TOWER OF HANOI

Recursive Algorithm

Origins

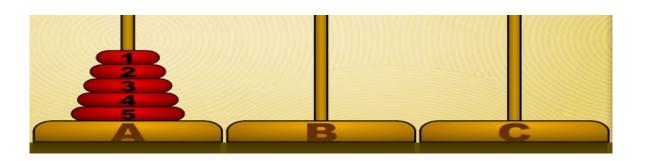
The french mathematician Édouard Lucas invented the Tower of Hanoi puzzle around 1883.

It is associated with a legend of a Hindu temple:

- It was used to increase mental discipline of young priests.
- 64 gold rings stacked on one of three post.
- Recreate the stack on another post: move 1 ring at a time, smaller ring on top of a larger one.
- How long would it take?

At a rate of one movement per second -> 2^{64} - 1 sec. = **585 billion years** > 42 times the age of a universe





Rules

- Move one ring at a time

No ring may be placed on top of a ring that is smaller than it.

Activities

https://www.mathplayground.com/logic_tower_of_hanoi.html (mute the tab so you do not get annoyed by the sound)

- 1. How many moves for 1 ring from tower A to tower C?
- 2. How many moves for 2 rings from tower A to tower C?
- 3. How many moves for 3 rings from tower A to tower C?

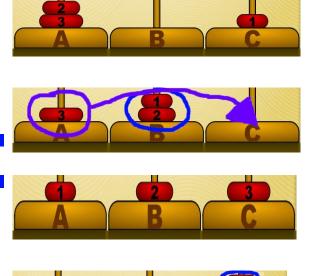
Solution for 3 rings

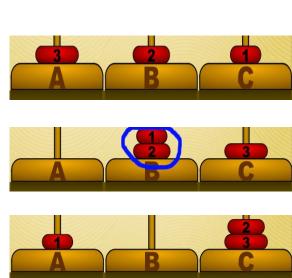




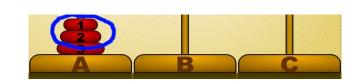
T(2, A, B, C)

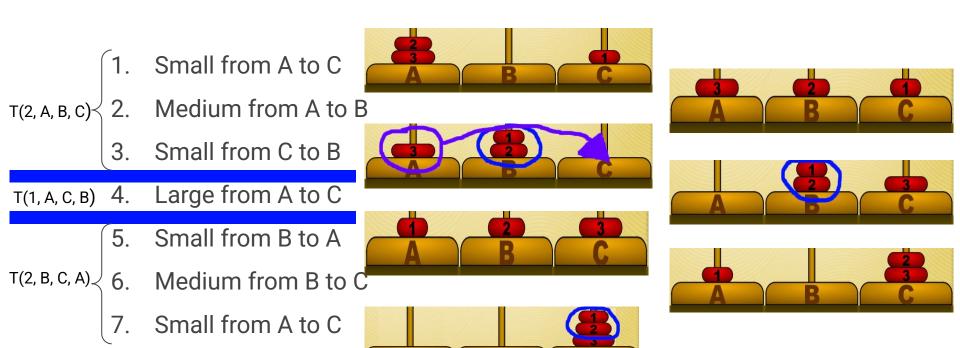
- 2. Medium from A to B
- 3. Small from C to B
- T(1, A, C, B) 4. Large from A to C
- 5. Small from B to A
 - 6. Medium from B to C
 - 7. Small from A to C





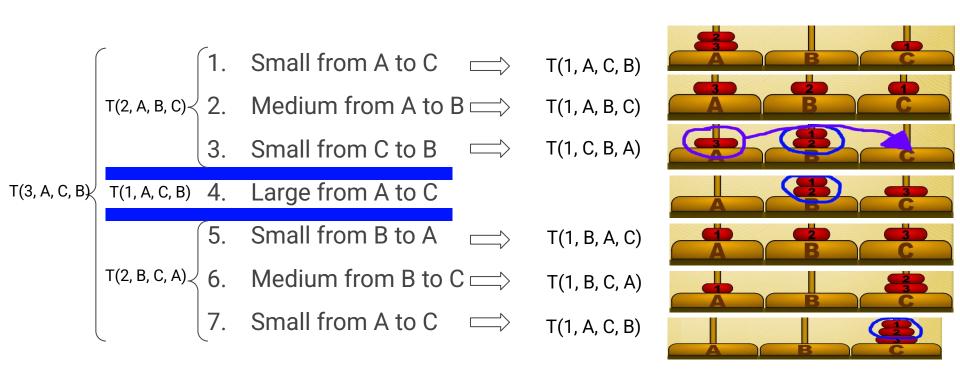
Solution for 3 rings



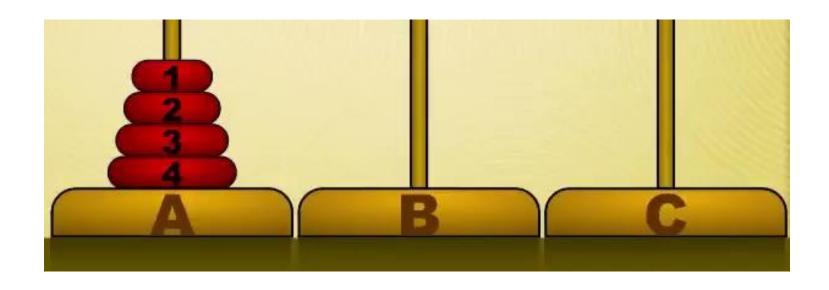


Solution for 3 rings

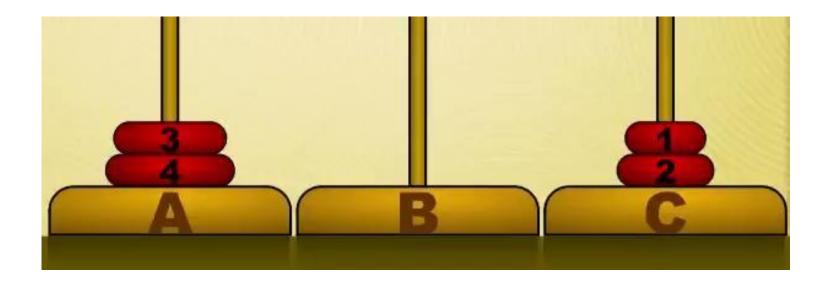




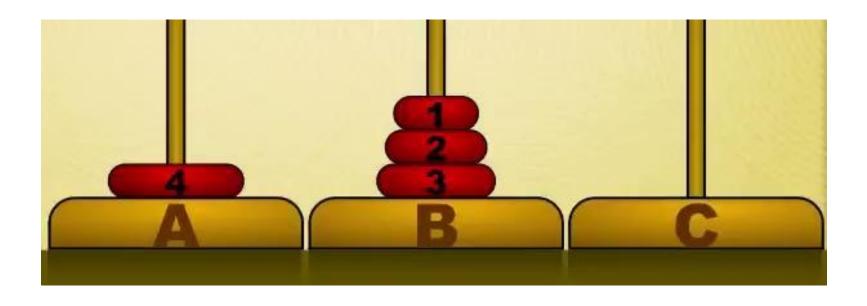
Solution for 4 ring (first step)



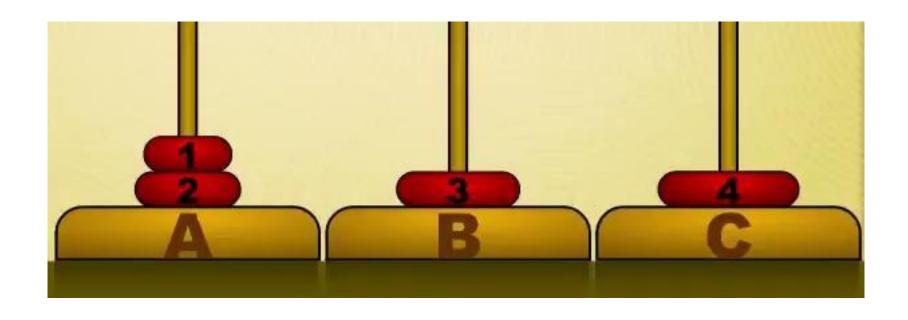
Solution for 4 ring (second step)

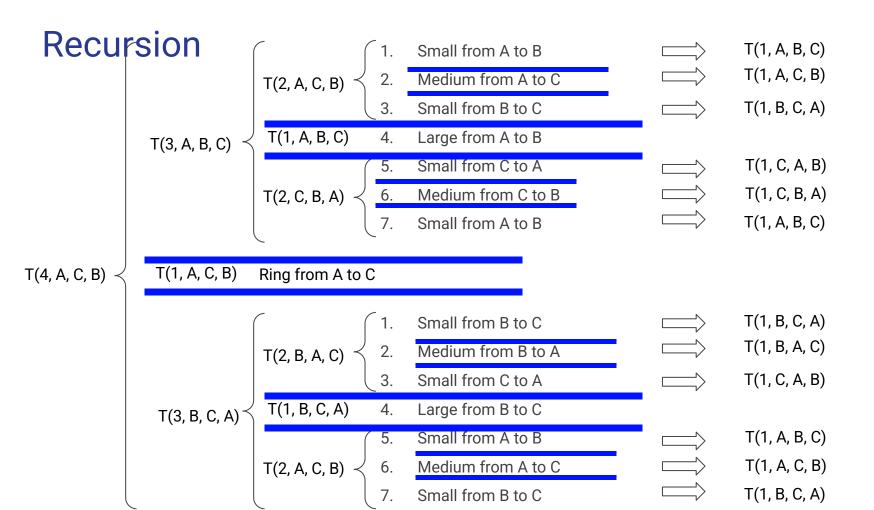


Solution for 4 ring (third step)



Solution for 4 ring (last step)





Recursion

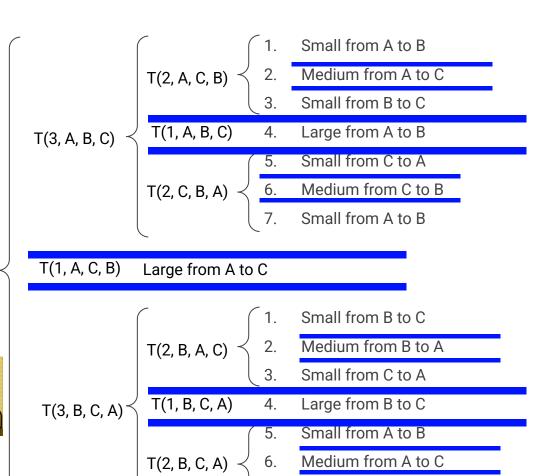
T(n, A, C, B):

T(n-1, A, B, C)

Move ring from A to C

T(n-1, B, C, A)

T(4, A, C, B)



Small from B to C

Numbers of moves

Minimal number of moves required $= 2^n - 1$

Where, *n*= number of rings.

For 3 rings: $2^3 - 1 = 7$ movements

Number of rings (N)	Number of Moves ((2**N)-1)	2**N
1	1	1
2	3	4
3	7	8
4	15	16
5	31	32
6	63	64
7	127	128
8	255	256

Coding Time !!!

Write a function to move n rings from source rod to destination rod, print the moves of each ring.

```
public static void hanoiMild(int n, char source_rod, char destination_rod, char
aux_rod) {
    YOUR CODE HERE
}
```

Output with 3 rings:

Move ring 1 from source A to destination C
Move ring 2 from source A to destination B
Move ring 1 from source C to destination B
Move ring 3 from source A to destination C
Move ring 1 from source B to destination A
Move ring 2 from source B to destination C
Move ring 1 from source A to destination C