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# Abstract

**Purpose:**

**Methods:** Four previously published histogram-based segmentation algorithms (i.e., linear binning, hierarchical k-means, fuzzy spatial c-means, and a Gaussian Mixture Model with a Markov Random Field prior) and an were used to segment two simulated data sets derived from a public () and a retrospective collection () of hyperpolarized 129Xe gas lung images transformed by common MRI artefacts in terms of measurement bias and precision.

**Results:** Although facilitating computational processing and providing discriminating clinically relevant measures of interest, histogram-based segmentation methods .

**Conclusions:** Direct optimization within the image domain using convolutional neural networks leverages spatial information which mitigates problematic issues associated with histogram-based approaches and suggests a preferred future research direction. Further, the entire processing and evaluation framework, including the newly reported deep learning functionality, is available as open-source through the well-known Advanced Normalization Tools ecosystem.

# Introduction

## Historical overview of quantification

Early attempts at quantification of images were limited to enumerating the number of ventilation defects or estimating the proportion of ventilated lung (1–3) which has evolved to more sophisticated techniques used currently. A brief outline of major contributions can be roughly sketched to include:

* binary thresholding based on relative intensities (4–6),
* linear intensity standardization via rescaling of the intensity histogram to a reference distribution based on healthy controls, i.e., “linear binning” (7,8),
* nonlinear intensity standardization using a customized hierarchical (9,10) or adaptive (11) k-means algorithm,
* nonlinear intensity standardization using fuzzy c-means (12) with spatial considerations based on local voxel neighborhoods (13), and
* Gaussian mixture modeling (GMM) of the intensity histogram with Markov random field (MRF) spatial prior modeling (14).

Given the functional nature of hyperpolarized gas images and the consequent sophistication of the segmentation task, these algorithmic approaches reduce the complex spatial image information to primarily intensity-only optimization considerations, contextualized in terms of the intensity histogram. Although facilitating computational processing, this simplifying transformation results in the loss of important spatial cues for identifying salient image features, such as ventilation defects (a well-studied correlate of lung pathophysiology), as spatial objects.

Each of these algorithms can be viewed as a type of MR intensity standardization (15) with varying degrees of flexibility and algorithmic sophistication. Due to hard threshold values, intensity-only approaches are unable to account for various MRI artefacts such as noise (16,17) and the intensity inhomogeneity field (18) which prevent such threshold values from distinguishing tissue types precisely consistent with that of human experts. These MR intensity nonlinearities have been well-studied (15,19–22) and are known to cause significant intensity variation even in the same region of the same subject. As stated in (19):

Intensities of MR images can vary, even in the same protocol and the same sample and using the same scanner. Indeed, they may depend on the acquisition conditions such as room temperature and hygrometry, calibration adjustment, slice location, B0 intensity, and the receiver gain value. The consequences of intensity variation are greater when different scanners are used.

Ignoring these nonlinearities is known to have significant consequences in the well-studied (and somewhat analogous) area of brain tissue segmentation in T1-weighted MRI (e.g., (23–25)) where the well-known relative intensities of major tissue types (i.e., cerebrospinal fluid (CSF), gray matter (GM), and white matter (WM)), which characteristically correspond to visible histogram peaks, as landmarks to determine the nonlinear intensity mapping (i.e., 1-D piecewise affine mapping) between structural features found within the histograms themselves (e.g., peaks and valleys) (15,21). However, in hyperpolarized gas imaging of the lung, no such characteristic structural features exist, generally, between histograms. Additionally, because of the functional nature of these images, the segmentation clusters that correspond to features of interest are not necessarily guaranteed to exist (e.g., ventilation defects in the case of healthy normal subjects with no lung pathology).

Additional sophistication incorporating spatial considerations is found in the fuzzy spatial c-means (26) and Gaussian mixture-modeling (GMM) with a Markov random field (MRF) prior algorithms. The former, similar to k-means, optimizes over the within-class sample variance but includes a per-sample membership weighting (27) whereas the latter is optimized via the expectation-maximization (EM) algorithm (28). These algorithms have the advantage, in contrast to histogram-only algorithms, the intensity thresholds between class labels are softened which demonstrates some relative robustness to certain imaging distortions, such as noise. However, all these algorithms are flawed in the inherent assumption that meaningful structure is found, and can be adequately characterized, within the associated image histogram in order to optimize a multi-class labeling.

Additionally, many of these segmentation algorithms use N4 bias correction (29), an extension of the nonuniform intensity normalization (N3) algorithm (18), to mitigate MR intensity inhomogeneity artefacts. Interestingly, N3/N4 iteratively optimizes towards a final solution using information from both the histogram and image domains. Based on the intuition that the bias field acts as a smoothing convolution operation on the original image intensity histogram, N3/N4 optimizes a nonlinear (i.e., deformable) intensity mapping based on histogram deconvolution. This nonlinear mapping is constrained such that its effects smoothly vary across the image. Additionally, due to the deconvolution operation, this mapping sharpens the histogram peaks which presumably correspond to distinct tissue types. While such assumptions are appropriate for the domain in which N3/N4 was developed (i.e., T1-weighted brain tissue segmentation) and while it is assumed that the enforcement of low-frequency modulation of the intensity mapping prevents new image features from being generated, it is not clear what effects N4 parameter choices have on the final segmentation solution, particularly for those algorithms that are limited to intensity-only considerations and less robust to the specified MR artefacts.

## Motivation for current study

Investigating the assumptions outlined above, particularly those associated with the intensity mappings due to both the MR acquisition and inhomogeneity mitigation preprocessing, we became concerned by the susceptibility of the histogram structure to such variations and the potential effects on current clinical measures of interest derived from these algorithms (e.g., ventilation defect percentage). Specifically, we noticed that histogram-based intensity perturbations can produce virtually little, if any, changes in the features of the image despite a relatively significant change in the histogram structure. Such effects imply that MR artefacts could profoundly impact histogram-based algorithmic performance. Figure provides a sample visualization representing some of the structural changes that we observed when simulating these nonlinear mappings.

To briefly explore these effects further for the purposes of motivating additional experimentation, we provide a summary illustration from a set of image simulations in Figure which are detailed later in this work and used for algorithmic comparison. Simulated MR artefacts were applied to each image which included both noise and nonlinear intensity mappings (and their combination) using two separate data sets: one in-house data set consisting of 51 129Xe gas lung images and the publicly available data described in (30) and made available at Harvard’s Dataverse online repository (31) consisting of 29 hyperpolarized gas lung images . These two data sets resulted in a total simulated cohort of 51 + 29 = 80 images ( simulations per image types of artefact simulations). Prior to any algorithmic comparative analysis, we quantified the difference of each simulated image with the corresponding original image using the structural similarity index measurement (SSIM) (32). SSIM is a highly cited measure which quantifies structural differences between a reference and distorted (i.e., transformed) image based on known properties of the human visual system. SSIM has a range where 0 indicates no structural similarity and 1 indicates perfect structural similarity. We also generated the histograms corresponding to these images. Although several histogram similarity measures exist, we chose Pearson’s correlation primarily as it resides in the same min/max range as SSIM with analogous significance. In addition to the fact that the image-to-histogram transformation discards important spatial information, from Figure it should be apparent that this transformation also results in greater variance in the resulting information under common MR imaging artefacts, according to these measures. Thus, prior to any algorithmic considerations, these observations strongly suggest that optimizing in the domain of the histogram will be generally less informative and less robust than optimizing directly in the image domain.

Ultimately, we are not claiming that these algorithms are erroneous, per se. Much of the relevant research has been limited to quantifying differences with respect to ventilation versus non-ventilation in various clinical categories and these algorithms have demonstrated the capacity for advancing such research . Furthermore, as the sample segmentations in Figure illustrate, when considered qualitatively, each segmentation algorithm appears to produce reasonable segmentations even though the voxelwise differences are significant as are the corresponding histograms. However, the artefact issues influence quantitation in terms of core scientific measurement principles such as precision (e.g., reproducibility and repeatability (11,33)) and bias which are obscured in isolated considerations but become increasingly significant with multi-site (34) and large-scale studies. In addition, refinements in measuring capabilities correlate with scientific advancement so as acquisition and analysis methodologies improve, so should the level of sophistication and performance of the underlying measurement tools.

In assessing these segmentation algorithms for hyperpolarized gas imaging, it is important to note that human expertise leverages more than relative intensity values to identify salient, clinically relevant features in images—something more akin to the complex structure of deep-layered neural networks (37), particularly convolutional neural networks (CNN). Such models have demonstrated outstanding performance in certain computational tasks, including classification and semantic segmentation in medical imaging (38). Their potential for leveraging spatial information from images surpasses the perceptual capabilities of previous approaches and even rivals that of human raters (39). Importantly, CNN optimization occurs directly in the image space to learn complex spatial features, in contrast to the previously discussed methods where optimization (primarily) concerns image intensity-only information. We introduced a deep learning approach in (40) and further expand on that work for comparison with existing approaches below. Although we find its performance to be quite promising, more fundamental to this work than the network itself is simply pointing to the general potential associated with deep learning for analyzing hyperpolarized gas images *as spatial samplings of real-world objects*, as opposed to lossy representations of such objects. In the spirit of open science, we have made the entire evaluation framework, including our novel contributions, available within the Advanced Normalization Tools software ecosystem (ANTsX) (41).

# Methods

## Hyperpolarized gas imaging acquisition

### University of Virginia cohort

A retrospective dataset was collected consisting of young healthy (), older healthy (), cystic fibrosis (CF) (), interstitial lung disease (ILD) (), and chronic obstructive pulmonary disease (). MR imaging with hyperpolarized 129Xe gas was performed under an Institutional Review Board (IRB) approved protocol with written informed consent obtained from each subject. In addition, all imaging was performed under a Food and Drug Administration (FDA) approved physician’s Investigational New Drug application. MRI data were acquired on a 1.5 T whole-body MRI scanner (Siemens Avanto, Siemens Medical Solutions, Malvern, PA) with broadband capabilities and a flexible 129Xe chest radiofrequency coil (RF; IGC Medical Advances, Milwaukee, WI; or Clinical MR Solutions, Brookfield, WI). During a breath-hold following the inhalation of mL of hyperpolarized 129Xe mixed with nitrogen up to a volume equal to 1/3 forced vital capacity (FVC) of the respective subject, a set of 15-17 contiguous coronal lung slices were collected to cover the entire lungs. Parameters of the gradient echo (GRE) sequence with a spiral k-space sampling with 12 interleaves for 129Xe MRI were as follows: repetition time msec / echo time msec, 7/1; flip angle, 20; matrix, 128 128: in-plane voxel size, 4 4 mm; section slice thickness, 15 mm; and intersection gap, none. The data were deidentified prior to analysis. These data are available upon request and through a data sharing agreement.

### Harvard Dataverse cohort

In addition to the data acquired at the University of Virginia, we also processed a publicly available lung dataset (31) available at the Harvard Dataverse and detailed in (30). These data comprised the original 129Xe acquisitions from 29 subjects (10 healthy controls and 19 mild intermittent asthmatic individuals) with corresponding lung masks. In addition, seven artificially SNR-degraded images per acquisition were also part of this data set but not used for the analyses reported below. The image headers were corrected for proper canonical anatomical orientation according to Nifti standards and uploaded to the GitHub repository associated with this work.

### Data simulations

## Algorithmic implementations

In support of the discussion in the Introduction, we performed various experiments to compare the algorithms previously, viz. linear binning (7), hierarchical k-means (9), fuzzy spatial c-means (13), GMM-MRF (specifically, ANTs-based *Atropos* tailored for functional lung imaging) (14), and a trained CNN with roots in our earlier work (40), which we have dubbed “El Bicho.” A fair and accurate comparison between algorithms necessitates several considerations which have been outlined previously (42). In designing the evaluation study:

* All algorithms and evaluation scripts have been implemented using open-source tools by the first author and have been made available as part of the GitHub repository corresponding to this work (<https://github.com/ntustison/Histograms>). (40) (31).
* An important algorithmic hyperparameter is the number of ventilation clusters. In order to minimize differences in our set of evaluations, we merged the number of resulting clusters, post-optimization, to only three clusters: “ventilation defect,” “hypo-ventilation,” and “other ventilation” where the first two clusters for each output are the same as the original implementations and the remaining clusters are merged into the third category.
* Another significant issue was whether to apply N4 bias correction as a preprocessing step. We ultimately decided to include it for two reasons. First, it is explicitly used in multiple algorithms (e.g., (4,7,11,14,43)) despite the issues raised previously since it qualitatively improves image appearance. Another practical consideration for N4 preprocessing was due to the parameters of the reference distribution required by the linear binning algorithm (discussed in greater detail below).
* We extended the deep learning functionality first described in (40) to improve performance and provide a more clinically granular labeling (i.e., four clusters here instead of two in the previous work). This network is a 2-D U-net (44) with enhancements including additional training data with augmentation, attention gating (45), and recommended hyperparameters (46). These include four encoding/decoding layers with 32 filters at the base layer (and doubled at each subsequent layer). Training incorporated an 80/20 data split using categorical cross entropy and a multi-label Dice function (47) where and refer to the source and target regions, respectively, as loss functions.

# Results

We performed several comparative evaluations to probe the previously mentioned issues broadly categorized in terms of measurement bias and precision, with most of the focus being on the latter. Given the lack of ground-truth in the form of segmentation images, addressing issues of measurement bias is difficult. In addition to the fact that the number of ventilation clusters is not consistent across algorithms, it is not clear that the ventilation categories across algorithms have identical clinical definition. This prevents application of various frameworks accommodating the lack of ground-truth for segmentation performance analysis (e.g., (48)) to these data.

As mentioned in the Introduction, the cited algorithms have all demonstrated research utility and potential clinical utility. This is supported by our first evaluation which is based on diagnostic prediction of given clinical categories assigned to the imaging cohort using derived random forest models (49). This approach also provides an additional check on the validity of the algorithmic implementations. However, it is important to recognize that this evaluation is extremely limited as the underlying data are gross measures which do not provide accuracy estimates on the level of the algorithmic output (i.e., voxelwise segmentation).

Having established the general validity of the gross algorithmic output, we then switch to our primary focus which is the comparison of measurement precision between algorithms. We first analyzed the unique requirement of a reference distribution for the linear binning algorithm. Specifically, we quantify the effects of the choice of reference cohort on the clustering parameters for the linear binning algorithm. We then incorporate the trained El Bicho model in exploring additional aspects of measurement variance based on simulating both MR noise and intensity nonlinearities.

, we performed the following evaluations/experiments:

* Global algorithmic bias (in the absence of ground truth)
  + Diagnostic prediction
* Voxelwise algorithmic precision
  + Input/output variance based on reference distribution (linear binning only)
  + Effects of simulated MR artefacts on multi-site data

## Diagnostic prediction

Due to the absence of ground-truth, we adopted the strategy from previous work (41,50) where we used cross-validation to build and compare prediction models from data derived from the set of segmentation algorithms. Specifically, we use pathology diagnosis (i.e., “CF,” “COPD,” and “ILD”) as an established research-based correlate of ventilation levels from hyperpolarized gas imaging (e.g., (35,36,43)) and quantified the predictive capabilities of corresponding binary random forest classifiers (49) of the form:

where is the volume of the cluster and is total lung volume We used a training/testing split of 80/20. Due to the small number of subjects, we combined the young and old healthy data into a single category. 100 permutations were used where training/testing data were randomly assigned and the corresponding random forest model was constructed at each permutation.

The resulting receiver operating characteristic (ROC) curves for each algorithm and each diagnostic scenario are provided in Figure . All four algorithms perform significantly better than a random classifier. In the absence of ground truth, this type of evaluation does provide evidence that all these algorithms produce measurements which are clinically relevant although, it should be noted, that this is a very coarse assessment strategy given the global measures used (i.e., cluster volume percentage) and the general clinical categories employed. In fact, even spirometry measures can be used to achieve highly accurate diagnostic predictions with machine learning techniques (51).

## Effects of reference image set selection

One of the additional input requirements for linear binning over the other algorithms is the generation of a reference distribution. Therefore, we additionally investigated the influence of reference data set on the outcome of linear binning classification, since this is an integral aspect unique to this method. In addition to the output measurement variation caused by choice of the reference image cohort, this played a role in determining whether or not to use N4 preprocessing. As mentioned, a significant portion of N4 processing involves the deconvolution of the image histogram to sharpen the histogram peaks which decreases the standard deviation of the intensity distribution and can also result in a histogram shift. Using the original set of 10 young healthy data with no N4 preprocessing, we created a reference distribution according to (7), which resulted in an approximate distribution of . This produced 0 voxels being classified as belonging to Cluster 1 (Figure (a)) because two standard deviations from the mean is less than 0 and Cluster 1 resides in the region below -2 standard deviations. However, using N4-preprocessed images produced something closer, , to the published values, , reported in (7), resulting in a non-empty set for that cluster. This is consistent, though, with linear binning which does use N4 bias correction for preprocessing. We also mention that the Harvard Dataverse images used were preprocessed using N4 (30) which provides a third reason for its use on the University of Virginia image dataset (to maximize cross cohort consistency). In the case of the former image set, we did use the previously reported linear binning mean and standard deviation algorithm parameter values (i.e., ). This was the only parameter difference between analyzing the two image sets.

The previous implications of the chosen image reference set also caused us to look at this choice as a potential source of both input and output variance in the measurements utilized and produced by linear binning. Regarding the former, we took all possible combinations of our young healthy control subject images and looked at the resulting mean and standard deviation values. As expected, there is significant variation for both mean and standard deviation values (see top portion of Figure ) which are used to derive the cluster threshold values. This directly impacts output measurements such as ventilation defect percentage. For the reference sets comprising eight or nine images, we compute the corresponding linear binning segmentation and estimate the volumetric percentage for each cluster. Then, for each subject, we computed the min/max range for these values and plotted those results cluster-wise on the bottom of Figure . This demonstrates that the additional requirement of a reference distribution is a source of potentially significant measurement variation for the linear binning algorithm.

## Effects of MR-based simulated image distortions

As we mentioned in the Introduction, noise and nonlinear intensity artefacts common to MRI can have a significant distortion effect on the image with even greater effects seen with respect to change in the structure of the corresponding histogram. This final evaluation explores the effects of these artefacts on the algorithmic output on a voxelwise scale using the Dice metric (Equation ()) which has a range of [0,1] where 1 signifies perfect agreement between the segmentations and 0 is no agreement.

Ten simulated images for each of the subjects of both the University of Virginia and Harvard Dataverse cohort were generated for each of the three categories of randomly generated artefacts: noise, nonlinearities, and combined noise and intensity nonlinearities. The original image as well as the simulated images were segmented using each of the five algorithms. Following our earlier protocol, we maintained the original Clusters 1 and 2 per algorithm and combined the remaining clusters into a single third cluster. This allowed us to compare between algorithms and maintain separate those clusters which are the most studied and reported in the literature. The Dice metric was used to quantify the amount of deviation, per cluster, between the segmentation produced by the original image and the corresponding simulated distorted image segmentation which is summarized in Figures and . The algorithms were then compared, on a per-cluster and per-artefact basis, using one-way ANOVA followed by Tukey’s Honest Significant Difference (HSD) test in Figures and .

# Discussion

(54)

(40) (55)

(52,53)

## Acknowledgments

Support for the research reported in this work includes funding from the National Heart, Lung, and Blood Institute of the National Institutes of Health (R01HL133889).

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