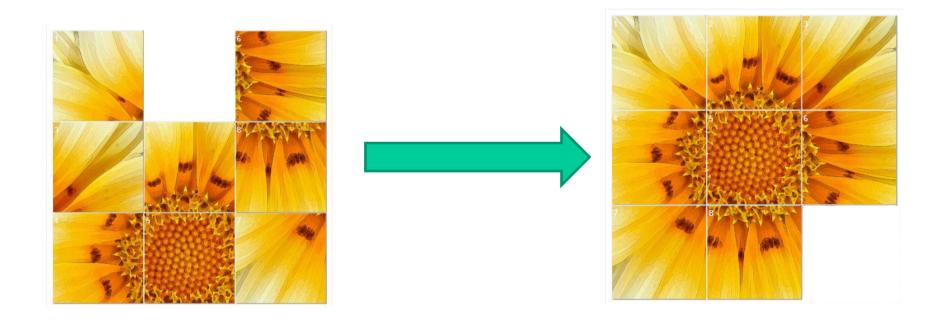
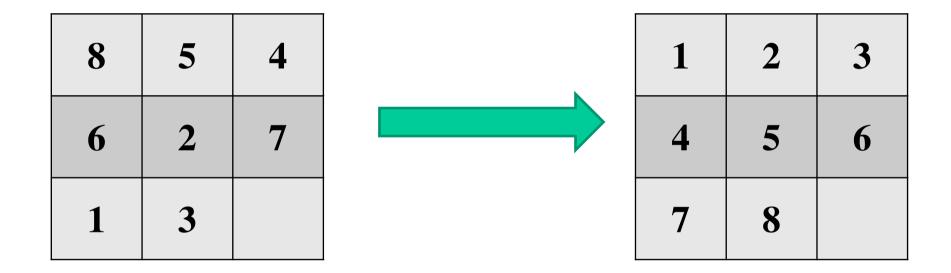
The A* Algorithm





• The goal is to go from the **initial state** to the **goal state**

8	5	4
6	2	
1	3	7

8	5	4
6	2	7
1	3	

8	5	4
6	2	7
1		3

5	4
2	
3	7
	2

8	5	
6	2	4
1	3	7

8	5	4
6	2	7
1	3	

8	5	4
6		2
1	3	7

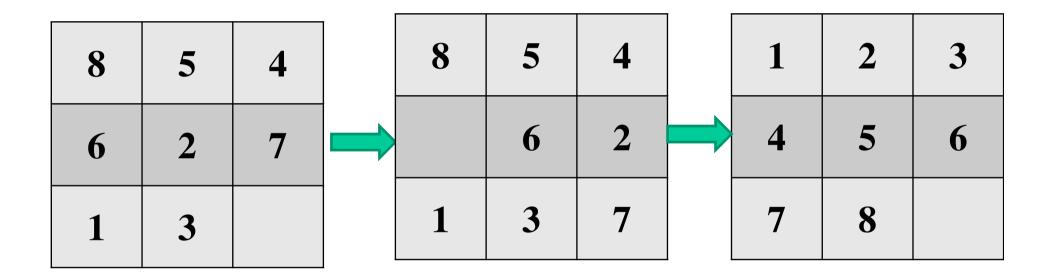
8	5	4
6	2	
1	3	7

8	5	4
6		2
1	3	7

8		4
6	5	2
1	3	7

8	5	4
6	3	2
1		7

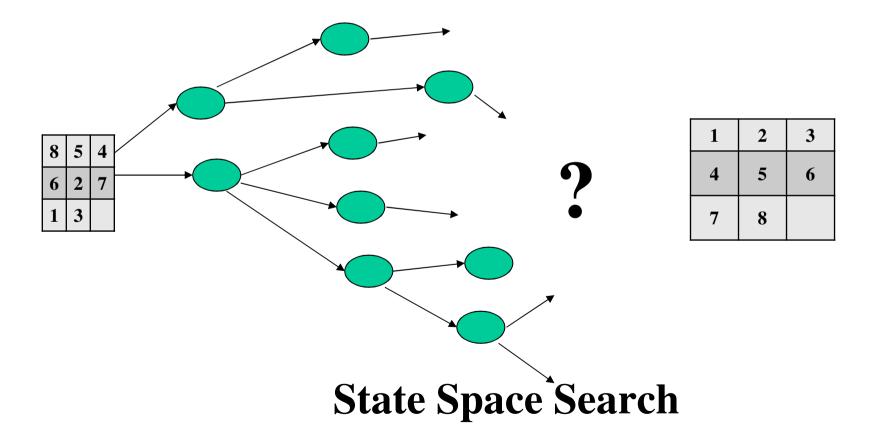
8	5	4
	6	2
1	3	7



• The goal is to go from the initial state to the goal state via other states in minimum number of moves

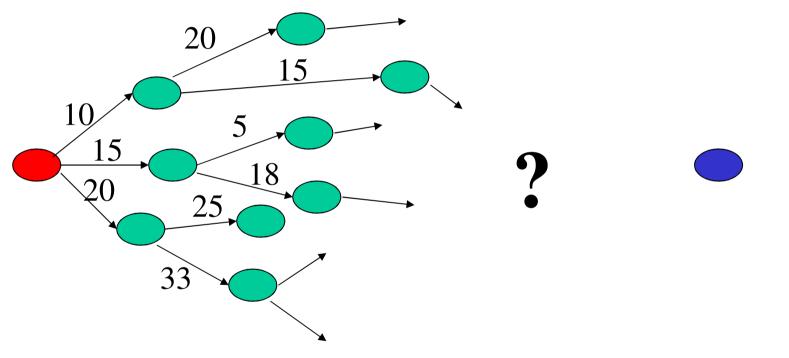
Can be considered as a graph

Starting from a node n find the shortest path to a goal node g



The Generalized Search Problem

Starting from a node n find the shortest path to a goal node g



We want: A path
$$\rightarrow$$
 v1 \rightarrow v2 \rightarrow ... \rightarrow

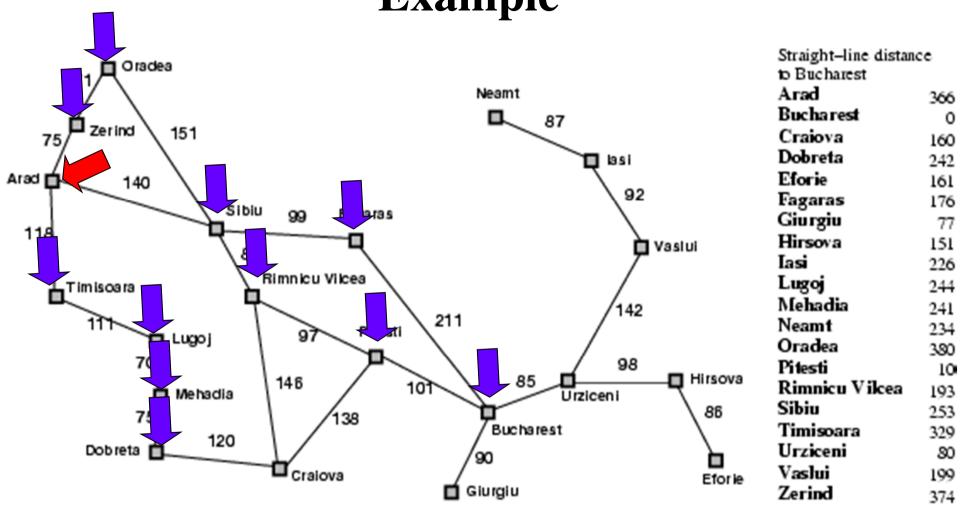
Such that
$$g(\bullet) = cost(\bullet \rightarrow v1) + cost(v1 \rightarrow v2) + ...$$

+ $cost(vn-1 \rightarrow \bullet)$ is minimum

How to solve this problem ??

Djikstra Algorithm???

Example



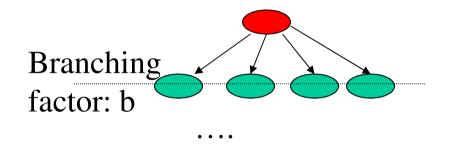
What does Djikstra's algorithm will do? (minimizing g(n))

Problem: Visit too many nodes, some *clearly* out of the question

Complexity

- Actual complexity is $O(|E|\log_2|E|)$
- Is this good?

 Actually it is bad for very large graphs!



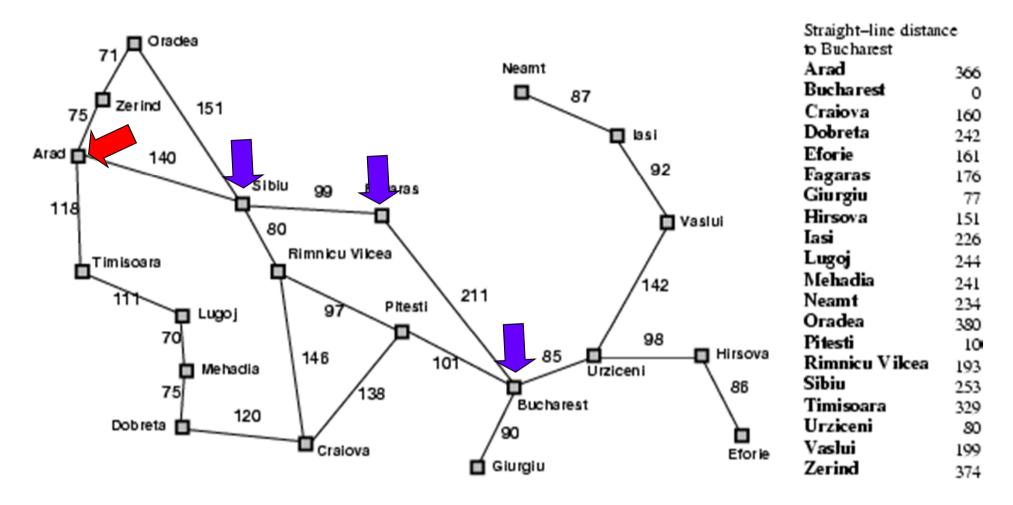
$$\#$$
 nodes = $b^{(\# levels)}$

Another Example: think of the search space in chess

Better Solution: Make a "hunch"!

- Use *heuristics* to guide the search
 - Heuristic: estimation or "hunch" of how to search for a solution
- We define a heuristic function:
 - h(n) = "estimate of the cost of the cheapest path from the initial state to the goal state"

Lets Try A Heuristic



Heuristic: minimize h(n) = "Euclidean distance to destination"

Problem: not optimal (through Rimmici Viicea and Pitesti is shorter)

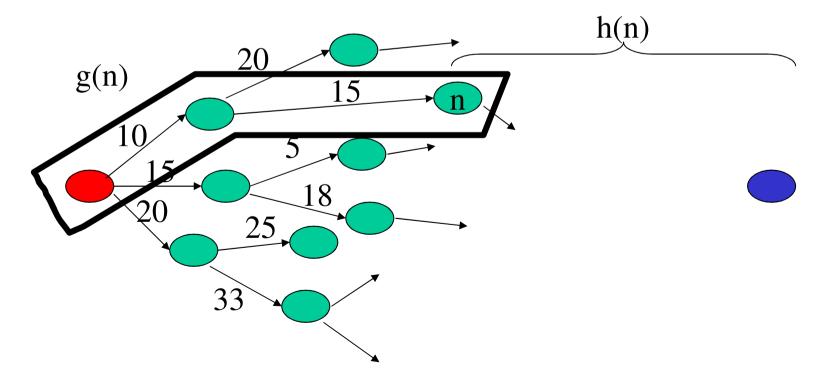
The A* Search

- **Difficulty**: we want to still be able to generate the path with minimum cost
- A* is an algorithm that:
 - Uses heuristic to guide search
 - While ensuring that it will compute a path with minimum cost

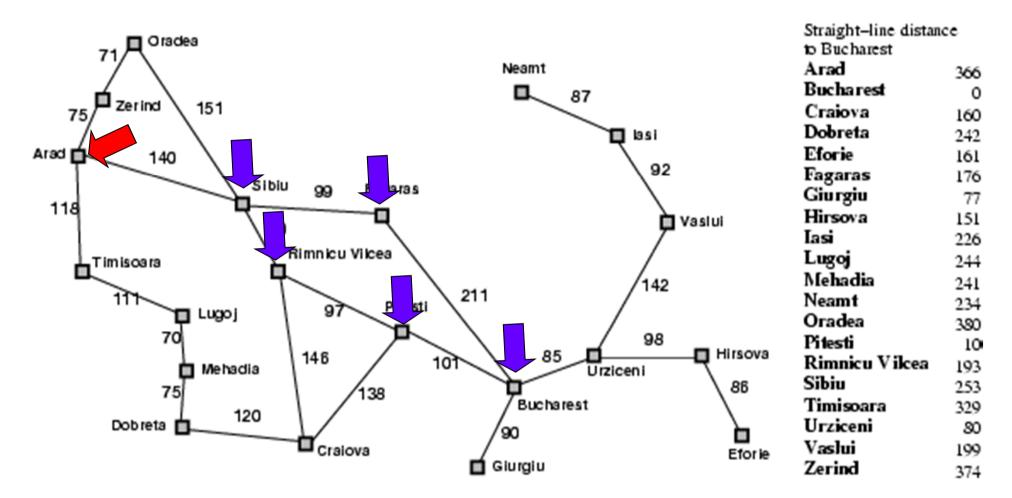
• A* computes the function f(n) = g(n) + h(n) "estimated cost"

"actual cost"

- f(n) = g(n) + h(n)
 - -g(n) = "cost from the starting node to reach n"
 - h(n) = "estimate of the cost of the cheapest path from n to the goal node"



Example

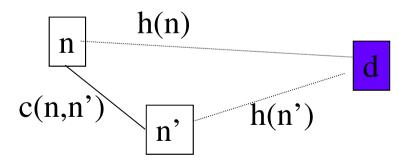


 A^* : minimize f(n) = g(n) + h(n)

Properties of A*

- A* generates an optimal solution if h(n) is an admissible heuristic and the search space is a tree:
 - h(n) is admissible if it never overestimates the cost to reach the destination node
- A* generates an optimal solution if h(n) is a consistent heuristic and the search space is a graph:
 - h(n) is **consistent** if for every node n and for every successor node n' of n:

$$h(n) \le c(n,n') + h(n')$$



- If h(n) is consistent then h(n) is admissible
- •Frequently when h(n) is admissible, it is also consistent

Admissible Heuristics

• A heuristic is admissible if it is optimistic, estimating the cost to be smaller than it actually is.

• Example:

In the road map domain,

h(n) = "Euclidean distance to destination"

is admissible as normally cities are not connected by roads that make straight lines

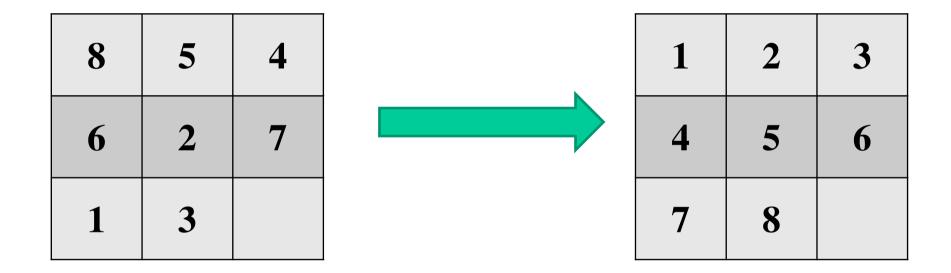
What if the heuristic is **too** optimistic??

How to Create Admissible Heuristics

- Relax the conditions of the problem
 - This will result in admissible heuristics!
- Lets look at an 8-puzzle game:

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• Possible heuristics?



• The goal is to go from the **initial state** to the **goal state**

Example: Admissible Heuristics in 8-Puzzle Game

- Heuristic: a tile A can be moved to any tile B
 - H1(n) = "number of misplaced tiles in board n"
- Heuristic: a tile A can be moved to a tile B if B is adjacent to A
 - H2(n) = "sum of distances of misplaced tiles to goal positions in board n"
- Some experimental results reported in Russell & Norvig (2002):
 - A* with h2 performs up to 10 times better than A* with h1
 - A* with h2 performs up to 36,000 times better than a classical uninformed search algorithm (iterative deepening)

A* in Games

- Path finding
 - http://aigamedev.com/open/interviews/mario-ai/
- A* can be used for planning moves computer-controlled player (e.g., chess)

