

# Dou Shou Qi

## Adversarial Search Methods for a Two-Player Board Game

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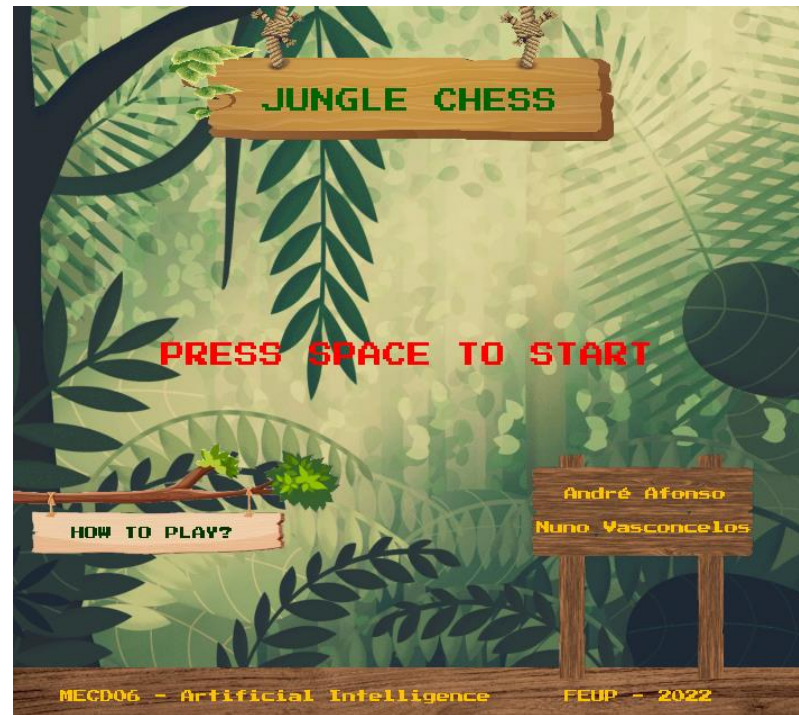
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# **Introduction to the game**

# Game Rules

## 1. The Pawns

Each player has 8 pawns, numbered 1 to 8, according to their strength. All pieces can only move horizontally or vertically. Each piece can capture every weaker or equally strong opponent. The rat is the only exception to this rule, as it can capture the elephant.

## 2. The game board

Three types of special squares are indicated: Lake, Den, Trap. All others are considered normal.

## 3. Den squares

Each player possesses a Den. It is illegal to move your own pawn to your Den. As soon as an enemy Den is occupied by an adversary's pawn, the game ends.

## 4. Lake squares

Each of the two lakes contains 6 squares. The lion and the tiger may jump over the lake. But only the rat can swim through them.

## 5. Trap squares

Surrounding each Den are 3 trap squares. Each animal in a trap is considered to have 0 strength, and therefore it cannot defend itself.

## 6. Objective

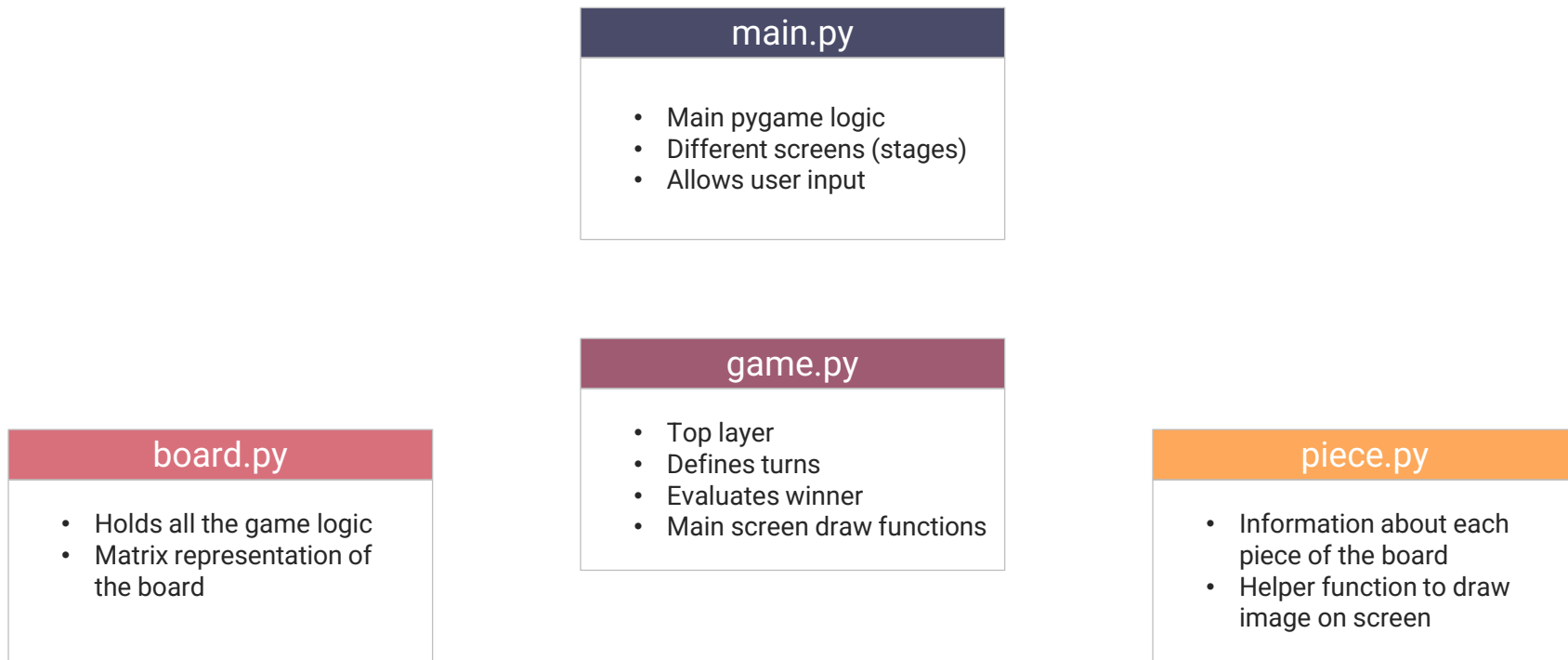
Move a piece into the opponent's Den, or capture all their pawns.

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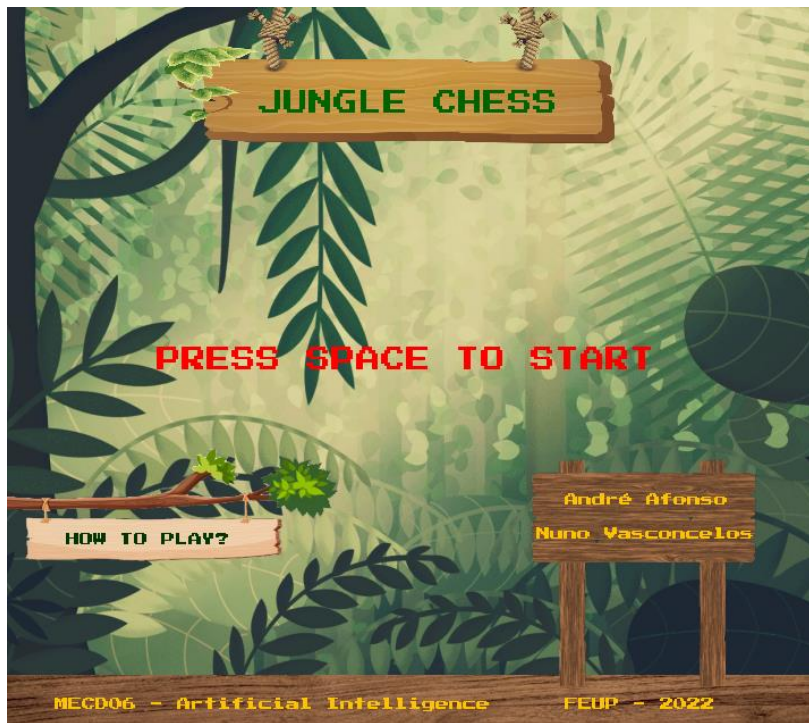
**Development  
environment**

# Development environent

Class diagram for the game



# Demonstration



# Adversarial Search

Evaluation functions developed



# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

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## 1. Simple piece count

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A very simple function where the AI keeps a tally of the **total number of** Red and Black **pieces**

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## 2. Piece strength evaluation

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An improvement of the previous evaluation function where the **pieces'** **relative strength** is taken into account

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## 3. Distance-based evaluation

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Gives the AI an **incentive to advance** in the board regardless of capturing moves in the “near-future” (tree depth)  
– Manhattan distance

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## 4. Strength + Distance eval.

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Combines the previous two functions for decent human-like behaviour where **board advancement and captures** are taken into account

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## 5. Position score matrices

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Developed after dozens of Human-Human and Human-AI sessions and considering the different aspects of the game's strategy: **piece strength**, **development** and **cooperation/relation**

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 1. Simple piece count



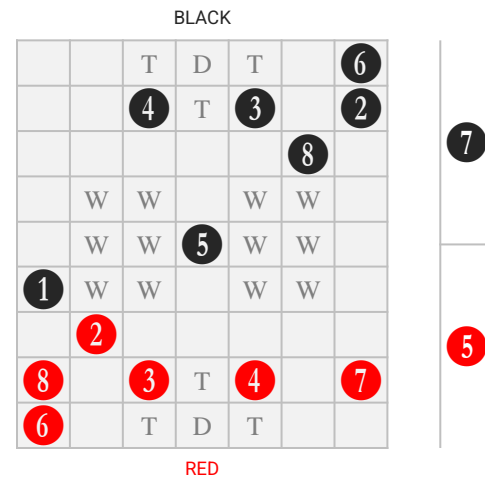
Initial Setup

8 vs 8



Black is missing its Lion (7)

7 vs 8



Black captured Red Puma (5)

7 vs 7

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 2. Piece strength evaluation



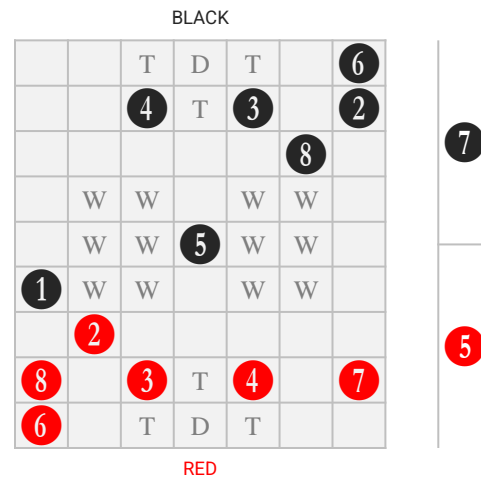
Initial Setup

36 vs 36



Black is missing its Lion (7)

29 vs 36



Black captured Red Puma (5)

29 vs 31

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 2. Piece strength evaluation



Initial Setup



Black is missing its Lion (7)

7



7

5

Black captured Red Puma (5)

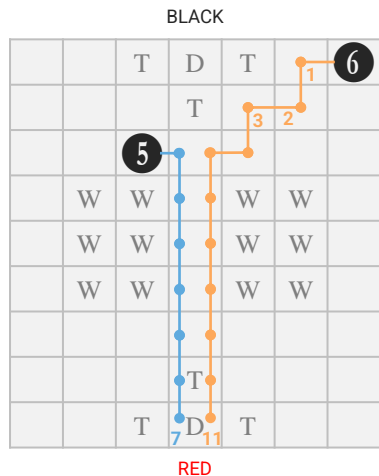


Due to the **rat's special ability**, a value of 5 was considered, making the initial board value for each player 40

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 3. Distance-based evaluation

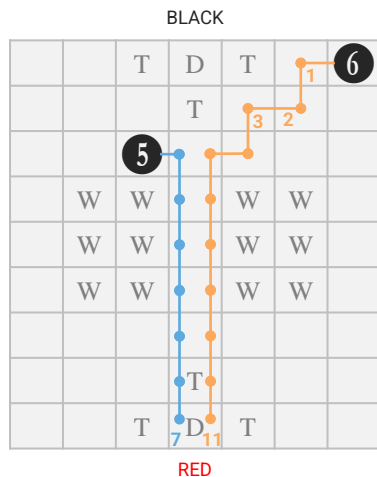


- I At the beginning of the game each player has a combined distance of **72**
- II As the game progresses, both players try to **minimize their distance** to the opponents' den
- III This creates an interesting "**center-rush**" mechanic for both players

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 4. Strength + Distance eval.



Manhattan Distance

- I Combines the previous two functions tackling **board advancement** and **captures**
- II **Simulates** decent **human-like behaviour** and is a good proxy for low-difficulty levels
- III **Prioritizes capturing pieces** near the traps rather than attacking the enemy's den

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

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## 5. Position score matrices

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We considered 4 factors to **strategically evaluate the position** on the board:

### 1. Material relationship

The **number of pieces** left for each player on the board

### 2. Piece value

The **strength relationship** between each player's pieces.

### 3. Development of the pieces

The **incentive to advance** in the board while keeping the den safe

### 4. Cooperation / relationship between the pieces

The best placement of the pieces considering their **tactical role** in the game and their supporting / complementary roles

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK

		T	0	T		
			T			
	0	0		0	0	
	0	0		0	0	
	0	0		0	0	
			T			
		T	inf	T		

RED



Evaluating distance to the opponent's den by **incrementing the marginal utility** of the squares



# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK

10	10	T	0	T	10	10
11	11	11	T	11	11	11
12	12	12	12	12	12	12
13	0	0	13	0	0	13
14	0	0	14	0	0	14
15	0	0	15	0	0	15
16	16	16	16	16	16	16
17	17	17	T	17	17	17
18	18	T	Inf	T	18	18

RED



Evaluating distance to the opponent's den by  
**incrementing the marginal utility** of the squares

- Increase the square value **vertically**

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK

10	10	T	0	T	10	10
11	11	11	T	11	11	11
12	12	12	12	12	12	12
13	0	0	13	0	0	13
14	0	0	14	0	0	14
15	0	0	15	0	0	15
16	16	16	16	16	16	16
17	17	17	T	17	17	17
18	18	T	Inf	T	18	18

RED



Evaluating distance to the opponent's den by  
**incrementing the marginal utility** of the squares

- Increase the square value **vertically**

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK

10	11	T	0	T	11	10
11	12	13	T	13	12	11
12	13	14	15	14	13	12
13	0	0	16	0	0	13
14	0	0	17	0	0	14
15	0	0	18	0	0	15
16	17	18	19	18	17	16
17	18	19	T	19	18	17
18	19	T	inf	T	19	18

RED



Evaluating distance to the opponent's den by  
**incrementing the marginal utility** of the squares

- Increase the square value **vertically**
- Increase the square value **inwards**

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK

10	11	4	0	4	11	10
11	12	13	5	13	12	11
12	13	14	15	14	13	12
13	0	0	16	0	0	13
14	0	0	17	0	0	14
15	0	0	18	0	0	15
16	17	18	19	18	17	16
17	18	19	50	19	18	17
18	19	50	inf	50	19	18

RED



Evaluating distance to the opponent's den by  
**incrementing the marginal utility** of the squares

- Increase the square value **vertically**
- Increase the square value **inwards**
- **Penalize** own den; **incentivize attacking** opponent den

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK						
10	11	4	0	4	11	10
11	12	13	5	13	12	11
1	13	14	15	14	13	12
13	0	0	16	0	0	13
14	0	0	17	0	0	14
15	0	0	18	0	0	15
16	17	18	19	18	17	16
17	18	19	50	19	18	17
18	19	50	inf	50	19	18

RED

- I Evaluating distance to the opponent's den by **incrementing the marginal utility** of the squares
- II Accounting for the **non-centered starting position** of each piece

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK						
7	11	4	0	4	11	6
11	4	13	5	13	2	11
1	13	5	15	3	13	8
13	0	0	16	0	0	13
14	0	0	17	0	0	14
15	0	0	18	0	0	15
8	17	3	19	5	17	1
17	2	19	50	19	4	17
6	19	50	inf	50	19	7

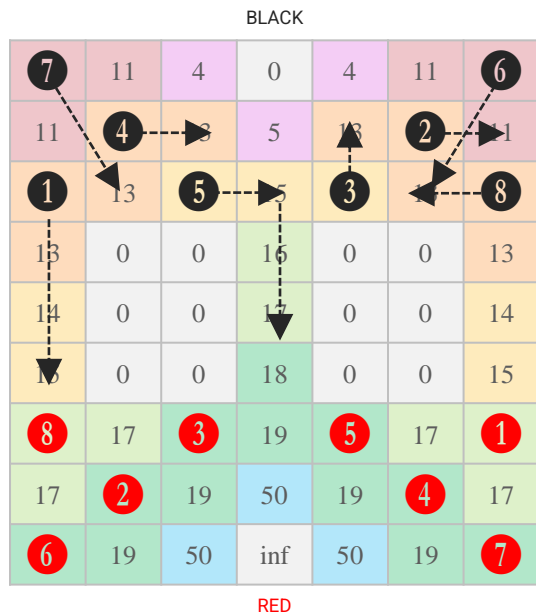
RED

- I Evaluating distance to the opponent's den by **incrementing the marginal utility** of the squares
- II Accounting for the **non-centered starting position** of each piece
- III Considering each piece's **tactical role** in the game and their **supporting / complementary roles**

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices



- I Evaluating distance to the opponent's den by **incrementing the marginal utility** of the squares
- II Accounting for the **non-centered starting position** of each piece
- III Considering each piece's **tactical role** in the game and their **supporting / complementary roles**

- **Rat**: attack the elephant, safe on water
- **Dog and Wolf**: weak pieces, guard the player's traps
- **Tiger and Lion**: attacking pieces
- **Cat**: weak piece, defend the elephant from mouse
- **Puma**: center-lane control and rush
- **Elephant**: development blocked by mouse, defend against lion attack

# Evaluation functions developed

An iterative process was applied in the development of ever-improving evaluation functions for the game's AI

## 5. Position score matrices

BLACK						
8	8	4	0	4	8	8
9	9	9	5	8	8	8
1	10	10	9	8	8	8
11	12	12	10	9	9	8
12	12	12	11	9	9	8
13	12	12	11	9	9	8
13	13	13	13	11	11	10
13	13	13	50	13	12	11
13	13	50	inf	50	13	11
RED						

MOUSE DEVELOPMENT SCORES

BLACK						
7	12	4	0	4	12	10
12	14	12	5	12	12	12
14	16	16	14	16	16	14
15	W	W	15	W	W	15
15	W	W	15	W	W	15
15	W	W	15	W	W	15
18	20	20	30	20	20	18
25	25	30	50	30	25	25
25	30	50	inf	50	30	25
RED						

LION DEVELOPMENT SCORES

Piece		Value
Mouse	1	500
Cat	2	200
Dog	3	300
Wolf	4	400
Puma	5	500
Tiger	6	800
Lion	7	900
Elephant	8	1000



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# Adversarial Search

Search algorithms used and  
performance evaluation

# Search algorithms used

Several algorithms were implemented in order to test their relative efficiency and computational performance

## Standard function

Runs the selected algorithm up to a **predefined search depth**

## Iterative Deepening function

Runs repeatedly with **increasing depth limits** until the goal is found or a **predefined time limit** is reached

Allows the search for “shallower” victories

1

Standard **Minimax**

2

**Alpha-Beta** pruning

3

**Alpha-Beta** pruning w/ **move-ordering**

# Alpha-Beta pruning with move-ordering

Search algorithms used

**GOAL:** evaluate moves which can result in **faster pruning as early as possible**



## Check for captures

Determine if there are immediate capturing moves for the current board position



## Check for lion – tiger – elephant - mouse

Search for moves made by more valuable / stronger pieces currently on the board



## Check for the remaining pieces

Only then resume the search for every other piece on the board

# Performance evaluation

Analysing efficiency and computational performance for each algorithm

## Analysing the impact of pruning and move-ordering

Depth 3: **Position scores**

	Minimax		Alphabeta		Move-ordering	
	Without capture	With capture	Without capture	With capture	Without capture	With capture
avg Processing time <i>per play (milliseconds)</i>	1.524	1.569	1.046	515	632	458
max Processing time <i>per play (milliseconds)</i>	3.282	2.940	2.013	733	1.668	632
			- 31,4%	- 67,2%	- 58,5%	- 70,8%
avg Searched boards	5.929	6.221	1.311	816	909	516
max Searched boards	12.240	11.461	3.239	1.024	1.802	651
			- 77,9%	- 86,9%	- 84,7%	- 91,7%

# Performance evaluation

## Analysing the impact of pruning and move-ordering

Iterative deepening, 1 sec timeout: **Position scores**

	Minimax		Alphabeta		Move-ordering	
	Without capture	With capture	Without capture	With capture	Without capture	With capture
avg Processing time <i>per play (milliseconds)</i>	2.796	2.084	4.367	3.340	3.032	4.623
max Processing time <i>per play (milliseconds)</i>	13.871	3.486	11.776	5.772	12.441	11.871
avg Searched boards	11.173	8.395	4.644	3.090	1.677	1.562
max Searched boards	50.530	14.886	24.569	7.218	10.824	3.122
			- 58,4%	- 63,2%	- 85,0%	- 81,4%
avg Depth	3,21	3,13	3,76	3,92	3,33	3,87
max Depth	4	4	4	4	5	4
			+ 17,1%	+ 25,2%	+ 3,7%	+ 23,6%

# Determining AI difficulty levels

Framework to define the available AI difficulty levels

Reasoning behind the **parameter selection** for the **three** available **difficulty levels** (easy, medium, hard):

- **Avoid “blind guesses”** regarding the choices of depth level and evaluation function
- Determine the previous parameters based **on real Human versus AI plays** and outcomes
- Set the parameters according to the **win percentile of the Humans**
- Approx. **200 games** played with varying parameters

## Easy

Around the **75<sup>th</sup>** percentile

Evaluation function: **Strength + Distance**

Search depth: **3** (or 1 second timeout)

Human win percentage: **79%**

## Medium

Around the **50<sup>th</sup>** percentile

Evaluation function: **Position score matrices**

Search depth: **3** (or 1 second timeout)

Human win percentage: **56%**

## Hard

Around the **25<sup>th</sup>** percentile

Evaluation function: **Position score matrices**

Search depth: **7** (or 15 seconds timeout)

Human win percentage: **22%**

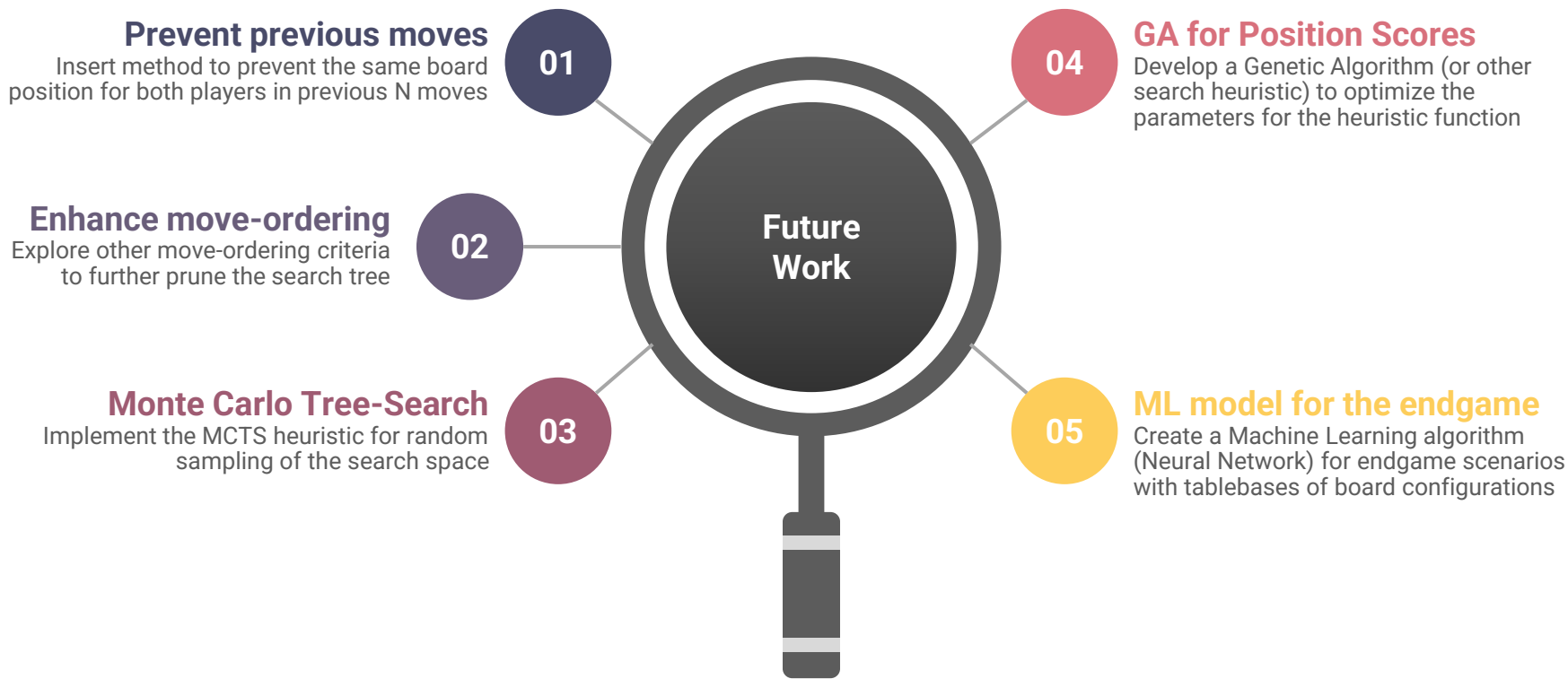
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# Future work

Topics and study subjects  
for further exploration

# Future Work

Topics and study subjects for further exploration







**QUESTIONS**

