

### Definition: Peano Axioms

- Zero is a Natural Number,  $0 \in \mathbb{N}$
- Every successor of a Natural Number is a Natural Number,  $n \in \mathbb{N} \rightarrow n + 1 \in \mathbb{N}$
- Zero is not the successor of any Natural Number,  $n + 1 = 0 \rightarrow n \notin \mathbb{N}$
- Every successor is unique,  $n + 1 = m + 1 \rightarrow n = m$
- Principle of Mathematical Induction,  $\forall n \in \mathbb{N}: P(n) \leftrightarrow P(0) \wedge \forall k \in \mathbb{N}: P(k) \rightarrow P(k + 1)$