

Reliability, Safety and Risk Analysis

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CHAPTER 1

Introduction

1.1 Why reliability is so important?



Figure 1.1: Evolution to failure...

A component, even if very well designed, built with durable materials from the best manufacturer in the world, will eventually start degrading → *onset of a degradation process*.

Degradation won't stop and, without proper countermeasures, the component will fail at a given point. We cannot ignore it!

Availability and Maintainability

2.1 Introduction

Can I repair the system after a failure? We can classify systems into two categories according to the answer to this question.

- **Non maintained systems** These systems cannot be repaired after a failure (e.g. a telecommunication satellite, a F1 engine, a vessel of a nuclear power plant).
→ a good *performance parameter* is the *reliability*, as it quantifies the system capability of satisfying a specified mission within an assigned period of time (T_M): $R(T_M) = P(T > T_M)$
- **Maintained systems** These systems can be repaired after the failure (e.g. pump of an energy production plant, a component of the reactor emergency cooling systems).
→ a good *performance parameter* is the *availability*, as it quantifies the system ability to fulfill the assigned mission at any specific moment in the lifetime: $A(t)$.

We will now try to give now a more rigorous definition of *availability*.

2.2 Definition of Availability

Let's tackle the problem from a mathematical point of view.

We introduce an indicator variable $X(t)$ such that:

$$X(t) = \begin{cases} 1 & \text{system is operating at time } t \\ 0 & \text{system is failed at time } t \end{cases}$$

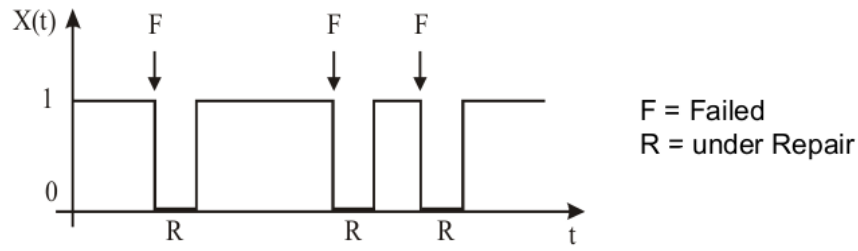


Figure 2.1: An example of $X(t)$ for a given system

2.2.1 Instantaneous availability

$$p(t) = P\{X(t) = 1\} = E[X(t)]$$

Notice that:

$$E[X(t)] = \sum_{i=0}^1 iP\{X(t) = i\} = 0 \cdot P\{X(t) = 0\} + 1 \cdot P\{X(t) = 1\} = p(t)$$

2.2.2 Instantaneous unavailability

$$q(t) = P\{X(t) = 0\} = 1 - p(t)$$

where the last equivalence comes from the fact that the two events "system is operating at time t " and "system is failed at time t " are mutually exclusive.

2.3 Contributions to Unavailability

2.3.1 Repair

A component can be unavailable because it is under repair after a failure.

2.3.2 Testing / Preventive Maintenance

2.3.3 Unrevealed failure

2.4 Average availability descriptors

