## CSE 573 - Project 2

Amlan Gupta (#50288686)

November 2018

## 1 Image Features and Homography

```
def perform_sift(img):
             sift_img = np.zeros(img.shape)
3
             sift = cv2.xfeatures2d.SIFT_create()
6
             kp, desc = sift.detectAndCompute(img, None)
             sift_img = cv2.drawKeypoints(img, kp, sift_img)
10
             return sift_img, kp, desc
11
12
     def find_knn_match(img_1, img_2, kp_1, kp_2, desc_1, desc_2):
13
             bf = cv2.BFMatcher()
             matches = bf.knnMatch(desc_1,desc_2, k=2)
             # Apply ratio test
18
             good_matches = []
19
             pts1 = []
20
             pts2 = []
21
             for m,n in matches:
22
                 if m.distance < 0.75*n.distance:</pre>
23
                      good_matches.append(m)
24
                      pts2.append(kp_2[m.trainIdx].pt)
25
                      pts1.append(kp_1[m.queryIdx].pt)
26
27
28
             knn_matched_img = np.zeros(img_1.shape)
29
             knn_matched_img = cv2.drawMatches(img_1, kp_1, img_2, kp_2, good_matches, knn_matched_img, flags=2)
30
             return knn_matched_img, good_matches, pts1, pts2
31
32
33
     def find_homography_and_match_images(good_matches, kp_1, kp_2, img_1, img_2):
34
35
             src_pts = np.float32([ kp_1[m.queryIdx].pt for m in good_matches ]).reshape(-1,1,2)
36
             dst_pts = np.float32([ kp_2[m.trainIdx].pt for m in good_matches ]).reshape(-1,1,2)
37
             M, mask = cv2.findHomography(src_pts, dst_pts, cv2.RANSAC, 5.0)
             matchesMask = mask.ravel()
             good_matches_np = np.asarray(good_matches)
42
43
             matchesMask = matchesMask[mask.ravel()==1]
44
             good_matches_np = good_matches_np[mask.ravel()==1]
45
46
             randIndx = np.random.randint(low=0, high=good_matches_np.shape[0], size=10)
47
48
             good_matches_np = good_matches_np[randIndx]
49
```

```
matchesMask = matchesMask[randIndx]
50
51
52
              draw_params = dict(matchColor = (0, 0, 255),
53
                          singlePointColor = None,
54
                          matchesMask = matchesMask.tolist(),
55
                          flags = 2)
56
57
58
              matches_img = cv2.drawMatches(img_1, kp_1, img_2, kp_2, good_matches_np.tolist(), None, **draw_params)
59
              return M, matches_img
60
61
62
63
      def do_image_stitching(img_1, img_2, M):
64
65
              (h1, w1) = img_1.shape[:2]
66
              (h2, w2) = img_2.shape[:2]
67
68
              #remap the coordinates of the projected image onto the panorama image space
69
              top_left = np.dot(M,np.asarray([0,0,1]))
70
              top_right = np.dot(M,np.asarray([w2,0,1]))
71
              bottom_left = np.dot(M,np.asarray([0,h2,1]))
72
              bottom_right = np.dot(M,np.asarray([w2,h2,1]))
73
74
              #normalize
75
              top_left = top_left/top_left[2]
76
              top_right = top_right/top_right[2]
77
              bottom_left = bottom_left/bottom_left[2]
78
              bottom_right = bottom_right/bottom_right[2]
79
80
81
82
              pano_left = int(min(top_left[0], bottom_left[0], 0))
83
              pano_right = int(max(top_right[0], bottom_right[0], w1))
84
              W = pano_right - pano_left
85
86
              pano_top = int(min(top_left[1], top_right[1], 0))
87
              pano_bottom = int(max(bottom_left[1], bottom_right[1], h1))
88
89
              H = pano_bottom - pano_top
              size = (W, H)
91
92
              # offset of first image relative to panorama
93
              X = int(min(top_left[0], bottom_left[0], 0))
94
              Y = int(min(top_left[1], top_right[1], 0))
95
              offset = (-X, -Y)
96
97
              panorama = np.zeros((size[1], size[0]), np.uint8)
98
99
              (ox, oy) = offset
100
101
              translation = np.matrix([
102
                                                [1.0, 0.0, ox],
103
                                                [0, 1.0, oy],
104
                                                [0.0, 0.0, 1.0]
105
                                                1)
106
107
108
              M = translation * M
109
110
111
              cv2.warpPerspective(img_1, M, size, panorama)
```

```
panorama[oy:h1+oy, ox:ox+w1] = img_2
113
114
              return panorama
115
116
117
      def image_feature_and_homography(mountain_1_img, mountain_2_img):
118
119
              # task 1.1
120
121
              kp_mountain_1_img, kp_1, desc_1 = perform_sift(mountain_1_img)
122
              write_image(kp_mountain_1_img, 'task1_sift1.jpg')
123
124
125
              kp_mountain_2_img, kp_2, desc_2 = perform_sift(mountain_2_img)
126
              write_image(kp_mountain_2_img, 'task1_sift2.jpg')
127
128
129
              # task 1.2
130
131
              knn_matched_img, good_matches, _, _ = find_knn_match(mountain_1_img, mountain_2_img,
132
              kp_1, kp_2, desc_1, desc_2)
133
              write_image(knn_matched_img, 'task1_matches_knn.jpg')
134
135
136
              #task 1.3, task 1.4
137
138
              h_matrix, task1_matches = find_homography_and_match_images(good_matches, kp_1, kp_2,
139
              mountain_1_img, mountain_2_img)
140
              print(h_matrix)
141
              write_image(task1_matches, 'task1_matches.jpg')
142
143
144
              panorama = do_image_stitching(mountain_1_img, mountain_2_img, h_matrix)
145
              write_image(panorama,'task1_pano.jpg')
146
147
148
149
150
      def main():
151
152
              mountain_1_img = cv2.imread(SOURCE_FOLDER + "mountain1.jpg", 0)
              mountain_2_img = cv2.imread(SOURCE_FOLDER + "mountain2.jpg", 0)
              image_feature_and_homography(mountain_1_img, mountain_2_img)
157
158
159
      main()
160
```

1. Given two images mountain1.jpg and mountain2.jpg, extract SIFT features and draw the keypoints for both images. Include the resulting two images (task1\_sift1.jpg, task1\_sift2.jpg) in the report.

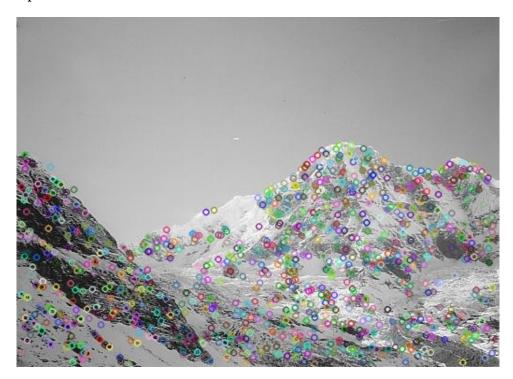


Figure 1: Keypoints for mountain1.jpg

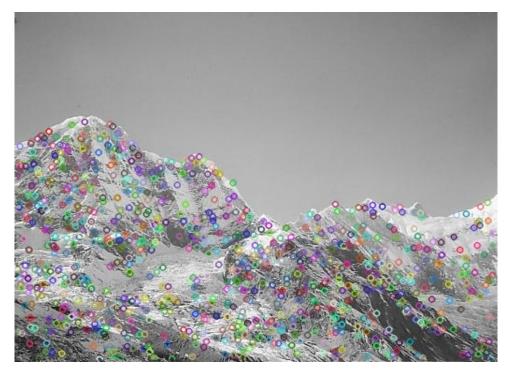


Figure 2: Keypoints for mountain 2.jpg

2. Match the keypoints using k-nearest neighbour (k=2), i.e., for a keypoint in the left image, finding the best 2 matches in the right image. Filter good matches satisfy m.distance <0.75 n.distance, where m is the first match and n is the second match. Draw the match image using cv2.drawMatches for all matches (your match image should contain both inliers and outliers). Include the result image (task1\_matches\_knn.jpg) in the report.

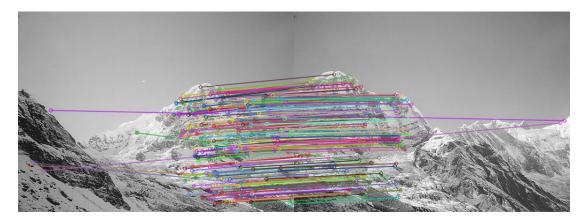


Figure 3: Matched keypoints using k-nearnest neighbour (k = 2)

3. Compute the homography matrix H (with RANSAC) from the first image to the second image. Include the matrix values in the report.

```
\begin{bmatrix} 1.589302 & -0.291559 & -395.969265 \\ 0.449424 & 1.431109 & -190.613988 \\ 0.001213 & -0.000063 & 1.000000 \end{bmatrix}
```

4. Draw the match image for around 10 random matches using only inliers. Include the result image (task1\_matches.jpg) in the report.

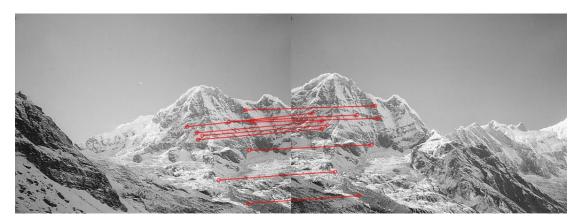


Figure 4: 10 random matches using only inliers

5. Warp the first image to the second image using H. The resulting image should contain all pixels in mountain1.jpg and mountain2.jpg. Include the result image (task1\_pano.jpg) in the report.

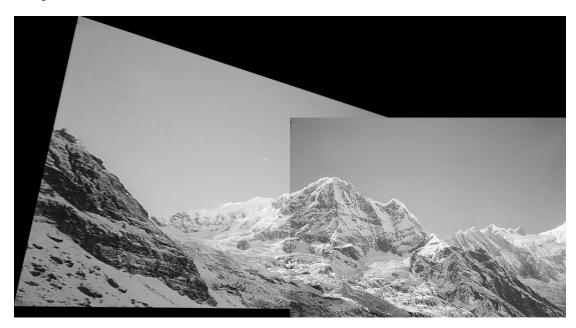


Figure 5: Warped image using Homography matrix

## 2 Epipolar Geometry

```
def perform_sift(img):
2
             sift_img = np.zeros(img.shape)
             sift = cv2.xfeatures2d.SIFT_create()
             kp, desc = sift.detectAndCompute(img, None)
             sift_img = cv2.drawKeypoints(img, kp, sift_img)
10
             return sift_img, kp, desc
11
12
     def find_knn_match(img_1, img_2, kp_1, kp_2, desc_1, desc_2):
13
14
             bf = cv2.BFMatcher()
15
             matches = bf.knnMatch(desc_1,desc_2, k=2)
16
17
             # Apply ratio test
18
             good_matches = []
19
             pts1 = []
20
             pts2 = []
21
             for m,n in matches:
22
                 if m.distance < 0.75*n.distance:</pre>
23
                      good_matches.append(m)
24
                      pts2.append(kp_2[m.trainIdx].pt)
25
                      pts1.append(kp_1[m.queryIdx].pt)
27
             knn_matched_img = np.zeros(img_1.shape)
             knn_matched_img = cv2.drawMatches(img_1, kp_1, img_2, kp_2, good_matches, knn_matched_img, flags=2)
30
             return knn_matched_img, good_matches, pts1, pts2
31
32
```

```
33
34
     def drawlines(img1,img2,lines,pts1,pts2, color):
35
             r,c = img1.shape
36
             img1 = cv2.cvtColor(img1,cv2.COLOR_GRAY2BGR)
37
             img2 = cv2.cvtColor(img2,cv2.COLOR_GRAY2BGR)
38
             for r,pt1,pt2,colr in zip(lines,pts1,pts2,color):
39
                      x0,y0 = map(int, [0, -r[2]/r[1]])
40
                      x1,y1 = map(int, [c, -(r[2]+r[0]*c)/r[1]])
41
                      img1 = cv2.line(img1, (x0,y0), (x1,y1), tuple(colr),1)
42
43
                      img1 = cv2.circle(img1,tuple(pt1),5,tuple(colr),-1)
                      img2 = cv2.circle(img2,tuple(pt2),5,tuple(colr),-1)
44
45
             return img1,img2
46
47
     def find_disparity_map(imgL, imgR):
49
             window_size = 3
50
             min_disp = 16
             num_disp = 64-min_disp
             stereo = cv2.StereoSGBM_create(minDisparity = min_disp,
                      numDisparities = num_disp,
53
                      blockSize = 9,
54
                      P1 = 8*3*window_size**2,
55
                      P2 = 32*3*window_size**2,
56
                      disp12MaxDiff = 1,
57
                      uniquenessRatio = 10,
58
                      speckleWindowSize = 100,
59
                      speckleRange = 32
60
             )
61
62
             disp = stereo.compute(imgL, imgR).astype(np.float32) / 16.0
63
             disp = (disp-min_disp)/num_disp
64
65
             disp = disp*300
66
67
69
             write_image(disp,'task2_disparity.jpg')
70
71
72
     def epipolar_geometry(tsucuba_left_img, tsucuba_right_img):
73
             # task 2.1
74
75
             kp_tsucuba_left_img, kp_1, desc_1 = perform_sift(tsucuba_left_img)
76
             write_image(kp_tsucuba_left_img, 'task2_sift1.jpg')
77
78
             kp_tsucuba_right_img, kp_2, desc_2 = perform_sift(tsucuba_right_img)
79
             write_image(kp_tsucuba_right_img, 'task2_sift2.jpg')
80
81
             # task 2.2, 2.3
82
83
             knn_matched_img, good_matches, pts1, pts2 = find_knn_match(tsucuba_left_img, tsucuba_right_img,
84
                              kp_1, kp_2, desc_1, desc_2)
85
86
             pts1 = np.int32(pts1)
87
             pts2 = np.int32(pts2)
89
             F, mask = cv2.findFundamentalMat(pts1,pts2,cv2.FM_RANSAC)
90
             pts1 = pts1[mask.ravel()==1]
             pts2 = pts2[mask.ravel()==1]
             print(F)
94
             randIndx = np.random.randint(low=0, high=pts1.shape[0], size=10)
```

```
pts1 = pts1[randIndx]
              pts2 = pts2[randIndx]
99
              color = np.random.randint(0,255, size=(10, 3)).tolist()
100
101
              lines1 = cv2.computeCorrespondEpilines(pts2.reshape(-1,1,2), 2, F)
102
              lines1 = lines1.reshape(-1,3)
103
              tsucuba_left_ep , _ = drawlines(tsucuba_left_img, tsucuba_right_img, lines1, pts1, pts2, color)
104
105
              write_image(tsucuba_left_ep, 'task2_epi_left.jpg')
106
107
              lines2 = cv2.computeCorrespondEpilines(pts1.reshape(-1,1,2), 1, F)
108
              lines2 = lines2.reshape(-1,3)
109
              tsucuba_right_ep, _ = drawlines(tsucuba_right_img,tsucuba_left_img,lines2, pts2, pts1, color)
110
111
              write_image(tsucuba_right_ep, 'task2_epi_right.jpg')
112
113
114
              # task 2.4
115
              find_disparity_map(tsucuba_left_img, tsucuba_right_img)
116
117
118
119
120
      def main():
121
122
              tsucuba_left_img = cv2.imread(SOURCE_FOLDER + "tsucuba_left.png", 0)
123
              tsucuba_right_img = cv2.imread(SOURCE_FOLDER + "tsucuba_right.png", 0)
124
125
              epipolar_geometry(tsucuba_left_img, tsucuba_right_img)
126
127
128
129
130
      main()
131
```

1. Given two images tsucuba\_left.png and tsucuba\_right.png, do the same process for Task 1.1 and 1.2. Include the three images (2 for task 1.1 and 1 for task 1.2) (task2\_sift1.jpg, task2\_sift2.jpg, task2\_matches\_knn.jpg) in the report.





(a) for tsucuba\_left.png

(b) for tsucuba\_right.png

Figure 6: Detected Keypoints

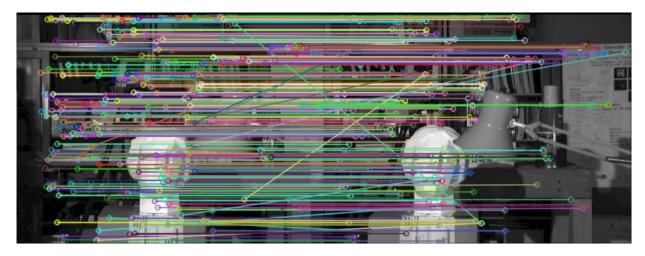
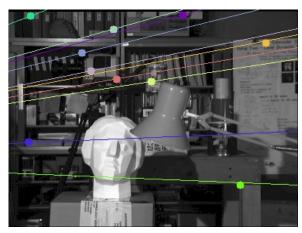


Figure 7: Matched keypoints using k-nearnest neighbour (k = 2)

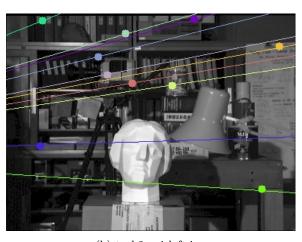
2. Computer the fundamental matrix F (with RANSAC). Include the matrix values in the report.

$$\begin{bmatrix} 3.88435667e^{-06} & -2.28e^{-04} & 4.41240231e^{-02} \\ 2.42e^{-04} & -1.90e^{-05} & 9.95e^{-02} \\ -4.58e^{-02} & -1.02e^{-01} & 1 \end{bmatrix}$$

3. Randomly select 10 inlier match pairs. For each keypoint in the left image, compute the epiline and draw on the right image. For each keypoint in the right image, compute the epiline and draw on the left image [Using different colors for different match pairs, but the same color for epilines on the left and right images with the same match pair.] Include two images (task2\_epi\_right.jpg, task2\_epi\_left.jpg) with epilines in the report.



(a) task2\_epi\_right.jpg



(b)  $task2\_epi\_left.jpg$ 

Figure 8: Epilines

4. Compute the disparity map for tsucuba\_left.png and tsucuba\_right.png. Include the disparity image (task2\_disparity.jpg) in the report.

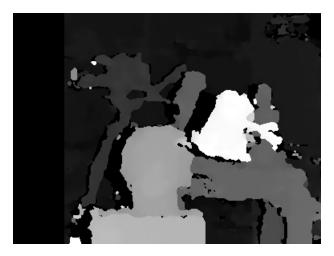


Figure 9: Disparity map for tsucuba\_left.png and tsucuba\_right.png

## 3 K-means Clustering

```
def measure_euclidean_distance(pt1 , pt2):
2
         dis = math.sqrt(((pt1[0] - pt2[0])**2) + ((pt1[1] - pt2[1])**2))
3
         return dis
5
     def calculate_distances_from_centroids(mu, mu_c, X, it_n):
6
         cluster_c = []
         for pt in X:
             isFirst = True
10
             for m, mc in zip(mu,mu_c):
11
                 if isFirst == True:
12
                      d = measure_euclidean_distance(pt,m)
13
14
                      c = mc
                      isFirst = False
15
                  {\tt elif \ (measure\_euclidean\_distance(pt,m) < d):}
16
                      d = measure_euclidean_distance(pt,m)
17
                      c = mc
19
              cluster_c.append(c)
20
21
22
         fig = plt.figure()
23
         ax = fig.add_subplot(111)
         plt.scatter(X[:,0], X[:,1], marker= "^", facecolors="None", edgecolors= cluster_c)
         plt.scatter(mu[:,0], mu[:,1], c= mu_c)
25
         for xy in zip(mu[:,0], mu[:,1]):
26
                 ax.annotate('(\%.2f, \%.2f)' \% xy, xy=xy, textcoords='data')
27
         # plt.show()
28
         plt.savefig(OUTPUT_FOLDER + 'task3_iter'+str(it_n+1)+'_a.jpg')
29
         plt.clf()
30
31
         return np.asarray(cluster_c)
32
33
     def vector_classification():
34
35
              X = np.array([
36
              [5.9, 3.2],
37
              [4.6, 2.9],
```

```
[6.2, 2.8],
39
               [4.7, 3.2],
40
               [5.5, 4.2],
41
               [5.0, 3.0],
42
               [4.9, 3.1],
43
              [6.7, 3.1],
44
              [5.1, 3.8],
45
              [6.0, 3.0]])
46
47
              mu = np.array([[6.2, 3.2], [6.6, 3.7], [6.5, 3.0]])
48
              mu_c = ['r','g','b']
49
50
              for i in range(2):
51
52
53
                   cluster_c = calculate_distances_from_centroids(mu, mu_c, X, i)
54
                  print(cluster_c)
55
56
                  clusters = []
57
                  for mc in zip(mu_c):
                       clusters.append(X[cluster_c == mc])
59
60
                  mu = []
61
                  for clus in clusters:
62
                       mu.append(np.mean(clus, axis=0))
63
64
                  mu = np.asarray(mu)
65
                  print(mu)
66
67
68
                  fig = plt.figure()
69
                  ax = fig.add_subplot(111)
70
                  plt.scatter(X[:,0], X[:,1], marker= "^", facecolors="None", edgecolors= cluster_c)
71
                  {\tt plt.scatter(mu[:,0], mu[:,1], c= mu\_c)}
72
                  for xy in zip(mu[:,0], mu[:,1]):
73
                           ax.annotate('(%.2f, %.2f)' % xy, xy=xy, textcoords='data')
74
                  plt.savefig(OUTPUT_FOLDER + 'task3_iter'+str(i+1)+'_b.jpg')
75
                  plt.clf()
76
77
78
80
      def measure_euclidean_distance_3d(color1 , color2):
81
              dis = ((color1[0] - color2[0])**2) + ((color1[1] - color2[1])**2) + ((color1[2] - color2[2])**2)
82
83
              print(color1, color2)
84
          return dis
85
86
87
      def calculate_distances_from_centroids_3d(mu, mu_c, image):
88
          cluster_c = np.zeros([image.shape[0],image.shape[1]])
89
90
          h, w, 1 = image.shape
91
92
93
94
          for i in range(h):
95
              for j in range(w):
                  pixel = image[i][j]
96
97
                  isFirst = True
98
                   for m, mc in zip(mu,mu_c):
100
                       if isFirst == True:
101
                           d = measure_euclidean_distance_3d(pixel,m)
```

```
102
                           isFirst = False
103
                       elif (measure_euclidean_distance_3d(pixel,m) < d):</pre>
104
                            d = measure_euclidean_distance_3d(pixel,m)
105
                           c = mc
106
107
                   cluster_c[i][j] = c
108
109
110
111
          return np.asarray(cluster_c)
112
113
      def color_quantization(image):
114
115
              k = [3, 5, 10, 20]
117
118
               \# k = [20]
              for kval in k:
120
121
                   mu = np.random.randint(0,255, size=(kval, 3))
122
                   mu_indx = np.random.randint(0,image.shape[0], size=(kval, 2))
123
124
125
                   for i in range(mu_indx.shape[0]):
126
                           mu.append(image[mu_indx[i][0]][mu_indx[i][1]])
127
                   mu = np.asarray(mu).astype(float)
128
129
                   mu_c = np.arange(kval)
130
131
132
                   for zz in range(30):
133
134
                       cluster_c = calculate_distances_from_centroids_3d(mu, mu_c, image)
135
136
137
                       h, w, l = image.shape
138
                       clusters = []
139
140
                       for mc in zip(mu_c):
141
                           clustered_img_np = []
142
                           for i in range(h):
143
                                for j in range(w):
144
                                    if(cluster_c[i][j] == mc):
145
                                        clustered_img_np.append(image[i][j])
146
                            clusters.append(np.asarray(clustered_img_np))
147
148
                       mu = []
149
                       for clus in clusters:
150
                            c_mean = np.nanmean(clus, axis=0)
151
                           mu.append(c_mean)
152
153
154
                       mu = np.asarray(mu)
155
156
                       h, w, l = image.shape
                       output_img = np.zeros([h,w,1])
157
                       for i in range(h):
                            for j in range(w):
                                index =int(cluster_c[i][j])
161
                                output_img[i][j] = mu[index]
162
163
                       op = output_img.astype(int)
164
```

```
165
                   write_image(op, 'task3_baboon_'+ str(kval) +'.jpg')
166
                        # print('boboon for ' + str(kval) + 'k means generated!')
167
168
169
170
      def k_means_clustering(image):
171
172
               #task 3.1, 3.2, 3.3
173
               vector_classification()
174
175
               #task 3.4
176
               color_quantization(image)
177
178
179
180
      def main():
181
182
183
               baboon_img = cv2.imread(SOURCE_FOLDER + "baboon.jpg")
               k_means_clustering(baboon_img)
185
186
               print('DONE!!')
187
188
189
190
191
      main()
192
```

1. Classify N = 10 samples according to nearest  $\mu_i$  (i = 1, 2, 3). Plot the results by coloring the empty triangles in red, blue or green. Include the classification vector and the classification plot (task3\_iter1\_a.jpg) in the report.

The classification vector is  $[\mathbf{r} \ \mathbf{r} \ \mathbf{b} \ \mathbf{r} \ \mathbf{g} \ \mathbf{r} \ \mathbf{r} \ \mathbf{b} \ \mathbf{r} \ \mathbf{r}]$ 

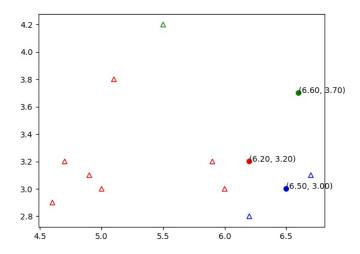


Figure 10: Classification plot for N=10 samples

2. Recompute  $\mu_i$ . Plot the updated  $\mu_i$  in solid circle in red, blue, and green respectively. Include the updated  $\mu_i$  values and the plot in the report (task3\_iter1\_b.jpg).

The value of updated  $\mu_i$  in first iteration is:

```
\begin{bmatrix} 5.17142857 & 3.17142857 \\ 5.5 & 4.2 \\ 6.45 & 2.95 \end{bmatrix}
```

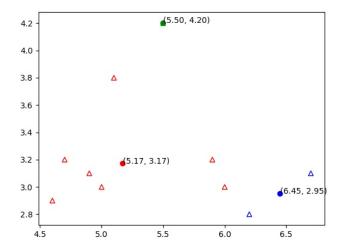


Figure 11: Updated  $\mu_i$  in plot

3. For a second iteration, plot the classification plot and updated  $\mu_i$  plot for the second iteration. Include the classification vector and updated  $\mu_i$  values and these two plots (task3\_iter2\_a.jpg, task3\_iter2\_b.jpg) in the report.

Classification vector for second iteration:  $[\mathbf{b} \ \mathbf{r} \ \mathbf{b} \ \mathbf{r} \ \mathbf{g} \ \mathbf{r} \ \mathbf{r} \ \mathbf{b} \ \mathbf{g} \ \mathbf{b}]$ 

The value of updated  $\mu_i$  in second iteration is:

$$\begin{bmatrix} 4.8 & 3.05 \\ 5.3 & 4.0 \\ 6.2 & 3.025 \end{bmatrix}$$

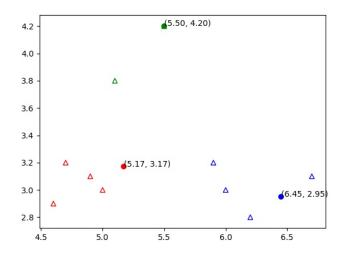


Figure 12:  $task3\_iter2\_a.jpg$ 

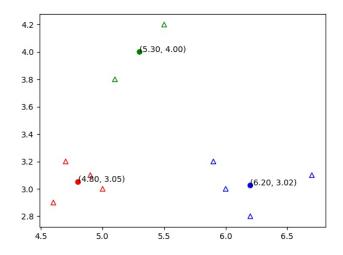


Figure 13: task3\_iter2\_b.jpg

4. Apply k-means to image color quantization. Using only k colors to represent the image baboon.jpg. Include the color quantized images for  $k=3,\,5,\,10,\,20$  (task3\_baboon\_3.jpg, task3\_baboon\_5.jpg, task3\_baboon\_20.jpg



Figure 14: Color quantied baboon image for k=3



Figure 15: Color quantied baboon image for k =5

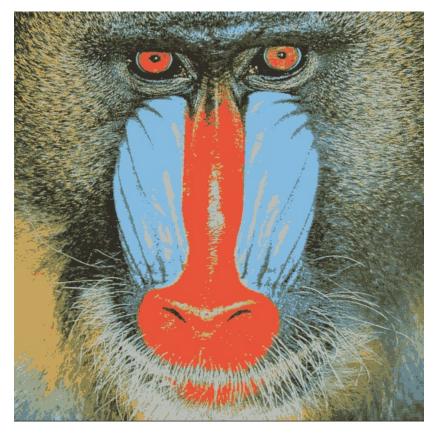


Figure 16: Color quantied baboon image for  $k=\!10$ 

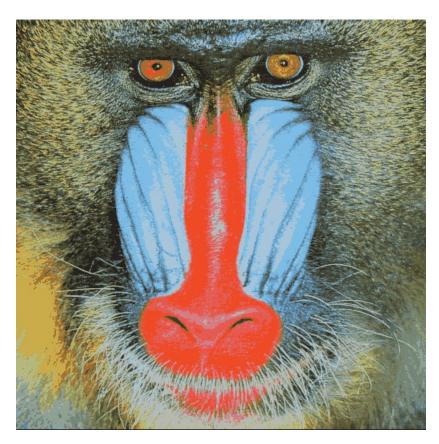


Figure 17: Color quantied baboon image for k =20  $\,$