

$$V_{\rm cap} = \frac{1}{6} \pi h \left(3 a^2 + h^2 \right).$$

Using the Pythagorean theorem gives

$$(R-h)^2+a^2=R^2,$$

which can be solved for a^2 as

$$a^2 = 2Rh - h^2$$

so the radius of the base circle is

$$a = \sqrt{h(2R - h)},$$

and plugging this in gives the equivalent formula

$$V_{\rm cap} = \frac{1}{3} \pi h^2 (3 R - h).$$

The surface area of the spherical cap is given by the same equation as for a general zone:

$$S_{\text{cap}} = 2 \pi R h$$
$$= \pi (a^2 + h^2).$$

h: altura do corte

VOLUME:

```
a = sqrt(h * (2 * R - h));
V = (1.0/6.0) * PI * h * (3 * a * a - h * h)
V = 1/3 * PI * h * h * (3 * R - h)
```

SURFACE AREA:

S = 2 * PI * R * h

```
S = PI * (a * a - h * h)

1d volSphericalCap(esfera E, ld h) {
   return 1.0/3.0 * PI * h * h * (3 * E.r - h);
}

1d surfaceArea(esfera E, ld h) {
   return 2 * PI * E.r * h;
}
```