

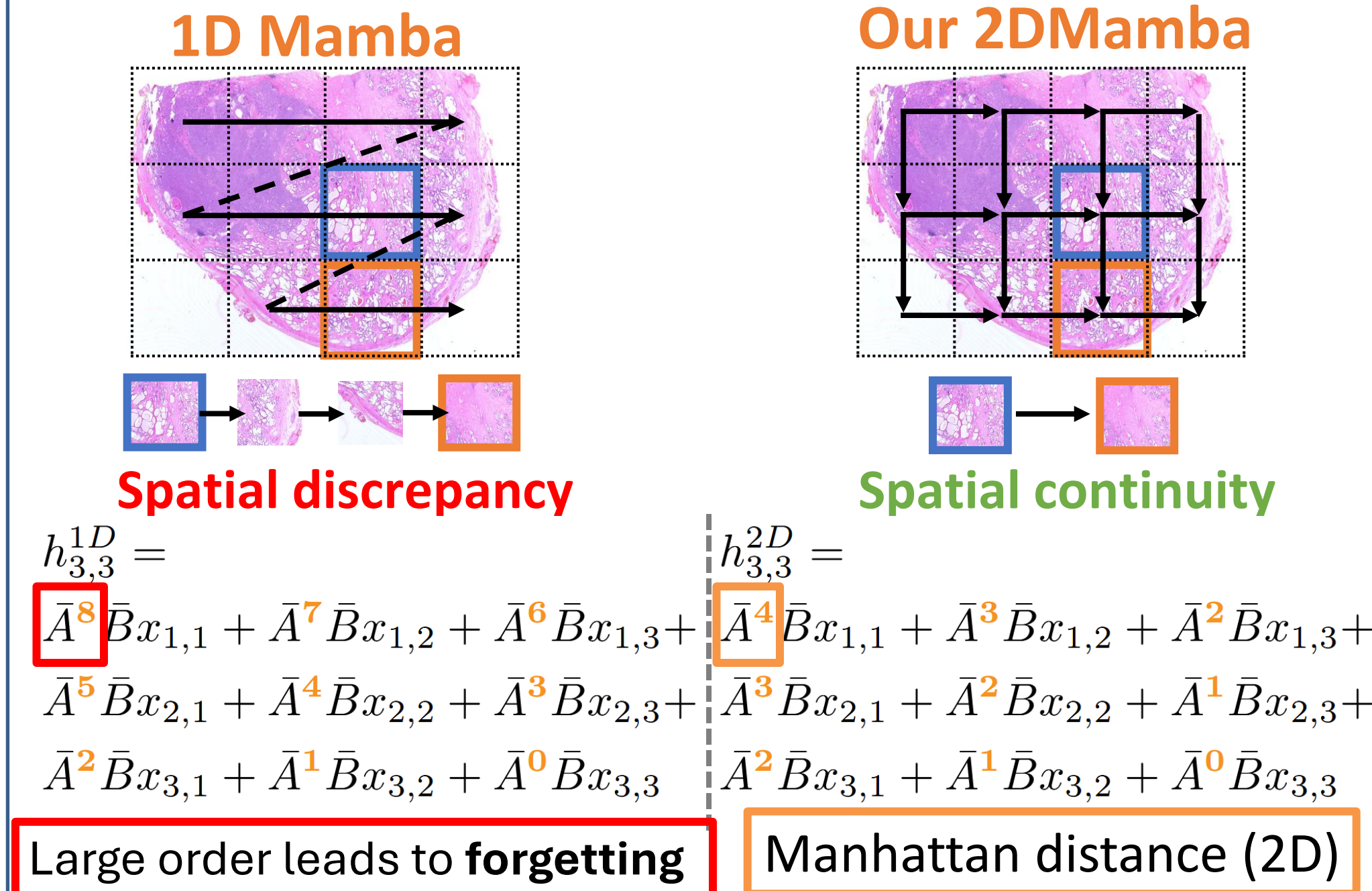
2DMamba: Efficient State Space Model for Image Representation with Applications on Giga-Pixel Whole Slide Image Classification

Jingwei Zhang^{1*}, Anh Tien Nguyen^{2*}, Xi Han^{1*}, Vincent Quoc-Huy Trinh⁵, Hong Qin¹, Dimitris Samaras¹, Mahdi S. Hosseini^{3,4}
¹Stony Brook University; ²Korea University; ³Concordia University; ⁴Mila–Quebec AI Institute; ⁵University of Montreal Hospital Center

Introduction

- Mamba [1], a state space model (SSM) with **linear time complexity** and **high GPU parallelism**, shows strong results on both natural images [2, 3] and Whole Slide Images (WSI) [4].

- Limitation #1: Spatial discrepancy** in all current mamba variants [2-4]. They are **inherently 1D** as they flatten 2D images into 1D sequences, losing spatial context.



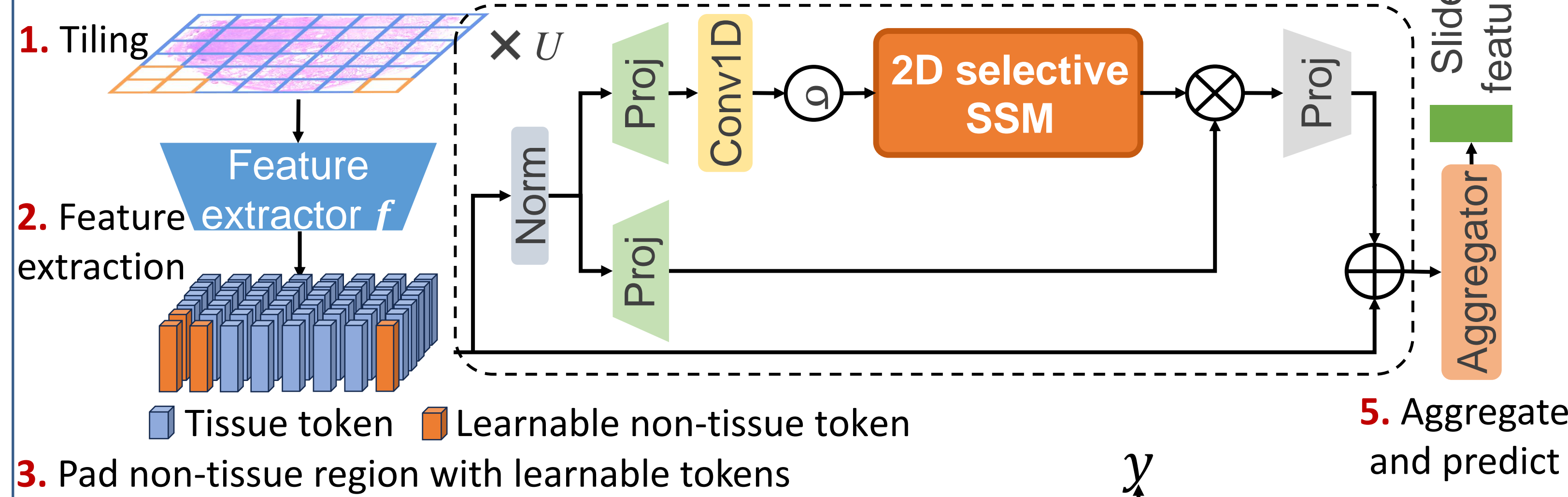
- Limitation #2: Speed** in existing 2D SSM methods [5]. They still lack an efficient **parallel algorithm** because of their formulation and thus **slow**.

Our contributions:

- A novel **2D SSM** architecture that directly scans a 2D image without first flattening it into a 1D sequence, maintaining the **2D structure**.
- A fast **hardware-aware 2D** CUDA operator to extend the 1D Mamba **parallelism** into 2D.

Method

Overall framework:



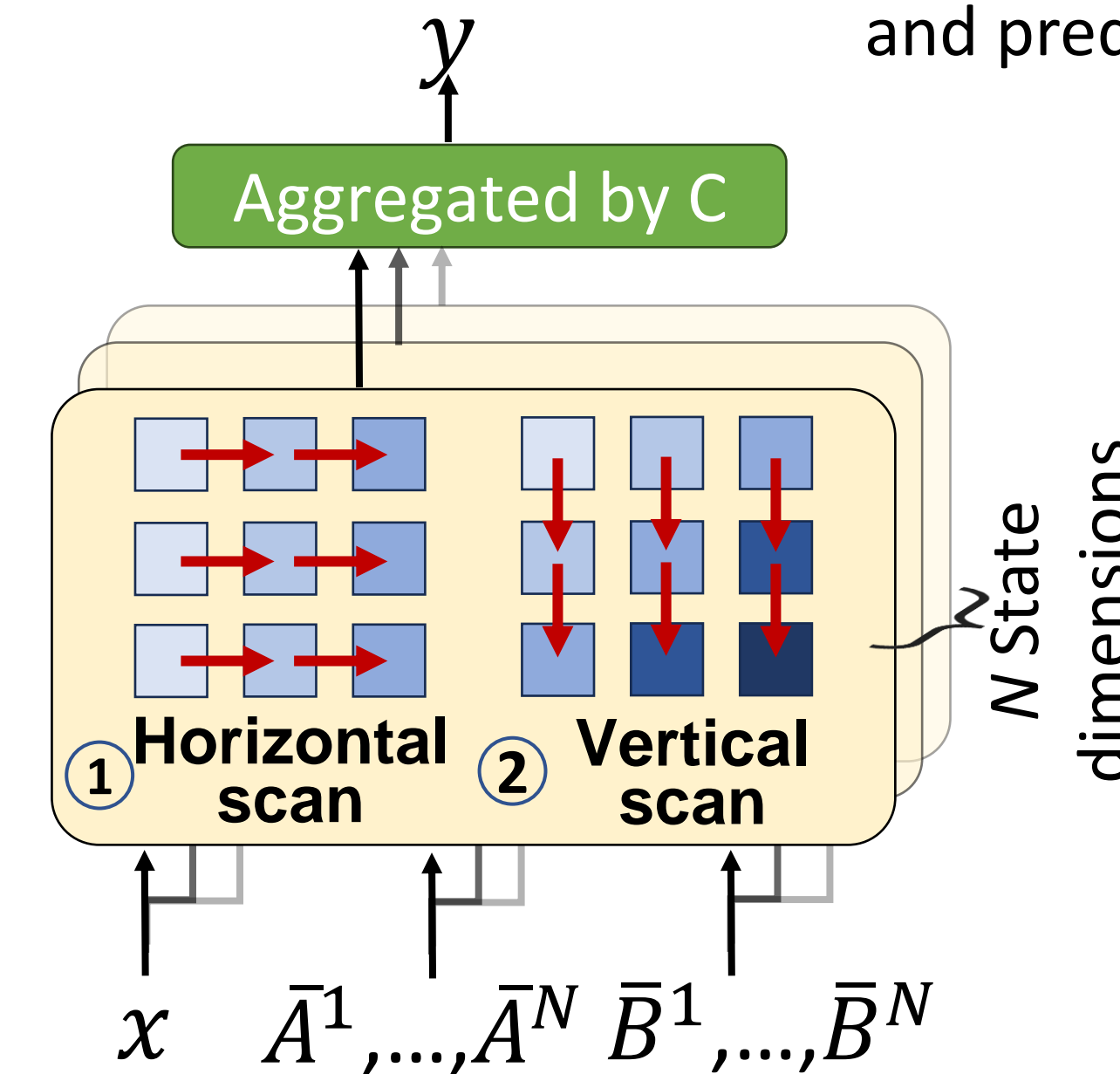
2D selective SSM:

- Horizontal scan:

$$h_{i,j}^{hor} = \bar{A}_{i,j} h_{i,j-1}^{hor} + \bar{B}_{i,j} x_{i,j}$$
- Vertical scan (without duplicated $\bar{B}_{i,j}$):

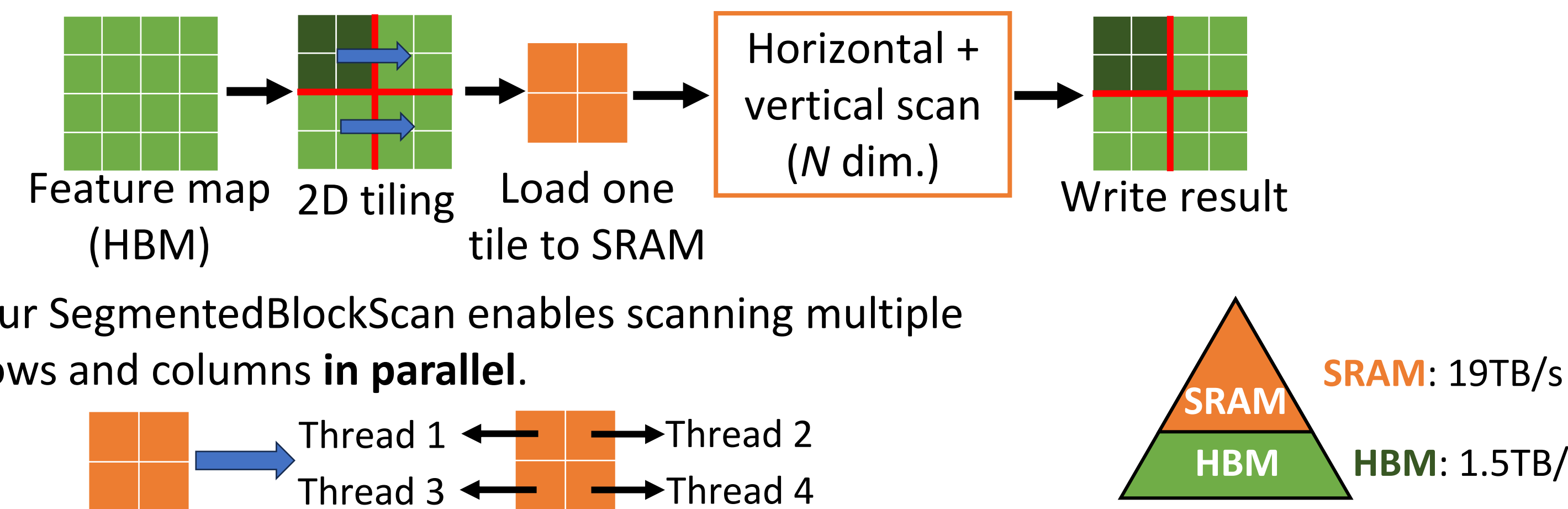
$$h_{i,j} = \bar{A}_{i,j} h_{i-1,j}^{hor} + h_{i,j}^{hor}$$
- Aggregated by C :

$$y_{i,j} = C h_{i,j}$$



Hardware-Aware 2D Selective Scan:

- Tile the feature map into **2D blocks**, scan each block in two directions, removing the naïve $N \times$ memory blow-up and delivers a **10 \times speed-up**.



Experiments

WSI benchmarks on 10 datasets

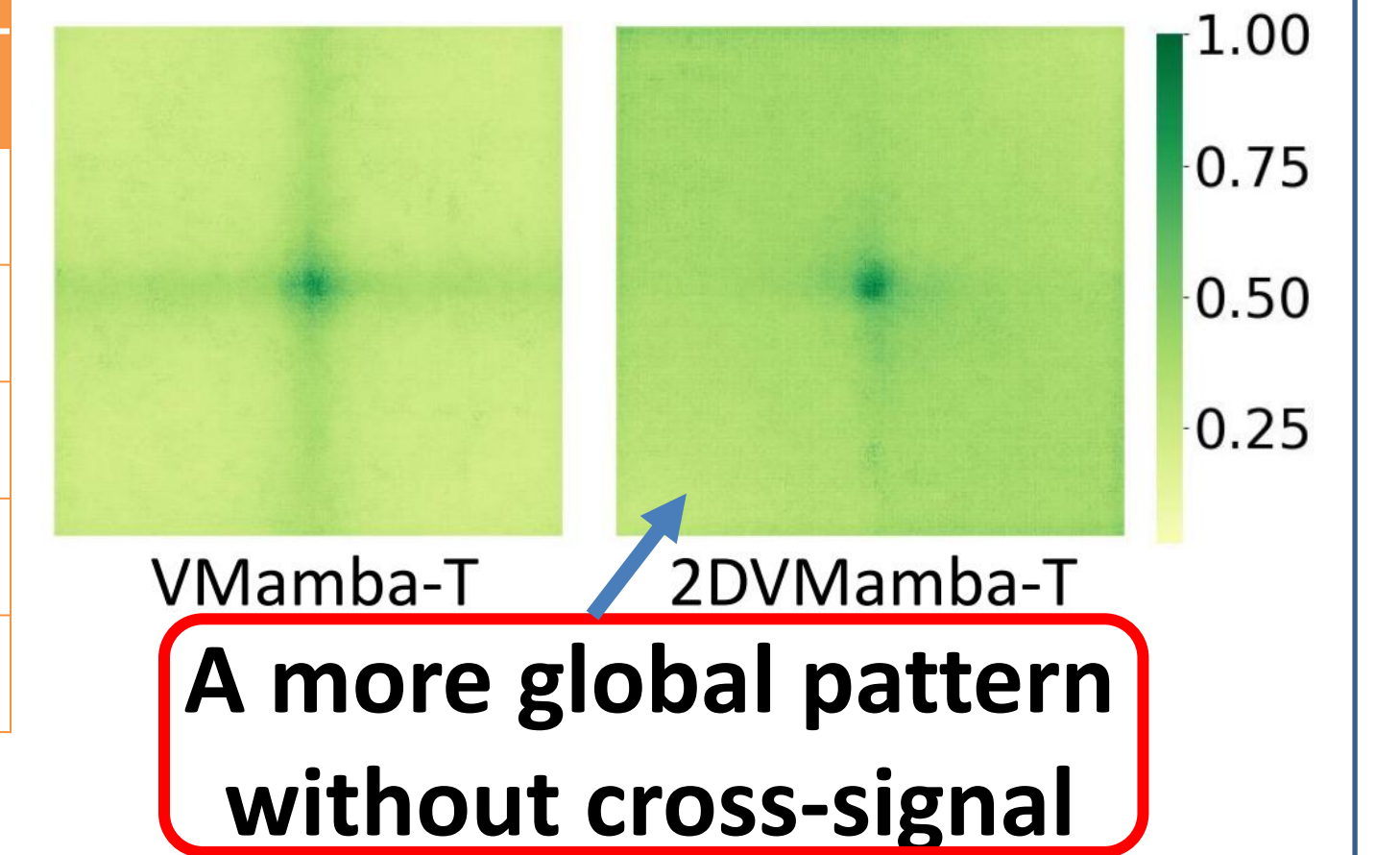
Method	WSI classification (Accuracy)					Survival analysis (C-index)				
	BRCAS	DHMC	PANDA	NSCLC	BRCA	KIRC	KIRP	LUAD	STAD	UCEC
DTFD-MIL	0.701	0.871	0.470	0.874	0.927	0.727	0.793	0.602	0.617	0.746
TransMIL	0.692	0.807	0.464	0.885	0.938	0.694	0.732	0.614	0.598	0.700
S4MIL	0.662	0.864	0.505	0.885	0.946	0.723	0.791	0.595	0.600	0.746
MmambaMIL	0.738	0.855	0.468	0.876	0.933	0.710	0.782	0.595	0.624	0.742
SRMambaMIL	0.738	0.859	0.471	0.885	0.931	0.718	0.742	0.588	0.613	0.740
2DMmambaMIL	0.752	0.893	0.508	0.885	0.946	0.731	0.803	0.620	0.643	0.754

Natural image benchmarks

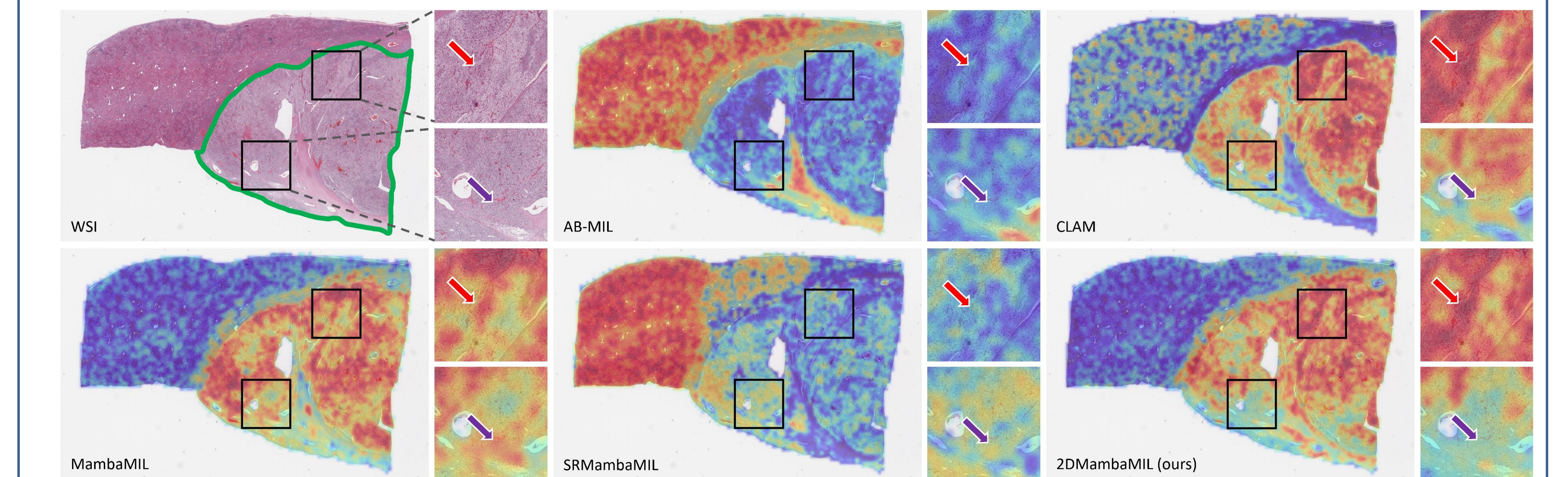
Method	ImagNet-1K	ADE20K	
	Top-1 Acc.	mIoU (SS)	mIoU (MS)
Vim-S	80.3%	44.9	-
EfficientVMamba-B	81.8%	46.5	47.3
LocalVMamba-T	82.7%	47.9	49.1
VMamba-T	82.6%	47.9	48.8
2DVMamba-T	82.8%	48.6	49.3

2DMamba outperforms the SOTA methods

Effective Receptive Fields



Qualitative Evaluation on WSI



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