Finite difference scheme

# Function approximation

We consider being a function sufficiently smooth (i.e. a sufficiently high number of time derivable).

It is possible to define different approximations of this function. Also we do not have the effective formulas for the moment we will write them the following [[1](#LeV07)].

|  |  |  |
| --- | --- | --- |
| Left approximation | Centered approximation | Right approximation |
|  |  |  |

The preceding notation is for an approximation of the first order. Second and higher approximation may be indicated by an exponent. For instance the 3 order approximation of the function from the right would be indicated by the following: [[1](#LeV07)].

# Taylor expansion

We will now give the basic formula of a Taylor expansion and other more convenient forms of these formulas that once assemble allow producing schemes.

For our function of a scale variable the Taylor formula sufficiently near a point may be written the following:

|  |  |  |
| --- | --- | --- |
|  |  | (1) |

This may be rewritten the following by letting :

|  |  |  |
| --- | --- | --- |
|  |  | (1) |

# Bibliography

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| [1] | LeVeque R J., *Finite Difference Methods for Ordinary and Partial Differential Equations*. Philadelphia: Society for Industrial and Applied Mathematics (SIAM), 2007. |

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