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# Clinical trial design based on a multistate model that jointly models progression-free and overall survival

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# Who

Meller *et al.* (2019):



Erdmann *et al.* (2023):



**Power gains through exploiting correlations:**

**Group-sequential designs: over time.**

**Enrichment designs:  
over nested subpopulations.**

**Goal:**

**design trial with PFS and OS**

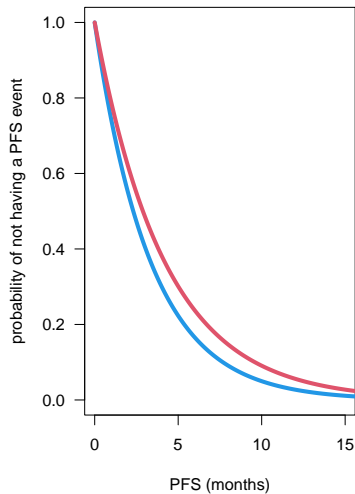
**Co-primary (win both) or multiple (win  $\geq 1$ )**

## **Typical approach:**

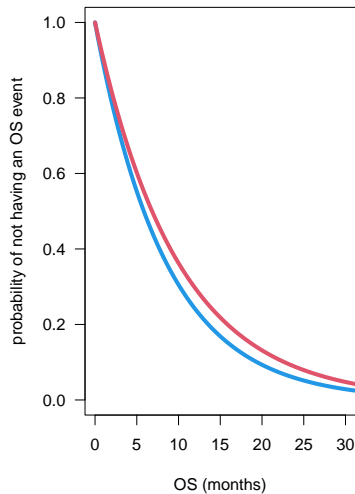
- 1) Split significance level**
- 2) PFS: exponential, plan GSD**
- 3) OS: exponential (or NPH), plan GSD,  
align OS interim with PFS final**

## Example: exponential for PFS and OS

$m1 = 2.31$  /  $m2 = 2.89$   
hazard ratio = 0.80



$m1 = 5.84$  /  $m2 = 6.83$   
hazard ratio = 0.86



Compute necessary #events based on  $\alpha$ -split and GSD assumptions.

Why is this not necessarily optimal?

1) Ignores  $\text{cor}(\text{PFS}, \text{OS})$ .

2) PFS + OS both involve death  
 $\Rightarrow$  OS not independent from PFS!

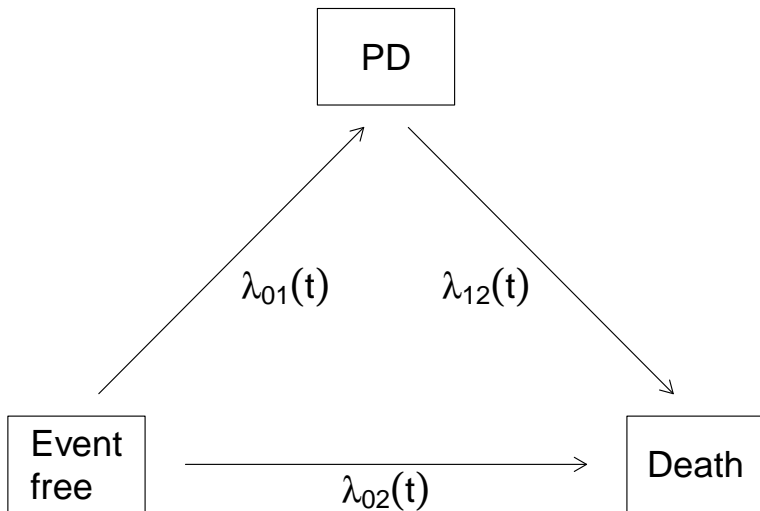
3) OS cannot be PH.

**How can we fix that?**

**PFS and OS are connected through  
illness-death model.**



## Canonical extension of survival analysis



# Illness-death multistate model for PFS and OS

Transition probabilities to move from state  $l$  at time  $s$  to state  $m$  at time  $t$ :

$$P_{lm}(s, t) := P(X(t) = m | X(s) = l, \text{history}).$$

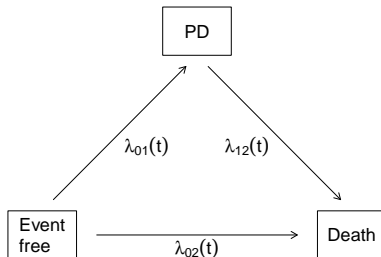
If  $X(t)$  non-Markov:  $P_{11}$  and  $P_{12}$  depend on **PFS time  $t_1$** .

Estimate  $P_{lm}$ 's **nonparametrically** by **Aalen-Johansen** estimator.

Illness-death model w/o recovery,  $P_{lm}$  as functions of transition intensities, [Aalen et al. \(2008\)](#):

$$\begin{aligned}P_{00}(s, t) &= \exp \left( - \int_s^t \lambda_{01}(u) + \lambda_{02}(u) \, du \right), \\P_{11}(s, t; \mathbf{t}_1) &= \exp \left( - \int_s^t \lambda_{12}(u; \mathbf{t}_1) \, du \right), \\P_{22}(s, t) &= 1, \\P_{01}(s, t) &= \int_s^t P_{00}(s, u-) \lambda_{01}(u) P_{11}(u, t; u) \, du, \\P_{12}(s, t; \mathbf{t}_1) &= 1 - P_{11}(s, t; \mathbf{t}_1), \\P_{02}(s, t) &= 1 - (P_{00}(s, t) + P_{01}(s, t)).\end{aligned}$$

# Illness-death model for PFS and OS



**PFS:** waiting time in initial state 0,  $\text{PFS} = \inf\{t : X(t) \neq 0\}$ .

$$S_{\text{PFS}}(t) = P(\text{PFS} > t) = P_{00}(0, t).$$

**OS:** time until reaching state 2,  $\text{OS} = \inf\{t : X(t) = 2\}$ .

$$S_{\text{OS}}(t) = P(\text{OS} > t) = P_{00}(0, t) + P_{01}(0, t).$$

# **(Non-)Proportional hazards**

# Induced survival functions

Meller *et al.* (2019):

$$\begin{aligned}S_{PFS}(t) &= P(\text{PFS} > t) = P_{00}(0, t), \\S_{OS}(t) &= P(\text{OS} > t) = S_{PFS}(t) + P_{01}(0, t).\end{aligned}$$

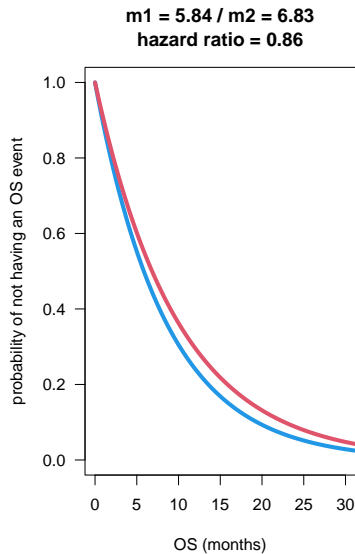
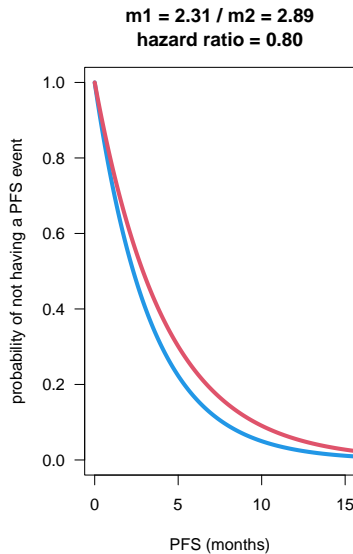
Assume **constant** transition hazards:

$$\begin{aligned}S_{PFS}(t) &= \exp\left(-(\lambda_{01} + \lambda_{02})t\right), \\S_{OS}(t) &= \frac{S_{PFS}(t)}{\lambda_{012}} \left(\lambda_{12} - \lambda_{02} - \lambda_{01} \exp(-\lambda_{012}t)\right)\end{aligned}$$

with abbreviation  $\lambda_{012} := \lambda_{12} - \lambda_{01} - \lambda_{02}$ .

Hazard functions via  $h(t) = -S'(t)/S(t)$ .

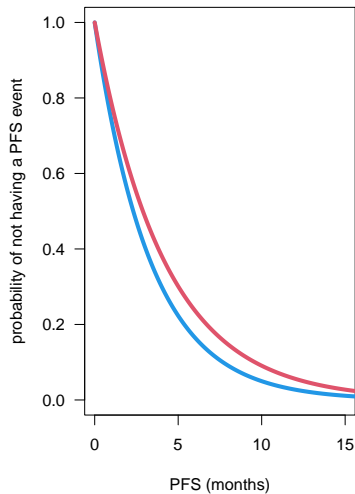
## Example: exponential for PFS and OS



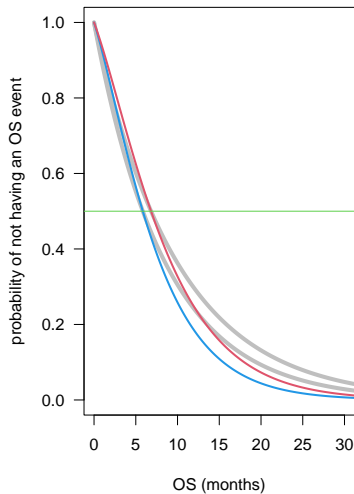
Compute necessary #events based on  $\alpha$ -split and GSD assumptions.

## Example: median-matching survival functions induced by IDM

$m1 = 2.31$  /  $m2 = 2.89$   
hazard ratio = 0.80

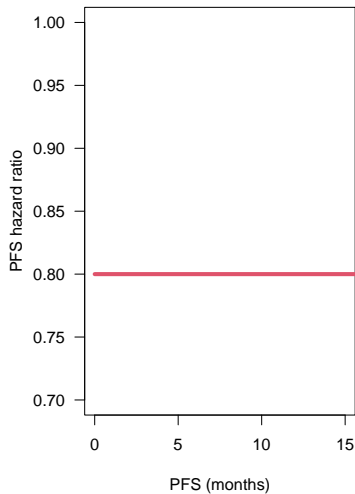


$m1 = 5.84$  /  $m2 = 6.83$   
hazard ratio = 0.86 / average HR = 0.83

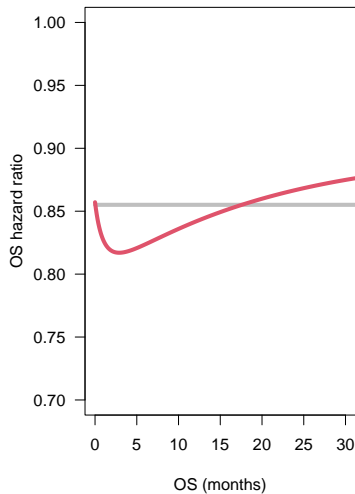


## Example: hazard ratio as function of time - **mind y-axis!**

$m1 = 2.31 / m2 = 2.89$   
hazard ratio = 0.80



$m1 = 5.84 / m2 = 6.83$   
hazard ratio = 0.86 / average HR = 0.83





# Proportional hazards for OS

**PH for PFS** for time-homogeneous transition hazards.

Hazard ratio for OS:

$$h_{OS}(t) = \frac{(\lambda_{12} - \lambda_{02})(\lambda_{01} + \lambda_{02}) - \lambda_{01}\lambda_{12} \exp(-\lambda_{012}t)}{(\lambda_{12} - \lambda_{02}) - \lambda_{01} \exp(-\lambda_{012}t)}.$$
$$\theta_{OS}(t) = h_{OS,A}(t)/h_{OS,B}(t).$$

When is  $\theta_{OS}(t)$  independent of  $t$ ?

- $\lambda_{12} = \lambda_{02}$  **in both groups**: progression has no impact on death hazard.
- $\lambda_{01} = 0$  **in both groups**: no progression occurs.
- $\lambda_{012} := \lambda_{12} - \lambda_{01} - \lambda_{02} = 0$ : denominator of  $h_{OS}$  equal to 0.

Assumption that we have PH for PFS AND OS  
unrealistic to hold in real clinical trial.

# Clinical trial design via simulation from IDM

# Clinical trial planning

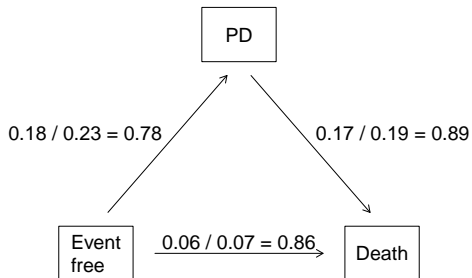
- Type I error:  $P(\text{reject at least one } H_0 \text{ irrespective of which are true})$ .
- Power: assume  $\geq 1$   $H_1$  is true:
  - ▶ **Endpoint-specific:**  $P(\text{reject } H_0)$  for each endpoint separately.
  - ▶ **At least:**  $P(\text{reject } \geq 1 H_0 \text{ of PFS and OS})$ .
  - ▶ **Joint:**  $P(\text{reject both } H_0 \text{ for PFS and OS})$ .

# Clinical trial design

Design feature	Standard approach	Illness-death model
<b>Assumptions to make</b>	Control medians and hazard ratios for PFS and OS	Transition-specific hazards
<b>#quantities</b>	4	6
<b>Cor(PFS, OS)</b>	Not exploited	Explicitly modelled through IDM
<b>Proportional hazards</b>	Assumed for OS, although not met	NPH properly induced through IDM
<b><math>\alpha</math> allocation</b>	Bonferroni	Bonferroni
<b>Number of events</b>	Schoenfeld's formula	Tune through simulation
<b>Power</b>	Disjoint per endpoint	Any type of power

# Simulation of PFS - OS

## Scenario 4



Features:

- Drug effect on all transitions.
- PFS HR = 0.8.
- Average hazard ratio for OS: 0.832.

# How to plan a trial?

## Co-primary endpoints PFS and OS, one analysis each

Global significance level: 0.05.

Design feature	PFS	OS
Local significance level	0.01	0.04
Critical value	2.576	2.054
Hazard ratio	0.80	0.832 (AHR)
Power	80%	80%
Events using Schoenfeld	939	992
Simulate from IDM under $H_0$	Empirical type I error: 0.0499	
Joint power of Schoenfeld sample size with these critical values	Joint power: 0.708	
Tune number of events to get endpoint-specific power of 80%	939	905
Empirical power per endpoint	0.797	0.801
Empirical joint power	Joint power: 0.686	



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Empirical joint power	Joint power: 0.686	

**Before you ask...**

## ...let me make a few comments

**NPH for OS:** should we use something else than logrank test and hazard ratio?

- Hypothesis test and effect quantification **independent** of MSM.

What is role of the **Markov** assumption?

- Markov assumption: probability of future transition only depends on (i) state currently occupied and (ii) time  $t$ .
- If violated: individual transition hazards random quantities through dependence on history.
- $S_{PFS}$ ,  $S_{OS}$ : estimation straightforward even if  $X$  non-Markov.
- [Meller et al. \(2019\)](#): joint distribution of PFS and OS for non-Markov. Can be leveraged.

## ...let me make a few comments

Do we always **gain power** for OS? **No!**

Power for OS depends on:

- **Knowledge of PFS to "predict" OS.**
- **Induced shape** of survival functions. Relative effect can be smaller than, e.g., that of median-matching exponential survival functions.

Interim analysis for OS: see paper.

Does the IDM approach make some "regulatory-incompatible" assumptions?

- In our opinion **not at all.**
- Need to assume 6 transition-specific hazards. Maybe more uncommon to inform, but **conceptually no different** from PFS / OS medians.
- Current approach: assumes PH for OS  $\Rightarrow$  we know can't be true!
- $\pm$  Markov.

# Conclusions

# Conclusions and outlook

## Conclusions:

- Illness-death model for PFS and OS:
  - ▶ Properly account for **induced** hazard ratio as a function of time,  $\theta_{OS}(t)$ , for OS.
  - ▶ Exploit correlation between PFS and OS.
- Sample size for OS might **decrease** or **increase**!
- **Proper simulation** of PFS and OS on patient-level.

## Outlook:

- **Broadly applicable:** surrogacy, interim decisions based on PFS, OS prediction, ...
- Combine subpopulation + illness-death model for PFS - OS. **Tira trials**.
- Extendable to more states, [Beyer et al. \(2020\)](#).

# Resources

## Resources:

- Meller et al., [Meller et al. \(2019\)](#).
- [Paper on arxiv](#).
- Package **simIDM** on [github](#) and [CRAN](#). Exponential, Weibull, piecewise exponential transition hazards.
- [Linkedin post](#).
- Further MSM resources:
  - ▶ [Beyer et al. on use of MSMs for early-phase decision-making](#), [Beyer et al. \(2020\)](#).
  - ▶ [MS example](#).
  - ▶ [Material of BBS seminar "Competing Risks and Multi-State Models"](#).
  - ▶ [oncomsm: R package by Boehringer colleagues, "Bayesian Multi-State Models for Early Oncology"](#).

**Slides can be downloaded on**  
**[www.kasparrufibach.ch](http://www.kasparrufibach.ch).**



**Thank you for your attention.**

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**<http://www.kasparrufibach.ch>**

# References I

- ▶ Aalen, O., Borgan, O., and Gjessing, H. (2008). *Survival and event history analysis: a process point of view*. Springer Science & Business Media.
- ▶ Andersen, P. K., Borgan, O., Gill, R. D., and Keiding, N. (1993). *Statistical Models Based on Counting Processes*. Springer.
- ▶ Beyer, U., Dejardin, D., Meller, M., Rufibach, K. and Burger, H. U. (2020). A multistate model for early decision-making in oncology. *Biometrical journal* **62** 550–567.
- ▶ Erdmann, A., Beyersmann, J., and Rufibach, K. (2023). Oncology clinical trial design planning based on a multistate model that jointly models progression-free and overall survival endpoints.
- ▶ Gaschler-Markefski, B., Schiefele, K., Hocke, J., and Fleischer, F. (2014). *Multi-state Models Used in Oncology Trials*, pages 283–304. Springer Berlin Heidelberg, Berlin, Heidelberg.
- ▶ Meller, M., Beyersmann, J., and Rufibach, K. (2019). Joint modeling of progression-free and overall survival and computation of correlation measures. *Statistics in medicine*, **38**, 4270–4289.

# Backup

# Advantages of illness-death model for PFS and OS

Illness-death model:

- Assumptions on  $X(t)$  **induce** properties of transition intensities, (joint) probabilities, survival functions of PFS and OS.
- Estimation of derived quantities straightforward by plugging in estimated intensities.
- Can reflect disease specifics and drug mode-of-action in transition hazards, see also [Beyer et al. \(2020\)](#).

# Multistate model formulation

Transition probabilities:

- **Full description** of multistate model by only assuming existence of intensities  $\lambda_{01}$ ,  $\lambda_{02}$  and  $\lambda_{12}$ .
- Formulas, even for **non-Markov** case: *Aalen et al. (2008)*.

*Meller et al. (2019)*:

- Embed PFS and OS in multistate model framework,
- formulas for  $P_{lm}$ 's assuming **Weibull** transition hazards for time-inhomogeneous Markov and semi-Markov (explicit),
- inference via **counting process likelihood**,
- $P(\text{PFS} \leq u, \text{OS} \leq v)$  for  $X$  non-Markov (generic).

Allows derivation of any functional of PFS and OS.

# Assumptions for multistate model

Multistate model **sufficiently smooth** so that following intensities exist:

$$\begin{aligned}\lambda_{0j}(t) &= \lim_{\Delta t \searrow 0} \frac{P(\text{PFS} \in [t, t + \Delta t), X(\text{PFS}) = j \mid \text{PFS} \geq t)}{\Delta t}, j = 1, 2, \\ \lambda_{12}(t; t_1) &= \lim_{\Delta t \searrow 0} \frac{P(X(t + \Delta t) = 2 \mid X(t-) = 1, \text{PFS} = t_1)}{\Delta t} \\ &= \lim_{\Delta t \searrow 0} \frac{P(\text{OS} - \text{PFS} \in [t - t_1, t - t_1 + \Delta t) \mid \text{OS} \geq t, \text{PFS} = t_1)}{\Delta t} \quad \text{for } t_1 < t.\end{aligned}$$

$t_1$ : observed PFS time, i.e. time when leaving state 0.

# Assumptions for multistate model

$X(t)$  **Markov**:

- **Time-inhomogeneous**: intensity of death after progression does not depend on time of progression,  $\lambda_{12}(t; t_1) = \lambda_{12}(t)$  for all  $t_1 < t$ .
- **Homogeneous**: intensities are time-constant, i.e. **Exponential**,  $\lambda_{ij}(t) = \lambda_{ij}, i, j = 0, 1, 2$ .

$X(t)$  **non-Markov** (= semi-Markov for illness-death model without recovery):

- Intensities depend on state patient is in at  $s$  and entire history  $\leq s$ , i.e. all transitions.
- Relevant for  $1 \rightarrow 2$  transition only, as  $0 \rightarrow 1, 2$  are rooted in initial state 0.

As soon as a quantity depends on  **$1 \rightarrow 2$  transition** we need to be specific about assumption on  $X(t)$ .

# Illness-death multistate model for PFS and OS

Transition probabilities to move from state  $l$  at time  $s$  to state  $m$  at time  $t$ :

$$P_{lm}(s, t) := P(X(t) = m | X(s) = l, \text{history}).$$

Illness-death model w/o recovery,  $P_{lm}$  as functions of transition intensities, Aalen *et al.* (2008):

$$\begin{aligned}P_{00}(s, t) &= \exp\left(-\int_s^t \lambda_{01}(u) + \lambda_{02}(u) \, du\right), \\P_{11}(s, t; \mathbf{t}_1) &= \exp\left(-\int_s^t \lambda_{12}(u; \mathbf{t}_1) \, du\right), \\P_{22}(s, t) &= 1, \\P_{01}(s, t) &= \int_s^t P_{00}(s, u_-) \lambda_{01}(u) P_{11}(u, t; u) \, du, \\P_{12}(s, t; \mathbf{t}_1) &= 1 - P_{11}(s, t; \mathbf{t}_1), \\P_{02}(s, t) &= 1 - \left(P_{00}(s, t) + P_{01}(s, t)\right).\end{aligned}$$

If  $X(t)$  non-Markov:

- $P_{11}$  and  $P_{12}$  depend on **PFS time  $t_1$** .
- Although  $P_{01}, P_{02}$  depend on  $\lambda_{12}$  they **do not depend on  $t_1$** .



# Intuition behind transition probabilities

$P_{00}(s, t)$ ,  $P_{11}(s, t; t_1)$ : exp of cumulative hazards  $\Rightarrow$  standard survival functions.

$P_{01}(s, t) = \int_s^t P_{00}(s, u_-) \lambda_{01}(u) P_{11}(u, t; u) \, du$ : integral of

- $P_{00}(s, u_-) \lambda_{01}(u)$ : “infinitesimal probabilities” to move from 0 to 1 at time  $u$ ,  $u \in (s, t]$ ,
- $P_{11}(u, t; u)$ : subsequently stay in state 1 until at least time  $t$ , with progression happened in  $u$ .

# Multistate model for PFS and OS

**Joint** distribution:

$$\begin{aligned}P(\text{PFS} \leq u, \text{OS} \leq v) &= P(X(u) \in \{1, 2\}, X(v) = 2) \\&= P(X(v) = 2 | X(u) = 1) \cdot P_{01}(0, u) + P_{02}(0, u).\end{aligned}$$

**$X$  inhomogeneous Markov:**  $P(X(v) = 2 | X(u) = 1) = P_{12}(u, v)$  independent of progression time  $t_1 \leq u$ .

**$X$  non-Markov:**

- Integrate  $P_{12}(u, v; t_1)$  over conditional distribution of all possible progression times  $t_1 \leq u$ .
- Formula tedious (see [Meller et al. \(2019\)](#))  $\Rightarrow$  **simulate** in applications.

# Simulation of PFS and OS on patient level

In the past when simulating PFS and OS how did you make sure...

- ...PFS  $\leq$  OS for each patient,
- ...PFS = OS possible,
- ...association between PFS and OS transparent.

Simulation of (Markov) MSM:

- **Nested series of competing risk experiments.**
- MSM trajectories of individual in IDM can generated:
  1. Waiting time  $t_0$  in initial state: Generated from CDF  $F(t) = 1 - P_{00}(0, t)$ .
  2. State entered at  $t_0$ : binomial experiment which decides with probability  $\frac{\lambda_{01}(t_0)}{\lambda_{01}(t_0) + \lambda_{02}(t_0)}$  on State 1.  
If death  $\Rightarrow$  stop,
  3. otherwise waiting time  $t_1$  in State 1 is generated from CDF  $F(t) = 1 - \exp(-\int_{t_0}^{t_0+s} \lambda_{12}(u) \, du)$ .
  4. Death will happen at time  $t_0 + t_1$ .
- Add **drop-out** (random censoring) and **administrative censoring**.
- Non-Markov: model  $\lambda_{12}$  as function of entry time  $t_0$  and time since time origin in Step 3 above.
- All implemented in **simIDM** on **github** and **CRAN**.

# *Doing now what patients need next*

## **R version and packages used to generate these slides:**

R version: R version 4.2.3 (2023-03-15 ucrt)

Base packages: stats / graphics / grDevices / utils / datasets / methods / base

Other packages: checkmate / survival / rpact / reporttools / xtable / prodlim / simIDM

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