

DELFT UNIVERSITY OF TECHNOLOGY

MASTER THESIS

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## INTRODUCTION

## INTRODUCTION

The subject of my Master's thesis will be on ways of improving T1 and T2 coherence times for qubits. The past few months I have been learning about superconducting circuit quantum electrodynamics. I have learned what set-ups are used for performing measurements on cQED samples, and about the types of measurements that are performed.

Traditionally the measurements were performed using Labview software. However, in the months that I have been working in the DiCarlo lab, a transition in measurement software has taken place from Labview to the Python-based QTLab. I have been very involved in this transition, as an important part of my research will be to characterize a sample quickly and accurately. This will enable a fast cycle from sample fabrication to characterization, hopefully leading to rapid progress in the development of quantum computing using cQED.

The past few weeks the focus of my measurements has shifted towards the characterization of resonators. This is largely due to the fact that two of my colleagues, Alessandro Bruno and Gijs de Lange, are working on a paper on ways of improving the quality factor of resonators. A large part of the data was already obtained before I joined the group, but a last set of measurements was required using the dilution refrigerator I most often operate at. The reason is that its base temperature is at 15 mK, which is considerably lower than the base temperature of the refrigerator at which the other measurements were performed, namely 250 mK. Because my focus so far has been more on resonators than on qubits, the main topic of this report will be on resonators, and I will include the topic of qubits in my final thesis.

Because the relevant regime where resonators interact with qubits is the single-photon regime, a very weak signal must be applied to determine its properties in that regime. At this point noise becomes a relevant issue. I will therefore also devote a section of this report on the subject of noise.

# **Part I**

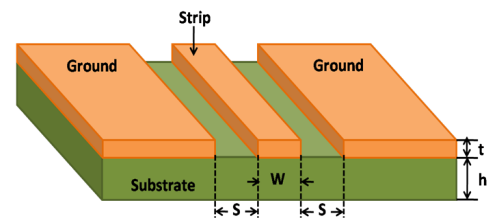
## **Resonators**

When a signal enters a fridge it is attenuated in several stages and eventually reaches the sample being measured. In the sample the signal travels through a feedline. One or more resonators can then be capacitively coupled to the feedline. Qubits can then also be capacitively coupled to the resonators, and a resonator can even be used to connect qubits, in which case the resonator is known as a 'bus'. However in this report only resonators connected to a central feedline will be discussed.

## 0.1 COPLANAR WAVEGUIDE

In the context of circuit QED, one of the most common types of resonators are coplanar waveguides (CPW). Coplanar waveguides consist of a long central conducting track, with on both sides a neighbouring grounded track. The conducting track is separated from the grounded tracks by a fixed distance.

One end is usually capacitively coupled to a feedline and has an open end, while the other end can either be open or shorted. This determines whether the resonant frequencies have a node or an antinode at that end. In the case of a shorted end, the resonant frequencies have an antinode at that end, resulting in a quarter wave resonator. This means that the wavelength of the fundamental mode fits a quarter times into the resonator. In the case of an open end, the resonant frequencies have a node at that end, resulting in a half wave resonator.



**Figure 1:** Schematic of a coplanar waveguide.

## 0.2 QUALITY FACTOR

The quality of a resonator can be quantified through its quality factor. Generally speaking, the quality factor of a resonator determines the ratio between energy stored in a resonator and the energy leaking away from the resonator. For cQED resonators this corresponds to the rate at which photons dissipate from the resonator. A high quality factor corresponds to a low dissipation rate.

The quality factor can also be defined in two different ways [7, p. 23-24]:

$$Q = \omega_0 \tau_1 = \omega_0 / \Delta\omega \quad (1)$$

Here  $\omega_0$  is the resonance frequency of the resonator, and  $\tau_1$  is the decay time of the resonator. The decay time is the time taken by a resonator to dissipate its energy to  $1/e$  of its original energy. One can see that this definition is in accordance with the first definition, as the energy is related to frequency through the Planck-Einstein relation:  $E = \hbar\nu$ , and therefore increases with increasing frequency.

Photons can dissipate from the resonator through the resonator's different loss channels. Each of these loss channels has a corresponding quality factor. One such loss channel is due

to resonators in cQED being capacitively coupled to a feedline. The quality factor associated to this loss channel is known as the coupling quality factor  $Q_c$ . This coupling quality factor depends on the amount of capacitive coupling between the resonator and the feedline. It can therefore be engineered to have a certain value, depending on the amount of interaction wanted between resonator and feedline.

The other loss channels are usually unwanted, and therefore desired to be as low as possible. These individual channels are usually lumped together, resulting in a combined quality factor, known as the intrinsic quality factor  $Q_i$ .

The total quality factor of the resonator is known as the loaded quality factor  $Q_l$ . It is related to  $Q_c$  and  $Q_i$  through:

$$\frac{1}{Q_l} = \frac{1}{Q_c} + \frac{1}{Q_i} \quad (2)$$

From equation 2 it can be seen that if the difference between  $Q_c$  and  $Q_i$  is large, then the loaded quality factor  $Q_l$  will be approximately equal to the minimum of the two.

For a quarter wave resonator the amplitude of transmission has a minimum  $S_{21}^{min}$ , given by [7, p. 29]:

$$S_{21}^{min} = \frac{Q_c}{Q_c + Q_i} \quad (3)$$

With knowledge of the resonant frequency  $\omega_0$ , the resonant width  $\Delta\omega$ , and the transmitted signal at resonance  $S_{21}^{min}$ , it is possible through equations 1 and 3 to determine both the coupling quality factor  $Q_c$  and the intrinsic quality factor  $Q_i$ . Note that as equation 3 depends on the ratio of the two quality factors, to get an accurate estimate of both quality factors, they should have a comparable value.

One reason why a high quality factor is important in the context of cQED is that a qubit can be coupled to a resonator. This qubit therefore experiences dissipation due to its coupling to the resonator, known as the Purcell effect. The result of dissipation is that when the qubit is in its excited state, it will relax to its ground state. The amount of relaxation due to the Purcell effect can be quantified through its relaxation time  $T_1^{\text{Purcell}}$ . The reason a high quality factor is important is because the Purcell relaxation time is proportional to the quality factor [5, p. 22]. The Purcell relaxation time  $T_1^{\text{Purcell}}$  places an upper limit on the relaxation time  $T_1$  of a qubit. If the qubit's relaxation time  $T_1$  is close to this value, the qubit is said to be Purcell limited.

### 0.3 LOSSES

When a resonator is being driven at its resonance frequency, it is absorbing photons from the external source. When this external driving stops, the resonator slowly loses its photons through its different loss channels.

One loss channel has already been discussed in section 0.2, namely through the coupling to the feedline. This loss channel is not unwanted, as the amount of coupling to the feedline determines how fast the resonator and feedline can interact with each other. The other loss channels, however, are unwanted. They cause dissipation of energy, and hence information. Some of the main causes of loss will be discussed in this section.

### 0.3.1 Causes of loss

#### 0.3.1.1 Two-level systems

Two-level systems (TLS) are systems which can be in a ground state or in an excited state. In some cases they can be useful. In fact a qubit itself is an example of a TLS. In other cases, however, TLS can also be a source of dissipation such as in the case of dielectric loss [6]. Study suggests that in cQED, most TLS reside in a thin oxide layer at the metal-substrate interface and the substrate-air interface [12].

Resonators are surrounded by a large quantity of TLS, each of which has its own resonance frequency, depending on its energy landscape. When the resonance frequency of a TLS is close to that of the resonator, it can absorb a photon from the resonator, upon which it tunnels to an excited meta-stable state. TLS have a finite lifetime in their excited state, after which they decay back to their ground state and are then again able to absorb a photon. The rate at which a TLS absorbs a photon depends on the electric field surrounding the TLS.

In the low power, low temperature regime, TLS reside mostly in their ground state, and only occasionally tunnel to the excited state, upon absorption of a photon. It is theorized that, in this regime, TLS are the main source of dissipation for resonators [4]. At higher powers and/or temperatures, TLS will tunnel to an excited state at a higher rate. Due to their finite lifetime they become saturated at a certain point. Since the quality factor depends on the ratio between energy stored and energy dissipated, when the TLS are saturated the amount of dissipation is limited, while the energy stored in the resonator can still increase. Therefore, in the low power, low temperature regime, increasing either of the two parameters results in an increase in quality factor. At a certain point, however, further increasing either of the two will not improve the quality factor. This is due to other effects dominating the dissipation rate in these regimes.

#### 0.3.1.2 Quasiparticles

Another source of dissipation for resonators is due to quasiparticles being present in the superconducting layer. When a Cooper-pair is broken up, Bogoliubov quasiparticles are formed [2, p. 16]. Once formed, the quasiparticles have a finite lifetime, depending on the temperature of the system. These quasiparticles can have either electron-like or hole-like properties. They are a source of dissipation for resonators, since they are non-superconducting and therefore cause the surface impedance to be slightly resistive [7, p. 18].

The breaking up of Cooper-pairs is due to excitations. These excitations can either be thermal, or due to photon absorption. Therefore an increase in temperature or an increase in photon density will result in a higher density of quasiparticles. The quasiparticle density increases exponentially with increasing temperature [7, p. 44].

#### 0.3.1.3 Radiation

A third source of dissipation is due to radiation from the resonator. This radiation is due to the spontaneous emission of photons.



The amount of dissipation due to radiation is directly related to the geometry of the resonator through [10, 7]:

$$Q_{\text{rad}} = \alpha \left( \frac{L}{s + w} \right)^{n_r} \quad (4)$$

As shown in Figure 1,  $s$  is the distance between the conducting and grounded track,  $w$  is the width of the conducting track, and  $L$  is the length of the resonator. The parameter  $\alpha$  depends on properties such as impedance and the dielectric constant of the substrate, and  $n_r$  depends on the shape of the resonator, and is equal to 2 in the case of a straight resonator. From Formula 4 it is clear that a decrease of the conducting track width or the distance between tracks leads to an increase in  $Q_{\text{rad}}$ . However, with a decrease of either of the two parameters, the field strength close to the resonator becomes higher. If the TLS are not saturated (i.e. low power and temperature), this will increase the amount of dissipation through TLS. Therefore it is not necessarily advantageous to minimize  $s$  and  $w$ .

Radiation loss becomes the dominant source of dissipation at high powers and/or temperatures, but otherwise usually is not the limiting factor. Since measurements relevant for quantum computing are usually operated at low power and temperature, this source of dissipation is usually less important than other sources, such as TLS dissipation.

#### 0.3.1.4 Vortices

When a sample is cooled down to a superconducting state there may still be a small, but nonnegligible magnetic field present. The presence of a magnetic field can cause vortices to appear in superconducting materials. These vortices have a non-superconducting core. Current passing through superconductive material exerts a Lorentz force on vortices. For a resonator being driven on resonance, this AC current results in the vortices near the resonator experiencing a dissipative oscillatory motion [9].

It is interesting to note that the presence of vortices does not necessarily lead to a lower internal quality factor. The influence of a vortex on a resonator depends on its location. As reported by Nsanzineza et al. [8], a vortex close to a current antinode of a resonator, can result in a significant loss of the quality factor. A vortex close to a current node, however, may even increase the quality factor of the resonator. They attribute this increase in quality factor to quasiparticles, which would otherwise lead to dissipation, being trapped in the vortex.

### 0.3.2 Minimizing losses

#### 0.3.2.1 Surface treatment

Previous research has determined that for resonators, TLS are mostly present at the surfaces [4]. These oxides may reside at the interface between metal and dielectric, or between the dielectric and vacuum, or possibly between metal and vacuum (depending on the type of metal used). One explanation for TLS being present is the presence of an amorphous oxide layer at the interfaces. These oxides may act as TLS. During deposition of the metal on the dielectric, this oxide layer can become trapped between the two interfaces. For a silicon

dielectric, this oxide layer can be removed by shortly treating the sample with hydrophluoric acid. This process is also known as an 'HF dip'.

Aside from the HF dip, additional surface treatment can be applied. For the resonators measured in this report, before depositing the metal on the substrate, an additional exposure to hexamethyldisilazane (HMDS) was applied. The reason for this additional step is that there is a lattice mismatch between the metal and substrate. The intermediate layer of HMDS can possibly mediate this lattice mismatch. See [3] for more information.

### **0.3.2.2 Infrared shielding**

Aside from thermal excitation, quasiparticles are also formed from the absorption of photons. High-frequency photons (UV-range or higher) are usually not a significant contribution, as they are easily absorbed by materials, well before they reach the inner layers of the fridge. Lower-frequency photons, such as in the infrared range, however, can penetrate through the fridge to the sample. These infrared photons can cause the excitation of quasiparticles. By using infrared shielding, such as a coating film inside the fridge, the amount of infrared radiation reaching the sample can be lowered.

### **0.3.2.3 Deep-reactive ion etching**

Another technique applied to the resonators studied in this report is deep-reactive ion etching (DRIE), which is a type of Bosch process [3]. In this technique two alternating steps are performed:

1. An etching step in which an  $\text{SF}_6$  plasma is used to etch the substrate layer.
2. A passivation step in which  $\text{C}_4\text{H}_8$  is released. The gas forms a protective layer on the substrate, except for the direction in which the etching plasma is accelerated. The result is that the sidewalls are protected from the etching process

Using DRIE, nearly vertical sidewalls can be created for the substrate. The result is that the substate-air interface is removed from the regions between the CPW tracks, which are the regions where the electric field strength is high. As the dissipation due to TLS depends on the electric field strength, it is expected that DRIE will result in a lower TLS dissipation rate at this interface.

### **0.3.2.4 Magnetic shielding and vortex trapping**

Vortices are created when a magnetic field is present. One method to lower the amount of vortices is to use proper magnetic shielding around the sample. Furthermore, using nonmagnetic materials also result in lower amounts of vortices being present.

Even when using these methods to counter the presence of magnetic fields, there may still be a small amount of vortices present in the sample, which may lead to dissipation. To counter their movement a grid-like structure can be added in the superconducting material, effectively pinning the vortices.

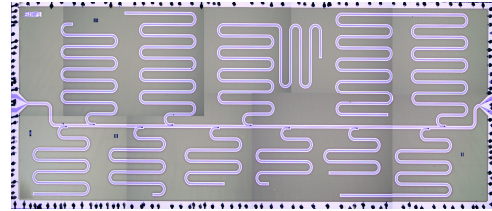
## 0.4 EXPERIMENTAL SET-UP

The fridge used in this experiment is a dilution refrigerator, made by Leiden Cryogenics. The refrigerator has a base temperature of  $\sim 15$  mK. An input signal was generated using a Rohde & Schwarz ZVM vector network analyzer, connected to an Aeroflex 8310 step attenuator, which has an attenuation range of 120 dB. The signal out of the fridge was measured using the same vector network analyzer.

Using this set-up, quarter wave resonators, fabricated by Alessandro Bruno, were measured in a frequency range between 1–9 GHz. The sample is shown in Figure 2. The resonators were made using NbTiN on a silicon substrate. The advantage of NbTiN is that the metal atoms are bound to nitrogen, thereby inhibiting bond formation with oxides. In a way to minimize losses, all resonators were treated with HMDS and deep-reactive ion etching.

By driving a signal through the feedline, the resulting transmitted signal  $S_{21}$  can be measured. At or close to the resonance frequency of a resonator, the resonator will either cause enhanced transmission (half wave resonator), or diminished transmission (quarter wave resonator).

Unless stated otherwise, all measurements were performed with the fridge at base temperature ( $\sim 15$  mK).



**Figure 2:** Optical microscopy image of the sample measured in this report. The sample consists of ten quarter wave resonators, with frequencies ranging between 1–11 GHz, connected to a central feedline. The resonators are made using NbTiN on a Si substrate. The sample is treated with HMDS and DRIE.

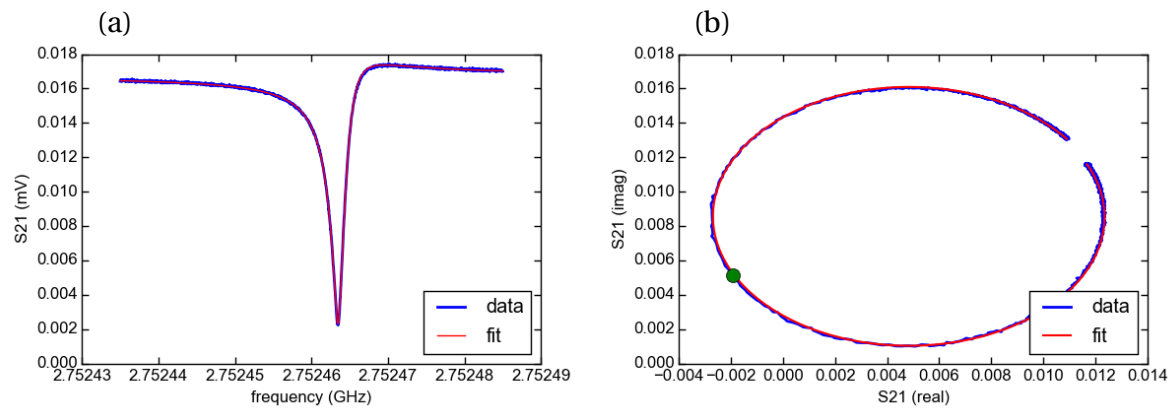
## 0.5 RESULTS AND DISCUSSION

### 0.5.1 Resonator measurement

In Figure 3 the transmission  $S_{21}$  of a resonator is shown. Figure 3(a) shows the transmitted voltage  $|S_{21}|$  of the resonator as a function of frequency. As one can see, the resonator has a shape similar to a Lorentzian dip. One interesting point is that the Lorentzian exhibits an asymmetry, which is often attributed to reflections in the feedline [5, p. 192]. This could be caused by impedance mismatching.

### 0.5.2 Power dependence

To be able to study the behaviour of the resonators, measurements were performed for several powers. Using proper calibrations for the attenuation down to the sample, the power can be converted to the input power at the sample. This value can then be converted to the mean number of photons present in the resonator [3]. The results are shown in Figure 4.



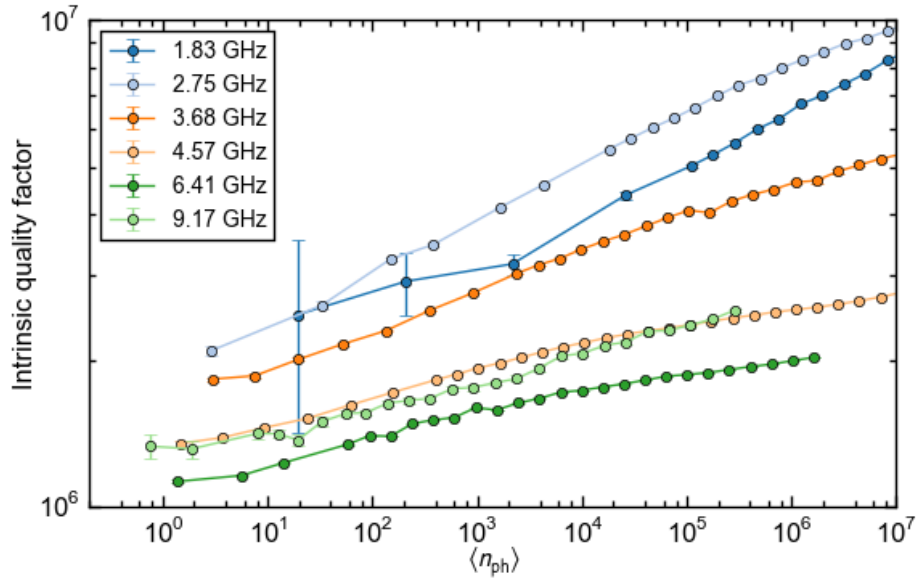
**Figure 3:** Forward transmission  $S_{21}$  spectrum of a resonator around 2.75 GHz. Panel (a) shows the amplitude of  $S_{21}$ , along with a fit (red). Panel (b) shows the path of  $S_{21}$  in the complex path, along with a fit (red). The green dot indicates the resonance frequency of the resonator. Measurement was performed at 15 mK at an input power of  $-123$  dBm corresponding to  $\sim 5 \times 10^4$  photons.

As can be seen, the internal quality factor  $Q_i$  of all resonators decrease with decreasing photon number. One explanation for this phenomenon is that the dissipation is mainly due to TLS. Since measurements were performed at  $\sim 15$  mK, the TLS are not saturated since the rate of thermal excitation is low. As discussed in section 0.3.1.1, the relative loss due to TLS is highest at low power, in the regime where they are not saturated. Therefore the fact that the internal quality factor  $Q_i$  rises with the mean number of photons present in the resonator can be attributed to a larger amount of TLS being saturated. This would suggest that, even with HMDS and DRIE treatment of the sample, at low power and temperature, the internal quality factor is still limited by TLS being present.

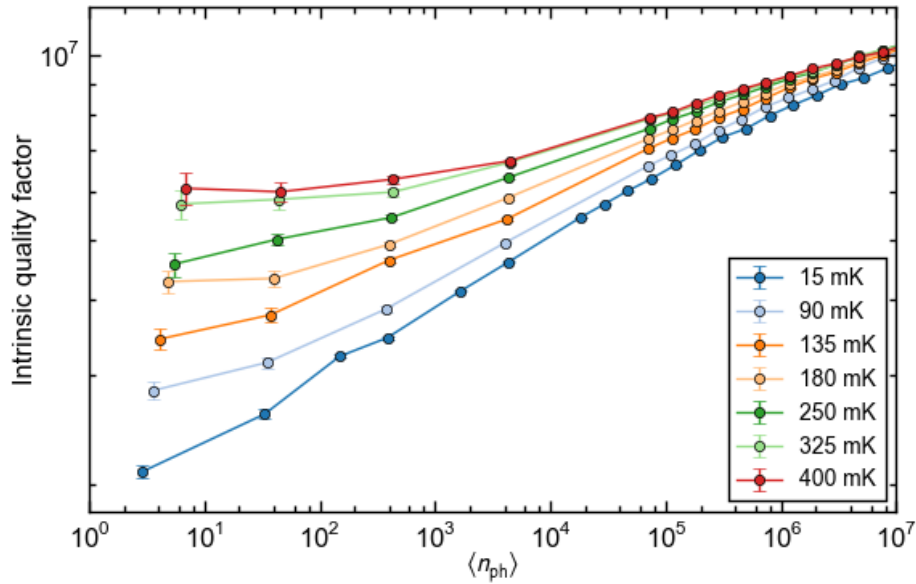
The mean photon number of a resonator is inversely proportional to the square of frequency [3], so for resonators with a low frequency a lower input power is required than with a high frequency. At high photon numbers this is not a concern, as the transmitted signal is high enough to be accurately measured in a short period of time. For the single-photon powers, however, which is the region of interest for quantum computation, acquiring enough signal took up to five hours for the lowest frequencies. The reason that for the resonator with a resonance frequency at 1.83 GHz has large error bars at low powers can be partly attributed to this, but as we will see in section A.4, the main reason is that its frequency lies outside the bandwidth of the amplifiers and circulators of the set-up, resulting in a large amount of additional noise.

### 0.5.3 Temperature dependence

Aside from power, some of the dissipation channels also depend on the temperature of the system. To be able to study the effect of temperature on resonators, the resonator with frequency 2.75 GHz has been studied as a function of power for several temperatures ranging from 15 mK up to 400 mK. The reason for choosing this resonator is that it has the highest internal quality factor of all the resonators measured, and so any change in quality factor



**Figure 4:** Intrinsic quality factor of resonators as a function of mean number of photons present in the resonator. Measurements were performed at 15 mK.



**Figure 5:** Intrinsic quality factor versus photon number for temperatures ranging from 15 mK up to 400 mK. All measurements were performed for a resonator with resonance frequency  $f_0 = 2.75$  GHz.

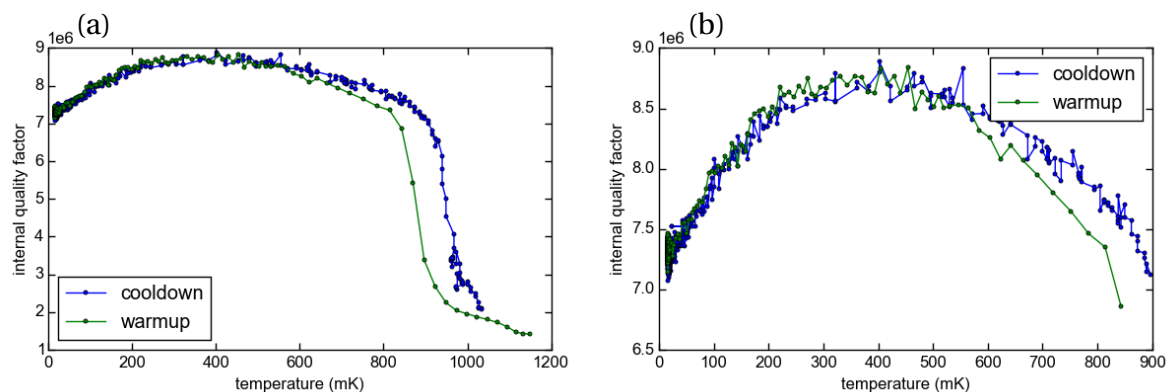
would be most clearly visible.

The results are shown in Figure 5. As can be clearly seen, the quality factor increases with increasing temperature. This is likely due to the fact that TLS are thermally excited for a larger percentage of time. Therefore, the relative energy dissipation with respect to total energy in the resonator will be lower, resulting in an increase in quality factor.

Another interesting point is that the increase in quality factor as a function of temperature is largest at low powers. This can also be explained when the limiting factor is due to TLS. With low powers, the TLS are almost exclusively excited thermally, while at higher powers, the excitation of TLS is not only due to thermal excitations, but also from photon absorption.

If one looks at the highest temperatures, it seems that the increase in quality factor as a function of temperature seems to slowly approach a saturation point. One reason is that the TLS are approaching their saturation, and so increasing the temperature further will have little effect on the percentage of time that the TLS are in the excited state. As will be shown in the next section, at 400 mK the quality factor of the resonator is close to its maximum value, and will decrease as temperature is further increased.

### 0.5.4 Temperature tracking

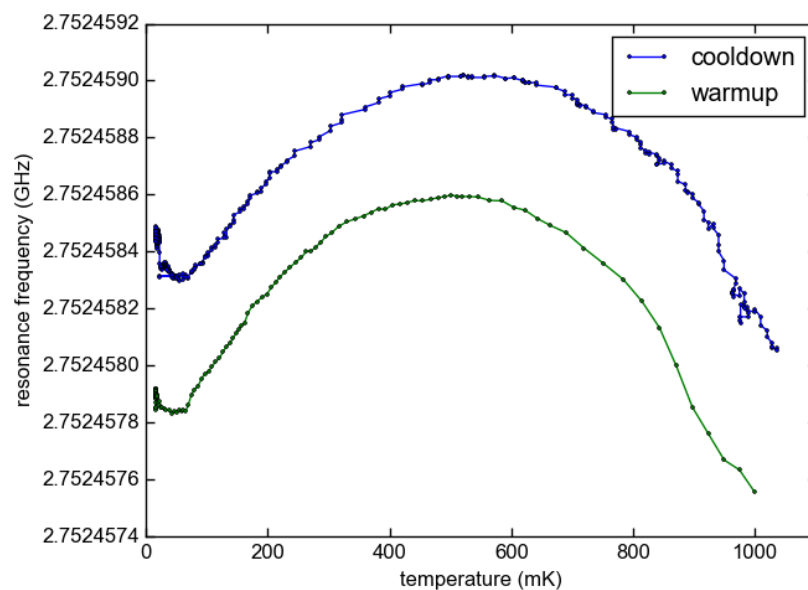


**Figure 6:** Internal quality factor versus temperature for the resonator with resonance frequency  $f_0 = 2.75$  GHz. Quality factor was continuously measured as the sample was cooled down and warmed up four days later. Panel (a) shows the full temperature range up to the helium condensation cycle. Panel (b) shows a close-up of the region until 900 mK.

To further investigate the temperature dependence of the resonator, a continuous measurement was performed on the resonator with resonance frequency 2.75 GHz during a cool-down and a subsequent warm-up of the fridge four days later. Measurements were performed for temperatures ranging from base temperature (15 mK) to roughly 1 K. Above this temperature, the fridge entered a cyclic helium condensation/evaporation process. All temperatures were measured at an input power of  $-113$  dBm, corresponding to roughly  $5 \times 10^5$  photons. In Figure 6 the internal quality factor versus temperature is shown during a cooldown and subsequent warm-up of the fridge. As can be seen, the quality factor reaches a maximum quality factor at a temperature of  $\sim 400$  mK. Below this temperature, the quality factor is likely

limited by the presence of TLS (see sections 0.5.2 and 0.5.3). Above this temperature however, the quality factor decreases, indicating that TLS are not the limiting factor anymore for  $Q_i$ . One likely explanation is that the main source of dissipation is now due to the presence of quasiparticles in the resonator. At even higher powers other effects, such as vortices and enhanced radiation, contribute more and more significantly to the decay of the quality factor.

From Figure 6 it seems that there is some hysteresis at high temperatures. However, this is likely due to the fact that the thermometer is at a different position in the fridge as the sample, and does not thermalize equally fast. There may therefore be a delay between the temperature of the thermometer, and the actual temperature of the sample.



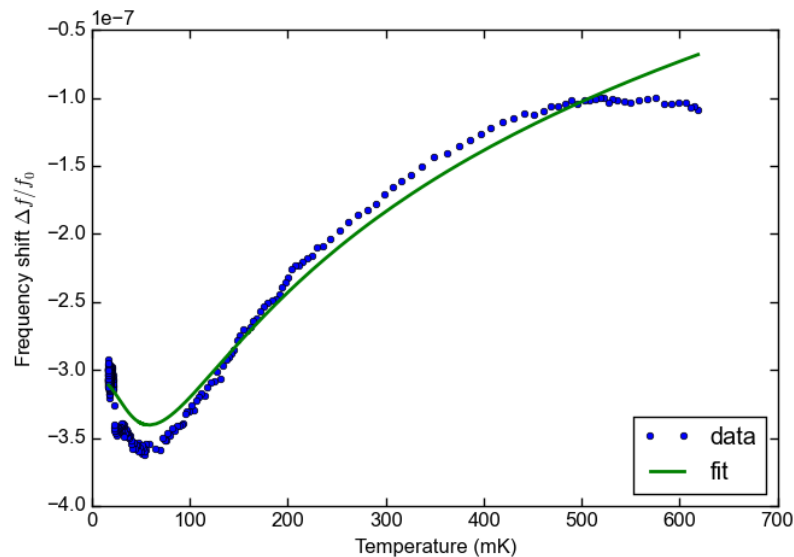
**Figure 7:** Resonance frequency versus temperature during a cooldown and subsequent warm-up four days later. In the period between cooldown and warm-up the resonance frequency has shifted by  $\sim 500$  Hz, possibly due to phase noise.

Aside from the internal quality factor, another quantity of interest is the resonance frequency  $f_0$  of the resonator, which also depends on the temperature. The result from tracking the resonance frequency of the resonator during cooldown and subsequent warm-up is shown in Figure 7. As can be seen in both cases, the resonance frequency reaches a maximum around 500 mK.

Between the cooldown and warm-up the resonance frequency seems to have shifted by roughly 500 Hz. As the sample was kept at 15 mK, it is unlikely that this decrease in resonance frequency is due to degradation of the sample. One possible explanation is that this change in resonance frequency is due to phase noise, which is known to shift the resonance frequency of the resonator. Further measurements are, however, required to determine if this is the case.

The decrease in resonance frequency at higher temperatures can be explained by the presence of quasiparticles, which increase the kinetic inductance [5, p. 91]. The resonance

frequency is inversely proportional to the square root of the total conductance [1], and so an increase in kinetic inductance leads to a decrease in resonance frequency. For measurements done by Barends et al. [1], the change in resonance frequency due to changes in the kinetic inductance seem to roughly correspond with the decrease in center frequency measured in Figure 7.



**Figure 8:** Frequency shift versus temperature for low temperatures, along with fit (green). The fit was performed using the model by Gao et al. [4]. The fit corresponds well with data, even describing the frequency peak at the lowest temperatures.

The decrease in resonance frequency at lower temperatures can be explained due to TLS still being present. A model is presented by Gao et al. [4], in which they describe the decrease in resonance frequency due to the presence of TLS. As can be seen in Figure 8 the model corresponds well with the data at low temperatures. At higher temperatures the model deviates from data, which may be explained by quasiparticles dominating as source of dissipation. An interesting thing to note is that an increase in resonance frequency was predicted at the lowest temperatures, but as they did not reach temperatures sufficiently low they could not confirm this effect. In Figure 8 however, this increase in resonance frequency is observed. This supports the claim that at low temperatures the resonator is still limited by TLS, even after treatment of HMDS and DRIE.

## 0.6 CONCLUSION AND FUTURE WORK

Since the quality factor of all resonators is found to decrease with decreasing input power, this indicates that at low temperatures and powers the limiting factor is still due to TLS. The fact that the quality factor initially increases with higher temperatures, supports this claim. By also measuring the resonance frequency as a function of temperature, the curve obtained is



in good agreement with a model describing the resonance frequency shift due to TLS [4]. The curve even shows an increase in resonance frequency at the lowest temperatures, which was also predicted by the model. These results suggest that even after HMDS surface treatment and deep-reactive ion etching was applied, the internal quality factor of the resonator at low temperatures and power is still limited by the presence of TLS.

Nevertheless, As shown by Bruno et al. [3], the application of HMDS surface treatment and DRIE resulted in an improvement of the internal quality factor of the resonators by almost an order of magnitude. More research must be done to determine at what interface the dissipation due to TLS is greatest after these two treatments.

The next step is to perform the same treatments (HMDS and DRIE) on transmon qubits, to study what the influence will be on coherence times.

# **Appendices**

# Appendix A

## Noise

When performing measurements one is faced with the reality that no component is ideal. When a signal passes through the different parts of a set-up, noise is constantly being added. Noise is the term given for all the random fluctuations that are added to the signal. These fluctuations are the cumulative result of several noise source contributions.

Thermal noise is one of the most common sources of noise. It is the result of the random thermal fluctuations of electrons. It is an example of frequency-independent noise, also known as white noise. Noise sources can also be frequency-dependent, such as TLS, as discussed in Chapter I. This is an example of  $1/f$ -noise: the amount of noise added increases with decreasing frequency. In fact, truly frequency-independent noise does not exist, as even white noise has been observed to decrease at extremely high frequencies ( $\sim 10^{15}$  Hz). At these frequencies a quantum correction needs to be added [11, p. 50].

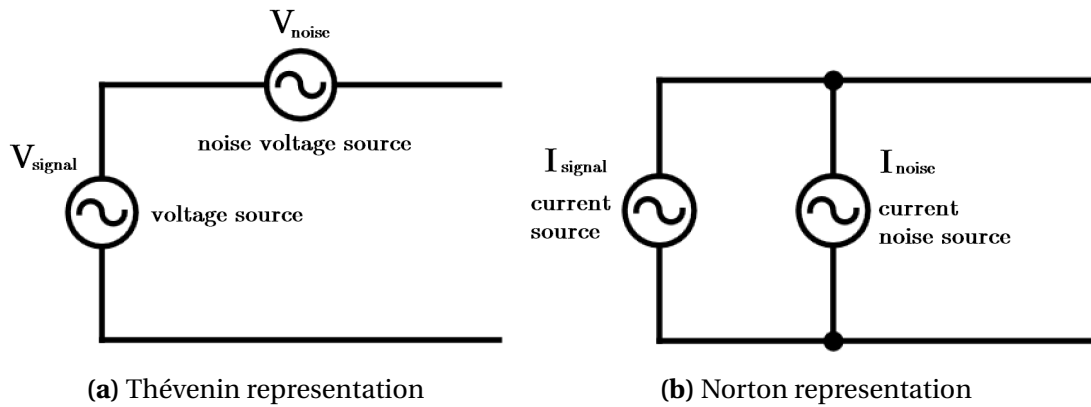
When performing measurements one important question to ask is how much noise is being contributed to the signal. In this chapter a model is presented for the general set-up used for measuring superconducting resonators and qubits. Using this model it is possible to characterize the amount of noise by determining its associated noise temperature. Finally, this model is applied to the set-up used to characterize the resonators presented in Chapter I.

### A.1 CHARACTERIZING NOISE

#### A.1.1 Circuit representations

There are two circuit representations in which we can depict a system with a noise contribution: The Thévenin representation, and the Norton representation. In the Thévenin representation we can model the system as a voltage source, and the noise added to the system is a noise voltage source connected in series. In the Norton representation the system is a current source and the noise added is a noise current source connected in parallel to the current source. These two representations are identical and can be converted to each other. In this section we will adopt the Thévenin representation, and so the signal will be a voltage source combined in series with a noise voltage source.

Assuming the signal to be at a fixed frequency  $\omega$  and amplitude  $A$ , the combined voltage



**Figure A.1:** Two equivalent representations of a system containing noise. Panel (a) shows the Thévenin representation, in which a noiseless voltage source is connected in series with a noise voltage source. Panel (b) shows the Norton representation, in which a noiseless current source is connected in parallel with a noise current source.

$v(t)$  is then given by:

$$v(t) = v_{\text{signal}}(t) + v_{\text{noise}}(t) = A \cos \omega t + v_n(t) \quad (\text{A.1})$$

Note that the mean value of the noise voltage  $\overline{v_n}$  is equal to zero. The amount of noise can be quantified by the root-mean square noise voltage  $v_n^{\text{rms}}$ :

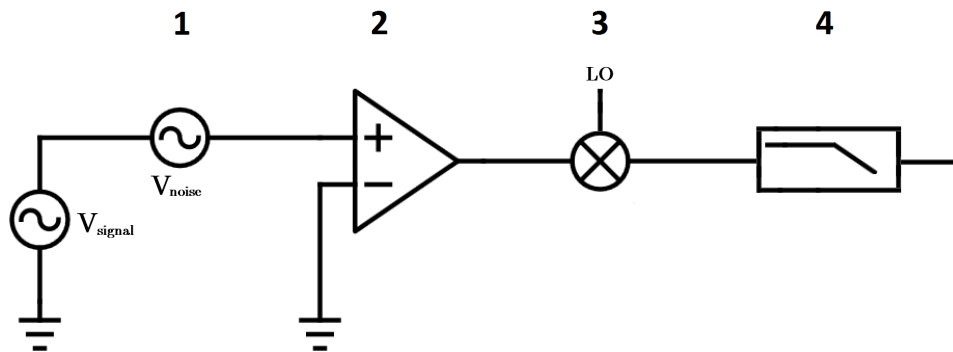
$$v_n^{\text{rms}} = \sqrt{\overline{v^2} - \overline{v}^2} = \sqrt{\overline{v_n^2}} \quad (\text{A.2})$$

### A.1.2 Noise power spectral density

One way of quantifying the noise of the system is through the noise power spectral density  $S(f)$ , which is the distribution of noise power per unit bandwidth as a function of frequency. For the Thévenin representation, the noise spectral density is defined in terms of voltage. When the only noise in the system is white noise, the spectral density is independent of frequency. It is then given by:

$$S = \frac{\overline{v_n^2}}{\Delta f} \quad [\text{V}^2/\text{Hz}] \quad (\text{A.3})$$

In this equation  $\Delta f$  is the noise bandwidth. This is the bandwidth over which the noise is measured.



**Figure A.2:** Schematic representation of the measurement set-up including a noise source.

## A.2 THE MODEL

As shown in the schematic in Figure A.2, we can model our set-up as a combination of four elements:

1. A noise source.
2. An amplifier to amplify the weak signal exiting the fridge.
3. A mixer to downconvert the signal.
4. A low-pass filter to remove unwanted high-frequency signal.

### A.2.1 Noise source

Using the Thévenin model, we can approximate the components up to the first amplifier in the fridge as a voltage source, with a noise voltage source connected in series.

We can include the noise added by the amplifier in the noise voltage source, in which case we assume the amplifier to be ideal. Furthermore, we assume the signal to be amplified sufficiently, such that the mixer and low-pass filter add a negligible amount of noise. We also ignore effect such as mixer leakage. With these assumptions all of the noise is originated from the noise voltage source.

We can associate an effective noise temperature to the noise voltage source. The noise temperature is defined as the temperature at which a resistor would produce an equal amount of noise. Note that, since we are comparing the system to a resistor, the noise needs to have an (approximately) white spectrum.

According to Nyquist's theorem [11, p. 47], if the system experiences white noise, and is in thermal equilibrium, the root-mean square noise voltage  $v_n^{\text{rms}}$  is given by:

$$v_n^{\text{rms}} = \sqrt{v_n^2} = \sqrt{4k_B T R \Delta f} \quad (\text{A.4})$$

In this equation  $\Delta f$  is the bandwidth over which the noise is integrated,  $k_B$  is the Boltzmann constant,  $T$  is the noise temperature of the noise source, and  $R$  is the impedance of

the system. We see that the noise added depends linearly on the bandwidth over which is integrated.

Combining Equations A.3 and A.4, the noise power spectral density  $S_{v_n}$  can be rewritten as:

$$S = \frac{\overline{v_n^2}}{\Delta f} = 4k_B T R \quad (\text{A.5})$$

### A.2.2 Amplification

During the amplification stage both the signal and the noise is amplified by the same amount. This amount of amplification is determined by the gain  $G$ , which is defined as the ratio between the output voltage and the input voltage:

$$G = \frac{V_{\text{out}}}{V_{\text{in}}} \quad (\text{A.6})$$

According to the maximum power transfer theorem, the maximum power transfer between a source and load occurs when the impedances of source and load are matched, in which case half of the power is transferred. From this it follows that in the amplification process half of the signal is dissipated. However, as  $G$  is defined as the ratio between  $v_{\text{out}}$  and  $v_{\text{in}}$  (Equation A.6), the factor  $\frac{1}{2}$  is included in  $G$ .

During amplification not only the signal is amplified with gain  $G$ : the noise is amplified by the same amount. Defining the noise power spectral density before amplification as  $S^{\text{in}}$ , and after amplification as  $S^{\text{out}}$ , the following relation holds:

$$S^{\text{out}} = G^2 S^{\text{in}} = G^2 4k_B T R \quad (\text{A.7})$$

Note that in Equation A.7, the gain  $G$  is squared. This is due to the fact that the noise power spectral density depends quadratically on the root-mean square noise voltage (Equation A.3).

In our actual set-up the amplification occurs in multiple stages. Aside from amplifying the signal and its noise, at each stage additional noise, originating from the amplifier itself, is added as well. This added noise is then also amplified in the next amplification stage. Therefore it is always best to have the amplifier with highest gain and lowest noise temperature as the first amplifier in the chain. For more information see Friis formula [11, p. 103].

### A.2.3 Downconversion

After amplification the frequency  $\omega$  of the signal is still in the GHz range. In homodyne or heterodyne detection the signal is downconverted to DC (homodyne) or to a lower frequency (heterodyne), such that it can be measured more easily. To downconvert the signal, it is mixed in a mixer with a local oscillator (LO) signal having the same frequency  $\omega$  (homodyne) or a slightly higher frequency  $\omega + \Delta\omega$  (heterodyne). The mixer effectively multiplies the two signals. If the signal exiting the amplifier is given by  $v(t) = A \cos \omega t$ , then, ignoring a possible phase difference, the signal at the output of the mixer is given by:

$$\begin{aligned}
v(t) \cdot \cos \omega t &= A \cos \omega t \cdot \cos (\omega + \Delta \omega) t \\
&= \frac{1}{2} A [\cos (2\omega + \Delta \omega) t + \cos \Delta \omega t]
\end{aligned} \tag{A.8}$$

As can be seen from Equation A.8, the output signal contains both the sum and the difference of the two signals. However, as the sum of both frequencies is in the GHz range, it can be filtered out using a low-pass filter, leaving only the downconverted signal, which is the result of the difference between the two frequencies. Note that the amplitude of the signal is reduced by a factor two. The noise amplitude is also reduced by a factor 2. Furthermore, in the case of a homodyne set-up, the difference signal is simply a DC signal ( $\Delta \omega = 0$ ), while in the case of heterodyne the signal still contains a slow frequency  $\Delta \omega$ . For simplification we assume our set-up to be a homodyne set-up, although the result is similar in the case of a heterodyne set-up.

### A.2.4 Low-pass filtering

In the case of homodyne detection the signal at the frequency of interest is downconverted to DC. However, the signal at other frequencies have not disappeared; in the mixer these have also shifted in frequency. Since the signal of interest is at DC, a low-pass filter can be used to filter out signal above a certain frequency.

The frequency above which a low-pass filter will filter out the signal is defined by its cut-off frequency  $f_c$ . The cut-off frequency  $f_c$  is the frequency at which the signal is attenuated by 3 dB. For first-order low-pass filters the noise bandwidth  $\Delta f$  is related to the filter cut-off frequency  $f_c$  by [11, p. 81]:

$$\Delta f = \frac{\pi}{2} f_c \tag{A.9}$$

## A.3 NOISE TEMPERATURE

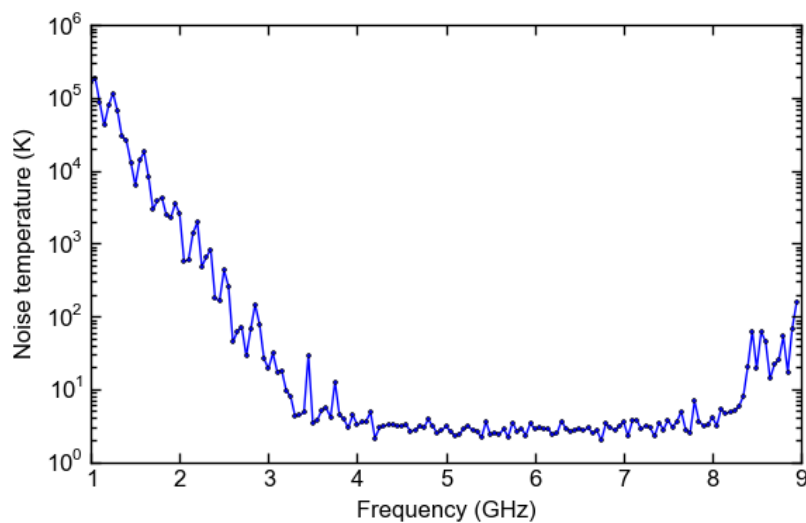
In the previous sections the influence of each of the components on the signal and on the noise has been analyzed. Using this information it is possible to determine the signal-to-noise ratio (SNR), which is the ratio between the average power of the signal and the average power of the noise. The SNR is a measure for how well a signal can be separated from the noise, and is given by:

$$\begin{aligned}
\text{SNR} &= \frac{\overline{v_{\text{out}}}^2}{\overline{v_n}^2} = \frac{1/4 G^2 \overline{v_{\text{in}}}^2}{S_{v_n}^{\text{out}} \Delta f} \\
&= \frac{1/4 G^2 \overline{v_{\text{in}}}^2}{G^2 S_{v_n}^{\text{in}} \frac{\pi}{2} f_c} \\
&= \frac{\overline{v_{\text{in}}}^2}{2 \pi k_B T R f_c}
\end{aligned} \tag{A.10}$$

Note that the factor  $1/4$  is because the amplitude is lowered by a factor of 2 due to mixing. Equation A.10 can be rewritten such that we have an expression for the noise temperature of the system:

$$T = \frac{\overline{v_{in}}^2}{2 \pi k_B R f_c \text{SNR}} \quad (\text{A.11})$$

## A.4 RESULTS



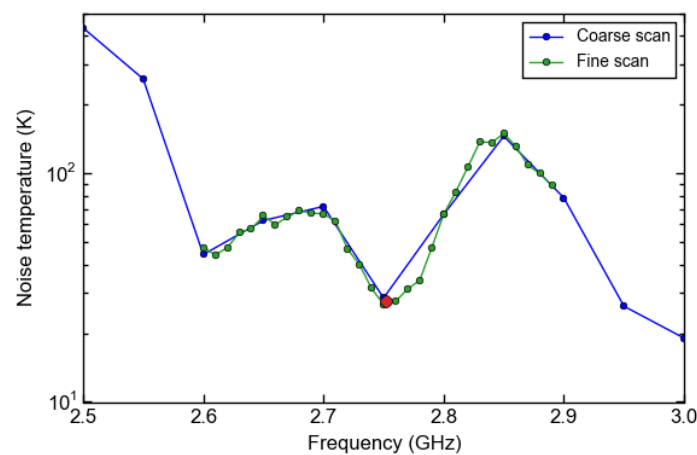
**Figure A.3:** Noise temperature versus frequency. The noise temperature has been calculated for 160 frequencies in the range 1–9 GHz. For each frequency 2001 points were measured, from which the signal, noise, SNR, and noise temperature was determined. Measurements were performed at an input power of  $-113$  dBm and an IF bandwidth of  $\Delta f = 300$  Hz.

Using the Rhode & Schwarz ZVM vector network analyzer, The transmission has been measured for 160 equidistant frequencies in the range 1–9 GHz. For each frequency a total of 2001 points was measured with an IF bandwidth  $\Delta f = 300$  Hz. From these measurements the signal-to-noise ratio has been determined for each frequency. With knowledge of the SNR, the noise temperature has then been determined as a function of frequency using Equation A.11 . The result is shown in Figure A.3.

From Figure A.3 it is clear that the noise temperature is highly temperature-dependent. In the frequency range 4–8 GHz the noise temperature is quite low, never reaching above 10 K. This is exactly the bandwidth of the cryogenic low-noise amplifier by Low Noise Factory, which is the first amplifier in the amplification chain. From the specifications of the amplifier, the noise temperature of the amplifier has been calculated at an ambient temperature of 8 K, and equals roughly 4 K for the entire bandwidth. Comparing the amplifier specifications with Figure A.3, it is likely that in the frequency range 4–8 GHz the first amplifier is the component contributing most to the total noise temperature.



Outside the 4–8 GHz frequency band, however, the noise temperature rapidly increases. This is partly due to the frequency lying outside of the bandwidth of the amplifier, in which case the amplification will be lower. However, this is not an adequate explanation for the fact that the noise temperature increases to several hundred thousand Kelvin. The reason for this unrealistic noise temperature is that in our model we did not take into account the noise added by components after the amplifier. While the gain of the amplifier decreases outside its bandwidth, the components after the amplification will still add the same amount of noise. When the gain decreases by a significant amount, the relative contribution of these post-amplification noise sources will increase. Furthermore the assumption that the noise spectrum is white is no longer correct at low frequencies, where  $1/f$  noise starts to contribute.



**Figure A.4:** Detailed scan of noise temperature versus frequency in the range 2.6–2.9 GHz. The resonator with  $f_0 = 2.75$  GHz (red dot) seems to reside at a local minimum of the noise temperature.

From Figure A.3 it can be seen that the noise temperature can vary by a large amount between consecutive points. To determine whether this variation is due to a large uncertainty, or due to the noise temperature actually fluctuating strongly with varying frequency, a more detailed scan has been performed in the frequency region 2.6–2.9 GHz, in which one resonator has a resonance frequency. The result is shown in Figure A.4. As the curve of the detailed scan follows the curve of the coarse scan pretty closely, it can be concluded that the noise temperature of the system in fact fluctuates quite strongly with varying frequency.

Another point of interest is that the resonance frequency of the resonator lies near the local minimum of the noise temperature in that region. This is quite a stroke of luck, as a slightly higher or lower frequency would have resulted in a much higher noise temperature.

## A.5 CONCLUSION AND FUTURE WORK

The noise temperature gives us an estimate of the noise added to the system. It has been shown that the noise temperature can fluctuate strongly with varying frequency. In the model used to estimate the noise temperature it has been shown that outside the bandwidth of the

amplifier the model breaks down. At this point the noise added by the components after the amplification, and indeed even the amplifiers themselves, needs to be taken into account to obtain accurate estimates of the noise temperature.

However, even outside of the bandwidth of the amplifier, there are frequency regions in which the noise temperature may still be acceptable. It is therefore a good idea to initially perform measurements of the noise temperature of the set-up. This will give an indication of the signal-to-noise ratio, from which accurate estimates can be made as to what the amount of measurement time is needed to obtain a desired SNR.

The noise temperature measurements were performed using the Rhode & Schwarz ZVM vector network analyzer. It would be interesting to see how other measurement set-ups would compare to the vector network analyzer. One interesting candidate would be a heterodyne detector. However, as the vector network analyzer can also measure phase, a fair comparison would also require the heterodyne detector to be able to measure the phase. This heterodyne detector is currently being set up, and will hopefully soon yield interesting results.

Aside from only comparing the noise temperature, other properties are also important when comparing two set-ups. One of these is the duty cycle, which is the percentage of time actually spent measuring. For the vector network analyser the duty cycle seems to be around 50%, provided that a single measurement sweep takes at least a few seconds. Other set-ups may therefore offer an improvement in the duty cycle. Furthermore, properties such as phase stability and uncertainty would also be interesting to compare.

Another interesting measurement would be to see if the noise temperature as a function of frequency remains the same in future cooldowns, and for different samples.

# Appendix B

## Additional notes

### B.1 QUBIT CHARACTERIZATION

#### B.1.1 Part I: Continuous-wave measurements

##### B.1.1.1 Powersweep

- If the resonator seems to disappear after the transition from dressed frequency to bare frequency (or vice versa), this is likely due to the qubit being extremely close to the resonator, and so the frequency shift is large.

##### B.1.1.2 Spectroscopy

- If the deviation in transmission becomes less due to more detuning, increasing the power can also increase the contrast.

#### B.1.2 Part I: Time-domain measurements

##### B.1.2.1 AllXY

TODO:

- Table of AllXY pulses

# **Appendix C**

## **Algorithms**

### **C.1 TRACKED SPECTROSCOPY**

- Information may lie in amplitude or in phase, or in a combination of the two. For most accurate measure, calculate distance from ground state.

### **C.2 PEAK FINDING**

#### **C.2.1 Normal peak finder**

#### **C.2.2 Derivative peak finder**

### **C.3 COMPILED RB?**

# Bibliography

- [1] R Barends, HL Hortensius, T Zijlstra, JJA Baselmans, SJC Yates, JR Gao, and TM Klapwijk. Contribution of dielectrics to frequency and noise of nbtin superconducting resonators. *Applied Physics Letters*, 92(22):223502, 2008.
- [2] Rami Barends. *Photon-detecting superconducting resonators*. PhD thesis, Delft University of Technology, 2009.
- [3] A. Bruno, G. de Lange, K. van der Enden, S. Asaad, N. Langford, and L. DiCarlo. Extending single-photon relaxation time in superconducting resonators by surface treatment and deep etching of silicon substrates. Unpublished.
- [4] Jiansong Gao, Miguel Daal, Anastasios Vayonakis, Shwetank Kumar, Jonas Zmuidzinas, Bernard Sadoulet, Benjamin A Mazin, Peter K Day, and Henry G Leduc. Experimental evidence for a surface distribution of two-level systems in superconducting lithographed microwave resonators. *Applied Physics Letters*, 92(15):152505–152505, 2008.
- [5] Kurtis L. Geerlings. *Improving Coherence of Superconducting Qubits and Resonators*. PhD thesis, Yale University, 2013.
- [6] John M Martinis and A Megrant. Ucsb final report for the csq program: Review of decoherence and materials physics for superconducting qubits. *arXiv preprint arXiv:1410.5793*, 2014.
- [7] Benjamin A. Mazin. *Microwave Kinetic Inductance Detectors*. PhD thesis, California Institute of Technology, 2004.
- [8] I Nsanzineza and BLT Plourde. Trapping a single vortex and reducing quasiparticles in a superconducting resonator. *arXiv preprint arXiv:1405.0256*, 2014.
- [9] Britton Plourde, C Song, TW Heitmann, MP DeFeo, and Kang Yu. Microwave response of vortices in superconducting thin films of re and al. 2009.
- [10] Jeremy M Sage, Vladimir Bolkhovsky, William D Oliver, Benjamin Turek, and Paul B Welander. Study of loss in superconducting coplanar waveguide resonators. *Journal of Applied Physics*, 109(6):063915, 2011.
- [11] Gabriel Vasilescu. *Electronic noise and interfering signals: principles and applications*. Springer, 2006.

- [12] J Wenner, R Barends, RC Bialczak, Yu Chen, J Kelly, Erik Lucero, Matteo Mariani, A Megrant, PJJ O'Malley, D Sank, et al. Surface loss simulations of superconducting coplanar waveguide resonators. *Applied Physics Letters*, 99(11):113513, 2011.