

DELFT UNIVERSITY OF TECHNOLOGY

MASTER THESIS

THREE MONTH REPORT

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January 11, 2015

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INTRODUCTION

The subject of my Master's thesis will be on ways of improving T1 and T2 coherence times for qubits. The past few months I have been learning about superconducting circuit quantum electrodynamics. I have learned what set-ups are used for performing measurements on cQED samples, and about the types of measurements that are performed.

Traditionally the measurements were performed using Labview software. However, in the months that I have been working in the DiCarlo lab, a transition in measurement software has taken place from Labview to the Python-based QTLab. I have been very involved in this transition, as an important part of my research will be to characterize a sample quickly and accurately. This will enable a fast cycle from sample fabrication to characterization, hopefully leading to rapid progress in the development of quantum computing using cQED.

The past few weeks the focus of my measurements has shifted towards the characterization of resonators. This is largely due to the fact that two of my colleagues, Alessandro Bruno and Gijs de Lange, are working on a paper on ways of improving the quality factor of resonators. A large part of the data was already obtained before I joined the group, but a last set of measurements was required using the dilution refrigerator I most often operate at. The reason is that its base temperature is at 15 mK, which is considerably lower than the base temperature of the refrigerator at which the other measurements were performed, namely 250 mK. Because my focus so far has been more on resonators than on qubits, the main topic of this report will be on resonators, and I will include the topic of qubits in my final thesis.

As I have spent a large part of my time at the lab performing measurements, I would also like to discuss this topic in my three month report. I will treat the types of set-up I have used so far, and the techniques used for measuring resonators.

Because the relevant regime where resonators interact with qubits is the single-photon regime, a very weak signal must be applied to determine its properties in that regime. At this point noise becomes a relevant issue. I will therefore also devote a section of this report on the subject of noise.

Chapter 1

Resonators

Possible additional topics:

- Material (Silicon, sapphire)
- Superconducting material NbTiN. Advantage is that
- Asymmetry (can refer to [9, p. 192])
- Lorentzian shape

Types of resonators studied:

- Halfmon
- DRIE resonators

When a signal enters a fridge it is attenuated in several stages and eventually enters the sample being measured. In the sample the signal travels through a feedline. One or more resonators can then be capacitively coupled to the feedline. Qubits can then also be capacitively coupled to the resonators, and a resonator can even be used to connect qubits, a so-called 'bus'. However in this report only discuss the resonators connected to a central feedline will be discussed.

1.1 COPLANAR WAVEGUIDE

In the context of circuit QED, one of the most common types of resonators are coplanar waveguides (CPW). Coplanar waveguides consist of a long central conducting track, with on both sides a neighbouring grounded track. The conducting track is separated from the grounded tracks by a fixed distance.

One end is usually capacitively coupled to a feedline and has an open end, while the other end can either be open or shorted. This determines whether the resonant frequencies have a node or an antinode at that end. In the case of a shorted end, the resonant frequencies have a node at that end, resulting in a $1/4 - \lambda$ resonator. This means that the wavelength fundamental mode fits $1/4$ times into the resonator. In the case of an open end, the resonant frequencies have an antinode at that end, resulting in a $1/2\lambda$ resonator.

1.2 QUALITY FACTOR

One important property of a resonator is its quality factor. Generally speaking, the quality factor of a resonator determines the ratio between energy stored in a resonator and the energy leaking away from the resonator. For cQED resonators this corresponds to the rate at which photons dissipate from the resonator. A high quality factor corresponds to a low dissipation rate.

The quality factor can also be defined as [13, p. 23]:

$$Q = \omega_0 \tau_1 \quad (1.1)$$

Here ω_0 is the resonance frequency of the resonator, and τ_1 is the decay time of the resonator. The decay time is the time taken by a resonator to dissipate its energy to $1/e$ of its original energy. One can see that this definition is in accordance with the first definition, as the energy is related to frequency through the Planck-Einstein relation: $E = \hbar\nu$, and therefore increases with increasing frequency.

$$Q = \omega_0 / \Delta\omega \quad (1.2)$$

Photons can dissipate from the resonator through its different loss channels. Each of these loss channels has a corresponding quality factor. One such loss channel is due to resonators in cQED being capacitively coupled to a feedline. The quality factor associated to this loss channel is known as the coupling quality factor Q_c . This coupling quality factor depends on the amount of capacitive coupling between the resonator and the feedline. It can therefore be engineered to have a certain value, depending on the amount of interaction wanted between resonator and feedline.

The other loss channels are usually unwanted, and therefore desired to be as low as possible. These individual channels are usually lumped together, resulting in a combined quality factor, known as the intrinsic quality factor Q_i .

The total quality factor of the resonator is known as the loaded quality factor Q_l . It is related to Q_c and Q_i through:

$$\frac{1}{Q_l} = \frac{1}{Q_c} + \frac{1}{Q_i} \quad (1.3)$$

From equation 1.3 it can be seen that if the difference between Q_c and Q_i is large, then the loaded quality factor Q_l will be approximately equal to the minimum of the two.

For a $1/4 - \lambda$ resonator the amplitude of transmission has a minimum S_{21}^{min} , given by [13, p. 29]:

$$S_{21}^{min} = \frac{Q_c}{Q_c + Q_i} \quad (1.4)$$

With knowledge of the resonant frequency ω_0 , the resonant width $\Delta\omega$, and the transmitted signal at resonance S_{21}^{min} , it is possible through equations 1.2 and 1.4 to determine both the coupling quality factor Q_c and the intrinsic quality factor Q_i . Note that as equation 1.4 depends on the ratio of the two quality factors, to get an accurate estimate of both quality factors, they should have a comparable value.

- $\tan \delta$: loss channels, sum?
- Photon number dependence
- nonlinear effects (can refer to [1])

1.3 LOSSES

When a resonator is being driven at its resonance frequency, it is absorbing photons from the external source. When this external driving stops, the resonator slowly loses its photons through its different loss channels.

One loss channel was already discussed in section 1.2, namely through the coupling to the feedline. This loss channel is not unwanted, as the amount of coupling to the feedline determines how fast the resonator and feedline can interact with each other. The other loss channels, however, are unwanted. They cause dissipation of information. Some of the main causes of loss will be discussed in this section.

1.3.1 Causes of loss

1.3.1.1 Two-level systems

Two-level systems (TLS) are systems which can be in a ground state or an excited state. In some cases they can be useful, such as in the case of a qubit. In other cases, however, TLS can also be a source of dissipation. In cQED TLS which cause dissipation are most often oxides residing in amorphous materials (TODO: ref). In fact, study suggests that most TLS reside in a thin oxide layer at the interface between two substances (TODO: ref).

Resonators are surrounded by a large quantity of TLS, each of which has its own resonance frequency, depending on its energy landscape. When the resonance frequency of a TLS is close to that of the resonator, it can absorb a photon from the resonator, upon which it tunnels to an excited meta-stable state. TLS have a finite lifetime in their excited state, after which they decay back to their ground state.

In the low power, low temperature regime, TLS reside mostly in their ground state, and only occasionally tunnel to the excited state, upon absorption of a photon. It is theorized that, in this regime, TLS are the main source of dissipation for resonators [8]. At higher powers and/or temperatures, TLS will tunnel to an excited state at a higher rate. Due to their finite lifetime they become saturated at a certain point. Since the quality factor depends on the ratio between energy stored and energy dissipated, when the TLS are saturated the amount of dissipation is limited, while the energy stored can still increase. Therefore, in the low power, low temperature regime, increasing either of the two parameters results in an increase in quality factor. At a certain point, however, further increasing either of the two will not improve the quality factor. This is due to other effects dominating in these regimes.

- To our knowledge, dielectric loss at low temperature arises from the presence of two-level states (TLS) formed by random bonds that tunnel between two sites. [12]

- Mostly reside at surface [8]
- 1/f noise [5]
- Dielectric materials (Table [12])

1.3.1.2 Quasiparticles

Another source of dissipation for resonators is due to quasiparticles being present in the superconducting layer. When a Cooper-pair is broken up, Bogoliubov quasiparticles are formed. These quasiparticles can have either electron-like or hole-like properties. Quasiparticles are a source of dissipation for resonators, since they are non-superconducting and therefore cause the surface impedance to be slightly resistive [13, p. 18].

The breaking up of Cooper-pairs is due to excitations. These excitations can either be thermal, or due to photon absorption. Therefore an increase in temperature or an increase in photon density will result in a higher density of quasiparticles.

- Quasiparticle excitation energy $E = \xi^2 + \Delta^2$, where ξ is the energy of the single particle in the normal state relative to the Fermi energy [3]
- Increases with increasing frequency
- ?Non-superconducting, thereby causing dissipation
- removal by infrared filter
- Decreases exponentially as the temperature decreases [13, p. 19?]
- Quasiparticles are created through thermal excitation, but can also be excited by photons with $h\nu > 2\Delta$ [7]
- Quasiparticles change the surface impedance of resonators, which can be measured. This technique is used to create MKID detectors [7]
- "[Surface impedance] change is caused by quasiparticles blocking the Cooper pairs from occupying some of the electron states (through the exclusion principle), which modifies the effective pairing energy and reduces the density of pairs." [13, p. 3]
- A lot of information in thesis by Lutchyn [11]

1.3.1.3 Radiation

A third source of dissipation is due to radiation from the resonator. This radiation is due to the spontaneous emission of photons.

The amount of dissipation due to radiation is directly related through [15, 13]:

$$Q_{rad} = \alpha \left(\frac{L}{S + W} \right)^{n_r} \quad (1.5)$$

In this formula S is the distance between the conducting and grounded track, W is the width of the conducting track, α depends on properties such as impedance and the dielectric constant of the substrate. From Formula 1.5 it is clear that a decrease of the conducting track width or the distance between tracks leads to an increase in Q_{rad} . However, with a decrease of either of the two parameters, the field strength close to the resonator becomes higher. If the TLS are not saturated (i.e. low power and temperature), this will increase the amount of dissipation through TLS. Therefore it is not necessarily advantageous to minimize S and W .

Radiation loss becomes the dominant source of dissipation at high powers and/or temperatures, but otherwise usually is not the limiting factor. Since measurements relevant for quantum computing are usually operated at low power and temperature, this source of dissipation is usually less important than other sources, such as TLS dissipation.

- Possible other useful sources: [6] [10]

1.3.1.4 Vortices

- Trapped vortices cause parts to be non-superconducting
- Combatting trapped vortices with grid-like structure

1.3.2 Minimizing losses

1.3.2.1 Surface treatment

Previous research has determined that for resonators, TLS are mostly present at the surfaces [8]. These oxides may reside at the interface between metal and dielectric, or between the dielectric and vacuum, or possibly between metal and vacuum (depending on the type of metal used). One explanation for TLS being present is the presence of an amorphous oxide layer at the interfaces. These oxides may act as TLS. During deposition of the metal on the dielectric, this oxide layer can become trapped between the two interfaces. For a silicon dielectric, this oxide layer can be removed by shortly treating the sample with hydrofluoric acid. This process is also known as an 'HF dip'.

Aside from the HF dip, additional surface treatment can be applied. For the resonators measured in this report, before depositing the metal on the substrate, an additional exposure to hexamethyldisilazane (HMDS) was applied. The reason for this additional step is that there is a lattice mismatch between the metal and substrate. The intermediate layer of HMDS can possibly mediate this lattice mismatch. See [4] for more information.

1.3.2.2 Infrared shielding

Aside from thermal excitation, quasiparticles are also formed from the absorption of photons. High-frequency photons (UV-range or higher) are usually not a significant contribution, as they are easily absorbed by materials, well before they reach the inner layers of the fridge. Lower-frequency photons, such as in the infrared range, however, can penetrate through the fridge to the sample. These infrared photons can cause the excitation of quasiparticles.

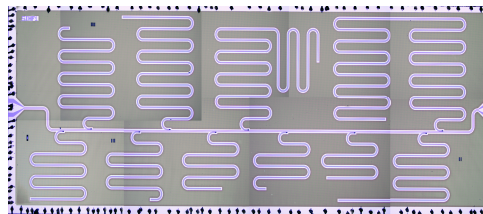
By using infrared shielding, such as a coating film inside the fridge, the amount of infrared radiation reaching the sample can be lowered.

1.3.2.3 Deep-reactive ion etching

Another technique applied to the resonators studied in this report is deep-reactive ion etching. In this technique alternating steps of reactive ion etching (TODO: is this true?), and sidewall passivation (TODO: what material?) are applied.

See [4] for more information.

1.4 EXPERIMENTAL SET-UP



The fridge used in this experiment is a dilution refrigerator, made by Leiden Cryogenics. The refrigerator has a base temperature of ~ 15 mK. An input signal was generated using a Rohde & Schwarz ZVM vector network analyzer, connected to an Aeroflex 8310 step attenuator, which has an attenuation range of 120 dB. The signal out of the fridge was measured using the same vector network analyzer.

Using this set-up $1/4 - \lambda$ resonators, fabricated by Alessandro Bruno, were measured in a frequency range between 1 – 9GHz. The sample is shown in Figure ???. The resonators were made using NbTiN on a silicon substrate. The advantage of NbTiN is that the metal atoms are bound to nitrogen, thereby inhibiting bond formation with oxides. In a way to minimize losses, all resonators were treated with HMDS and deep-reactive ion etching.

By driving a signal through the feedline, the resulting transmitted signal S_{21} can be measured. At or close to the resonance frequency of a resonator, the resonator will either cause enhanced transmission ($1/2\lambda$ resonator), or diminished transmission ($1/4\lambda$ resonator).

Unless stated otherwise, all measurements were performed with the fridge at base temperature (~ 15 mK).

1.5 RESULTS AND DISCUSSION

1.5.1 Measurement of a resonator

In Figure ?? the transmission S_{21} of a resonator is shown. Figure ?? shows the transmitted voltage $|S_{21}|$ of the resonator as a function of frequency. As one can see, the resonator has a shape similar to a Lorentzian dip. One interesting point is that the Lorentzian exhibits an

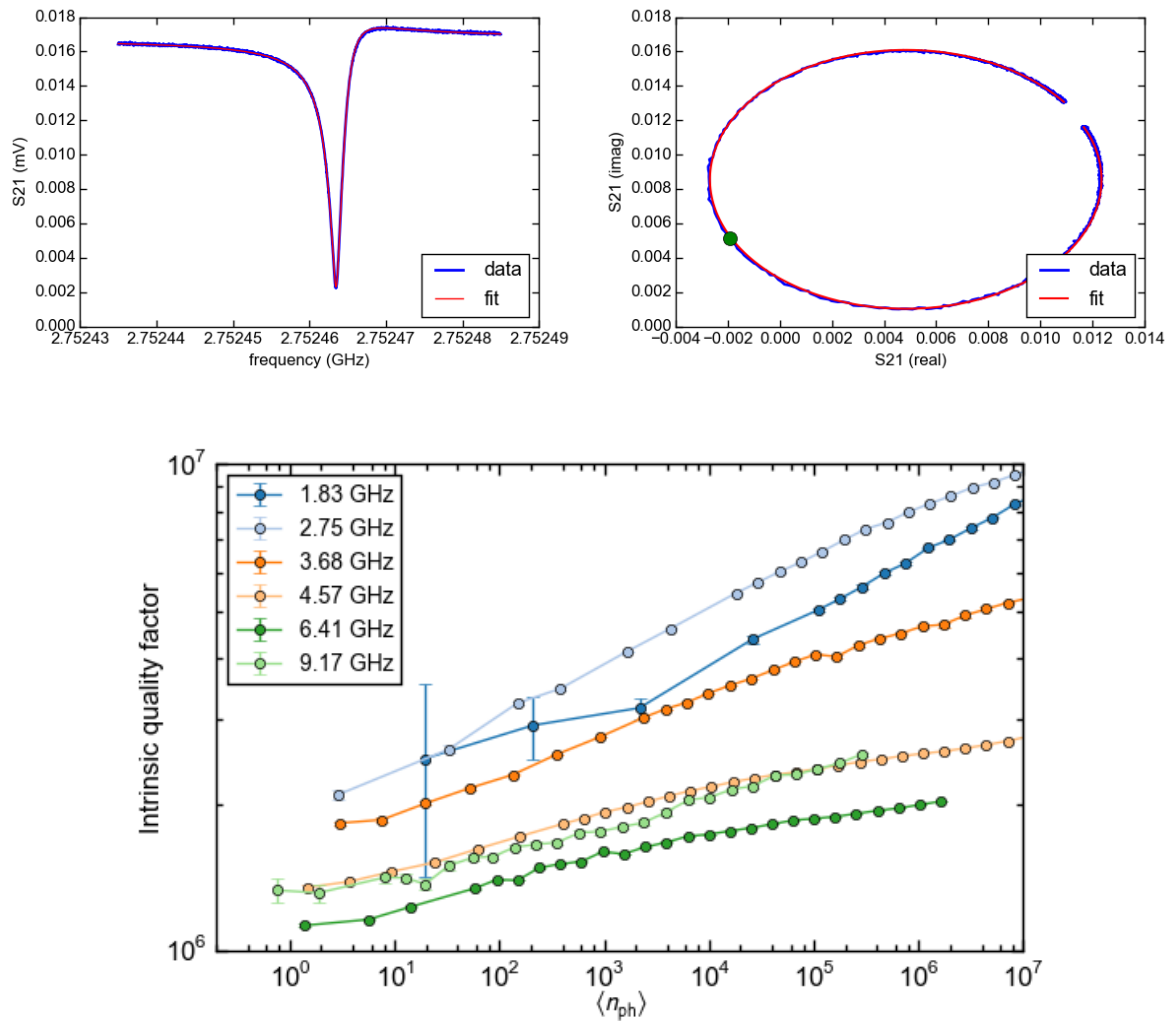


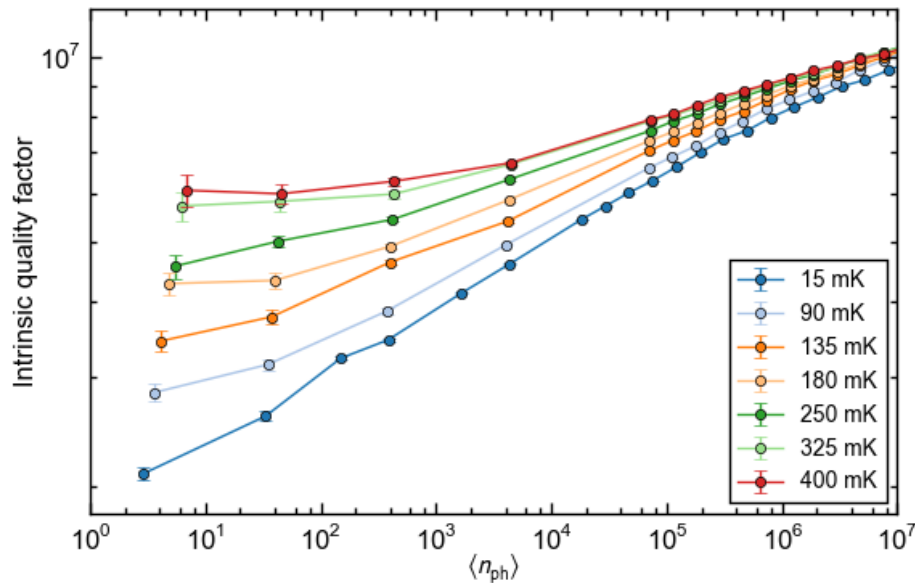
Figure 1.2: Quality factor of resonators versus mean number of photons present in the resonator.

asymmetry, which is often attributed to reflections in the feedline [9, p. 192]. This could be caused by impedance mismatching.

1.5.2 Power dependence

To be able to study the behaviour of the resonators, measurements were performed for several powers. Using proper calibrations for the attenuation down to the sample, the power can be converted to the input power at the sample. This value can then be converted to the mean number of photons present in the resonator [4]. The results are shown in Figure 1.2.

As can be seen, the internal quality factor Q_i of all resonators decrease with decreasing photon number. One explanation for this phenomenon is that the dissipation is mainly due to TLS. Since measurements were performed at ~ 15 mK, the TLS are not saturated since the rate of thermal excitation is low. As discussed in section 1.3.1.1, the loss due to TLS



is highest at low power, in the regime where they are not saturated. Therefore the fact that the internal quality factor Q_i rises with the mean number of photons present in the resonator can be attributed to a larger amount of TLS being saturated. This would suggest that, even with HMDS and DRIE treatment of the sample, the internal quality factor is still limited by TLS being present.

The mean photon number of a resonator is inversely proportional to the square of frequency [4], so for resonators with a low frequency a lower input power is required than with a high frequency. At high photon numbers this is not a concern, as the transmitted signal is high enough to be accurately measured in a short period of time. For the single-photon powers, however, which is the region of interest for quantum computation, acquiring enough signal took up to five hours for the lowest frequencies. The reason that for the resonator with a resonance frequency at 1.83 GHz has large error bars at low powers can be partly attributed to this, but as we will see in section 2.4, the main reason is that its frequency lies outside the bandwidth of the amplifiers and circulators of the set-up.

- Quality factor depends on frequency?
- One can also see that the quality factor is lower for resonators with higher resonance frequency.

1.5.3 Temperature dependence

Aside from power, some of the dissipation channels also depend on the temperature of the system. To be able to study the effect of temperature on resonators, the resonator with frequency 2.75 GHz has been studied as a function of power for several temperatures ranging from 15 mK up to 400 mK. The reason for choosing this resonator is that it has the highest

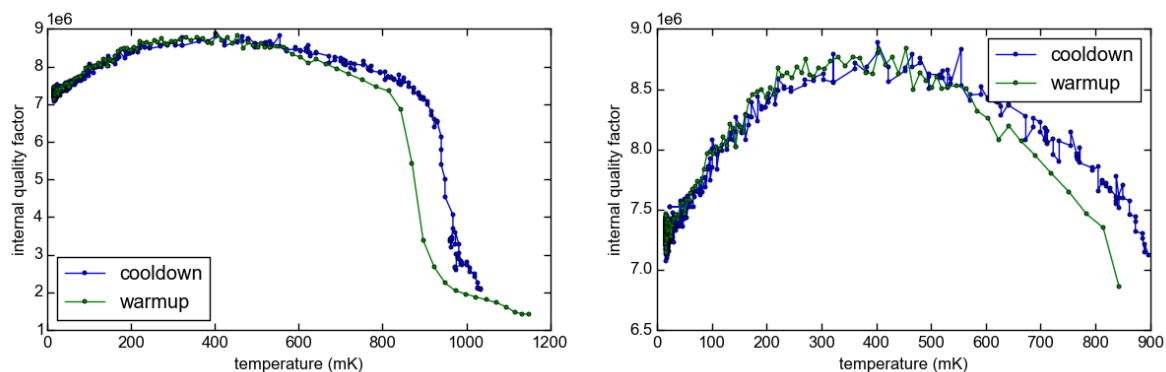
internal quality factor of all the resonators measured, and so any change in quality factor would be most clearly visible.

The results are shown in Figure ?? . As can be clearly seen, the quality factor increases with increasing temperature. This is likely due to the fact that TLS are thermally excited for a larger percentage of time. Therefore, the relative energy dissipation with respect to total energy in the resonator will be lower, resulting in an increase in quality factor.

Another interesting point is that the increase in quality factor as a function of temperature is largest at low powers. This can also be explained when the limiting factor is due to TLS. With low powers, the TLS are almost exclusively excited thermally, while at higher powers, the excitation of TLS is not only due to thermal excitations, but also from photon absorption.

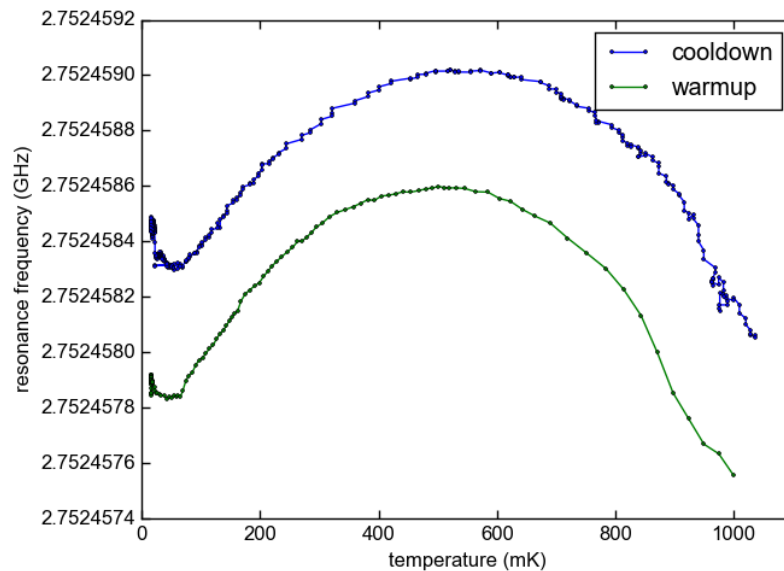
If one looks at the highest temperatures, it seems that the increase in quality factor as a function of temperature seems to slowly approach a saturation point. One reason is that the TLS are approaching their saturation, and so increasing the temperature further will have little effect on the percentage of time that the TLS are in the excited state. As will be shown in the next section, the quality factor is close to its maximum value, and will decrease as temperature is increased further.

1.5.4 Temperature tracking



To further investigate the temperature dependence of the resonator, a continuous measurement was performed on the resonator with resonance frequency 2.75 GHz during a cool-down and a subsequent warm-up of the fridge four days later. Measurements were performed for temperatures ranging from base temperature (15 mK) to roughly 1 K. Above this temperature, the fridge entered a cyclic ... TODO. All temperatures were measured at an input power of TODO, corresponding to roughly 5×10^5 photons. In Figure ?? the internal quality factor versus temperature is shown during a cooldown and subsequent warm-up of the fridge. As can be seen, the quality factor reaches a maximum quality factor at a temperature of ~ 600 mK. Below this temperature, the quality factor is likely limited by the presence of TLS (see sections 1.5.2 and 1.5.3). Above this temperature however, the quality factor decreases, indicating that TLS are not the limiting factor anymore for Q_i . One possibility is that the main source of dissipation is now due to the presence of quasiparticles in the resonator. At even

higher powers other effects, such as vortices and enhanced radiation, contribute more and more significantly to the decay of the quality factor.

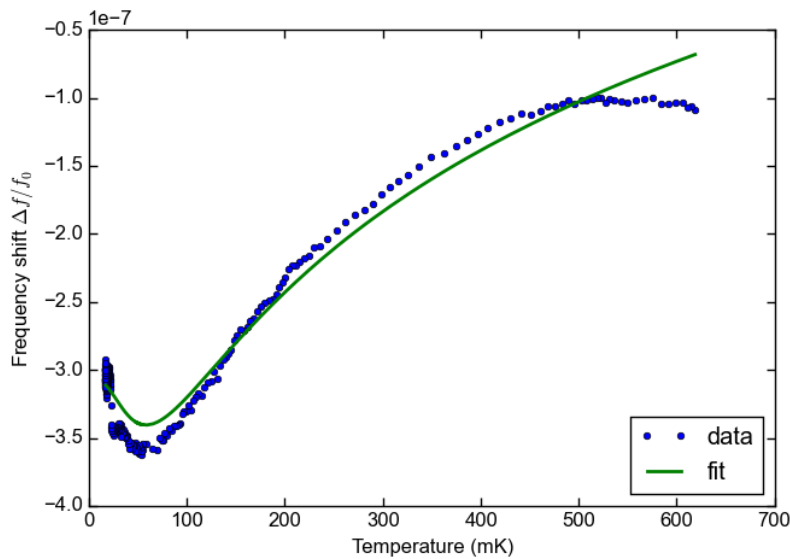


Aside from the internal quality factor, another quantity of interest is the resonance frequency f_0 of the resonator, which also depends on the temperature. The result from tracking the resonance frequency of the resonator during cooldown and subsequent warm-up is shown in Figure ???. As can be seen in both cases, the resonance frequency reaches a maximum around 500 K.

Between the cooldown and warm-up the resonance frequency seems to have shifted by roughly 500 Hz. As the sample was kept at 15 mK, it is unlikely that this decrease in resonance frequency is due to degradation of the sample. One possible explanation is that this change in resonance frequency is due to phase noise, which is known to shift the resonance frequency of the resonator. Further measurements are, however, required to determine if this is the case.

The decrease in resonance frequency at higher temperatures can be explained by the presence of quasiparticles, which increase the kinetic inductance [9, p. 91]. The resonance frequency is inversely proportional to the square root of the total conductance [2], and so an increase in kinetic inductance leads to a decrease in resonance frequency. For measurements done by Barends et al. [2], the change in resonance frequency due to changes in the kinetic inductance seem to roughly correspond with the decrease in center frequency measured in Figure ??.

The decrease in resonance frequency at lower temperatures can be explained due to still being present. A model is presented by Gao et al. [8], in which they describe the decrease in resonance frequency due to the presence of TLS. As can be seen in Figure ?? the model corresponds well with the data at low temperatures. At higher temperatures the model deviates from data, which may be explained by quasiparticles dominating as source of dissipation. An interesting thing to note is that an increase in resonance frequency was



predicted at the lowest temperatures, but as they did not reach temperatures sufficiently low they could not confirm this effect. In Figure ?? however, this increase in resonance frequency is observed. This supports the claim that at low temperatures the resonator is still limited by TLS, even after treatment of HMDS and DRIE.

- Info at Geerlings [9, p. 106]. Seems to say that resonance frequency depends on kinetic inductance, but also on TLS
- Mention that resonance frequency also depends on TLS
- At higher temperatures kinetic inductance takes over: [2], [7, ch. 3]

1.6 CONCLUSION AND FUTURE WORK

Since the quality factor of all resonators is found to decrease with decreasing input power, this indicates that at low temperatures and powers the limiting factor is still due to TLS. The fact that the quality factor initially increases with higher temperatures, supports this claim. By also measuring the resonance frequency as a function of temperature, the curve obtained is in good agreement with a model describing the resonance frequency shift due to TLS [8]. The curve even shows an increase in resonance frequency at the lowest temperatures, which was also predicted by the model. These results suggest that even after HMDS surface treatment and deep-reactive ion etching was applied, the internal quality factor of the resonator at low temperatures and power is still limited by the presence of TLS.

Nevertheless, As shown by Bruno et al. [4], the application of HMDS surface treatment and DRIE resulted in an improvement of the internal quality factor of the resonators by almost an order of magnitude. More research must be done to determine at what interface the dissipation due to TLS is greatest after these two treatments.

The next step is to perform the same treatments (HMDS and DRIE) on transmon qubits, to study what the influence will be on coherence times.

Chapter 2

Noise

- Noise level sets the lower limit on the magnitude of a signal that can be detected in the presence of the noise
- How does an attenuator affect the noise? Brief info at [14, p. 4]
- Quantities such as noise temperature work for white noise
- Mention that white noise can be due to thermal fluctuations
- noise can be frequency independent or frequency dependent (in fact not independent, as quantum mechanics sets upper limit (ref: noise theory). Also otherwise infinite power added by noise)

Pros

- Find out if the $1/2$ division is due to impedance matching of load and source

2.1 NOISE SOURCES

2.1.1 Johnson noise

2.1.2 Shot noise

2.1.3 $1/f$ noise

- Two-level systems

2.2 CHARACTERIZATION OF NOISE

When performing measurements one important question to ask is what the contribution of noise is to the system.

2.2.1 Noise spectral Density

There are two ways in which we can model our system: The Thévenin scheme, and the Norton scheme. In the Thévenin scheme we can model the system as a voltage source, and the noise added to the system is a noise voltage source connected in series. In the Norton scheme the system is a current source and the noise added is a noise current source connected in parallel to the current source. These two schemes are identical and can be converted into each other. In this section we will adopt the Thévenin scheme, and so the signal will be a voltage source combined in series with a noise voltage source.

One way of quantifying the noise of the system is through the noise spectral density $S(f)$, which is the distribution of noise per unit bandwidth as a function of frequency. For the Thévenin scheme, the noise spectral density is defined in terms of voltage. When the only noise in the system is white noise, the spectral density is independent of frequency. According to Nyquist's theorem (TODO: cite noise theory of linear and non-linear circuits), the noise voltage spectral density S_{v_n} is then given by:

$$S_{v_n} = \frac{v_n^2}{\Delta f} = 4k_B T R \quad (2.1)$$

In this equation v_n^2 (TODO) is the mean-squared voltage (TODO: correct name?), Δf is the bandwidth over which the noise is integrated, k_B is the Boltzmann constant, and R is the impedance of the system.

From this it follows that the root-mean square noise voltage v_n^{rms} is given by:

$$v_n^{rms} = \sqrt{v_n^2} = \sqrt{4k_B T R \Delta f} \quad (2.2)$$

From equation 2.2 we see that the noise added depends linearly on the bandwidth over which is integrated.

2.3 THE MODEL

We can model our set-up by as being a succession of four components:

1. A noise source.
2. An amplifier to amplify the weak signal exiting the fridge.
3. A mixer to downconvert the signal.
4. A low-pass filter to remove unwanted high-frequency signal.

2.3.1 Noise source

Using the Thévenin model, we can approximate the components up to the first amplifier in the fridge as a voltage source, with a noise voltage source connected in series.

We can include the noise added by the amplifier in the noise voltage source, in which case we assume the amplifier to be ideal. Furthermore, we assume the signal to be amplified sufficiently, such that the mixer and low-pass filter add a negligible amount of noise. We also ignore effect such as mixer leakage. With these assumptions all of the noise is originated from the noise voltage source.

We can associate an effective noise temperature to the noise voltage source. The noise temperature is defined as the temperature at which a resistor would produce an equal amount of noise. Note that, since we are comparing the system to a resistor, the noise needs to have an (approximately) white spectrum.

2.3.2 Amplification

- Talk about Maximum power transfer theorem (1/2 division)

2.3.3 Mixing and filtering

After amplification the frequency ω of the signal is still in the GHz range. In a heterodyne set-up the signal is then downconverted to a lower frequency, to be more easily measured. To downconvert the signal, it is mixed in a mixer with a local oscillator (LO) signal having the same frequency ω (homodyne) or a slightly higher frequency $\omega + \Delta\omega$ (heterodyne). The mixer effectively multiplies the two signals (TODO: mention why amplitude of LO signal is unimportant). If the signal exiting the amplifier is given by $v(t) = A \cos \omega t$, then, ignoring a possible phase difference, the signal at the output of the mixer is given by:

$$v(t) \cdot \cos(\omega)t = A \cos \omega t \cdot \cos(\omega + \Delta\omega)t \quad (2.3)$$

$$= \frac{1}{2} [\cos(2\omega + \Delta\omega)t + \cos \Delta\omega t] \quad (2.4)$$

As can be seen from Equation 2.4, the final signal contains both the sum and the difference of the two signals. However, as the sum of both frequencies is in the GHz range, it can easily be filtered out using a low-pass filter, leaving only the downconverted signal, which is the result of the difference between the two frequencies. Note that the amplitude of the signal is reduced by a factor two. Furthermore, in the case of a homodyne set-up, the difference signal is simply a DC signal, while in the case of heterodyne the signal still contains a slow frequency $\Delta\omega$. For simplification we assume our set-up to be a homodyne set-up.

In the case of homodyne detection

- Noise temperature is the equivalent amount of noise added by a resistor being at that temperature
- Formula for noise temperature
- Show plot of noise temperature
- Explain why first amplifier is most important

- low-pass filter

2.4 RESULTS

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