# Comparison of Cauchy EDA vs. Rosenbrock Algorithms Using BBOB 2010 Noiseless Testbed

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## **ABSTRACT**

Rosenbrock's algorithm is compared with the estimation-ofdistribution algorithm equipped with Cauchy distribution. Both algorithms were already presented at the BBOB 2009 workshop where Cauchy EDA usually ranked better than Rosenbrock's algorithm. This paper compares them in more detail and adds to understanding of their key differences.

# **Categories and Subject Descriptors**

G.1.6 [Numerical Analysis]: Optimization—global optimization, unconstrained optimization; F.2.1 [Analysis of Algorithms and Problem Complexity]: Numerical Algorithms and Problems

## **General Terms**

Algorithms

### **Keywords**

Benchmarking, Black-box optimization

#### 1. INTRODUCTION

The Rosenbrock's algorithm was introduced [9]. Its performance on the BBOB 2009 noiseless test suite was reported in [7]. The second algorithm in this comparison, Cauchy EDA, is an estimation of distribution algorithm with isotropic Cauchy distribution [5]. To fight the premature convergence, it uses a constant multiplier to enlarge the variance of the distribution (as suggested in [4]).

# 2. ALGORITHM PRESENTATION

The descriptions of the algorithms along with the paparemetr settings can be found in [7] and [5], respectively. For both algorithms, the crafting effort CrE= 0.

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#### 3. RESULTS

Results from experiments according to [2] on the benchmark functions given in [1, 3] are presented in Figures 1, 2 and 3 and in Table 1. The expected running time (ERT), used in the figures and table, depends on a given target function value,  $f_t = f_{\rm opt} + \Delta f$ , and is computed over all relevant trials as the number of function evaluations executed during each trial while the best function value did not reach  $f_{\rm t}$ , summed over all trials and divided by the number of trials that actually reached  $f_t$  [2, 8]. Statistical significance is tested with the rank-sum test for a given target  $\Delta f_{\rm t}$  (10<sup>-8</sup> in Figure 1) using, for each trial, either the number of needed function evaluations to reach  $\Delta f_{\rm t}$  (inverted and multiplied by -1), or, if the target was not reached, the best  $\Delta f$ -value achieved, measured only up to the smallest number of overall function evaluations for any unsuccessful trial under consideration.

Rosenbrock's algorithm ouperforms Cauchy EDA on functions 1, 2, 5, 6, 20, 21, 22, 23, while Cauchy EDA beats G3PCX on functions 7, 10, 11, 13, 17, 18, i.e. in this small competition the G3PCX wins 8:6. (The results on the other functions are mixed, or neither algorithm solved the problem successfuly.)

In Fig. 1, we can often see a peek at the beginning of the ERT ratio lines (funtions 1, 5, 11, 13). In the biginning of evolution, both algorithms need adapt their models to the fitness landscape. The peak means that Cauchy EDA probably needs more time for this adaptation.

Interesting situation can be seen when comparing results for functions 2 and 10 (separable and non-separable version of the ellipsoid function). In the first case, the model of Rosenbrock's algorithm is actually initialized to the correct one, and it does not need to adapt it (however, it is not clear if any adaptation takes place or not). Thanks to this correct initialization, the Rosenbrock's algorithm is faster for the separable problem. The picture for non-separable ellipsoid is, however, completely different. For 2- and 3-dimensional version, Rosebrock's algorithm is still about 2 times faster than Cauchy EDA, but for dimensions 5 and higher the Rosenbrock's adaptation mechanism looses its efficiency and the algorithm becomes very slow.

Rosenbrock's algorithm failed on functions 7 (Step-ellipsoid) and on both Schaffer's functions 17 and 18. It seems that for these functions the batch model adaptation using tens or hundreds samples is a better approach than sequential adaptation after each sampled point. Also for function 13

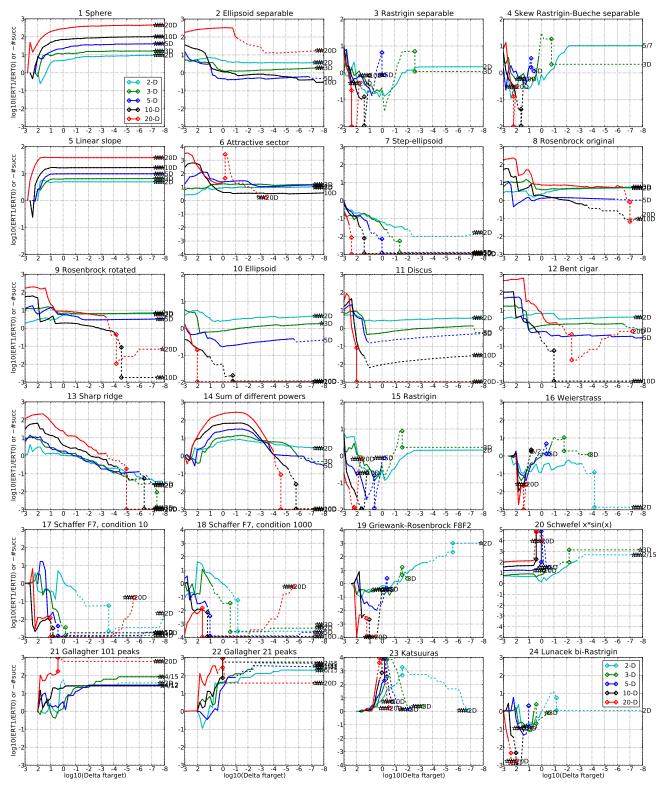


Figure 1: ERT ratio of CauchyEDA divided by Rosenbrock versus  $\log_{10}(\Delta f)$  for  $f_1-f_{24}$  in 2, 3, 5, 10, 20, 40-D. Ratios  $<10^{0}$  indicate an advantage of CauchyEDA, smaller values are always better. The line gets dashed when for any algorithm the ERT exceeds thrice the median of the trial-wise overall number of f-evaluations for the same algorithm on this function. Symbols indicate the best achieved  $\Delta f$ -value of one algorithm (ERT gets undefined to the right). The dashed line continues as the fraction of successful trials of the other algorithm, where 0 means 0% and the y-axis limits mean 100%, values below zero for CauchyEDA. The line ends when no algorithm reaches  $\Delta f$  anymore. The number of successful trials is given, only if it was in  $\{1...9\}$  for CauchyEDA (1st number) and non-zero for Rosenbrock (2nd number). Results are significant with p=0.05 for one star and  $p=10^{-\#*}$  otherwise, with Bonferroni correction within each figure.

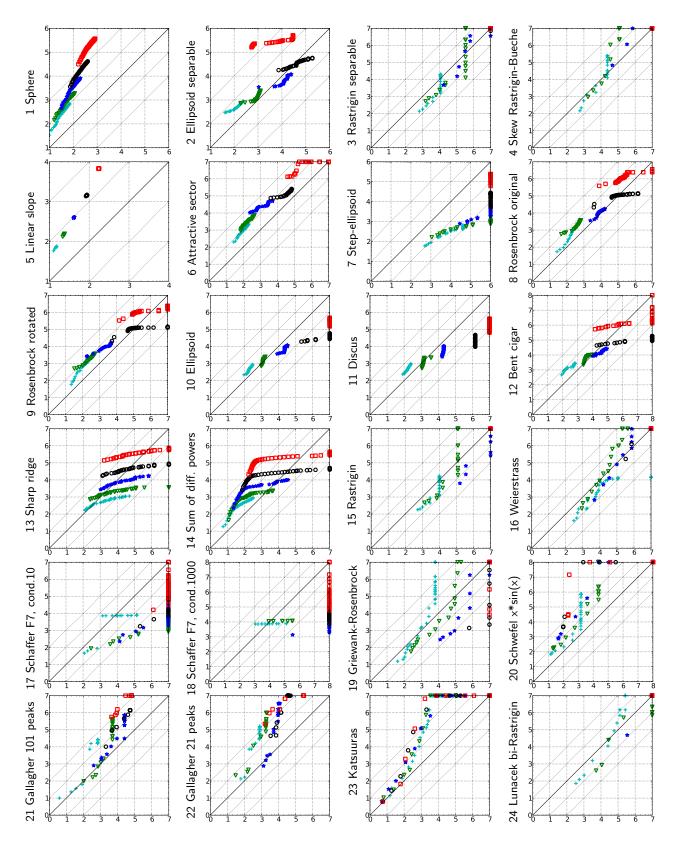


Figure 2: Expected running time (ERT in log10 of number of function evaluations) of CauchyEDA versus Rosenbrock for 46 target values  $\Delta f \in [10^{-8}, 10]$  in each dimension for functions  $f_1-f_{24}$ . Markers on the upper or right egde indicate that the target value was never reached by CauchyEDA or Rosenbrock respectively. Markers represent dimension: 2:+,  $3:\triangledown$ ,  $5:\star$ ,  $10:\circ$ ,  $20:\square$ ,  $40:\diamondsuit$ .

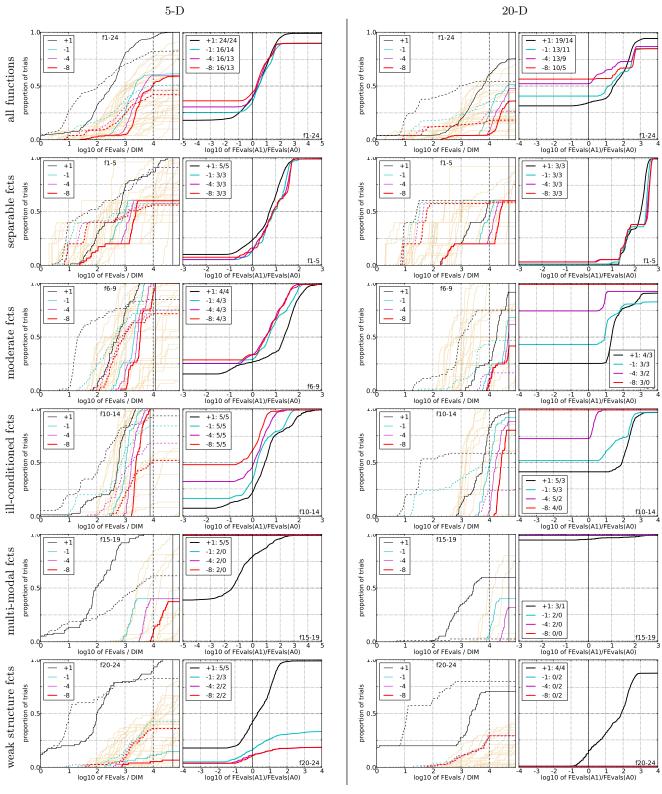


Figure 3: Empirical cumulative distributions (ECDF) of run lengths and speed-up ratios in 5-D (left) and 20-D (right). Left sub-columns: ECDF of the number of function evaluations divided by dimension D (FEvals/D) to reach a target value  $f_{\rm opt} + \Delta f$  with  $\Delta f = 10^k$ , where  $k \in \{1, -1, -4, -8\}$  is given by the first value in the legend, for CauchyEDA (solid) and Rosenbrock (dashed). Light beige lines show the ECDF of FEvals for target value  $\Delta f = 10^{-8}$  of algorithms benchmarked during BBOB-2009. Right sub-columns: ECDF of FEval ratios of CauchyEDA divided by Rosenbrock, all trial pairs for each function. Pairs where both trials failed are disregarded, pairs where one trial failed are visible in the limits being > 0 or < 1. The legends indicate the number of functions that were solved in at least one trial (CauchyEDA first).

5-	-D	20-D

$\Delta f \mid 1e+$	1 1e+0	1e-1	1e-3	1e-5	1e-7	#succ	$\Delta f$	1e+1	1e+0	1e-1	1e-3	1e-5	1e-7	#succ
f <sub>1</sub> 11	12	12	12	12	12	15/15	$\mathbf{f_1}$	43	43	43	43	43	43	15/15
0: Ros 2.9			8.7*3	12*3	15*3	15/15	0: Ros 1: Cau	3.8*3	5.8*3 1.6e3	7.2*3 2.5e3	3 <b>11</b> *3 4.3e3	14*3 6.1e3	1 <b>7</b> *3 7.8e3	$\frac{15}{15}$
1: Cau 41 f <sub>2</sub> 83	90 87	170 88	310 90	460 92	600 94	15/15	f <sub>2</sub>	380	390	390	390	390	390	15/15
0: Ros 13*	100	140		190	240	12/15	0: Ros	1.4*3		5.8*3		<b>73</b> *3	<b>73</b> *3	14/15
1: Cau 42	49	58		100	120	15/15	1: Cau		510	610	800	990	1.2e3	15/15
f <sub>3</sub> 720 0: Ros 24	1600 390	1600 ∞	1600 ∞	1700 ∞	1700	15/15 0/15	63 0: Ros	5100 ~	7600 ~	7600 ~	7600 ∞	7600 ~	$7700$ $\infty 1.4e5$	15/15 0/15
1: Cau 6.7	2.2e3	∞ ∞	∞	∞	$\infty$ 4.6e4 $\infty$ 2.5e5	0/15	1: Cau	∞ ∞	∞	∞	∞	∞	$\infty$ 1.4e5 $\infty$ 1.0e6	0/15
f <sub>4</sub> 810		1700	1800	1900	1900	15/15	$_{ m f_4}$	4700	7600	7700	7700	7800	1.4e5	9/15
0: Ros 57	$\infty$	$\infty$	$\infty$	$\infty$	$\infty 5.0e4$	0/15	0: Ros 1: Cau	∞ ∞	∞ ∞	∞	∞ ∞	$\infty$	$\infty 1.6e5$ $\infty 1.0e6$	0/15 0/15
1: Cau 85 f <sub>5</sub> 10	∞ 10	$\infty$ 10	∞ 10	 10	$\infty 2.5e5$ 10	0/15	f <sub>5</sub>	41	41	41	41	41	41	15/15
0: Ros 4*3						15/15	0: Ros	4.2*3	4.3*3	3 4.3*3	4.3*	3 <b>4.3</b> *		15/15
1: Cau 39	41	41	41	41	41	15/15	1: Cau	160	170	170	170	170	170	15/15
f <sub>6</sub> 110	210	280	580	1000	1300	15/15	f <sub>6</sub>	1300 31*3	2300 <b>56</b> *3	3400 1 <b>50</b> *3	5200 <b>570</b> *3	6700	8400	15/15
0: Ros <b>2.2</b> 1: Cau 92	*3 <b>2.8</b> *3	2.4 <sup>*3</sup>	4.3 <sup>*3</sup>	2.8*3 35	34*3	$\frac{15/15}{15/15}$	0: Ros 1: Cau	1.0e3	1.3e3	∞ ∞	∞	∞ ∞	$\infty 2.0e5$ $\infty 1.0e6$	0/15 0/15
f <sub>7</sub> 24	320	1200	1600	1600	1600	15/15	f <sub>7</sub>	1400	4300	9500	1.7e4	1.7e4	1.7e4	15/15
0: Ros 1.2e	3 670	∞ .	$\infty$	~	$\infty$ 1.5e4	0/15	0: Ros	$\infty$	$\infty$	∞	$\infty$	$\infty$	$\infty 6.7e4$	0/15
1: Cau 33*3	3 4.9* <sup>2</sup>	2.4*3	2.9*3	2.9*3	3.4* <sup>3</sup>	15/15	1: Cau	44*3	29*3	18*3	14*3	14*3	14*3	15/15
68 73 0: Ros 32*2	270	340	390	410	420	15/15	<b>f</b> 8 0: Ros	2000 3.8*3	3900 <b>24</b> *3	4000 28*3	4200 42*3	4400 <b>62</b> *3	4500 670	15/15 0/15
0: Ros 32*2 1: Cau 49	23 31	<b>22</b> * 33	$\frac{25}{34}$	30 37	36 40	$\frac{13}{15}$ $\frac{15}{15}$	1: Cau		180	210	260	360	540	4/15
fo 35	130	210	300	340	370	15/15	f <sub>9</sub>	1700	3100	3300	3500	3600	3700	15/15
0: Ros 5.3	*3 9.8*3	3 <b>10</b> *3	$14^{*2}$	14*2	$14^{*2}$	15/15	0: Ros	8.4*3		<b>37</b> * <sup>3</sup>	63* <sup>3</sup>	$\infty$	$\infty2.0e5$	0/15
1: Cau 71	54	45 570	41	42 830	43	15/15	1: Cau	190 7400	270 8700	290 1.1e4	310 1.5e4	470 1.7e4	630 1.7e4	6/15
f <sub>10</sub> 350 0: Ros 24	500 44	40	630 37	29	880 37	15/15 10/15	f <sub>10</sub> 0: Ros		000	000	$\infty$	$\infty$	$\infty 2.0e5$	0/15
1: Cau 11	9	9.4	12	11	13	15/15	1: Cau	20 <sup>*3</sup>	<b>22</b> *3	<b>20</b> *3	20 <sup>*3</sup>	21 <sup>*3</sup>	25 <sup>*3</sup>	15/15
f <sub>11</sub> 140		760	1200	1500	1700	15/15	f <sub>11</sub>	1000	2200	6300	9800	1.2e4	1.5e4	15/15
0: Ros 120 1: Cau 18	88 17	26 6	18 5.3	14 5.6	13 5.9	$\frac{12/15}{15/15}$	0: Ros	∞ 64*3	$^{\infty}_{44^{\star3}}$	$22^{\star 3}$	$22^{\times 3}$	∞ 25 <sup>*3</sup>	∞2.0e5 <b>26</b> <sup>★3</sup>	0/15
f <sub>12</sub> 110		370	460	1300	1500	15/15	1: Cau f <sub>12</sub>	1000	1900	2700	4100	1.2e4	1.4e4	15/15 $15/15$
0: Ros 98	63	91	95	42	48	6/15	0: Ros	14*3	56*3	210*3	∞	∞	$\infty 2.0e5$	0/15
1: Cau 79 f <sub>13</sub> 130	41 ) 190	35 250	38 1300	17 1800	17 2300	15/15	1: Cau	510	440	420	380	390	1.1e3	0/15
0: Ros <b>7.6</b>		26	39	63	290	1/15	f <sub>13</sub>	650 2.5*3	2000 4.2* <sup>3</sup>	2800 8.3*3	1.9e4 17*3	2.4e4	3.0e4	15/15
1: Cau 21	24	25	7.4	7.3*	7.3 <sup>*3</sup>	15/15	0: Ros 1: Cau	2.5	100	100	23	120 23	$\infty 2.0e5$ 23	0/15 $15/15$
f <sub>14</sub> 9.8	41	58	140	250	480	15/15	f <sub>14</sub>	75	240	200	020	1600	1.6e4	15/15
0: Ros 2.4	*2 1.2*3	1.3*3	4.6*3	26*	43	10/15	0: Ros	2.4*3	1.2*3	3.3*3	7.4*	<sup>3</sup> ∞	$\infty2.0e5$	0/15
1: Cau 23 f <sub>15</sub> 510	29	40 1.9e4	33 2.0e4	28 2.1e4	19 2.1e4	$\frac{15/15}{14/15}$	1: Cau		270	350	210	180	25	15/15
0: Ros 310	$\infty$	∞	∞	∞	∞ 5.0e4	0/15	f <sub>15</sub> 0: Ros	3.0e4 ∞	1.5e5 ∞	3.1e5 ∞	3.2e5 ∞	4.5e5 ∞	4.6e5 $\infty 2.0e5$	$\frac{15/15}{0/15}$
1: Cau 12*2		$\infty$	$\infty$	$\infty$	$\infty2.5e5$	0/15	1: Cau	∞	∞	∞	∞	∞	$\infty 1.0e6$	0/15
f <sub>16</sub> 120		2700	1.0e4	1.2e4	1.2e4	15/15	f <sub>16</sub>	1400	2.7e4	7.7e4	1.9e5	2.0e5	2.2e5	15/15
0: Ros 40 1: Cau 5.6	1.2e3 1.2e3	∞ ∞	∞ ∞	∞	$\infty 5.0e4$ $\infty 2.5e5$	0/15 0/15	0: Ros 1: Cau	∞ ∞	∞ ∞	∞ ∞	∞	∞ ∞	$\infty 2.0e5$ $\infty 1.0e6$	0/15
f <sub>17</sub> 5.2		900	3700	6400	7900	15/15	f <sub>17</sub>	63	1000	4000	3.1e4	5.6e4	8.0e4	15/15
0: Ros 2.7e		∞	∞2	∞	$\infty 5.0e4$	0/15	0: Ros	2.1e4	$\infty$	$\infty$	$\infty$	$\infty$	$\infty2.0e5$	0/15
1: Cau 44 f <sub>18</sub> 100	13* <sup>3</sup>	7*3 4000	4.3 <sup>*3</sup> 9300	5.3*3 1.1e4	1.2e4	14/15 15/15	1: Cau	260*	120*3	62*3	16*3	23*3	∞1.0e6	0/15
f <sub>18</sub> 100 0: Ros 3.4e		∞	∞	∞	1.2e4 ∞5.0e4	0/15	f <sub>18</sub> 0: Ros	620 ∞	4000 ∞	2.0e4 ∞	6.8e4 ∞	1.3e5 ∞	1.5e5 ∞2.0e5	15/15 0/15
1: Cau 13*3	3 12*3	2.4*3	2.7*3	3.7*3	8.6*3	14/15	1: Cau	96* <sup>3</sup>	42 <sup>*3</sup>	15*3	12*3	38* <sup>3</sup>	$\infty 1.0e6$	0/15
f <sub>19</sub> 1	1	240	1.2e5	1.2e5	1.2e5	15/15	f <sub>19</sub>	1	1	3.4e5	6.2e6	6.7e6	6.7e6	15/15
0: Ros 1.3e 1: Cau300	4 7.1e5 2.1e4*2	2	$\infty$	$\infty$	$\infty 5.0e4$ $\infty 2.5e5$	0/15 0/15	0: Ros	∞ • • • • • 3	$\infty$	$\infty$	$\infty$	$\infty$	$\infty 2.0e5$	0/15
f <sub>20</sub> 16	2.1e4 850	$\frac{2}{3.8e4}$	$\infty$ 5.4e4	$\infty$ 5.5e4	5.5e4	14/15	1: Cau	8.4e3 <sup>*3</sup>	∞ 4.6e4	∞ 3.1e6	$\infty$ 5.5e6	∞ 5.6e6	0.0e6 5.6e6	0/15 $14/15$
0: Ros 2.9	*3 <b>4.6</b> *3		∞	∞	∞ 5.0e4	0/15	0: Ros	2.6*3	2.9*3	3	∞	∞	$\infty 2.0e5$	0/15
1: Cau 48	460	$\infty$	$\infty$	$\infty$	$\infty 2.5e5$	0/15	1: Cau	340	$\infty$	$\infty$	$\infty$	$\infty$	$\infty1.0e6$	0/15
f <sub>21</sub> 41	1200 7.9	1700	1700	1700 15	1800	14/15	f <sub>21</sub>	560	6500	1.4e4	1.5e4	1.6e4	1.8e4	15/15
0: Ros 9.7 1: Cau 20	27.9	15 190	15 420	420	15 410	$\frac{12/15}{4/15}$	0: Ros 1: Cau	7.8*3 1.0e3	7.6*3	3 4.7 <sup>★3</sup>	4.5*	3 4.3 <sup>★3</sup>	3 3.8 <sup>★3</sup> ∞1.0e6	$\frac{14/15}{0/15}$
f <sub>22</sub> 71	390	940	1000	1000	1100	14/15	f <sub>22</sub>	470	∞ 5600	2.3e4	$\frac{\infty}{2.5\text{e}4}$	$\frac{\infty}{2.7\text{e}4}$	1.3e5	12/15
0: Ros 19	13	10*	10 <sup>*2</sup>	$10^{*2}$	11*2	15/15	0: Ros	3.4*3	4.3*3		12*3	11*3	2.2 <sup>*3</sup>	8/15
1: Cau 11	280	780	3.5e3	3.4e3	3.3e3	1/15	1: Cau		1.2e3	$\infty$	$\infty$	$\infty$	$\infty 1.0e6$	0/15
f <sub>23</sub> 3 0: Ros 1.6	520 1.8* <sup>3</sup>	1.4e4 4.6*3	3.2e4 ∞	3.3e4 ∞	3.4e4 $\infty 2.5e4$	15/15 0/15	f23	3.2	1600 <b>4.6</b> * <sup>3</sup>	6.7e4	4.9e5	8.1e5	8.4e5	15/15
1: Cau 2.2	230	∞	∞	∞	$\infty$ 2.5e4 $\infty$ 2.5e5	0/15	0: Ros 1: Cau	1.7 1.9	4.6^	° ∞ ∞	∞ ∞	∞ ∞	$\infty 8.4e4$ $\infty 1.0e6$	0/15 0/15
f <sub>24</sub> 160		6.4e6	9.6e6	1.3e7	1.3e7	3/15	f <sub>24</sub>	1.3e6	7.5e6	5.2e7	5.2e7	5.2e7	5.2e7	3/15
0: Ros 210 1: Cau 30	∞	∞ ∞	∞ ∞	∞	$\infty 5.0e4$ $\infty 2.5e5$	0/15 0/15	0: Ros	∞	$\infty$	$\infty$	$\infty$	$\infty$	$\infty 2.0e5$	0/15
1. Cau 30	•	30	•	30	~ 2.000	1 0/10	1: Cau	$\infty$	$\infty$	$\infty$	$\infty$	$\infty$	$\infty 1.0e6$	0/15

Table 1: Expected running time (ERT in number of function evaluations) divided by the best ERT measured during BBOB-2009 (given in the respective first row) for different  $\Delta f$  values for functions  $f_1-f_{24}$ . The median number of conducted function evaluations is additionally given in *italics*, if  $\text{ERT}(10^{-7}) = \infty$ . #succ is the number of trials that reached the final target  $f_{\text{opt}} + 10^{-8}$ . 0: Ros is Rosenbrock and 1: Cau is CauchyEDA. Bold entries are statistically significantly better compared to the other algorithm, with p = 0.05 or  $p = 10^{-k}$  where k > 1 is the number following the  $\star$  symbol, with Bonferroni correction of 48.

Table 2: The average time demands per function evaluation (in microseconds) of the two compared algorithms.

Dim	2	3	5	10	20	40
Rosenbrock	310	312	320	334	350	370
CauchyEDA	51	17	9	9	11	NA

(sharp ridge problem), it seems that this kind of adaptation is better

Interesting results may be found for function 14. Rosenbrock's algorithm is orders of magnitude faster than Cauchy EDA for a broad range of target levels. But for target levels at about  $10^{-5}$  and tighter, Cauchy EDA takes over and its results are much better. It seems that Rosenbrock's algorithm is not even able to find some of the tighter target levels.

Another note can be made on the variance enlargment constant used by Cauchy EDA. It was set to be approximately optimal for the Rosenbrock's function. However, such setting may be too large for other functions. The ERT ratio for sphere function shows that with increasing problem dimensionality the gap between the algorithms gets larger. Also the results for function 21 and 22 (and possibly for function 23) suggest, that the slow convergence of Cauchy EDA prevents it to be restarted more often which is the key to solve these problems; on the contrary, Rosenbrock's algorithm converges probably much faster and is thus restarted more often which gives it a chance to have higher success rate.

Looking at Fig. 3, it can be stated that Rosenbrock's algorithm beats CauchyEDA mainly on the separable functions and on weak structure functions. On the other hand, Cauchy EDA wins on moderate, ill-conditioned and multimodal functions. It can be stated that if the Rosenbrock's algorithm solves a problem, it solves it very quickly, while Cauchy EDA is usually much slower but more robust (is able to solve broader range of problems).

# 4. CPU TIMING EXPERIMENTS

The time requirements of both algorithms are taken from the respective articles, [6] and [5]. The multistart algorithm was run with the maximal number of evaluations set to  $10^5$ , the basic algorithm was restarted for at least 30 seconds. The experiment was conducted on Intel Core 2 CPU, T5600, 1.83 GHz, 1 GB RAM with Windows XP SP3 in MATLAB R2007b. The comparison of the average time demands per function evaluation are shown in Table 2.

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