

Homework 6 Advanced Analytics and Metaheuristics

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1. Strategies for the problem

- (a) Two differing initialization solutions for the knapsack could be random or all zeros.

Empty We could also just ask that initially your knapsack is empty. We simply make the initial all zeros. We know this will be in the feasible set initially!

```
for i in range(n):  
    x.append(0)
```

Random Random has the benefit of being just that but it also has the serious issue of not being in the feasible set (nor any where close to the feasible set). This could be dealt with by re-seeding the random until it was inside the feasible regime.

```
for i in range(n):  
    x.append(myPRNG.randint(0,1)) #initial seeding
```

```
i = myPRNG.randint(0,n-1) #random index to make zero if needed  
while evaluate(x)[1] > maxWeight: #winnowing down randomly  
    x[i] = 0  
    i=myPRNG.randint(0,n-1)
```

- (b) Neighborhood

1 Flip We really like the 1-flip neighborhood that was provided in the sample code. We bring it up here to mention that using the 1-flip, zero initial vector and best improvement local search, we are doing a greedy search. We will take the highest value item each time until we fill the knapsack. When the knapsack is full, we will take the next highest object that can still fit.

Sliding window Take the x_{curr} and slide all the 1's and 0's to the left. Each time you move one unit, add to the neighborhood. This will add $n - 1$ items to the neighborhood. Unfortunately it will not add or subtract any items to our knapsack. It will not work with all initially 0 and will not work if we just have too many items to start.

```
for i in range(0, len(x)-1):
    newlist = x[i+1:]
    newlist.extend(x[:i+1])
    nbrhood.append(newlist)
```

Slide and Flip We combine the slide and flip method. This will create $n(n - 1)$, neighbors. Here is the code sample

```
for i in neighborhood(x):
    nbrhood.extend(neighborhood_slide(i))
```

Permutation We attempted to do permutation but could not execute without new package and some runtime errors. Size would have depended on number of 1's, n_1 , and would be $\binom{n}{n_1}$.

(c) Infeasible

Small Value If the weight is outside of allowed, simply make the value small (negative). While this works, the infeasible will match and end the while loop in the infeasible region.

```
if totalWeight > maxWeight:
    totalValue = -1000
```

This did not work well. Tried random value, that didn't work either. Maybe something with making the Value the opposite of its value so it will continue to decrease when you are out of the feasible region.

Negative of Total Value We went ahead and attempted the above comments. The random value did not work well. It was just that, too random. What does seem to work okay for us is

```
if totalWeight > maxWeight:
    totalValue = -totalValue
```

This has the benefit of increasing as you get rid of some of the items when you are outside of the feasible set. We will use this one.

2. Local Search with Best Improvement: We apply this method using the all zero's as the initial, the Negative of Total Value to deal with in-feasibility, and the Slide and Flip neighbors.

Algorithm	Iterations	# Items Selected	Weight	Objective
Local Search (Best Improvement)	581100	25	2331.3	16654.5

3. Local Search with First Improvement: We repeat the methods from above (zeros, negative, and slide/flip). We report results below in table. Only change in logic was introduction of the 'break' command to the for loop. This allowed the exit of the for loop when the first improvement of the model was found.

```

if evaluate(s)[0] > f_best[0]:
    x_best = s[:]           #find the best member and keep track o
    f_best = evaluate(s)[:]  #and store its evaluation
    break

```

Algorithm	Iterations	# Items Selected	Weight	Objective
Local Search (Best Improvement)	581100	25	2331.3	16654.5
Local Search (First Improvement)	37268	29	2497.9	15583.1

4. Random Restarts Best Improvements: To implement this we had to use one of our random initializers. We used the truly random one, knowing that the first objective would be to get into the feasible regime. This did not perform very quickly. We attempted again with the initializer that guaranteed a solution in feasible region to start. We made sure to use first improvement to juice the runtime a bit. We kept the neighbors to be the flip and slide.

Algorithm	Iterations	# Items Selected	Weight	Objective
Local Search (Best Improvement)	581100	25	2331.3	16654.5
Local Search (First Improvement)	37268	29	2497.9	15583.1
RR (Truly Random, FI, $k = 20$)	157279	34	2485.4	16366.8
RR (Random but Feasible, FI, $k = 20$)	26964	33	2496.1	17304.9
RR (Random but Feasible, FI, $k = 50$)	95386	33	2476	17442.7

```

k = 50
solns = [] #array for storing solutions values

for i in range(k):

```

```

x_curr = initial_solution_random_start_feasible() #x_curr will hold the current solution
x_best = x_curr[:] #x_best will hold the best solution
f_curr = evaluate(x_curr) #f_curr will hold the evaluation of the current solution
f_best = f_curr[:]
...
solns.append(solutionsChecked) #add pieces to solutions
solns.append(f_best[0])
solns.append(f_best[1])
solns.append(np.sum(x_best))
solns.append(x_best)

```

Then the coolest part of code found the best solution from this array:

```

weightsMax = []

for i in range(0,k*5,5): #five things added to the solution array each execution
    weightsMax.append(solns[i+1]) #objective is in 1 slot

iter = weightsMax.index(max(weightsMax)) #find iteration with best value

print ("\nFinal number of solutions checked: ", solns[5*iter]) #print results
print ("Best value found: ", solns[5*iter+1])
print ("Weight is: ", solns[5*iter+2])
print ("Total number of items selected: ", solns[5*iter+3])
print ("Best solution: ", solns[5*iter+4])

```

5. Local Search with Random Walk: To implement this, we needed a p to compare to and a p_{test} that is randomly generated in each iteration of the while loop. We use the all zero initial solution and the slide and flip neighborhood. The code that give us this result is a simple modification after the Neighborhood has been generated,

```

if p>p_test: #do the normal thing
    for s in Neighborhood: #evaluate every member in the neighborhood
        solutionsChecked = solutionsChecked + 1
        if evaluate(s)[0] > f_best[0]:
            x_best = s[:] #find the best member and keep track of it
            f_best = evaluate(s)[0] #and store its evaluation
        else: #set the best to a random member

```

```

randNbr = myPRNG.randint(0,len(Neighborhood)-1) #random integer smaller th
x_best = Neighborhood[randNbr][:]#make it the best
f_best = evaluate(x_best)[:] #do evaluations too

```

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RR (Random but Feasible, FI, $k = 50$)	95386	33	2476	17442.7
Random Walk ($p = 0.90$)	630000	31	2497	22337.1
Random Walk ($p = 0.75$)	540000	29	2498.6	20423.3
Random Walk ($p = 0.5$)	405000	34	2490.0	16676.8

We saw the best results yet for $p = 90\%$. We did test some other values in this area about 90% but none came out better than our reported result.

6. Stochastic Hill Climb: I start with empty and use the flip and slide. This is neither best nor first improvement as we record all improvements and then make a random choice in which we choose (This may have been a copy/pasta error in the assignment document). First I create a list of all the improvements that occur in the neighborhood (I compare to the current not the best!). Then we attempt two executions of random. In the first we do a totally random draw based solely on index. This returned marginal results. Next we took the same idea of recording the improvements in a list but utilized the weight functionality in random.choices. This gave use away to still be random and improving and weight our decision on how much we were improving. The results here were also marginal.

```

        if evaluate(s)[0] > f_curr[0]:#compare to current not best
            improvements.append(s[:])          #add to list
            improvements.append(evaluate(s)[:]) #and store its evaluation

if len(improvements)>0:
    w = []
    for i in range(int(len(improvements)/2)):
        w.append(improvements[2*i +1][0])

```

```

whichone = myPRNG.choices(range(int(len(improvements)/2)), weights = w, k
x_best = improvements[2*whichone]
f_best = improvements[2*whichone +1]

```

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Stochastic (random by index)	945000	33	2498.7	15959.7
Stochastic (random value as weight)	742500	32	2492.7	16712.2

In all, we saw marginal returns on our model complexity, with random walk being the best method. We partly attribute this to our insistence on using the all zero vector as the initial in many of our attempts (we did not use it in the random restart algorithm). We wonder how much different neighborhood generators and infeasible requirements might change these results.