation, and object localization and has led to co-optation by the medical imaging analysis community [14].

In this work, we develop and evaluate a convolutional neural network segmentation framework, based on the U-net architecture [15], for functional lung imaging using hyperpolarized gas. As part of this framework we include a deep learning counterpart to earlier work from our group targeting segmentation of proton lung MRI [16]. This is motivated by common use case scenarious in which proton images are used for quantifying corresponding ventilation images (e.g., [7–9]).

One of the drawbacks to deep learning approaches are the large data requirements for the training process oftentimes necessitating ad hoc strategies for simulating additional data from available data—a process termed data augmentation [17]. While common approaches to data augmentation include the application of randomized simulated linear (e.g., translation, rotation and affine) or elastic transformations and intensity adjustments (e.g., brightness and contrast), we propose an approach tailored to medical imaging scenarios. In the proposed approach, an optimal shape-based template is constructed from a subset of the available data. Subsequent pairwise image registration between all training data and the resulting template permits a "pseudo-geodesic" transformation of each image to every other image thus converting a data set of size N to an augmented data set of size N^2 . In this way, transformations are constrainted to the shape space representing the population of interest.

To enhance relevance to the research community, we showcase this work in conjunction with the introduction of *ANTsRNet*—a growing open-source repository of well-known deep learning architectures which interfaces with the Advanced Normalization Tools (ANTs) package [18] and its interface with the R statistical project (i.e., ANTsR) [18]. This permits the public distribution of all code, data, and models which can be found on the GitHub repository corresponding to this manuscript [19]. This allows other researchers to apply the developed models and software to their data and/or use the models to initialize their own model development tailored to their studies.

In the work described below, we first describe the acquisition protocols for both the helium and ventilation images followed by a description of the analysis methodologies for the proposed segmentation framework. This discussion is contextualized with a brief overview of existing quantification methods (including that previously proposed by our group and used for the evaluative comparison).

MATERIALS AND METHODS

Image acquisition

Both proton and ventilation mages used for this study were taken from current and previous studies from our group. Ventilation images comprised both Helium-3 and Xenon-129 acquisitions as our current segmentation processing does not distinguish between acquisition protocols and we expected

similar agnosticism for the proposed approach.

Ventilation. Hyperpolarized MR image acquisition was performed under an Institutional Review Board (IRB)-approved protocol with written informed consent obtained from each subject. In addition, all imaging was performed under an Food and Drug Administration (FDA)-approved physician's Investigational New Drug application (IND 57866) for hyperpolarized 3He. MRI data were acquired on a 1.5 T whole-body MRI scanner (Siemens Sonata, Siemens Medical Solutions, Malvern, PA) with broadband capabilities and a flexible 3He chest radiofrequency coil (RF; IGC Medical Advances, Milwaukee, WI; or Clinical MR Solutions, Brookfield, WI). During a 10–20-second breath-hold following the inhalation of hyperpolarized gas, a set of 19–28 contiguous axial sections were collected. Parameters of the fast low angle shot sequence were as follows: repetition time msec / echo time msec, 7/3; flip angle 10° ; matrix, 80×128 ; field of view, 26×42 cm; section thickness, 10 mm; and intersection gap, none. Total acquisition time varies between 5-8 seconds depending on the size of the subjects.

Proton. A three-dimensional (3D) proton gradient-echo sequence (repetition time [TR]:1.80 ms, echo time [TE] 0.78 ms, flip angle 10°, bandwidth per pixel 1090 Hz/Pixel, partial Fourier: phase direction 6/8, slice direction 6/8) was used to acquire multiple images sets from multiple subjects at varying inflation levels. Acquisition time was 4 sec per image set. All imaging studies were performed under a physician's Investigational New Drug application for Xe129 MRI using a protocol approved by Institutional Review Board of our institute. All subjects provided written informed consent and the data were deidentified prior to analysis.

Image Analysis

We first review our previous contributions to the segmentation of proton and hyperpolarized gas MR images [7, 16]. We then describe the proposed deep learning methods (including preprocessing) extending earlier work. Specifically, the proposed contributions include:

- convolution neural networks for structural/functional lung segmentation,
- · template-based data augmentation, and
- open-source (i.e., ANTsRNet) availability.

Previous approaches for lung and ventilation-based segmentation

In [16], we proposed a joint label fusion (JLF) approach for segmenting the left and right lungs in proton MRI as well as estimating the lobar volumes. An atlas set consisting of a cohort of both the proton MRI and the corresponding lung segmentation is spatially normalized to an unlabeled image. A weighted consensus from the normalized images and segmentations is used to determine each voxel label. Although the method yields high quality results, one of the drawbacks is the time and computational resources required to perform the image registration for each member of the atlas set and the subsequent voxelwise label estimation.

Automated ventilation-based segmentation, described in [7], employs a Gaussian mixture model using a Markov random field (MRF) spatial prior which is optimized via the expectation-maximization algorithm. Basically, the intensity histogram profile is modeled using Gaussians with means and standard deviations designed to model the intensities of the individual ventilation classes (e.g., ventilation defect, hypo-ventilation, and normal ventilation). At each iteration the resulting estimated labels are then refined based an MRF spatial modeling. The parameters of the class-specific Gaussians are then re-estimated. This iterative process continues until convergence. We also iterate this segmentation with application of N4 bias correction [20].

These approaches have been used in a number of clinical studies [21, 22]

A diagrammatic representation of the proposed workflow is provided in Figure 1.

Preprocessing

Because of the low-frequency artifacts introduced by such confounds as radiofrequency coil inhomogeneity, we perform a retrospective bias correction on both sets of images using the N4 algorithm [23]. These are included in our previously proposed ventilation [7] and structural [16] segmentation frameworks. Since the initial release of these pipelines we have also adopted an adaptive, patchbased denoising algorithm specific to MR [24] which we have reimplemented in the ANTs toolkit. The dual effects of these data cleaning techniques on both the proton images and ventilation images are shown in Figure 2.

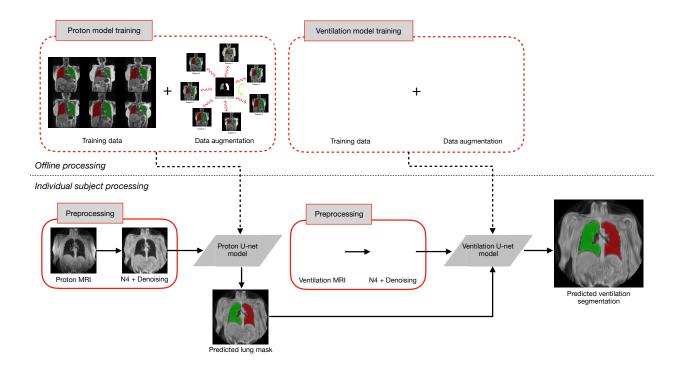


Figure 1: Illustration of the proposed workflow. Training the U-net models for both proton and ventilation imaging includes template-based data augmentation. This offline training is computationally intensive but is only performed once. Subsequent individual subject preprocessing includes MR denoising and bias correction. The proton mask determined from the proton U-net model is included as a separate "channel" for ventilation image processing.s

U-net architecture

Template-based data augmentation

In addition to these software contributions, a significant methodological contribution we have made is the design of a template-based data augmentation strategy. The need for large training data sets is a well-known limitation associated with deep learning algorithms. Whereas the architectures developed for such tasks as the ImageNet competition have access to millions of annotated images, such data access is not always is available and such is typically the case in medical imaging. In order to achieve data set sizes necessary for learning functional models, various data augmentation strategies have been employed. These include application of intensity transformations, such as brightening and enhanced contrast, and simple spatial transformations, such as arbitrary rotations and translations. Regarding the latter, such transformations are not ideal as they might not reflect what is

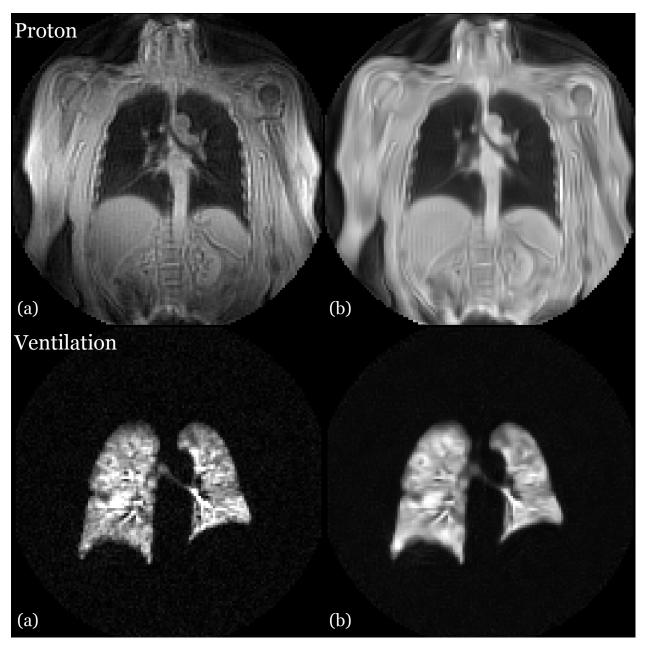


Figure 2: Side-by-side image comparison showing the effects of preprocessing on the proton (top) and ventilation (bottom) MRI. (a) Uncorrected image showing MR field inhomogeneity and noise. (b) Corresponding corrected image in which the bias and noise effects have been ameliorated.

typically seen in medical images and might not sufficiently sample the shape-space of the population currently being studied.

We currently use a template-based approach whereby image data sampled from the population is used to construct a representative template that is optimal in terms of both shape and intensity [25]. In addition to the representative template, this template-building process yields the transformations to/from each individual image to the template space. This permits a propagation of the training data to the space of each individual image. In the simplest case, the training data is used to construct the template and then each individual training data is propagated to the space of every other individual training data. In this way, a training data set of size N can be expanded to a data set of size N^2 (cf Figure 1). A more complicated use case could build a template from M data sets (where M > N). Transformations between the training data and the template could then be used to propagate the training data to the spaces of the individual members of the template-generating data for an augmented data set size of $M \times N$.

ANTsRNet

The recent interest in deep learning techniques and the associated successes with respect to a variety of applications has motivated adoption of such techniques within the medical imaging research community. Basic image operations such as classification, object identification, and segmentation (as well as more focused techniques) has significant potential for facilitating basic medical research. In light of these new developments, and in order to better meet the modern needs of the community, we have modified this specific aim for ITK-Lung to include the implementation and dissemination of open-source deep learning architectures relevant to the use cases of our partner investigators.

Towards this end, we have created *ANTsRNet*—a collection of well-known deep learning architectures ported to the R language. ANTsRNet is built using the Keras neural network library (available through R) and is highly integrated with the ANTsR package, the R interface of the ANTs toolkit. Consistent with our other software offerings, ongoing development is currently carried out on GitHub using a well-commented coding style, thorough documentation, and self-contained working examples.

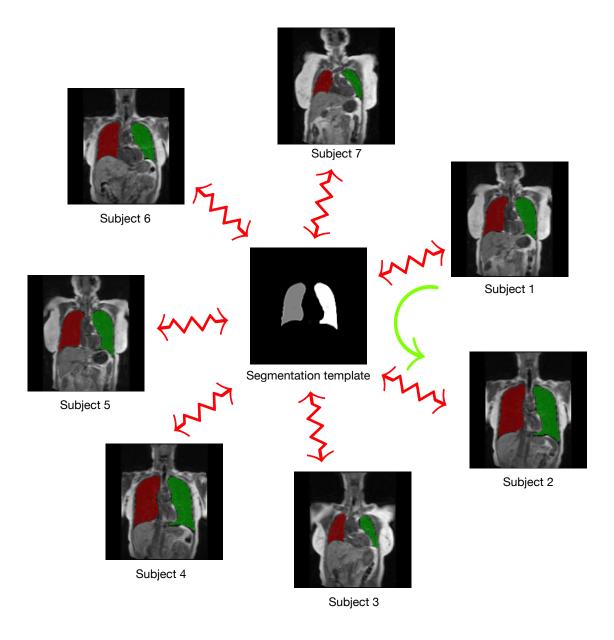


Figure 3: We introduce a novel data augmentation strategy for medical images using ANTs-based template construction. Shown here is the 2-D U-net example where we create a template from the training data segmentation images where the foreground designates the left and right lungs. This avoids the lack of internal correspondence while generating plausible global shape variations when mapping between individual training data. We used 60+ images to create such a template permitting $60^2=3600$ possible deformable shapes which can be further augmented by more conventional strategies (e.g., brightness transformations, translations, etc.).

It should be noted that various implementations of different deep learning architectures exist and are largely available to the public. However, we feel that this work fills an unmet need. Based on our own search, many publicly available implementations, while functional, are not developed with large-scale distribution and application as end goals. There is little, if any, coding consistency between the various implementations leading to non-standardized APIs and difficulties in code navigation for debugging and/or didactic reasons. In addition, the vast majority employ the Python language which is understandable given its widespread usage by data scientists. However, this work makes these powerful new developments available through a major platform heavily used by statisticians and data scientists alike. In addition, the R-based interface to the ANTs toolkit allows for preprocessing and data augmentation strategies specific to medical imaging. As a result of these current efforts, we were recently awarded a Titan XP GPU from the NVIDIA corporation for facilitating ongoing development.

Although much work remains to be completed, we have made significant progress. As noted below, several architectures have been implemented for both 2-D and 3-D images spanning the broad application areas of image classification, object detection, and image segmentation. It should be noted that most reporting in the literature has dealt exclusively with 2-D implementations. This is understandable due to memory and computational speed constraints limiting practical 3-D application on current hardware. However, given the importance that 3-D data has for medical imaging and the rapid progress in hardware, we feel it worth the investment in implementing corresponding 3-D architectures. Each architecture is accompanied by one or more self-contained examples for testing and illustrative purposes. In addition, we have made novel data augmentation strategies available to the user and illustrated them with Keras-specific batch generators. These contributions are outlined below.

Table 1: Current ANTsRNet capabilities comprising architectures for applications in image segmentation, image classification, and object localization. Self-contained examples with data are also provided to denstrate usage for each of the architectures. Although the majority of neural network architectures are originally described for 2-D images, we generalized the work to 3-D implementations where possible.

		ANTsRNet		
Image Segmentation	n			
U-net [?]	(2-D)	Extends fully convolutional neural networks by including an upsampling decoding path with skip connections linking corresponding encoding/decoding layers.		
V-net [?]	(3-D)	3-D extension of U-net which incorporates a customized Dice loss function.		
Image Classificatio	n			
AlexNet [?]	(2-D, 3-D)	Convolutional neural network that precipitated renewed interest in neural networks.		
VGG16/VGG19 [?]	(2-D, 3-D)	Also known as 'OxfordNet'. VGG architectures are much deeper than AlexNet. Two popular styles are implemented.		
GoogLeNet [?]	(2-D)	A 22-layer network formed from <i>inception blocks</i> meant to reduce the number of parameters relative to other architectures.		
ResNet [?]	(2-D, 3-D)	Characterized by specialized <i>residualized blocks</i> (and skip connections.		
ResNeXt [?]	(2-D, 3-D)	A variant of ResNet distinguished by a hyper-parameter called <i>cardinality</i> definining the number of independent paths.		
DenseNet [?]	(2-D, 3-D)	Based on the observation that performance is typically enhanced with shorter connections between the layers and the input.		
Object Localization	ı			
SSD300/SSD512 [?]	(2-D, 3-D)	The Multibox Single-Shot Detection (SSD) algorithm for determining bounding boxes around objects of interest.		
SSD7 [?]	(2-D, 3-D)	Lightweight SSD variant which increases speed by slightly sacrificing accuracy. Training size requirements are smaller.		

RESULTS

DISCUSSION

Significant progress has been made from earlier quantification approaches in which human labelers 12 manually identified areas of poor ventilation [???, ???] or applied simple thresholding techniques

[@]. More sophisticated automated and semi-automated techniques have advanced							

ACKNOWLEDGMENTS

Add ITK Lung grant here.

We also gratefully acknowledge the support of NVIDIA Corporation with the donation of the Titan Xp GPU used for this research.

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