

ELEC 341 – Graded Assignments

# Assignment A-3

## 12 Marks

### Learning Objectives

- Electro-Mech Equivalents
- CCT Analysis in Matlab
- Mixed Electro-Mech Systems
- Matlab
  - tf('s')
  - inv()
  - dcgain()
- Simulink
  - n/a

*If you prefer to solve an electric circuit rather than a mechanical circuit, just transform the mechanical model into an equivalent electrical circuit.*

**Fig 1 2 mark(s) Electro-Mechanical Transformation**

A mechanical system is modelled by the “Mechanical Circuit” shown.

- Draw the equivalent electric circuit
- Annotate it with component labels ( $R_1$ ,  $L_1$ ,  $C_1$ , etc.)

**Calc 1 2 mark(s) Spring & Damper Transfer Function**

Use nodal analysis to compute the following transfer functions.

Use **minreal()** to cancel any common factors.

- $G_1 = \tau K_2 M / \tau M$  = Separating Torque exerted by spring  $K_2 M$  (Nm/Nm)
- $G_2 = \tau B_1 / \tau M$  = Separating Torque exerted by damper  $B_1$  (Nm/Nm)

*The command **s=tf('s')** defines the Complex Frequency variable which can be used just like a constant in your equations.*

*Once you have an Admittance matrix (Y), you can use **inv()** to get an Impedance matrix (Z). If you make a mistake and get a matrix that isn't full-rank, **inv()** will fail.*

*Is the Final Value of the Natural Response = 0 or not ??? Is this what you expect from the mechanical system diagram use common sense ???*

*What is the electrical equivalent of angle ??? Can you measure it on a scope ???*

*Final Value is the value after a LONG TIME. To find a value at a SPECIFIC TIME, an easy way to get a quick answer is to plot the response and zoom in on curve at the time you're interested in. It won't be perfect but it should be pretty good.*

**Fig 2 2 mark(s) Value at 5s**

The input is a step function applied at  $t=0s$ .

Find the specified spring and damper separation torques at  $t=5s$ .

- spring torque =  $\tau K_2 M$  (Nm)
- damper torque =  $\tau B_1$  (Nm)

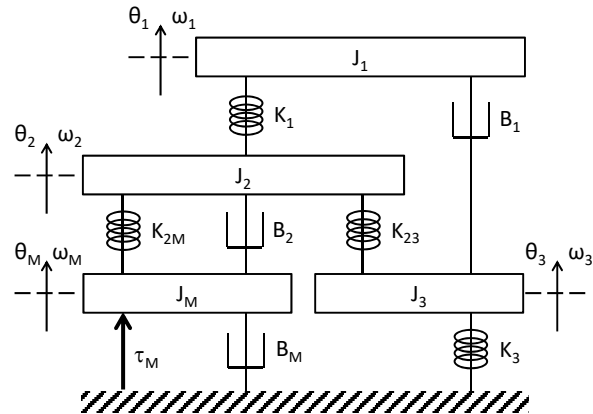
**Calc 2 2 mark(s) Accurate Value**

To find out how accurate your value is, calculate it and compute the %error with respect to the value you read from the figure.

- $\tau_{5fig} = \tau B_1$  from figure (Nm)
- $\tau_{5calc} =$  calculated  $\tau B_1$  (Nm)
- $err =$  error (%)

*Was it worth the extra trouble to do the calculation ???*

- $J1 = J2 =$  #F Kg $m^2$
- $J3 = J_M =$  #B Kg $m^2$
- $K1 = K3 =$  #D Nm
- $K_{2M} = K_{23} =$  #E Nm
- $B1 =$  #G Nms
- $B2 =$  #C Nms
- $B_M =$  #H Nms
- $\tau_M =$  3 Nm



*Do physical units matter ???*

### Electro-Mechanical Motor Model

- $L_w = 10 + \#A \mu\text{H}$
- $R_w = 50 + \#B \text{ m}\Omega$
- $B = \#C \mu\text{Nms}$
- $J = (\#D + \#E) \mu\text{Nms}^2$
- $K_b = (\#F + \#G + \#H) \text{ mVs}$
- $K_\tau = (\#F + \#G + \#H) \text{ mNm/A}$

