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NAME:

Computer Lab #3

Due Thursday November 3rd 2022 by 11:59 P.M.

All work is to be done in a mathematica or jupyter notebook.

Please refer to the blackboard site for commands and examples.

Submissions must be made electronically on Blackboard.

You will be graded on the output that I am able to generate from your commands.

Please delete all output before submitting.

Α	В	С	D	Е	F	G	Н	I	J	K	L	М	N	0	Р	Q	R	S	Т	U	V	W	Х	Υ	Z
1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26

1. Let a be the digit corresponding to your first initial in the table above. Consider the function

$$f(x) = \sqrt{\frac{x^4 - x + a}{x^4 + x + a}}$$

- (a) Graph the function on an appropriate interval.
- (b) Compute the derivative of the function.
- (c) Simplify the derivative and say in words what changed from part 1b.
- (d) Find the points on the graph where the function f has a horizontal tangent.
- (e) Graph f and f' on the same axis. Explain in words why or why not your graphs are consistent with the answer found in part 1d
- 2. Consider the curve (Tschirnhausen Cubic), where a is as defined above,

$$y^2 = x^3 + ax^2.$$

- (a) Graph the equation. I would suggest ContourPlot for Mathematica, plot_implicit for sympy python, or breaking into two pieces. Describe in words what you see.
- (b) Where does the graph have horizontal tangents?
- (c) Where does the graph have vertical tangents?
- (d) Explain in words how the picture supports your mathematics.
- 3. Consider the function,

$$g(x) = e^{-x^2/\left(2\sigma^2\right)}.$$

- (a) Start by setting $\sigma=a$. Find the asymptote, maximum value and inflection points. Plot the function and the points identified.
- (b) Change $\sigma = 2a$. Describe in words the changes you observe to all values found in 3a.
- (c) Graph at least four different values of σ to verify your predictions in 3b.