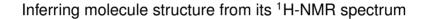
Molecular structure inference from molecular spectra – notes on machine learning methods

For context

- Computational Biology and Bioinformatics MSc (ETHZ)
- Background in numerical maths
- Machine learning or chemistry not so much
- One month in
- Today: own analysis of others' work



Inferring SMILES from simulated ¹H-NMR multiplets and the sum formula

Training dataset and transformers model

- Daniel Lowe. Chemical reactions from US patents (1976–Sep2016). figshare, 2017. 10.6084/m9.figshare.5104873.v1
- Marvin Alberts et al. "Unraveling Molecular Structure: A Multimodal Spectroscopic Dataset for Chemistry". In: NeurIPS 2024 Datasets and Benchmarks Track. 2024. 10.48550/arXiv.2407.17492
- Marvin Alberts et al. Learning the Language of NMR: Structure Elucidation from NMR spectra using Transformer Models. 2023. 10.26434/chemrxiv-2023-8wxcz

Training dataset and transformers model

- Dataset: USPTO reaction dataset¹
 - 1,435,481 reactions
 - Realistic molecules & common chemicals
- Unique molecules:
 - Initially: 1,675,439
 - Filter: 5 < # heavy atoms < 35
 - · Allowed elements: C, H, O, N, S, P, Si, B, halogens
 - After filtering: 1,416,499
 - Simulation w/ MestReNova (all spectra): 794,403 molecules
- Spectra simulated: ¹H-NMR, IR, ¹³C-NMR, HSQC-NMR, MS/MS
- "... deuterated chloroform as solvent. Default settings were used"
- Representation: SMILES

¹Lowe, 2017 [1]

Training dataset

SRC-TRAIN.TXT

- C 15 H 24 N 2 1HNMR | 6.86 6.83 d 1H J 0.68 | 5.98 5.96 s 1H | 4.22 4.19 s 2H | 3.83 3.74 p 1H J 6.74 | 3.55 3.50 m 2H | 2.24 2.21 s 3H | 2.05 1.99 m 2H | 1.35 1.32 s 5H | 1.26 1.22 d 6H J 6.67
- C 30 H 28 F N O 3 1HNMR | 7.39 7.30 m 4H | 7.30 7.05 m 11H | ... | 2.60 2.46 m 2H

...

TGT-TRAIN.TXT

- C c 1 c c 2 c (c c 1 N) N (C (C) C) ... (C) C
- O = C (C C c 1 c c c c c 1) N C (C c 1 c c c (O c 2 c c c c 2) c c 1) C (O) c 1 c c c (F) c c 1

...

Training dataset

SRC-TRAIN.TXT

- C 15 H 24 N 2 1HNMR | 6.86 6.83 d 1H J 0.68 | 5.98 5.96 s 1H | 4.22 4.19 s 2H | 3.83 3.74 p 1H J 6.74 | 3.55 3.50 m 2H | 2.24 2.21 s 3H | 2.05 1.99 m 2H | 1.35 1.32 s 5H | 1.26 1.22 d 6H J 6.67
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...

TGT-TRAIN.TXT with explicit hydrogens (new)

• [CH3] [c] 1 [cH] [c] 2 [c] ([cH] [c] 1 [NH2]) [N] ([CH] ([CH3]) [CH2] [CH2] [C] 2 ([CH3]) [CH3]

...

Input vocabulary

Constructed from 10k samples

```
|\times 92120,\ J\times 52692,\ 1H\times 46441,\ 2H\times 27470,\ m\times 25035,\ s\times 14414,\ d\times 13282,\ C\times 10000,\ H\times 10000,\ 1HNMR\times 10000,\ dd\times 9417,\ 3H\times 9343,\ O\times 9018,\ N\times 8443,\ t\times 7266,\ 2\times 6096,\ ddd\times 4820,\ 3\times 4683,\ dt\times 3241,\ 4H\times 3220,\ 4\times 2473,\ F\times 2346,\ S\times 2314,\ Cl\times 2132,\ ddt\times 1913,\ q\times 1820,\ td\times 1690,\ 5H\times 1627,\ 6H\times 1622,\ 5\times 1430,\ dddd\times 1430,\ 0.92\times 1393,\ 7.32\times 1286,\ dq\times 1266,\ 14\times 1166,\ tt\times 1163,\ 17\times 1152,\ 16\times 1144,\ 15\times 1112,\ 19\times 1098,\ 18\times 1096,\ 2.19\times 1064,\ 20\times 1060,\ 7.14\times 1058,\ p\times 1047,\ 1.47\times 1040,\ 7.33\times 1028,\ 7.69\times 1024,\ 12\times 1011,\ 2.20\times 1009,\ 7.26\times 1008,\ 13\times 994,\ 7.51\times 973,\ 11\times 956,\ 21\times 947,\ Br\times 941,\ 8H\times 929,\ 2.10\times 921,\ 22\times 918,\ \dots...
```

2019 tokens

a hard-coded dimension in the ML model on the input side

Output vocabulary

Constructed from 10k samples

```
C×94533, C×68425, (×39107, )×39107, 1×25622, O×23680, 2×17598, =×13822, N×11314, n×9750, 3×6992, F×5100, C1×2717, -×2531, 4×1826, S×1744, [C@@H]×1443, [C@H]×1257, Br×1000, [nH]×986, S×871, \#×869, /×522, O×498, 5×270, I×181, [C@]×148, [N+]×130, [O-]×112, \×106, [C@@]×100, P×62, [N-]×46, [n+]×30, 6×8, [S@]×7, [2H]×4, [C-]×3, [PH2]×1, [N@@+]×1, P×1, [S@@]×1, [N@]×1
```

43 tokens

a hard-coded dimension in the ML model on the output side

- The encoder converts input NMR tokens into 512-dimensional vectors via a trainable "embedding" with added "positional encoding" and random "dropout".
- These embeddings are processed through 4 layers of "self-attention" and feedforward networks, with "residual" (passthrough) connections and layer normalization (no masking)
- The decoder generates SMILES tokens in an autoregressive manner from a fixed output vocabulary.
- It first embeds the partial SMILES sequence with positional encoding, then, in each of its 4 layers, applies:
 - Masked self-attention (attending only to previous tokens),
 - · Cross-attention over the encoder output, and
 - A feedforward network.
- A linear generator converts the decoder output into "logits" over the SMILES vocabulary, interpreted as the probability of the next token.

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What is "attention"? – a glorified transistor

It is a mechanism that computes a weighted sum of input features, enabling the model to focus on the most relevant parts of a sequence. Introduced in "Attention is all you need" by Vaswani et al. [4].

$$\operatorname{softmax}_{\longleftrightarrow} \left(\frac{QK^T}{\sqrt{d_k}} \right) V$$

- For each token, a trainable query vector is compared to a set of trainable key vectors (from the same sequence in self-attention or from the encoder in cross-attention) via a dot-product.
- The resulting similarity scores are scaled and passed through a "softmax" (over the keys) to obtain attention weights.
- These weights determine how much each token's associated trainable value vector contributes to the output.

Training and model predictions

- Model by Alberts et al. [2], \sim 30M trainable parameters
- 679'195 training samples, batch size 4k
- Re-trained on NVIDIA 1×A10 GPU² (\sim 35h), up to 250k batches
- The model generates several hypotheses ranked by "score", i.e., log-likelihood of the prediction according to the model
- Top-N accuracy evaluated on 1'000 or 10'000 unseen samples
- "Beam search" is a heuristic to find the most likely hypotheses; use beams size 100 (i.e., 100 concurrent hypotheses, keep top 10)

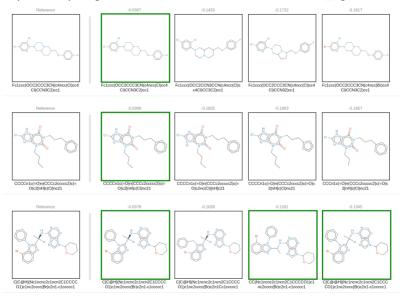
²Thanks to Lambda Cloud for compute credits

Evaluation

What is a *correct* prediction by the trained model?

- X Predicted SMILES matches exactly
- ✓ Canonicalize before comparison
- ✓ Chirality-aware
- ✓ Exclude hypotheses with the wrong molecular sum-formula

https://numpde.github.io/nmr-to-structure-lite/translate/f_figures.html



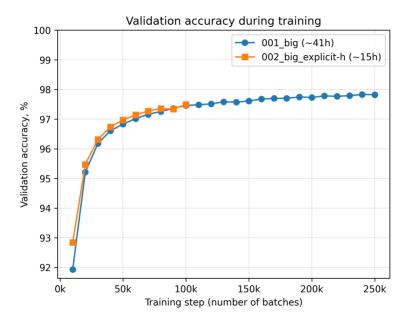
11/41

Evaluation

Validation accuracy during training -

next-token prediction accuracy over the unused validation dataset with "teacher forcing"

indicates training progress.

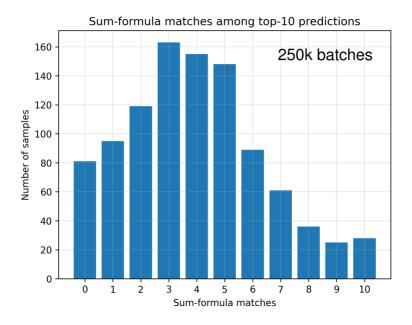


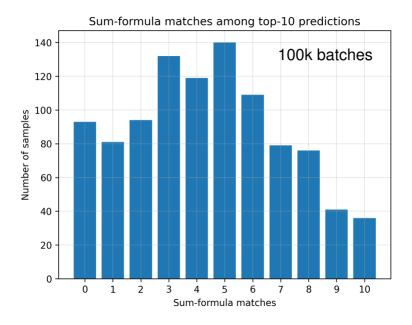
In generating SMILES token-by-token, "failures" could mean non-canonical branching

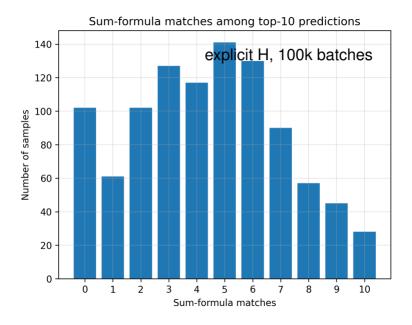
If the probability of wrong token is $\approx 2\%$ then among 50 tokens (typical size) we have at most one failure with probability $\approx 74\%$.

Evaluation

Do predictions have the correct sum-formula?



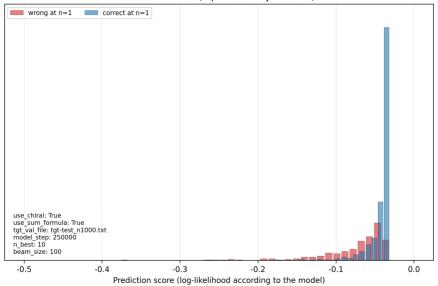




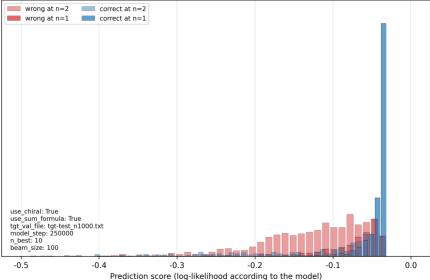
Evaluation

Which top-n predictions are correct?

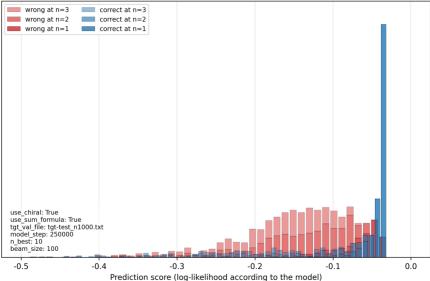
Inferred SMILES (top-1 accuracy: 62.80%)



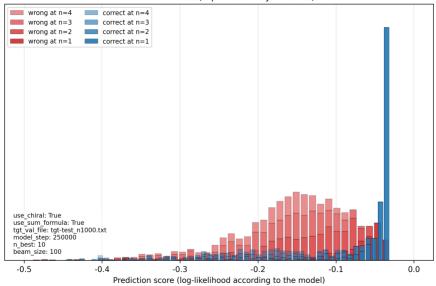
Inferred SMILES (top-2 accuracy: 71.30%)



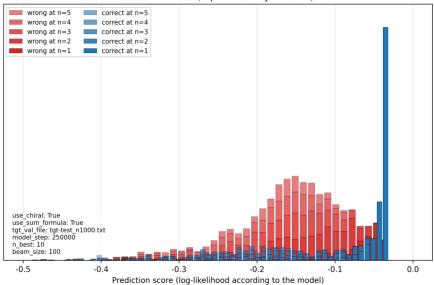
Inferred SMILES (top-3 accuracy: 74.50%)



Inferred SMILES (top-4 accuracy: 76.50%)



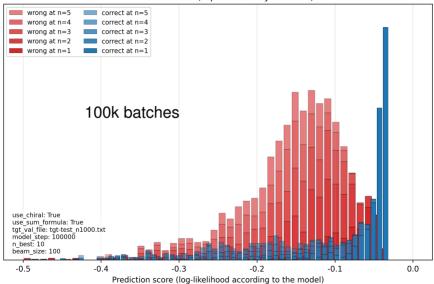
Inferred SMILES (top-5 accuracy: 77.30%)



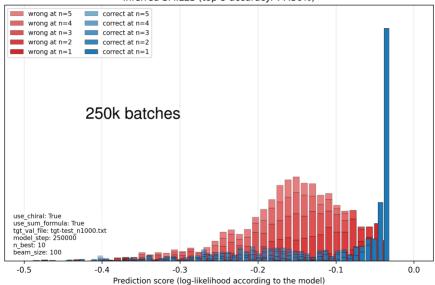
Evaluation

100k batches vs 250k batches

Inferred SMILES (top-5 accuracy: 74.70%)



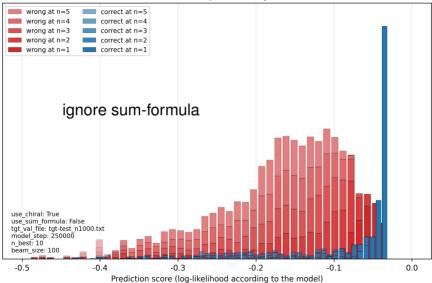
Inferred SMILES (top-5 accuracy: 77.30%)



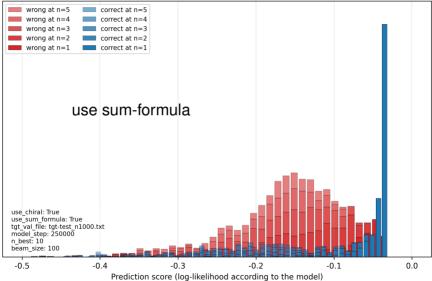
Evaluation

sum-formula: ignore or use

Inferred SMILES (top-5 accuracy: 75.80%)



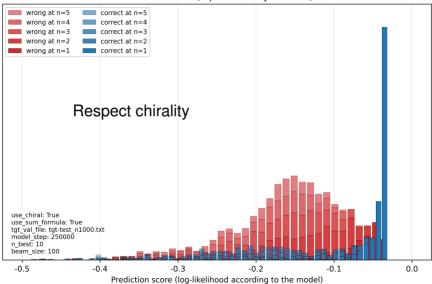
Inferred SMILES (top-5 accuracy: 77.30%)



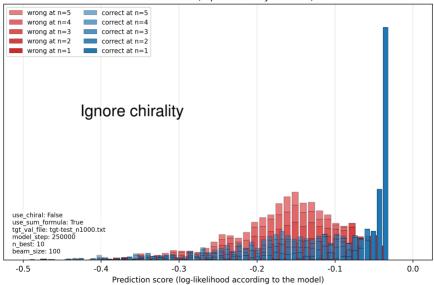
Evaluation

chirality: on vs off

Inferred SMILES (top-5 accuracy: 77.30%)



Inferred SMILES (top-5 accuracy: 78.70%)



Evaluation

explicit hydrogens: no vs yes

Inferred SMILES (top-1 accuracy: 58.40%) correct at n=1 No explicit hydrogens tgt_val_file: tgt-test_n1000.txt model_step: 100000

-0.2

Prediction score (log-likelihood according to the model)

-0.1

wrong at n=1

use chiral: True use sum formula: True

-0.4

-0.3

n best: 10 beam_size: 100 -0.5

Inferred SMILES (top-1 accuracy: 59.60%) correct at n=1 With explicit hydrogens tgt_val_file: tgt-test_n1000.txt

-0.2

Prediction score (log-likelihood according to the model)

-0.1

wrong at n=1

use chiral: True use sum formula: True

model_step: 100000 n best: 10 beam_size: 100 -0.5

-0.4

-0.3

Inferred SMILES (top-5 accuracy: 74.70%) correct at n=5 correct at n=4 correct at n=3 correct at n=2 correct at n=1 No explicit hydrogens tgt val file: tgt-test n1000.txt

-0.2

Prediction score (log-likelihood according to the model)

-0.1

wrong at n=5

wrong at n=4 wrong at n=3

wrong at n=2

wrong at n=1

use chiral: True use sum formula: True

model step: 100000 n best: 10 beam size: 100 -0.5

-0.4

-0.3

Inferred SMILES (top-5 accuracy: 74.70%) correct at n=5 correct at n=4 correct at n=3 correct at n=2 correct at n=1 With explicit hydrogens tgt val file: tgt-test n1000.txt

-0.2

Prediction score (log-likelihood according to the model)

-0.1

wrong at n=5

wrong at n=4 wrong at n=3

wrong at n=2

wrong at n=1

use chiral: True use sum formula: True

model step: 100000 n best: 10 beam size: 100 -0.5

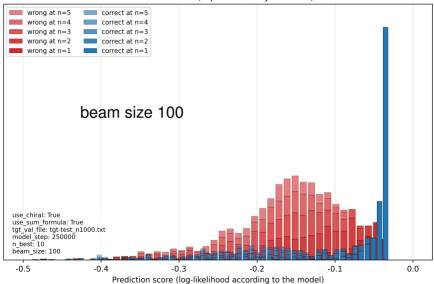
-0.4

-0.3

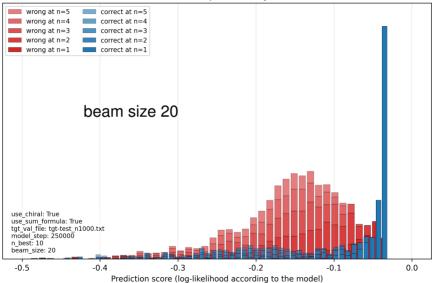
Evaluation

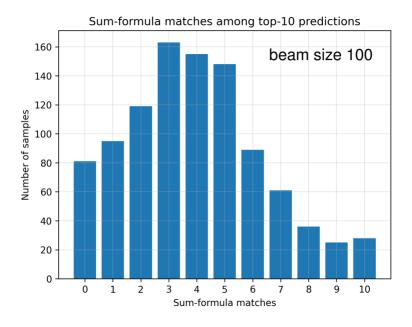
beam size (in hypothesis search): 100 vs 20

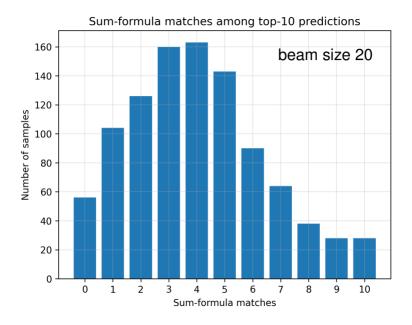
Inferred SMILES (top-5 accuracy: 77.30%)



Inferred SMILES (top-5 accuracy: 80.20%)





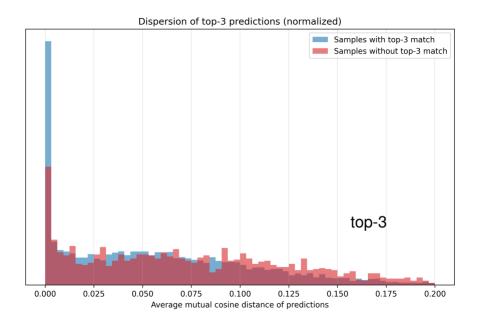


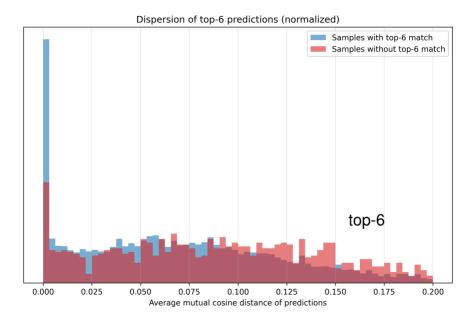
Evaluation

Average mutual cosine distance among top-n predictions, or "dispersion"

... computed using the molecule-to-vector mapping ChemBERTa³ (self-supervised transformer pretrained on SMILES)

³Ahmad et al., 2022 [5]





Bayes:

$$P(\checkmark \mid d \text{ is small}) = \frac{P(d \text{ is small} \mid \checkmark) P(\checkmark)}{P(d \text{ is small} \mid \checkmark) P(\checkmark) + P(d \text{ is small} \mid \checkmark) P(X)}$$

Given

$$\frac{P(d \text{ is small } | \textbf{X})}{P(d \text{ is small } | \textbf{V})} \approx \frac{1}{2}, \quad P(\textbf{V}) \approx 80\%, \quad P(\textbf{X}) \approx 20\%,$$

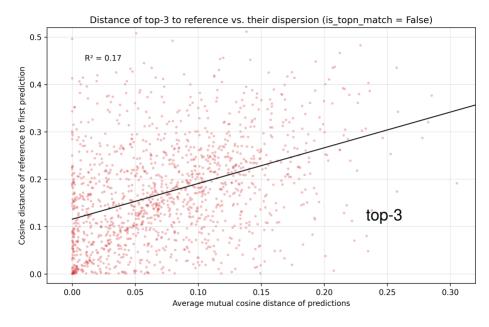
we have

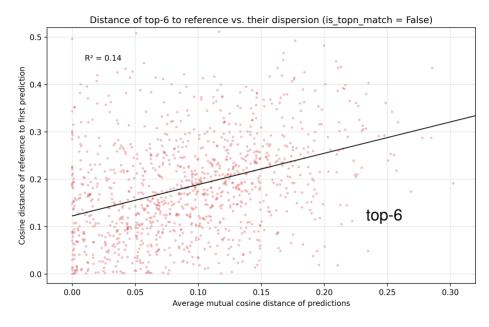
$$P(\checkmark \mid d \text{ is small}) \approx \frac{80\%}{80\% + \frac{1}{2} \times 20\%} \approx 89\%.$$

Very small prediction dispersion indicates a top-n match. Similarly, high dispersion indicates a mismatch.

Evaluation

Distance of the top prediction to the reference vs average distance among top-n predictions





Molecular descriptors

We have a baseline confidence of \sim 80%.

By looking at chemical properties of the molecules, can we improve our confidence of a top-n match?

In other words, construct a method such that: if it says "match", we are confident that the transformer model prediction is indeed correct.

This is called "precision", computed as

$$Precision = \frac{True\ Positives}{True\ Positives + False\ Positives}$$

→ What makes molecules easier/harder to predict?

Chemical descriptors I

- Molecular symmetry number: counts unique canonical atom ranks; a higher value indicates lower overall symmetry. [link]
- Number of chiral centers: counts stereogenic atoms that can lead to non-superimposable mirror images. [link]
- Number of diastereotopic protons: counts hydrogen atoms in non-equivalent chemical environments (via CIP assignments).
- Average Gasteiger charge: computes the mean partial atomic charge using the Gasteiger method, reflecting the electron distribution. [link]
- Fused ring count: counts rings that are fused (sharing at least two atoms) with another ring, affecting rigidity and aromaticity.

Chemical descriptors II

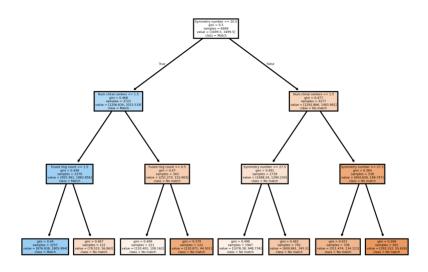
- Bridgehead protons: counts hydrogen atoms attached to heavy atoms shared by multiple rings, influencing steric effects and molecular stability.
- Rotatable bonds: enumerates bonds that are rotatable (typically single bonds outside rings), determining flexibility. [link]
- Internal hydrogen bonds: estimates potential intramolecular hydrogen bonding interactions by pairing donor (N/O with attached H) and acceptor (N/O with degree > 1) atoms.
- Alpha heteroatom protons: counts hydrogen atoms attached to carbons adjacent to heteroatoms (O or N).

cf. [code]

Chemical descriptors – decision tree

We train a "decision tree" on these molecular descriptors to predict whether there is a top-n match. Use the unseen validation dataset.

Caveat: we use the descriptors of the "unknown" reference molecule.

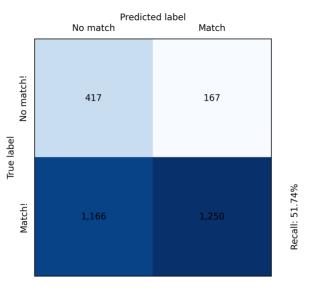


IF:

- Symmetry number ≤ 20 (basically, size)
- Num chiral centers < 1
- Fused ring count ≤ 1

then the decision tree indicates a top-n match.

In this case, we are ${\sim}90\%$ confident that the transformer model got it right.



Precision: 88.21%

In summary

- Slightly better prediction accuracy if:
 - ignore chirality
 - use sum-formula
 - longer training
 - explicit hydrogens
 - beam size 20 instead of 100
 - small prediction dispersion
- Don't understand what makes molecules hard to infer
 - → molecule length, chiral centers, fused rings

Outlook

- Functional groups as descriptors / additional input
- Multimodal input: better data?
- Noisy spectra / multiplets
- Fine-tuning & evaluation on experimental data
- Fine-tuning an off-the-shelf self-supervised model
- "Inductive bias" with graph generation
- Diffusion-like structure generation?
- Cycle consistency: re-simulate spectra from predictions
- Feedback loop (cf. Jonas [6], Devata et al. [7])

References I

- Daniel Lowe. Chemical reactions from US patents (1976–Sep2016). figshare, 2017. 10.6084/m9.figshare.5104873.v1.
- [2] Marvin Alberts, Oliver Schilter, Federico Zipoli, Nina Hartrampf, and Teodoro Laino. "Unraveling Molecular Structure: A Multimodal Spectroscopic Dataset for Chemistry". In: NeurIPS 2024 Datasets and Benchmarks Track. 2024. 10.48550/arXiv.2407.17492.
- [3] Marvin Alberts, Federico Zipoli, and Alain C. Vaucher. Learning the Language of NMR: Structure Elucidation from NMR spectra using Transformer Models. 2023.
 - 10.26434/chemrxiv-2023-8wxcz.

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- [6] Eric Jonas. "Deep Imitation Learning for Molecular Inverse Problems". In: *Advances in Neural Information Processing Systems.* Vol. 32, 2019.

References III

[7] Sriram Devata, Bhuvanesh Sridharan, Sarvesh Mehta, Yashaswi Pathak, Siddhartha Laghuvarapu, Girish Varma, and U. Deva Priyakumar. "DeepSPInN – Deep reinforcement learning for molecular structure prediction from infrared and 13C NMR spectra". In: *Digital Discovery* (2024).

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