

Recursion Methods

Agenda

- Recall recursion
- Define tail recursion
- Define non-tail recursion
- Process a String recursively
- Examples
- Classwork: CodingBat

Recall

Recursion: It is the process where a function calls itself to solve problems by breaking them into smaller subproblems.

```
public static int fact(int x)
{
    if (x == 1)
        return 1;
    else
        return x * fact(x - 1);
}
```



Base Case



Recursive Case

Tail Recursion

In tail recursion, **no other operation is needed** after the successful execution of a recursive function call.

The **function directly returns the result** of a recursive call without performing any operations on it.

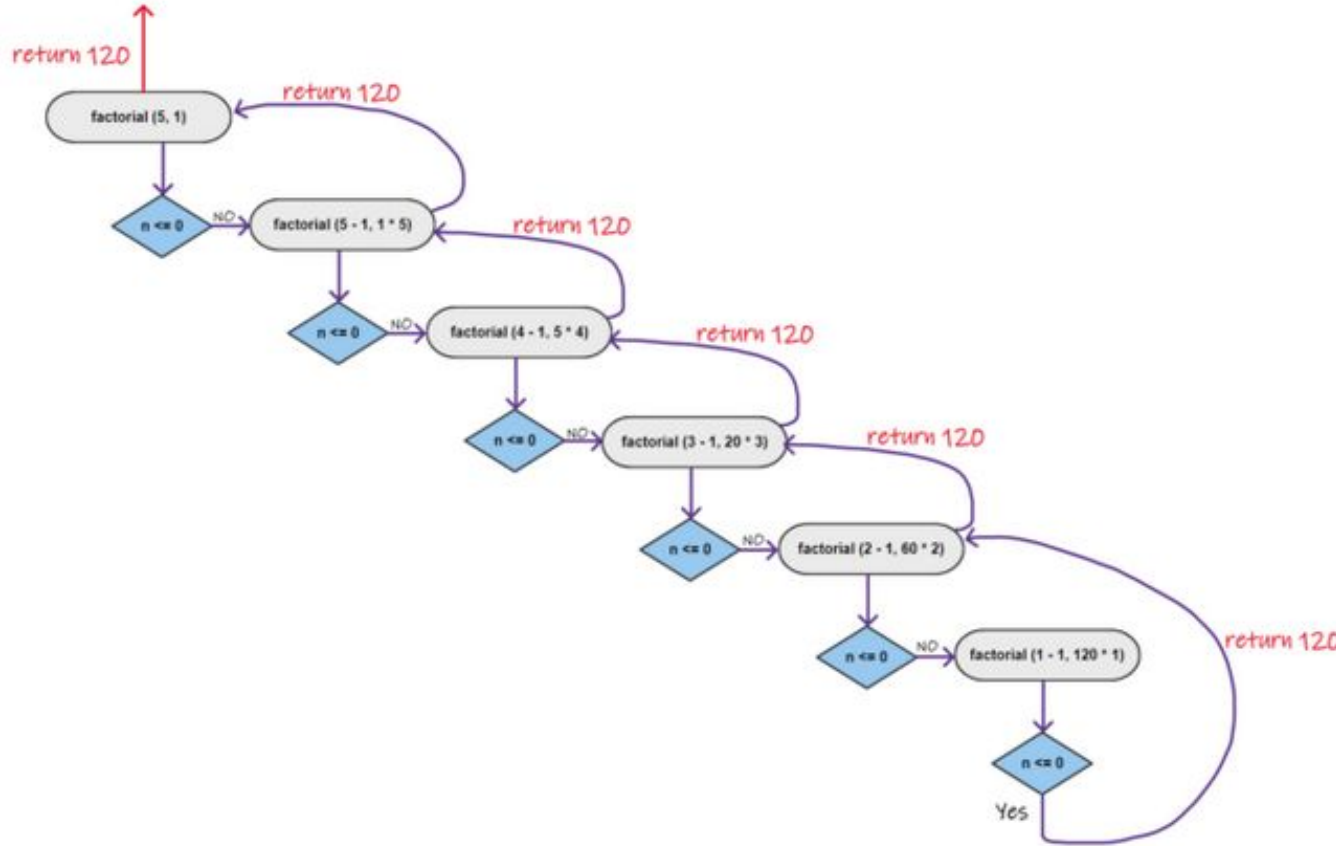
```
public static int fact(int x, int prevMult){  
    if (x <= 0)  
        return prevMult;  
    else  
        return fact(x - 1, x * prevMult);  
}
```

The **prevMult** parameter accumulates the product as the recursion progresses.

The base case stops when $x \leq 0$ and returns the accumulated product (prevMult). To ensure the multiplication starts correctly, **prevMult should be initialized to 1** because multiplying by 1 does not alter the result.

Example: fact(5, 1);

Tail Recursion



Non-Tail Recursion

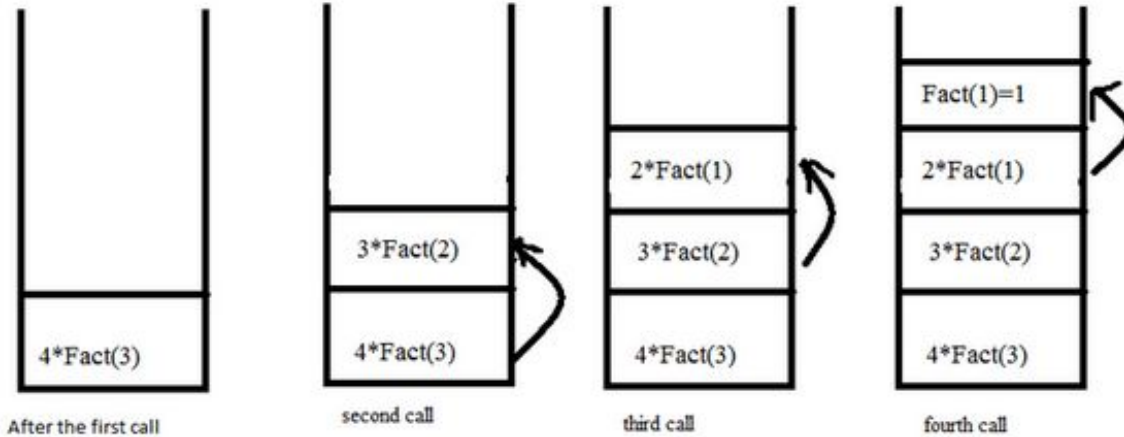
In non-tail recursion, some operations must be performed after successfully executing a recursive function.

The function **never directly returns the result of a recursive call**. It performs some operations on the returned value of the recursive call to achieve the desired output.

```
public static int fact(int x) {  
    if (x == 1)  
        return 1;  
    else  
        return x * fact(x - 1);  
}
```

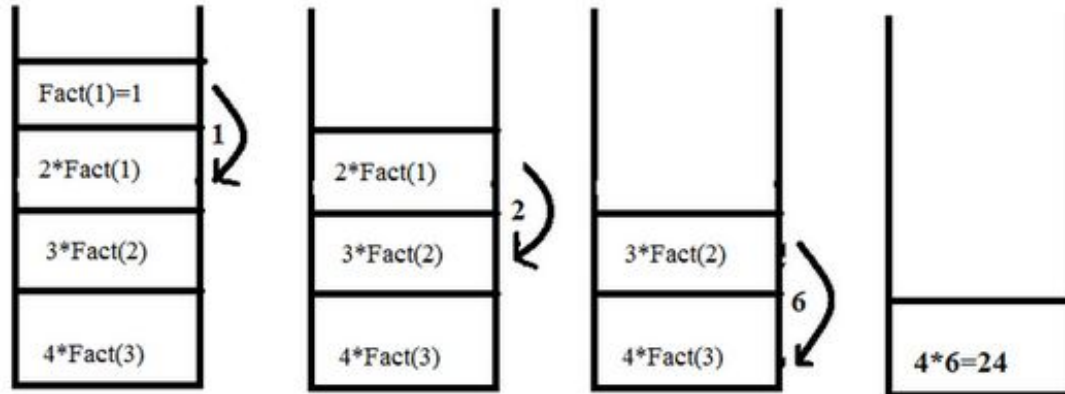


When function call happens previous variables gets stored in stack



Non-Tail Recursion

Returning values from base case to caller function



Tail Recursion vs. Non-Tail Recursion

Tail recursion is considered better than non-tail recursion because tail recursive functions can be **optimized by modern compilers**.

Tail recursion: modern compilers know that since it is tail recursive and no other operations will be performed after the recursive call, there is **no need to maintain a stack**. Thus retaining the current function call in the stack frame is of no use. **It avoids stack overflow when calling a recursive method.**

Non-tail recursion fully utilizes the stack frame and uses the value returned from the recursive call. **JVM must retain all the stack frames**, no matter how many they are, to compute the end result correctly. This leads to memory overuse and sometimes results in errors.

Java compiler does not currently optimize tail recursion.



Convert a Non-Tail Recursion to a Tail Recursion?

It is possible to make the conversion by **passing additional parameter to maintain the state of the recursive call.**

The idea is to maintain the result of calculation throughout the recursive calls, from start to end. Do not wait to compute the result until the terminal condition is met.

```
public static int factorial(int n) ;           // Non-tail recursion
```

```
public static int factorial(int n, int prevMult) ; // Tail recursion
```



How to process a String?

You know:

"A string is set of characters, so we can say a string is a **character followed by a string.**"

Let's say myStr is a string variable, and you have to write a recursive function that examines the character in that string.

Strategy:

- 1) Your recursive method should do something with the first element.
- 2) Use the rest of the string to make a recursive call to process it.



Use recursion to find the length of a String

```
public static int myLen(String s){  
    if (s.equals(""))    // Base Case  
        ???  
    else                  // Recursive Case  
        ???  
}
```



Solution: myLength

```
public static int myLen(String s){  
    if (s.equals(""))  
        return 0;  
  
    else  
        return myLen(s.substring(1)) + 1;  
  
}
```



Step by step

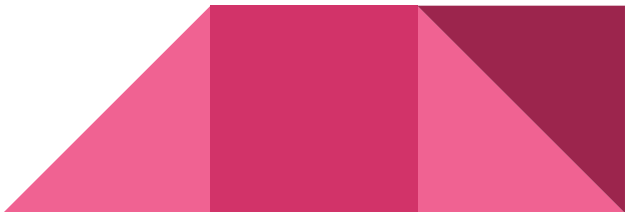
```
myLen("dog")  
  s = "dog"  
  myLen("og") + 1
```

```
myLen("og")  
  s = "og"  
  myLen("g") + 1
```

```
myLen("g")  
  s = "g"  
  myLen("") + 1
```

```
myLen("")  
  s = ""  
  Base case => return 0
```

```
public static int myLen(String s){  
    if (s.equals(""))  
        return 0;  
    else  
        return myLen(s.substring(1)) + 1;  
}
```



Example: pairStar

Given a string, compute recursively a new string where identical chars that are adjacent in the original string are separated from each other by a "*".

`pairStar("a")` → "a"

`pairStar("hello")` → "hel*lo"

`pairStar("xxyy")` → "x*xy*y"

`pairStar("aaaa")` → "a*a*a*a"



pairStar("a") → "a"
pairStar("hello") → "hel*lo"
pairStar("xxyy") → "x*xy*y"
pairStar("aaaa") → "a*a*a*a"

Strategy:

- 1) Your recursive method should do something with the first element.
- 2) Use the rest of the string to make a recursive call to process it.

1. What should be the base case? Hint: string length, what value should it be?
2. Recursive cases? Hint: Look at the strategy

```
public String pairStar(String str) {  
    if(str.length() <= 1)  
        return str;  
    else if(str.charAt(0) == str.charAt(1))  
        return str.charAt(0) + "*" + pairStar(str.substring(1));  
    else  
        return str.charAt(0) + pairStar(str.substring(1));  
}
```

Classwork

https://codingbat.com/home/jnovillo@stuy.edu/recursion_2_strings

https://codingbat.com/home/jnovillo@stuy.edu/recursion_3

Extra Problems:

https://codingbat.com/home/jnovillo@stuy.edu/apcsa_extra_recursion

