$\left|\psi(\tau)\right\rangle = e^{i\hat{H}t} \left|\psi(0)\right\rangle = e^{-\hat{H}\tau} \left|\psi(0)\right\rangle = \sum e^{-\hat{E}_i\tau} \left|\psi_i(0)\right\rangle$