Control of a Robotic Leg for Walking, Running and Hopping in Irregular Surfaces

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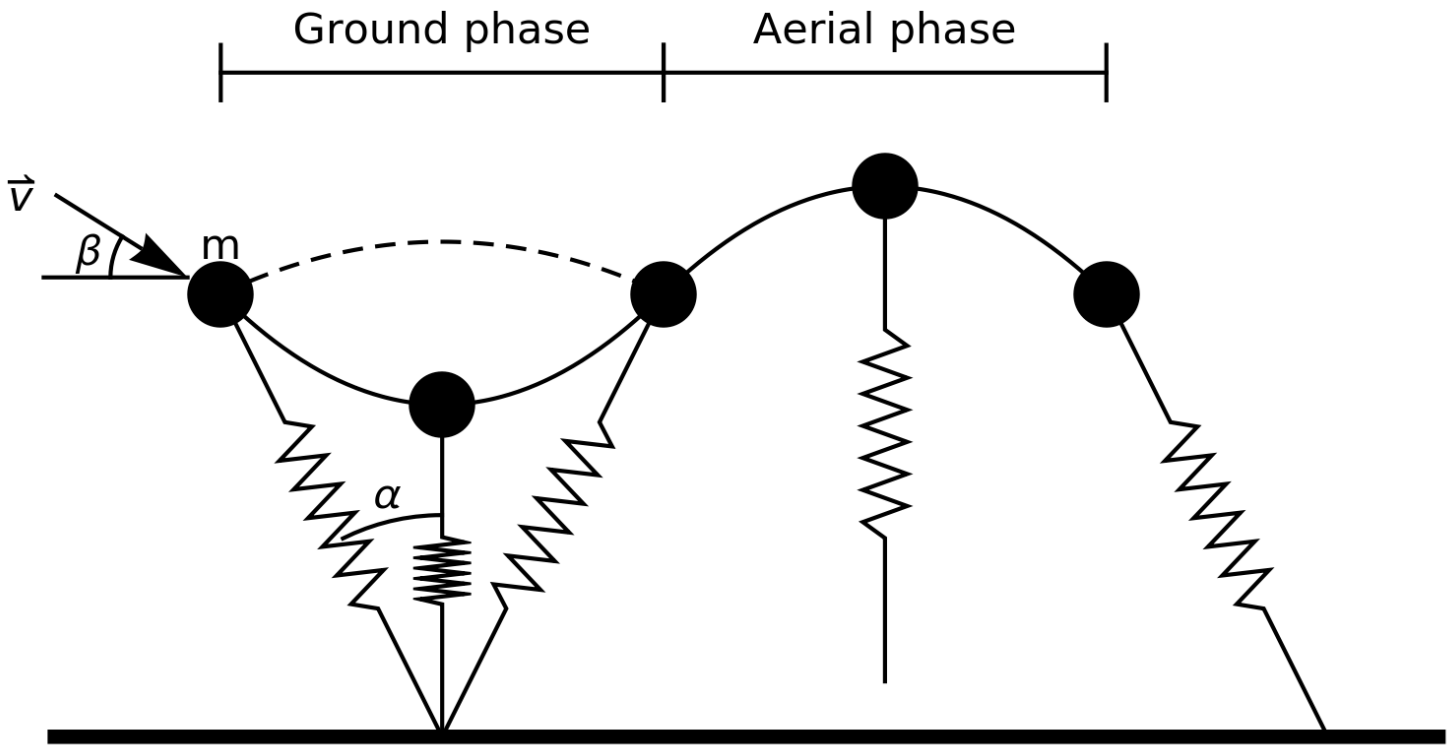
Running and hopping model



Equations

Ground phase

$$\ddot{x} = x\omega^2 \left(\frac{l}{\sqrt{x^2 + y^2}} - 1 \right), \tag{1}$$

$$\ddot{y} = y\omega^2 \left(\frac{l}{\sqrt{x^2 + y^2}} - 1 \right) - g, \tag{2}$$

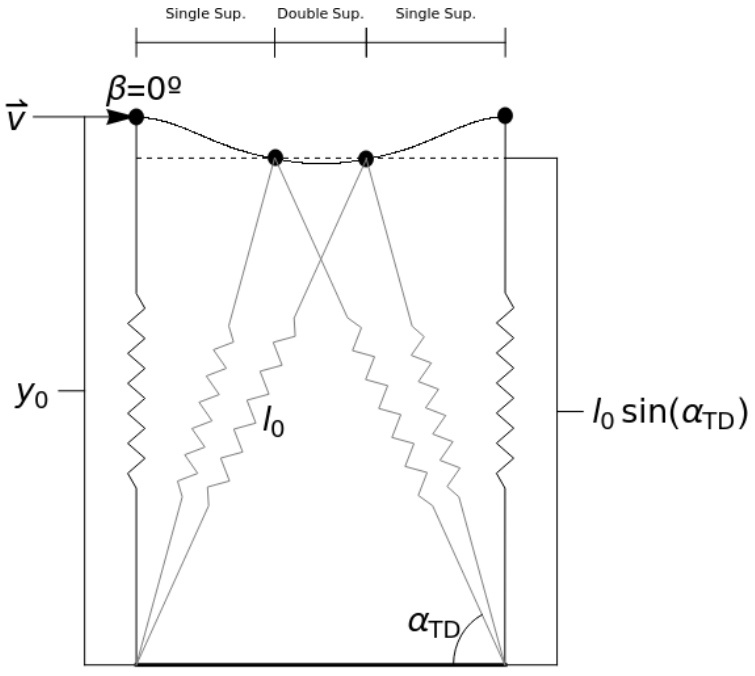
Aerial phase

$$\ddot{x} = 0, \tag{3}$$

$$\ddot{y} = -g. \tag{4}$$

with $\omega = \sqrt{k/m}$, the natural frequency of the spring

Walking model



Definitions:

- stride - Leg crosses the vertical leg orientation
- step -The moment when the system passes from single support to double support.

Equations

Single support

$$\ddot{x} = \frac{F_1}{m}\frac{x - x_{t1}}{l_1} \tag{5}$$

$$\ddot{y} = \frac{F_1}{m}\frac{y - y_{t1}}{l_1} - g \tag{6}$$

Double support

$$\ddot{x} = \frac{F_1}{m}\frac{x - x_{t1}}{l_1} + \frac{F_2}{m}\frac{x - x_{t2}}{l_2} \tag{7}$$

$$\ddot{y} = \frac{F_1}{m}\frac{y - y_{t1}}{l_1} + \frac{F_2}{m}\frac{y - y_{t2}}{l_2} - g \tag{8}$$

with F_i being the force applied on the mass by the respective leg,

$$F_i = k(l_0 - l_i) \geq 0 \quad i = 1, 2\,, \tag{9}$$

l_0 is the natural length of the spring, l_i is the respective length,

$$l_i = \sqrt{(x - x_{ti})^2 + (y - y_{ti})^2} \quad i = 1, 2\,. \tag{10}$$

Since the system is energetically conservative we can change the initial velocity by inverting

$$E = \frac{k(l_0 - y_0)^2}{2} + mgy_0 + m\frac{v_0^2}{2}. \tag{11}$$

Parameters

A scan is made with 3 parameters, *Energy*, y_0, α in two strides

- $Energy \in [800, 840]$ with 40 subdivisions.
- $\alpha \in [\pi/2 - \pi/5, \pi/2]$ with 30 subdivisions.
- $y_0 \in [l_0 \sin(\alpha), l_0]$ with 25 subdivisions

In all simulations the following parameters remained fixed.

- $\beta = 0$
- $m = 80Kg$
- $l_0 = 1m$
- $k = 14000$

Total number of configurations$= 40 \times 30 \times 25 = 30000$

Survival step configurations

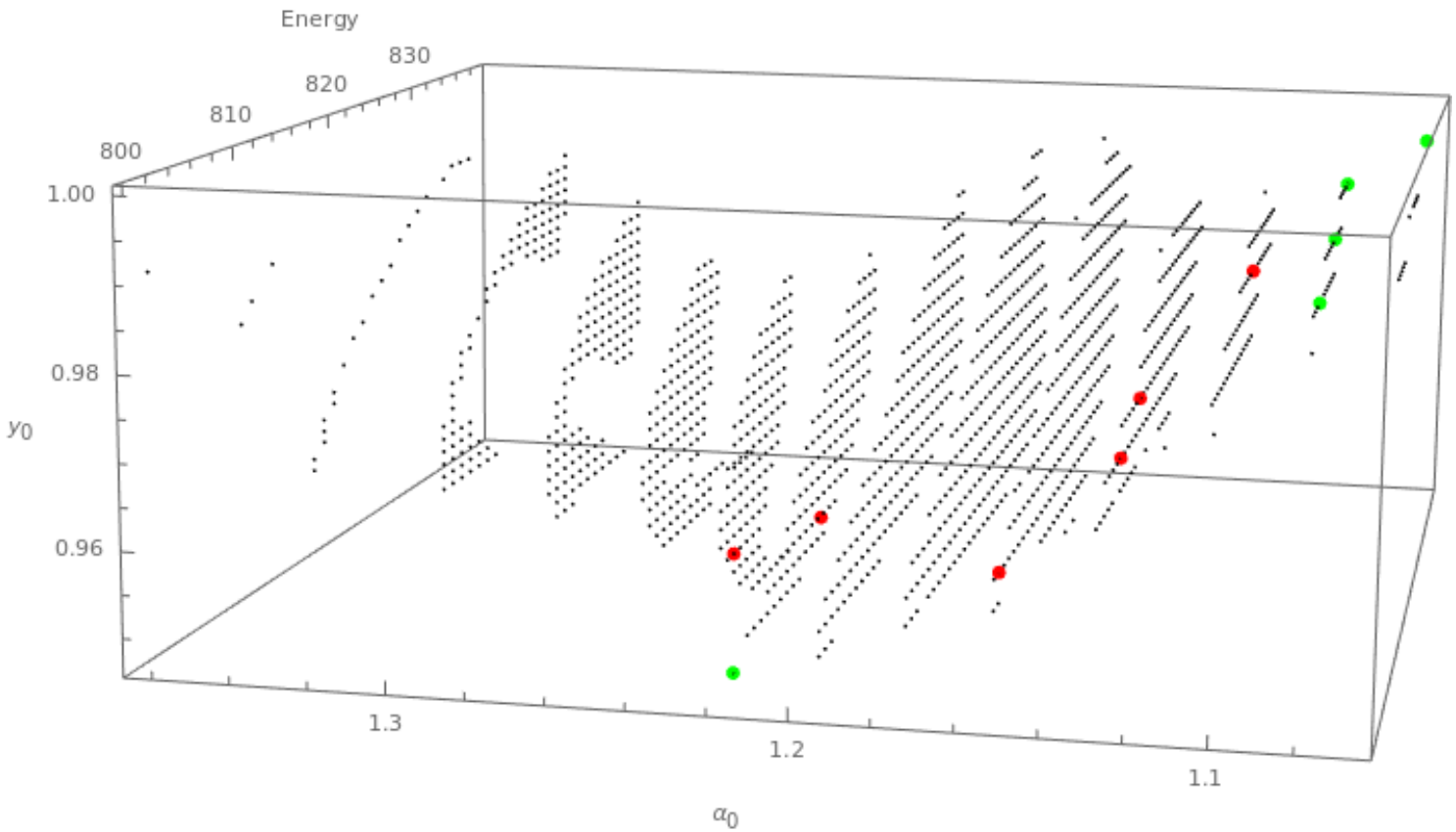
Out of the 30000 configurations in the parameter space, only 8195 were able to complete 2 strides. Of this subset of points, 11 fixed points were found, 5 stable and 6 unstable.

From here a survival test is applied to each of the 8195 configurations that completed 2 strides by incrementing steps instead of strides.

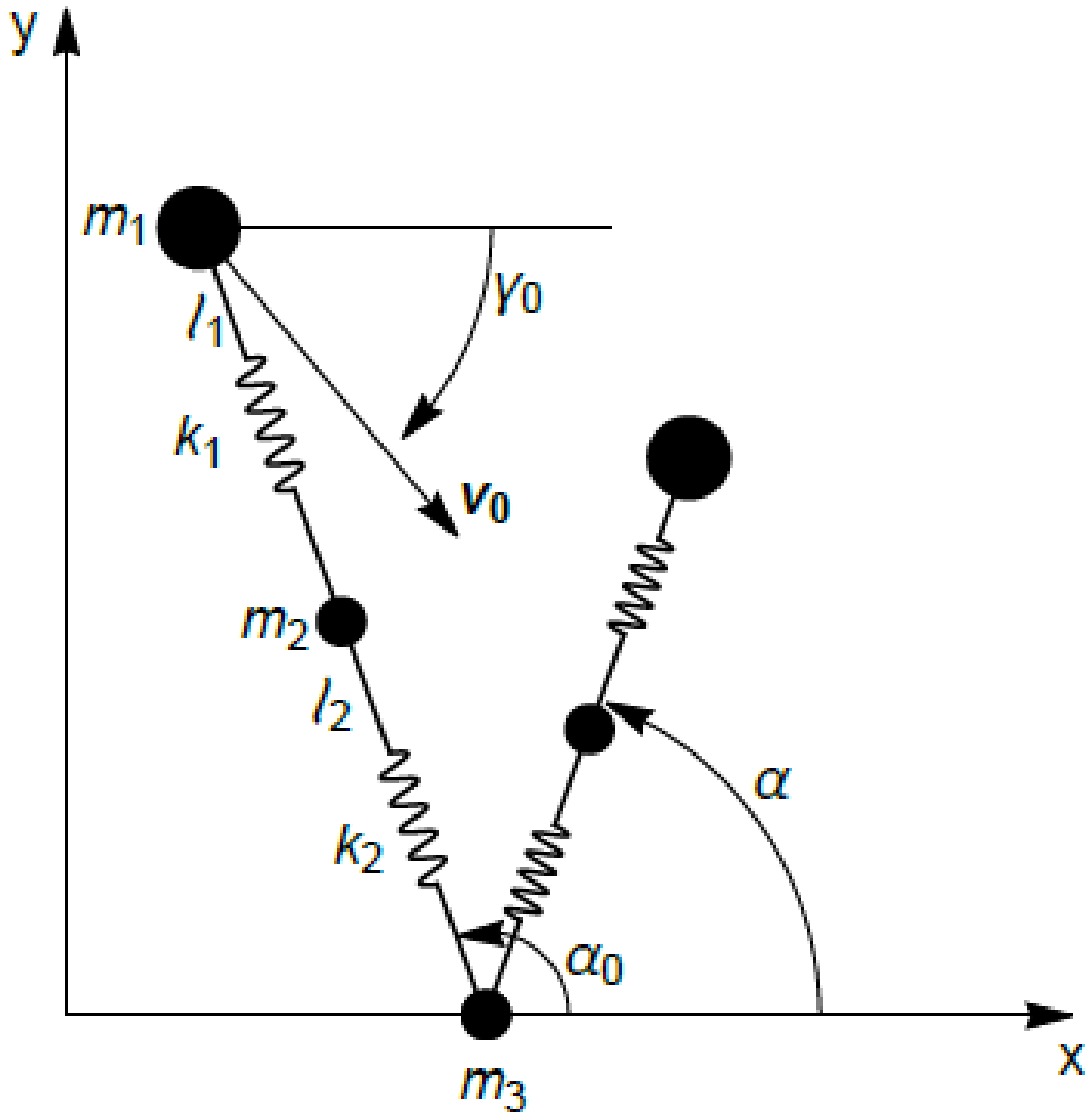
If the simulation fails, the maximum number of steps was assigned to that configuration.

Fixed points and 10 step configurations

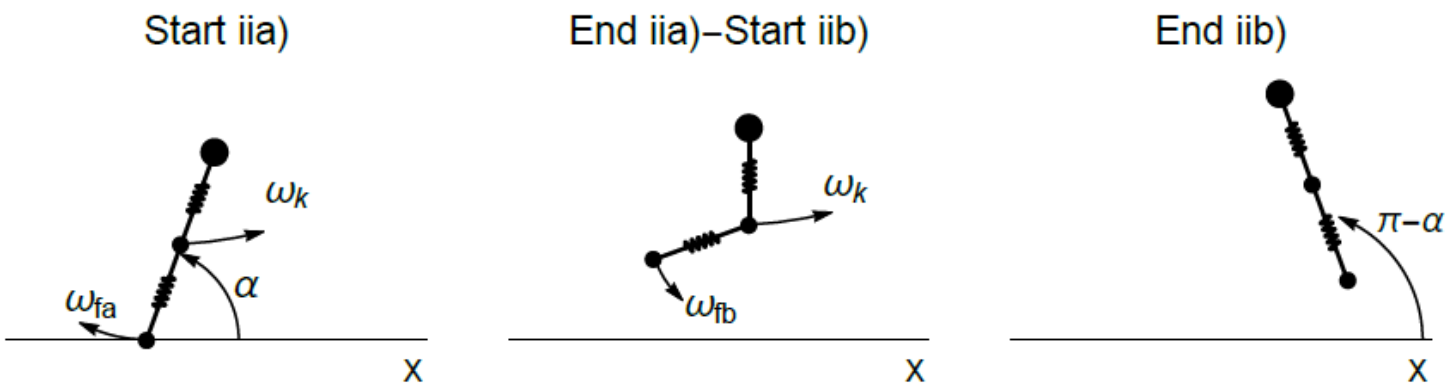
Iterating the number of steps where $\Delta t = 0.00075$ so that in maximum it was possible to achieve 10 steps, the configurations that achieve 10 steps can be ilustrated in the figure below along with the fixed points.



Running and hopping model - One knee



Running and hopping model - One knee



Running and hopping model - One knee