



Evaluation of Postfix Expressions

Do Now

What is a prefix expression?

What is an infix expression?

What is a postfix expression?



Infix expression

An operator is written in between two operands.

Example: $4 * 10$

Prefix Expression

It requires that all operators precede the two operands that they work on.

Example: $* 4 10$

Postfix Expression

In this type of expression an operator is written after its operands.

Example: $4 10 *$



Specifications to design your calculator to evaluate postfix expressions

- Operands could be valid numbers (int or double). For our calculator let's use double numbers.

- Valid operators:

Add (+) Subtract (-)

Multiply (*) Divide (/)

Remainder (%)



Specifications to design your calculator to evaluate postfix expressions

- The operators work on 2 values (4 10 *)
- The expressions we are going to evaluate are strings and all operands and operators are separated by a single space.

Examples:

"10 2.5 /"

"8 2 + 99 9 - * 2 + 9 -"

"4 5 - 2 + 1.5"

"2 4 6 8 10 + * - -"



Group discussion

Let's think on an algorithm that can help us evaluate a postfix expression.

Consider the following questions:

- How can you read postfix expression (string)?
- You must use a data structure to evaluate the expression, which one would you use?
- Explain how your algorithm would work.

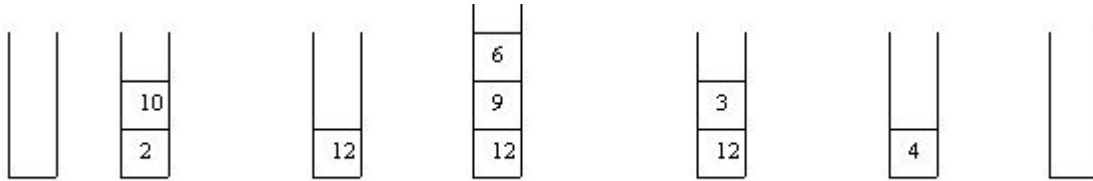


Would your algorithm work for the following postfix expressions?

Postfix Expression	Infix Equivalent	Result
4 5 7 2 + - ×	$4 \times (5 - (7 + 2))$	-16
3 4 + 2 × 7 /	$((3 + 4) \times 2) / 7$	2
5 7 + 6 2 - ×	$(5 + 7) \times (6 - 2)$	48
4 2 3 5 1 - + × + ×	$? \times (4 + (2 \times (3 + (5 - 1))))$	not enough operands
4 2 + 3 5 1 - × +	$(4 + 2) + (3 \times (5 - 1))$	18
5 3 7 9 ++	$(3 + (7 + 9)) \dots 5???$	too many operands

Could a stack work?

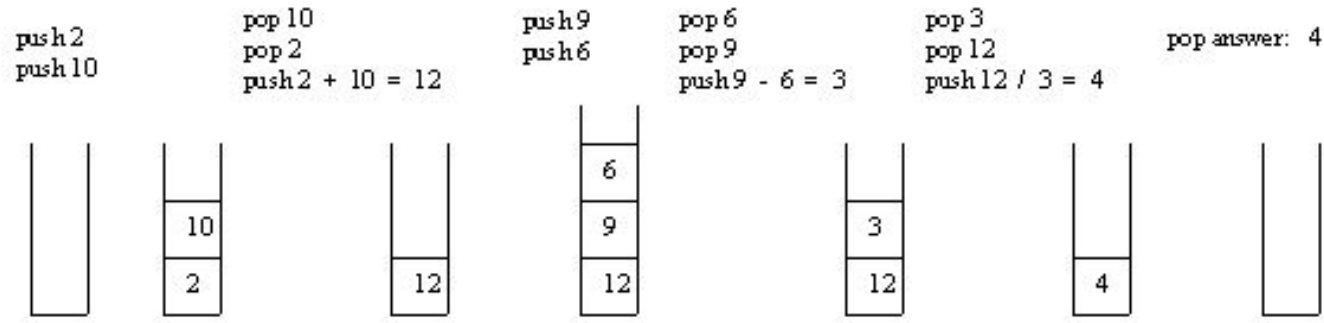
Postfix Expression: **2 10 + 9 6 - /**



- What happens when there is an operand in the expression?
- What happens when there is an operator in the expression?
- Is there a way to know if there are too many or too few operands/operators?

Postfix expression using a stack

Expression: **2 10 + 9 6 - /**



Stack Calculator - Implementation

- Save your work here:
.../APCSA_1/apcsa-assignments-YourUsername/classwork/42_stack_calculator/Calculator.java
- Write the method eval(String expression)

```
public class Calculator{  
  
    // Evaluate a postfix expression stored in expression  
    public static double eval(String expression){  
        return 0.0;  
    }  
  
}
```

- String expression: Contains ints, doubles, and operators (+ - / * and %) separated by one space
- You must use an ArrayDeque<Double> to store the values. It will act as a stack.
- Return a double value
- Throw an IllegalArgumentException when there are too many or too few operands/operators.

Some Examples

https://github.com/novillo-cs/apcsa_material/blob/main/classwork/33_postfix_expressions/examples.md

