

Leading one in the last column of U ?

Yes

System inconsistent.
No solutions.

No

Any *other* columns of U with leading ones?

Yes

System has ∞ -many solutions.

No

System has unique solution.