

Computational Companion to “Flexible 3×3 Nets of Equimodular Elliptic Type” — Example 2

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Tested on: Mathematica 14.0

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In[*]:= (*=====*)
(*=====*)
(*=====*)
(*Quit*)
(*All angle sets in degrees*)
anglesRad = {
  {ArcCos[1 / Sqrt[5]], ArcCos[7 / (5 Sqrt[2])],
   ArcCos[-1 / Sqrt[10]], ArcCos[0]}, (*Vertex 1*)
  {ArcCos[1 / (4 Sqrt[11])], ArcCos[7 Sqrt[7] / (4 Sqrt[22])],
   ArcCos[-1 / (2 Sqrt[2])], ArcCos[0]}, (*Vertex 2*)
  {ArcCos[1 / (4 Sqrt[11])], ArcCos[7 Sqrt[7] / (4 Sqrt[22])],
   ArcCos[1 / (2 Sqrt[2])], ArcCos[0]}, (*Vertex 3*)
  {ArcCos[1 / Sqrt[5]], ArcCos[7 / (5 Sqrt[2])],
   ArcCos[1 / Sqrt[10]], ArcCos[0]} (*Vertex 4*)};

anglesDeg = anglesRad * 180 / Pi;

(*-----*)
(*Function to compute sigma from 4 angles*)
computeSigma[{α_, β_, γ_, δ_}] := (α + β + γ + δ) / 2;

(*-----*)
(*Function to compute a,b,c,d from angles*)
computeABCD[{α_, β_, γ_, δ_}] :=
Module[{alpha = α Degree, beta = β Degree, gamma = γ Degree,
  delta = δ Degree, sigma}, sigma = computeSigma[{α, β, γ, δ} Degree];
{Sin[alpha] / Sin[sigma - alpha], Sin[beta] / Sin[sigma - beta],
 Sin[gamma] / Sin[sigma - gamma], Sin[delta] / Sin[sigma - delta]}];
```

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(*-----*)
(*Compute all  $\sigma$  values*)
sigmas = computeSigma /@ anglesDeg;

(*Compute all {a,b,c,d} values*)
results = computeABCD /@ anglesDeg;

(*Optional:extract individual values*)
{a1, b1, c1, d1} = results[[1]];
{a2, b2, c2, d2} = results[[2]];
{a3, b3, c3, d3} = results[[3]];
{a4, b4, c4, d4} = results[[4]];
{ $\sigma_1$ ,  $\sigma_2$ ,  $\sigma_3$ ,  $\sigma_4$ } = FullSimplify[sigmas];

(*=====
====*)
(*=====
      CONDITION (N.0)=====*)
(*=====
====*)
uniqueCombos = {{1, 1, 1, 1}, {1, 1, 1, -1}, {1, 1, -1, -1}, {1, 1, -1, 1},
  {1, -1, 1, 1}, {1, -1, -1, 1}, {1, -1, 1, -1}, {1, -1, -1, -1}};

checkConditionN0Degrees[{ $\alpha$ _,  $\beta$ _,  $\gamma$ _,  $\delta$ _}] :=
Module[{angles = { $\alpha$ ,  $\beta$ ,  $\gamma$ ,  $\delta$ }, results},
  results = Mod[uniqueCombos.angles, 360] // Chop;
  ! MemberQ[results, 0]];

conditionsN0 = checkConditionN0Degrees /@ anglesDeg;
allVerticesPass = And @@ conditionsN0;

Column[{TextCell[Style["===== CONDITION (N.0) =====",
  Darker[Green], Bold, 16], "Text"],
  If[allVerticesPass,
    Style["✓ All vertices satisfy (N.0).", Darker[Green], Bold],
    Style["✗ Some vertices fail (N.0).", Red, Bold]]}]

(*=====
====*)
(*=====
      CONDITION (N.3)=====*)
(*=====
====*)
Ms = FullSimplify[Times@@@ results];

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allEqualQ = Simplify[Equal @@ Ms];

Column[{TextCell[Style["===== CONDITION (N.3) =====",
  Darker[Blue], Bold, 16], "Text"], If[allEqualQ,
  Row[{Style["✓ M1 = M2 = M3 = M4 = ", Bold], Ms[[1]]},
  Style["✗ M_i are not all equal.", Red, Bold]]]}]

(*=====
====*)
(*=====CONDITION (N.4)=====*)
(*=====
====*)
aList = results[[All, 1]];
cList = results[[All, 3]];
dList = results[[All, 4]];

rList = FullSimplify /@ (aList * dList); {r1, r2, r3, r4} = rList;
sList = FullSimplify /@ (cList * dList); {s1, s2, s3, s4} = sList;

Column[{TextCell[Style["===== CONDITION (N.4) =====",
  Darker[Purple], Bold, 16], "Text"],
  If[r1 == r2 && r3 == r4 && s1 == s4 && s2 == s3, Column[
    {Row[{Style["✓ r1 = r2 = ", Bold], r1, Style["; ✓ r3 = r4 = ", Bold], r3}],
    Row[{Style["✓ s1 = s4 = ", Bold], s1, Style["; ✓ s2 = s3 = ", Bold],
    s2}]}], Style["✗ Condition (N.4) fails.", Red, Bold]}]
}]

(*=====
====*)
(*=====
CONDITION (N.5)=====*)
(*=====
====*)
fList = FullSimplify /@ (aList * cList); {f1, f2, f3, f4} = fList;
M1 = Ms[[1]];

m[M1_] := Piecewise[{{1 - M1, M1 < 1}, {(M1 - 1) / M1, M1 > 1}}] // N;
K = EllipticK[m[M1]] // N;
Kp = EllipticK[1 - m[M1]] // N;

computeTi[i_] :=
Module[{sigma = sigmas[[i]], r = rList[[i]], s = sList[[i]], f = fList[[i]], base},
  base = I * Im[InverseJacobiDN[Piecewise[
    {{Sqrt[f], M1 < 1}, {1 / Sqrt[f], M1 > 1}}], m[M1]]] / Kp;
  Which[sigma < 180, Which[r > 1 && s > 1, base, (r < 1 && s > 1) || (r > 1 && s < 1),

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1 + base, r < 1 && s < 1, 2 + base], sigma > 180, Which[r > 1 && s > 1,
2 + base, (r < 1 && s > 1) || (r > 1 && s < 1), 3 + base, r < 1 && s < 1, base]]];

tList = computeTi /@ Range[4];
RoundWithTolerance[x_, tol_ : 10^-6] := Module[{nearest}, nearest = Round[x];
If[Abs[x - nearest] ≤ tol, nearest, x]];

checkValidCombination[M1_, ε_ : 10^-6] :=
Module[{i, combo, dotProd, rePart, imPart, n2, expr, foundQ = False},
Print[Style["△ Approximate validation using ε-tolerance. For rigorous
proof, see the referenced paper.", Darker@Orange, Italic]];
Do[combo = uniqueCombos[[i];
dotProd = tList.combo;
rePart = Abs[Re[dotProd]];
imPart = Abs[Im[dotProd]];
If[M1 < 1,
If[Mod[RoundWithTolerance[rePart], 4] < ε,
If[Mod[RoundWithTolerance[imPart], 2] < ε, expr =
tList[[1]] + combo[[2]] × tList[[2]] + combo[[3]] × tList[[3]] + combo[[4]] × tList[[4]];
Print[Style["✔ Valid Combination Found (M < 1):",
Darker[Green], Bold], "\n", Style["e1 = ", Bold], combo[[2]],
Style["", e2 = ", Bold], combo[[3]], Style["", e3 = ", Bold], combo[[4]],
"\n", Style["t1 = ", Bold], Re[tList[[1]], "K + ", Im[tList[[1]], "iK'",
"\n", Style["t2 = ", Bold], Re[tList[[2]], "K + ", Im[tList[[2]], "iK'",
"\n", Style["t3 = ", Bold], Re[tList[[3]], "K + ", Im[tList[[3]], "iK'",
"\n", Style["t4 = ", Bold], Re[tList[[4]], "K + ", Im[tList[[4]],
"iK'", "\n", Style["t1 + e1*t2 + e2*t3 + e3*t4 = ", Bold],
Re[expr], "K + ", Im[expr], "iK'"];
foundQ = True;
Break[]]]];
If[M1 > 1,
If[Mod[RoundWithTolerance[imPart], 2] < ε,
n2 = Quotient[RoundWithTolerance[imPart], 2];
If[Mod[RoundWithTolerance[Abs[rePart - 2 n2]], 4] < ε, expr =
tList[[1]] + combo[[2]] × tList[[2]] + combo[[3]] × tList[[3]] + combo[[4]] × tList[[4]];
Print[Style["✔ Valid Combination Found (M > 1):",
Darker[Green], Bold], "\n", Style["e1 = ", Bold], combo[[2]],
Style["", e2 = ", Bold], combo[[3]], Style["", e3 = ", Bold], combo[[4]],
"\n", Style["t1 = ", Bold], Re[tList[[1]], "K + ", Im[tList[[1]], "iK'",
"\n", Style["t2 = ", Bold], Re[tList[[2]], "K + ", Im[tList[[2]], "iK'",
"\n", Style["t3 = ", Bold], Re[tList[[3]], "K + ", Im[tList[[3]], "iK'",
"\n", Style["t4 = ", Bold], Re[tList[[4]], "K + ", Im[tList[[4]],
"iK'", "\n", Style["t1 + e1*t2 + e2*t3 + e3*t4 = ", Bold],
Re[expr], "K + ", Im[expr], "iK'"];
foundQ = True;

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Break[]]]], {i, Length[uniqueCombos]}}];
If[! foundQ, Print[Style["✗ No valid combination found.", Red, Bold], "\n",
Style["t1 = ", Bold], Re[tList[[1]], "K + ", Im[tList[[1]], "iK'", "\n",
Style["t2 = ", Bold], Re[tList[[2]], "K + ", Im[tList[[2]], "iK'", "\n",
Style["t3 = ", Bold], Re[tList[[3]], "K + ", Im[tList[[3]], "iK'", "\n",
Style["t4 = ", Bold], Re[tList[[4]], "K + ", Im[tList[[4]], "iK'", "\n"]];];

Column[{TextCell[Style["===== CONDITION (N.5) =====",
Darker[Red], Bold, 16], "Text"]}]
res = checkValidCombination[M1];

(*=====
====*)
(*=====
OTHER PARAMETER=====*)
(*=====
====*)
cosSigmaAlt[Mi_, fi_, ri_, si_] :=
(Mi (fi + ri + si - 1) + ri fi si - ri fi - ri si - fi si) / (2 Sqrt[ri si fi] (1 - Mi));

Column[
{TextCell[Style["===== OTHER PARAMETERS =====",
Darker[Orange], Bold, 16], "Text"],
Row[{Style["u = ", Bold], 1 - M1}],
Row[{Style["σ1 = ", Bold], σ1 Degree, Style["", σ2 = ", Bold], σ2 Degree,
Style["", σ3 = ", Bold], σ3 Degree, Style["", σ4 = ", Bold], σ4 Degree}],
Row[{Style["σ1 ≈ ", Bold], N[σ1], Style["°", Bold], Style["", σ2 ≈ ", Bold],
N[σ2], Style["°", Bold], Style["", σ3 ≈ ", Bold], N[σ3],
Style["°", Bold], Style["", σ4 ≈ ", Bold], N[σ4], Style["°", Bold]}],
Row[{Style["cosσ1 = ", Bold], Simplify@cosSigmaAlt[M1, f1, r1, s1],
Style["", cosσ2 = ", Bold], Simplify@cosSigmaAlt[M1, f2, r2, s2],
Style["", cosσ3 = ", Bold], Simplify@cosSigmaAlt[M1, f3, r3, s3],
Style["", cosσ4 = ", Bold], Simplify@cosSigmaAlt[M1, f4, r4, s4]}],
Row[{Style["f1 = ", Bold], f1, Style["", f2 = ", Bold],
f2, Style["", f3 = ", Bold], f3, Style["", f4 = ", Bold], f4}],
Row[{Style["z1 = ", Bold], FullSimplify[1 / (f1 - 1)], Style["", z2 = ", Bold],
FullSimplify[1 / (f2 - 1)], Style["", z3 = ", Bold], FullSimplify[1 / (f3 - 1)],
Style["", z4 = ", Bold], FullSimplify[1 / (f4 - 1)]}],
Row[{Style["x1 = ", Bold], FullSimplify[1 / (r1 - 1)], Style["", x2 = ", Bold],
FullSimplify[1 / (r2 - 1)], Style["", x3 = ", Bold], FullSimplify[1 / (r3 - 1)],
Style["", x4 = ", Bold], FullSimplify[1 / (r4 - 1)]}],
Row[{Style["y1 = ", Bold], FullSimplify[1 / (s1 - 1)], Style["", y2 = ", Bold],
FullSimplify[1 / (s2 - 1)], Style["", y3 = ", Bold], FullSimplify[1 / (s3 - 1)],
Style["", y4 = ", Bold], FullSimplify[1 / (s4 - 1)]}],
Row[{Style["p1 = ", Bold], Simplify[Sqrt[r1 - 1]],

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Style["", p2 = "", Bold], Simplify[Sqrt[r2 - 1]], Style["", p3 = "", Bold],
Simplify[Sqrt[r3 - 1]], Style["", p4 = "", Bold], Simplify[Sqrt[r4 - 1]]}],
Row[{Style["q1 = ", Bold], Simplify[Sqrt[s1 - 1]],
Style["", q2 = "", Bold], Simplify[Sqrt[s2 - 1]], Style["", q3 = "", Bold],
Simplify[Sqrt[s3 - 1]], Style["", q4 = "", Bold], Simplify[Sqrt[s4 - 1]]}],
Row[{Style["p1.q1 = ", Bold], Simplify[Sqrt[r1 - 1] Sqrt[s1 - 1]],
Style["", p2.q2 = "", Bold], Simplify[Sqrt[r2 - 1] Sqrt[s2 - 1]],
Style["", p3.q3 = "", Bold], Simplify[Sqrt[r3 - 1] Sqrt[s3 - 1]],
Style["", p4.q4 = "", Bold], Simplify[Sqrt[r4 - 1] Sqrt[s4 - 1]]}]
}]

(*=====
====*)
(*=====
BRICARD's EQUATIONS=====*)
(*=====
====*)
(*=====
FLEXION 1=====*)
Z[t_] := t;
W1[t_] := 
$$\frac{6t - \sqrt{2(3t^2 - 1)(2 - 3t^2)}}{1 + 3t^2};$$

U[t_] := 
$$\frac{1}{t};$$

W2[t_] := 
$$\frac{5\sqrt{7}t - \sqrt{10(3t^2 - 1)(2 - 3t^2)}}{4 + 9t^2};$$


(*General polynomial constructor*)
BricardsEquation[{α_, β_, γ_, δ_}, σ_, x_, y_] :=
Module[{c22, c20, c02, c11, c00},
c22 = Sin[σ - δ] Sin[σ - δ - β];
c20 = Sin[σ - α] Sin[σ - α - β];
c02 = Sin[σ - γ] Sin[σ - γ - β];
c11 = -Sin[α] Sin[γ];
c00 = Sin[σ] Sin[σ - β];
c22 x^2 y^2 + c20 x^2 + c02 y^2 + 2 c11 x y + c00];

(*Compute and print all P_i for flexion 1*)
TextCell[
Style["===== FLEXIBILITY (FLEXION 1) =====",
Darker[Cyan], Bold, 16], "Text"]
funcs = {{Z, W1}, {Z, W2}, {U, W2}, {U, W1}};
Do[angles = anglesDeg[[i]] Degree;
sigma = sigmas[[i]] Degree;
{α, β, γ, δ} = angles;

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poly = Which[i == 1, BricardsEquation[{α, β, γ, δ}, sigma, Z[t], W1[t]],
  i == 2, BricardsEquation[{α, β, γ, δ}, sigma, Z[t], W2[t]],
  i == 3, BricardsEquation[{α, β, γ, δ}, sigma, U[t], W2[t]],
  i == 4, BricardsEquation[{α, β, γ, δ}, sigma, U[t], W1[t]]];
Print[Row[{Subscript["P", i], "[", funcs[[i, 1],
  ", ", funcs[[i, 2], "] = ", FullSimplify[poly]]}], {i, 1, 4}];

(*=====
FLEXION 2=====*)
Z2[t_] := t;
W12[t_] := 
$$\frac{6t + \sqrt{2(3t^2 - 1)(2 - 3t^2)}}{1 + 3t^2};$$

U2[t_] := 
$$\frac{1}{t};$$

W22[t_] := 
$$\frac{5\sqrt{7}t + \sqrt{10(3t^2 - 1)(2 - 3t^2)}}{4 + 9t^2};$$


(*General polynomial constructor*)
BricardsEquation[{α_, β_, γ_, δ_}, σ_, x_, y_] :=
Module[{c22, c20, c02, c11, c00},
  c22 = Sin[σ - δ] Sin[σ - δ - β];
  c20 = Sin[σ - α] Sin[σ - α - β];
  c02 = Sin[σ - γ] Sin[σ - γ - β];
  c11 = -Sin[α] Sin[γ];
  c00 = Sin[σ] Sin[σ - β];
  c22 x^2 y^2 + c20 x^2 + c02 y^2 + 2 c11 x y + c00];

(*Compute and print all P_i for flexion 2*)
TextCell[
  Style["===== FLEXIBILITY (FLEXION 2) =====",
    Cyan, Bold, 16], "Text"]
funcs = {{Z, W1}, {Z, W2}, {U, W2}, {U, W1}};
Do[angles = anglesDeg[[i]] Degree;
  sigma = sigmas[[i]] Degree;
  {α, β, γ, δ} = angles;
  poly = Which[i == 1, BricardsEquation[{α, β, γ, δ}, sigma, Z2[t], W12[t]],
    i == 2, BricardsEquation[{α, β, γ, δ}, sigma, Z2[t], W22[t]],
    i == 3, BricardsEquation[{α, β, γ, δ}, sigma, U2[t], W22[t]],
    i == 4, BricardsEquation[{α, β, γ, δ}, sigma, U2[t], W12[t]]];
  Print[Row[{Subscript["P", i], "[", funcs[[i, 1],
    ", ", funcs[[i, 2], "] = ", FullSimplify[poly]]}], {i, 1, 4}];

(*=====
=====*)
(*=====

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NOT TRIVIAL=====*)
(*=====
====*)
(*Define domain limits for t*)
tMin = 1 / Sqrt[3];
tMax = Sqrt[2 / 3];

(*=====
FLEXION 1=====*)
(*List of expressions to plot*)
expressions = {Z[t], W2[t], U[t], W1[t]};
labels = {"Z", "W2", "U", "W1"};

Column[{TextCell[
  Style["===== NOT TRIVIAL (FLEXION 1) =====",
    Darker[Brown], Bold, 16], "Text"],

  (*Explanatory text*)
  TextCell[Style["This configuration does not belong to the trivial class –
    even after switching the boundary strips – since none of the
    functions Z, W2, U, or W1 is constant.", GrayLevel[0.3]], "Text"],
  Spacer[12],

  (*Plots in a light panel*)
  Panel[GraphicsGrid[Partition[Table[Plot[expressions[[i]], {t, tMin, tMax},
    PlotLabel → Style[labels[[i]], Bold, 14], PlotRange → All,
    AxesLabel → {"t", None}, ImageSize → 250], {i, Length[expressions]}], 2],
    Spacings → {2, 2}], Background → Lighter[Gray, 0.95], FrameMargins → 15]

  ]}]

(*=====
FLEXION 2=====*)
(*List of expressions to plot*)
expressions = {Z2[t], W22[t], U2[t], W12[t]};
labels = {"Z", "W2", "U", "W1"};

Column[{TextCell[
  Style["===== NOT TRIVIAL (FLEXION 2) =====",
    Brown, Bold, 16], "Text"],

  (*Explanatory text*)
  TextCell[Style["This configuration does not belong to the trivial class –
    even after switching the boundary strips – since none of the
    functions Z, W2, U, or W1 is constant.", GrayLevel[0.3]], "Text"],
  Spacer[12],

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(*Plots in a light panel*)
Panel[GraphicsGrid[Partition[Table[Plot[expressions[[i]], {t, tMin, tMax},
    PlotLabel → Style[labels[[i]], Bold, 14], PlotRange → All,
    AxesLabel → {"t", None}, ImageSize → 250], {i, Length[expressions]}], 2],
    Spacings → {2, 2}], Background → Lighter[Gray, 0.95], FrameMargins → 15]

}]

(*=====
====*)
(*=====
NOT LINEAR COMPOUND & NOT LINEAR CONJUGATE=====*)
(*=====
====*)
(*Define domain limits for t*)
tMin = 1 / Sqrt[3];
tMax = Sqrt[2 / 3];

(*=====
FLEXION 1=====*)
(*List of expressions& labels*)
expressions =
{Z[t] * U[t], Z[t] / U[t], W1[t] * W2[t], W1[t] / W2[t], Z[t] * W2[t], Z[t] / W2[t],
U[t] * W1[t], U[t] / W1[t], Z[t] * W1[t], Z[t] / W1[t], W2[t] * U[t], W2[t] / U[t]};
labels = {"Z * U", "Z / U", "W1 * W2", "W1 / W2", "Z * W2", "Z / W2",
"U * W1", "U / W1", "Z * W1", "Z / W1", "W2 * U", "W2 / U"};

Column[
{TextCell[Style["===== NOT LINEAR COMPOUND & NOT LINEAR CONJUGATE
(FLEXION 1) =====", Darker[Magenta], Bold, 16], "Text"],

(*Explanatory text*)TextCell[
Style["This configuration does not belong to the Linear compound class nor
to the linear conjugate class – even after switching the boundary
strips – since none of the functions ZU, Z/U, W1W2, W1/W2, ZW2,
Z/W2, UW1, and U/W1 is constant. In addition, none of ZW1,
Z/W1, W2U, W2/U is constant as well.", GrayLevel[0.3]], "Text"],
Spacer[12],

(*Plots panel*)
Panel[GraphicsGrid[Partition[Table[Plot[expressions[[i]], {t, tMin, tMax},
    PlotLabel → Style[labels[[i]], Bold, 14], PlotRange → All,
    AxesLabel → {"t", None}, ImageSize → 250], {i, Length[expressions]}], 2],
    Spacings → {2, 2}], Background → Lighter[Gray, 0.95], FrameMargins → 15]

}]

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```

(*=====
FLEXION 2=====*)
(*List of expressions& labels*)
expressions = {Z2[t] * U2[t], Z2[t] / U2[t], W12[t] * W22[t], W12[t] / W22[t],
  Z2[t] * W22[t], Z2[t] / W22[t], U2[t] * W12[t], U2[t] / W12[t],
  Z2[t] * W12[t], Z2[t] / W12[t], W22[t] * U2[t], W22[t] / U2[t]};
labels = {"Z * U", "Z / U", "W1 * W2", "W1 / W2", "Z * W2", "Z / W2",
  "U * W1", "U / W1", "Z * W1", "Z / W1", "W2 * U", "W2 / U"};

Column[
  {TextCell[Style["===== NOT LINEAR COMPOUND & NOT LINEAR CONJUGATE
    (FLEXION 2) =====", Magenta, Bold, 16], "Text"],

  (*Explanatory text*)TextCell[
    Style["This configuration does not belong to the Linear compound class nor
      to the linear conjugate class – even after switching the boundary
      strips – since none of the functions ZU, Z/U, W1W2, W1/W2, ZW2,
      Z/W2, UW1, and U/W1 is constant. In addition, none of ZW1,
      Z/W1, W2U, W2/U is constant as well.", GrayLevel[0.3]], "Text"],
  Spacer[12],

  (*Plots panel*)
  Panel[GraphicsGrid[Partition[Table[Plot[expressions[[i]], {t, tMin, tMax},
    PlotLabel → Style[labels[[i]], Bold, 14], PlotRange → All,
    AxesLabel → {"t", None}, ImageSize → 250], {i, Length[expressions]}], 2],
    Spacings → {2, 2}], Background → Lighter[Gray, 0.95], FrameMargins → 15]
  ]
]

(*=====
=====*)
(*=====
SWITCHING BOUNDARY STRIPS=====*)
(*=====
=====*)
SwitchingRightBoundaryStrip[anglesDeg_List] := Module[{modified = anglesDeg},
  (*Indices:{row,column}={1,2},{1,3},{4,2},{4,3}*)
  modified[[1, 2]] = 180 - anglesDeg[[1, 2]]; (*β1*)
  modified[[1, 3]] = 180 - anglesDeg[[1, 3]]; (*γ1*)
  modified[[4, 2]] = 180 - anglesDeg[[4, 2]]; (*β4*)
  modified[[4, 3]] = 180 - anglesDeg[[4, 3]]; (*γ4*)
  modified]

SwitchingLeftBoundaryStrip[anglesDeg_List] := Module[{modified = anglesDeg},
  (*Indices:{row,column}={2,2},{2,3},{3,2},{3,3}*)
  modified[[2, 2]] = 180 - anglesDeg[[2, 2]]; (*β2*)
  modified[[2, 3]] = 180 - anglesDeg[[2, 3]]; (*γ2*)

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modified[[3, 2]] = 180 - anglesDeg[[3, 2]]; (*β3*)
modified[[3, 3]] = 180 - anglesDeg[[3, 3]]; (*γ3*)
modified]

SwitchingLowerBoundaryStrip[anglesDeg_List] := Module[{modified = anglesDeg},
  (*Indices:{row,column}={1,1},{1,2},{2,1},{2,2}*)
  modified[[1, 1]] = 180 - anglesDeg[[1, 1]]; (*α1*)
  modified[[1, 2]] = 180 - anglesDeg[[1, 2]]; (*β1*)
  modified[[2, 1]] = 180 - anglesDeg[[2, 1]]; (*α2*)
  modified[[2, 2]] = 180 - anglesDeg[[2, 2]]; (*β2*)
  modified]

SwitchingUpperBoundaryStrip[anglesDeg_List] := Module[{modified = anglesDeg},
  (*Indices:{row,column}={3,1},{3,2},{4,1},{4,2}*)
  modified[[3, 1]] = 180 - anglesDeg[[3, 1]]; (*α3*)
  modified[[3, 2]] = 180 - anglesDeg[[3, 2]]; (*β3*)
  modified[[4, 1]] = 180 - anglesDeg[[4, 1]]; (*α4*)
  modified[[4, 2]] = 180 - anglesDeg[[4, 2]]; (*β4*)
  modified]

(*=====
====*)
(*=====
NOT CONIC=====*)
(*=====
====*)
Column[{TextCell[Style["===== NOT CONIC =====",
  Pink, Bold, 16], "Text"],
  TextCell[Style["Condition (N.0) is satisfied ⇒
  this configuration is NOT equimodular-conic. Applying
  any boundary-strip switch still preserves (N.0), so
  no conic form emerges.", GrayLevel[0.3]], "Text"]
}]

(*Now the exact same Module for checking all switch combinations...*)
Module[{angles = anglesDeg, switchers, combinations, results},
  (*Define switch functions*)
  switchers = <|"Right" → SwitchingRightBoundaryStrip,
    "Left" → SwitchingLeftBoundaryStrip, "Lower" → SwitchingLowerBoundaryStrip,
    "Upper" → SwitchingUpperBoundaryStrip|>;
  (*Generate all combinations of switches (from size 1 to 4)*)
  combinations = Subsets[Keys[switchers], {1, Length[switchers]}];
  (*Evaluate condition after each combination of switches*) results = Table[
    Module[{switched = angles, name, passQ}, name = StringRiffle[combo, " + "];
    Do[switched = switchers[sw][switched], {sw, combo}];
    passQ = And@@ (checkConditionN0Degrees /@ switched);

```

```

(*Print the result after switching*)
(*Print["\nSwitch combination: ",name];
Print["Switched anglesDeg:"];
Print[MatrixForm[switched]];*)
{name, passQ}}, {combo, combinations}}];
(*Display results*)
Column[Prepend[Table[Module[{comboName = res[[1]], passQ = res[[2]]},
  Row[{Style[comboName <> ": ", Bold],
    If[passQ,
      Style["Condition (N.0) is still satisfied.", Darker[Green]],
      Style["Condition (N.0) fails.", Red, Bold]
    ]
  }, {res, results}], TextCell[
Style["CONDITION (N.0) AFTER SWITCHING BOUNDARY STRIPS", 14], "Text"]]]]

(*=====
====*)
(*=====
NOT ORTHODIAGONAL=====*)
(*=====
====*)
Column[
{TextCell[Style["===== NOT ORTHODIAGONAL =====",
  Purple, Bold, 16], "Text"],
TextCell[Style[
"cos( $\alpha_i$ )·cos( $\gamma_i$ )  $\neq$  cos( $\beta_i$ )·cos( $\delta_i$ ) for each i = 1...4  $\Rightarrow$  NOT orthodiagonal.
Switching boundary strips does not
correct this.", GrayLevel[0.3]], "Text"]
}]

Module[{angles = anglesDeg, switchers, combinations, results},
(*Define switch functions*)
switchers = <|"Right"  $\rightarrow$  SwitchingRightBoundaryStrip,
"Left"  $\rightarrow$  SwitchingLeftBoundaryStrip, "Lower"  $\rightarrow$  SwitchingLowerBoundaryStrip,
"Upper"  $\rightarrow$  SwitchingUpperBoundaryStrip|>;
(*Helper function:compute and print difference only*)
formatOrthodiagonalCheck[quad_List] := Module[{vals},
vals = Table[Module[{a, b, c, d, lhs, rhs, diff}, {a, b, c, d} = quad[[i]];
lhs = FullSimplify[Cos[a Degree] Cos[c Degree]];
rhs = FullSimplify[Cos[b Degree] Cos[d Degree]];
diff = Chop[lhs - rhs];
Style[Row[{"cos( $\alpha$ " <> ToString[i] <> ")·cos( $\gamma$ " <> ToString[i] <> ") - ",
"cos( $\beta$ " <> ToString[i] <> ")·cos( $\delta$ " <> ToString[i] <> ") = ", NumberForm[
diff, {5, 3}]]], If[diff == 0, Red, Black]]], {i, Length[quad]}];
Column[vals]];

```

```

(*Orthodiagonal check for anglesDeg before any switching*)
Print[TextCell[Style["\nInitial anglesDeg (no switches):", Bold]]];
Print[MatrixForm[angles]];
Print[TextCell[Style[
  "Orthodiagonal check:  $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$  for  $i = 1..4$ ",
  Italic]]];
Print[formatOrthodiagonalCheck[angles]];
(*Generate all combinations of switches (from size 1 to 4)*)
combinations = Subsets[Keys[switchers], {1, Length[switchers]}];
(*Evaluate condition after each combination of switches*)results = Table[
  Module[{switched = angles, name, passQ}, name = StringRiffle[combo, " + "];
    Do[switched = switchers[sw][switched], {sw, combo}];
    passQ = And@@(checkConditionN0Degrees/@switched);
    Print[Style["\nSwitch combination: ", Bold], name];
    Print[Style["Switched anglesDeg:", Italic]];
    Print[MatrixForm[switched]];
    Print[TextCell[Style[
      "Orthodiagonal check:  $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$  for  $i = 1..4$ ",
      Italic]]];
    Print[formatOrthodiagonalCheck[switched]];
    {name, passQ}], {combo, combinations}];

(*=====
====*)
(*=====
NOT ISOGONAL=====*)
(*=====
====*)
Column[
  {TextCell[Style["===== NOT ISOGONAL =====", Orange,
    Bold, 15], "Text"],
    TextCell[
      Style["Condition (N.0) holds AND for all  $i = 1..4$ :  $\alpha_i \neq \beta_i$ ,  $\alpha_i \neq \gamma_i$ ,  $\alpha_i \neq \delta_i$ ,  $\beta_i \neq \gamma_i$ ,  $\beta_i \neq \delta_i$ ,  $\gamma_i \neq \delta_i$ ,  $\alpha_i + \beta_i \neq \pi \neq \gamma_i + \delta_i$ ,  $\alpha_i + \gamma_i \neq \pi \neq \beta_i + \delta_i$ ,  $\alpha_i + \delta_i \neq \pi \neq \beta_i + \gamma_i \Rightarrow$  NOT isogonal. Switching boundary strips do not change this.", GrayLevel[0.3]], "Text"]}]}

Module[{angles = anglesDeg, switchers, combinations, results},
  (*Define switch functions*)
  switchers = <|"Right" → SwitchingRightBoundaryStrip,
    "Left" → SwitchingLeftBoundaryStrip, "Lower" → SwitchingLowerBoundaryStrip,
    "Upper" → SwitchingUpperBoundaryStrip|>;
  (*Helper function:extended angle relations*)
  formatAngleRelations[quad_List] :=
    Module[{vals}, vals = Table[Module[{a, b, c, d, exprs}, {a, b, c, d} = quad[[i]];
      exprs = {Row[{" $\alpha$ " <> ToString[i] <> " -  $\beta$ " <> ToString[i] <> " = "},

```

```

      NumberForm[N[a - b], {5, 3}]]], Row[{" $\alpha$ " <> ToString[i] <>
      " -  $\gamma$ " <> ToString[i] <> " = ", NumberForm[N[a - c], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " -  $\delta$ " <> ToString[i] <> " = ",
      NumberForm[N[a - d], {5, 3}]]], Row[{" $\beta$ " <> ToString[i] <>
      " -  $\gamma$ " <> ToString[i] <> " = ", NumberForm[N[b - c], {5, 3}]]],
      Row[{" $\beta$ " <> ToString[i] <> " -  $\delta$ " <> ToString[i] <> " = ",
      NumberForm[N[b - d], {5, 3}]]], Row[{" $\gamma$ " <> ToString[i] <>
      " -  $\delta$ " <> ToString[i] <> " = ", NumberForm[N[c - d], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\beta$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[a + b - 180], {5, 3}]]],
      Row[{" $\gamma$ " <> ToString[i] <> " +  $\delta$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[c + d - 180], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\gamma$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[a + c - 180], {5, 3}]]],
      Row[{" $\beta$ " <> ToString[i] <> " +  $\delta$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[b + d - 180], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\delta$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[a + d - 180], {5, 3}]]],
      Row[{" $\beta$ " <> ToString[i] <> " +  $\gamma$ " <> ToString[i] <> " - 180 = ",
      NumberForm[N[b + c - 180], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\beta$ " <> ToString[i] <> " -  $\gamma$ " <> ToString[i] <>
      " -  $\delta$ " <> ToString[i] <> " = ", NumberForm[N[a + b - c - d], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\gamma$ " <> ToString[i] <> " -  $\beta$ " <> ToString[i] <>
      " -  $\delta$ " <> ToString[i] <> " = ", NumberForm[N[a + c - b - d], {5, 3}]]],
      Row[{" $\alpha$ " <> ToString[i] <> " +  $\delta$ " <> ToString[i] <> " -  $\beta$ " <> ToString[i] <>
      " -  $\gamma$ " <> ToString[i] <> " = ", NumberForm[N[a + d - b - c], {5, 3}]]]]];
      Column[Prepend[exprs, Style["Vertex " <> ToString[i], Bold]]],
      {i, Length[quad]}}];
      Column[vals, Spacings -> 1.5]];
(*Angle relation check for anglesDeg before any switching*)
Print[TextCell[Style["\nInitial anglesDeg (no switches):", Bold]]];
Print[MatrixForm[angles]];
Print[TextCell[Style["Angle relation checks for i = 1..4:", Italic]]];
Print[formatAngleRelations[angles]];
(*Generate all combinations of switches (from size 1 to 4)*)
combinations = Subsets[Keys[switchers], {1, Length[switchers]}];
(*Evaluate condition after each combination of switches*)results = Table[
  Module[{switched = angles, name, passQ}, name = StringRiffle[combo, " + "];
  Do[switched = switchers[sw][switched], {sw, combo}];
  passQ = And@@ (checkConditionN0Degrees /@ switched);
  Print[Style["\nSwitch combination: ", Bold], name];
  Print[Style["Switched anglesDeg:", Italic]];
  Print[MatrixForm[switched]];
  Print[TextCell[Style["Angle relation checks for i = 1..4:", Italic]]];
  Print[formatAngleRelations[switched]];
  {name, passQ}], {combo, combinations}];]

```

```

(*=====
====*)
(*=====
NOT CONJUGATE-MODULAR=====*)
(*=====
====*)
Column[
{TextCell[Style["===== NOT CONJUGATE-MODULAR =====",
Brown, Bold, 16], "Text"],
TextCell[Style[" $M_i < 1$  and  $p_i \in \mathbb{R}$  for all  $i = 1...4 \Rightarrow$  NOT conjugate-modular.
Boundary-strip switches preserve this.", GrayLevel[0.3]], "Text"]
}]

Module[{angles = anglesDeg, switchers, combinations, results,
computeConjugateModularInfo}, (*Define switch functions*)
switchers = <|"Right" → SwitchingRightBoundaryStrip,
"Left" → SwitchingLeftBoundaryStrip, "Lower" → SwitchingLowerBoundaryStrip,
"Upper" → SwitchingUpperBoundaryStrip|>;
(*Computes  $M_i$  and  $p_i$  and prints them,
with classification*)computeConjugateModularInfo[quad_List] :=
Module[{abcdList, Ms, summary}, abcdList = computeABCD /@ quad;
Ms = FullSimplify[Times@@@ abcdList];
summary = If[AllTrue[Ms, # < 1 &], Style[" $M_i < 1$  for all  $i = 1, \dots, 4$ ",
Bold], Style[" $M_i \geq 1$  for some  $i = 1, \dots, 4$ ", Red, Bold]];
Column[{Style[" $M_i$  values:", Bold], Row[{"M1 = ", Ms[[1]], ", M2 = ",
Ms[[2]], ", M3 = ", Ms[[3]], ", M4 = ", Ms[[4]]}, summary]}}];
(*Original anglesDeg check*)
Print[
TextCell[Style["\nInitial configuration (no switches applied):", Bold]]];
Print[MatrixForm[angles]];
Print[computeConjugateModularInfo[angles]];
(*Generate all switch combinations (from size 1 to 4)*)
combinations = Subsets[Keys[switchers], {1, Length[switchers]}];
(*Evaluate each switched configuration*)results = Table[
Module[{switched = angles, name, passQ}, name = StringRiffle[combo, " + "];
Do[switched = switchers[sw][switched], {sw, combo}];
passQ = And@@ (checkConditionN0Degrees /@ switched);
Print[Style["\nSwitch combination: ", Bold], name];
Print[Style["Switched anglesDeg:", Italic]];
Print[MatrixForm[switched]];
Print[computeConjugateModularInfo[switched]];
{name, passQ}], {combo, combinations}];

(*=====

```

```

====*)
(*=====
NOT CHIMERA=====*)
(*=====
====*)
Column[
{TextCell[Style["===== NOT CHIMERA =====", Blue,
  Bold, 16], "Text"],
TextCell[
Style["Fails conic, orthodiagonal & isogonal tests for all i=1, ...,
  4  $\Rightarrow$  NOT chimera. Boundary-strip switches preserve these
  failures as demonstrated in the NOT CONIC, NOT ORTHODIAGONAL,
  and NOT ISOGONAL sections.", GrayLevel[0.3]], "Text"]
}]

```

Out[*]=

```

===== CONDITION (N.0) =====
✓ All vertices satisfy (N.0).

```

Out[*]=

```

===== CONDITION (N.3) =====
✓ M1 = M2 = M3 = M4 =  $\frac{1}{2}$ 

```

Out[*]=

```

===== CONDITION (N.4) =====
✓ r1 = r2 =  $\frac{4}{3}$ ; ✓ r3 = r4 =  $\frac{5}{2}$ 
✓ s1 = s4 = 3; ✓ s2 = s3 =  $\frac{11}{6}$ 

```

Out[*]=

```

===== CONDITION (N.5) =====
△ Approximate validation using
   $\epsilon$ -tolerance. For rigorous proof, see the referenced paper.
✓ Valid Combination Found (M < 1):
e1 = 1, e2 = 1, e3 = 1
t1 = 0.K + 0.554485iK'
t2 = 0.K + 0.509302iK'
t3 = 0.K + 0.490698iK'
t4 = 0.K + 0.445515iK'
t1 + e1*t2 + e2*t3 + e3*t4 = 0.K + 2.iK'

```


Out[]=

===== OTHER PARAMETERS =====

$$u = \frac{1}{2}$$

$$\sigma_1 = 135^\circ, \sigma_2 = \circ \left(135 + \frac{90 \operatorname{ArcCos}\left[\frac{15\sqrt{7}}{44}\right]}{\pi} \right)$$

$$, \sigma_3 = \frac{90^\circ \left(\pi + \operatorname{ArcTan}\left[\frac{4\sqrt{7}}{3}\right] \right)}{\pi}, \sigma_4 = \circ \left(135 - \frac{45 \operatorname{ArcTan}\left[\frac{24}{7}\right]}{\pi} \right)$$

$$\sigma_1 \approx 135.^\circ, \sigma_2 \approx 147.792^\circ, \sigma_3 \approx 127.087^\circ, \sigma_4 \approx 116.565^\circ$$

$$\cos\sigma_1 = -\frac{1}{\sqrt{2}}, \cos\sigma_2 = -\frac{3\sqrt{\frac{7}{22}}}{2}, \cos\sigma_3 = -\frac{2}{\sqrt{11}}, \cos\sigma_4 = -\frac{1}{\sqrt{5}}$$

$$f_1 = 2, f_2 = \frac{7}{4}, f_3 = \frac{5}{3}, f_4 = \frac{3}{2}$$

$$z_1 = 1, z_2 = \frac{4}{3}, z_3 = \frac{3}{2}, z_4 = 2$$

$$x_1 = 3, x_2 = 3, x_3 = \frac{2}{3}, x_4 = \frac{2}{3}$$

$$y_1 = \frac{1}{2}, y_2 = \frac{6}{5}, y_3 = \frac{6}{5}, y_4 = \frac{1}{2}$$

$$p_1 = \frac{1}{\sqrt{3}}, p_2 = \frac{1}{\sqrt{3}}, p_3 = \sqrt{\frac{3}{2}}, p_4 = \sqrt{\frac{3}{2}}$$

$$q_1 = \sqrt{2}, q_2 = \sqrt{\frac{5}{6}}, q_3 = \sqrt{\frac{5}{6}}, q_4 = \sqrt{2}$$

$$p_1 \cdot q_1 = \sqrt{\frac{2}{3}}, p_2 \cdot q_2 = \frac{\sqrt{\frac{5}{2}}}{3}, p_3 \cdot q_3 = \frac{\sqrt{5}}{2}, p_4 \cdot q_4 = \sqrt{3}$$

Out[]=

===== FLEXIBILITY (FLEXION 1) =====

$$P_1[Z, W1] = 0$$

$$P_2[Z, W2] = 0$$

$$P_3[U, W2] = 0$$

$$P_4[U, W1] = 0$$

Out[]=

===== FLEXIBILITY (FLEXION 2) =====

$$P_1[Z, W1] = 0$$

$$P_2[Z, W2] = 0$$

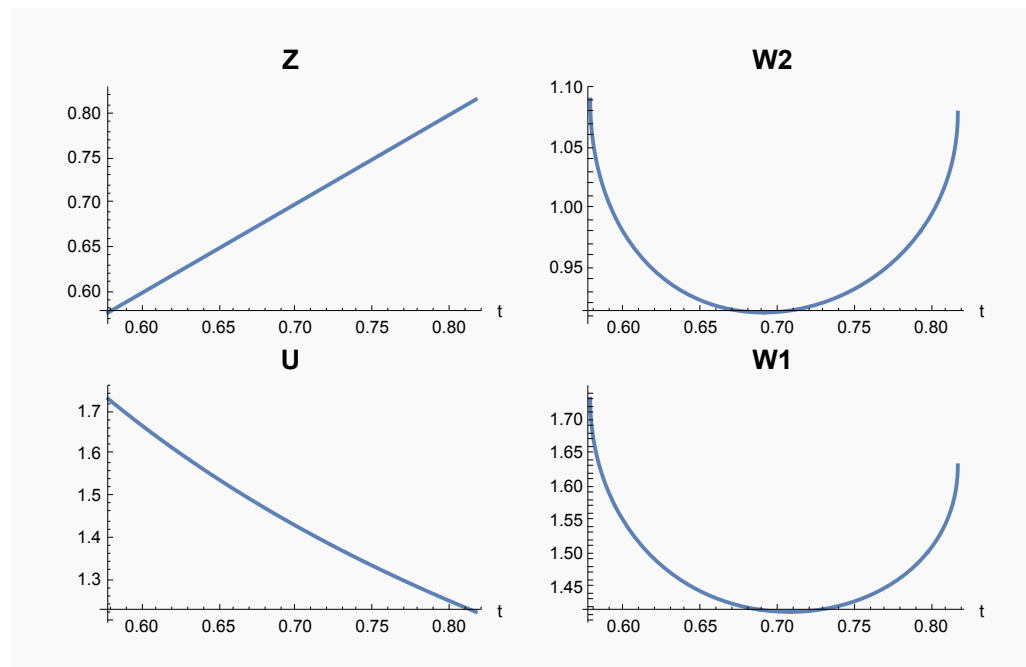
$$P_3[U, W2] = 0$$

$$P_4[U, W1] = 0$$

Out[]=

===== NOT TRIVIAL (FLEXION 1) =====

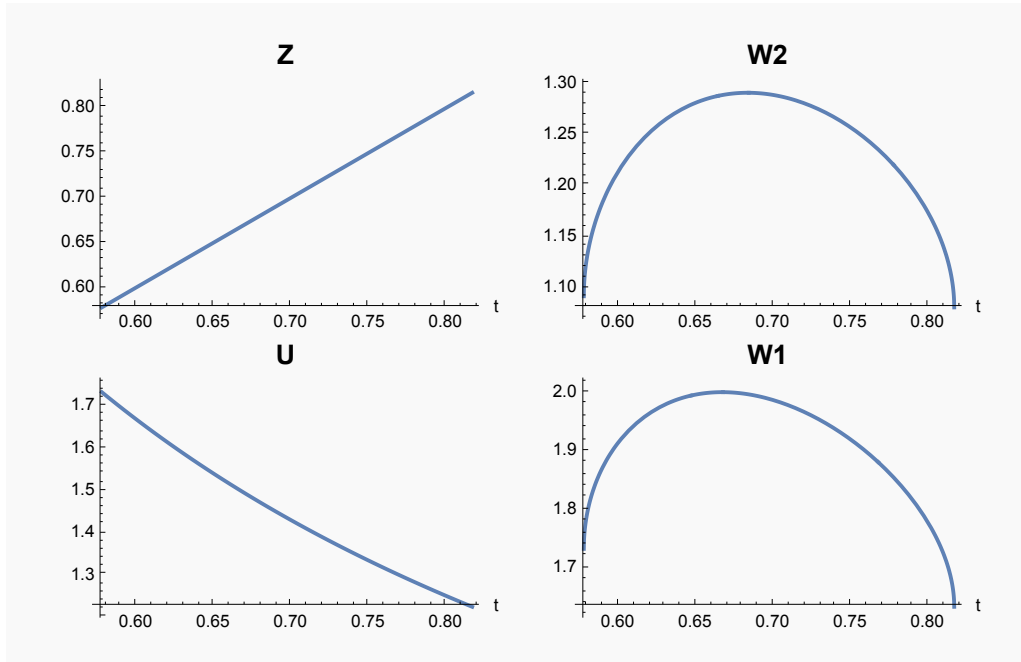
This configuration does not belong to the trivial class – even after switching the boundary strips – since none of the functions Z , $W2$, U , or $W1$ is constant.



Out[]=

===== NOT TRIVIAL (FLEXION 2) =====

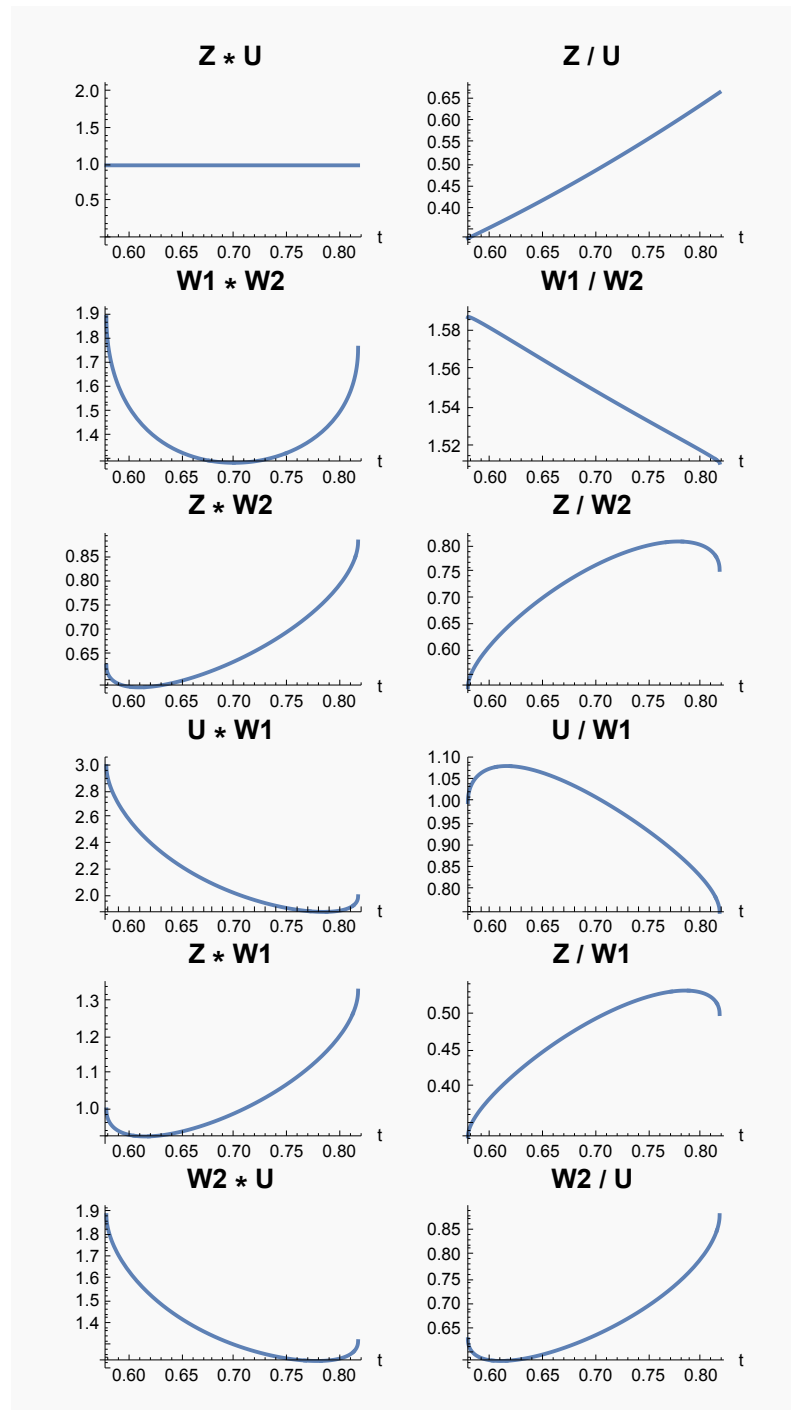
This configuration does not belong to the trivial class – even after switching the boundary strips – since none of the functions Z , $W2$, U , or $W1$ is constant.



Out[]=

===== NOT LINEAR COMPOUND &
NOT LINEAR CONJUGATE (FLEXION 1) =====

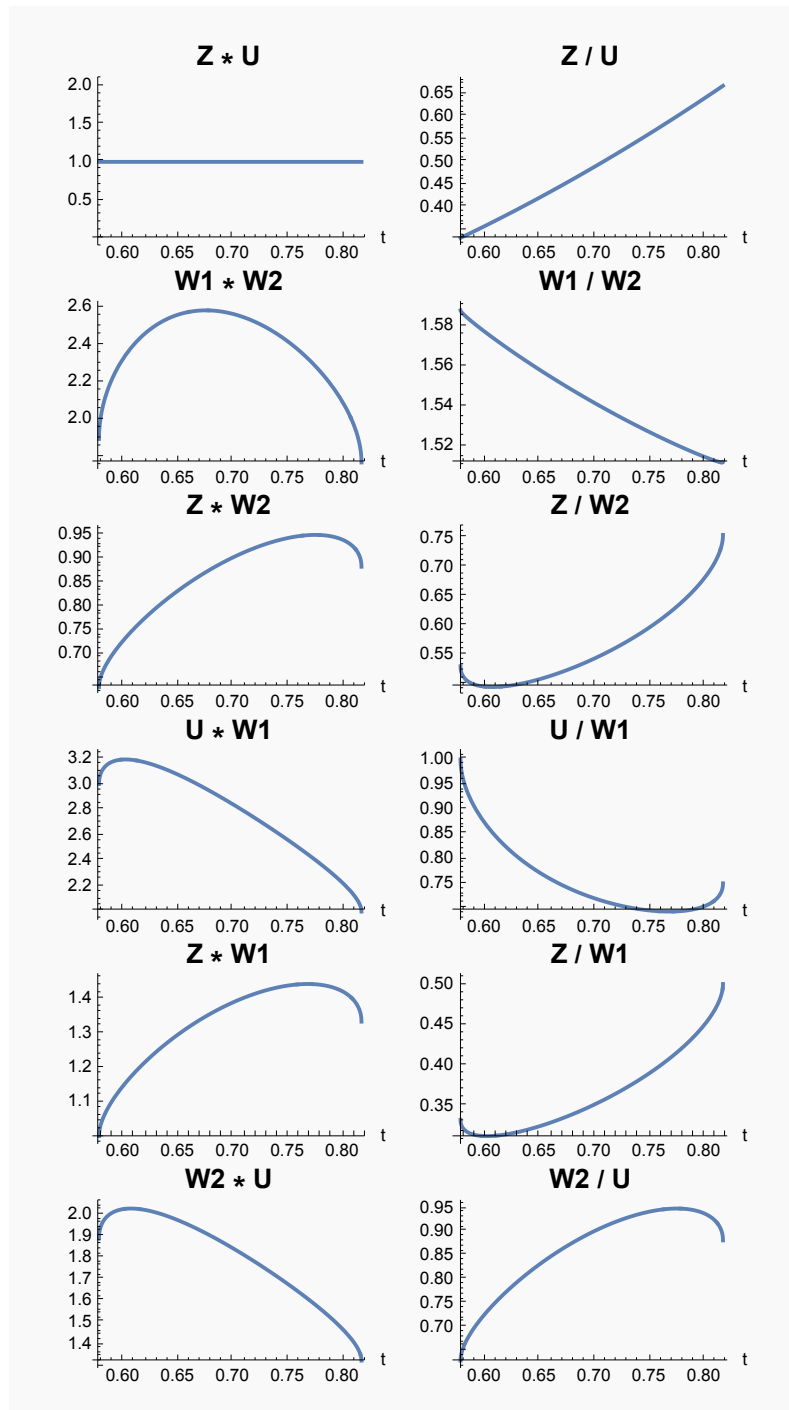
This configuration does not belong to the Linear compound class nor to the linear conjugate class – even after switching the boundary strips – since none of the functions ZU , Z/U , $W1W2$, $W1/W2$, $ZW2$, $Z/W2$, $UW1$, and $U/W1$ is constant. In addition, none of $ZW1$, $Z/W1$, $W2U$, $W2/U$ is constant as well.



Out[]=

===== NOT LINEAR COMPOUND &
 NOT LINEAR CONJUGATE (FLEXION 2) =====

This configuration does not belong to the Linear compound class nor to the linear conjugate class – even after switching the boundary strips – since none of the functions ZU , Z/U , $W1W2$, $W1/W2$, $ZW2$, $Z/W2$, $UW1$, and $U/W1$ is constant. In addition, none of $ZW1$, $Z/W1$, $W2U$, $W2/U$ is constant as well.



Out[*]=

===== NOT CONIC =====

Condition (N.0) is satisfied \Rightarrow this configuration
is NOT equimodular-conic. Applying any boundary-strip
switch still preserves (N.0), so no conic form emerges.

Out[*]=

CONDITION (N.0) AFTER SWITCHING BOUNDARY STRIPS

Right: Condition (N.0) is still satisfied.

Left: Condition (N.0) is still satisfied.

Lower: Condition (N.0) is still satisfied.

Upper: Condition (N.0) is still satisfied.

Right + Left: Condition (N.0) is still satisfied.

Right + Lower: Condition (N.0) is still satisfied.

Right + Upper: Condition (N.0) is still satisfied.

Left + Lower: Condition (N.0) is still satisfied.

Left + Upper: Condition (N.0) is still satisfied.

Lower + Upper: Condition (N.0) is still satisfied.

Right + Left + Lower: Condition (N.0) is still satisfied.

Right + Left + Upper: Condition (N.0) is still satisfied.

Right + Lower + Upper: Condition (N.0) is still satisfied.

Left + Lower + Upper: Condition (N.0) is still satisfied.

Right + Left + Lower + Upper: Condition (N.0) is still satisfied.

Out[*]=

===== NOT ORTHODIAGONAL =====

$\cos(\alpha_i) \cdot \cos(\gamma_i) \neq \cos(\beta_i) \cdot \cos(\delta_i)$ for each $i = 1..4 \Rightarrow$ NOT
orthodiagonal. Switching boundary strips does not correct this.

Initial anglesDeg (no switches):

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} \end{array} \right) \begin{array}{l} 90 \\ 90 \\ 90 \\ 90 \end{array}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned} \cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}} \end{aligned}$$

Switch combination: Right

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned} \cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}} \end{aligned}$$

Switch combination: Left

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned} \cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}} \end{aligned}$$

Switch combination: Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Upper

Switched anglesDeg:

$$\begin{pmatrix}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Right + Left

Switched anglesDeg:

$$\begin{pmatrix}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Right + Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) = -\frac{1}{5\sqrt{2}}$$

$$\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) = \frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) = \frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) = -\frac{1}{5\sqrt{2}}$$

Switch combination: Right + Upper

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) = \frac{1}{5\sqrt{2}}$$

$$\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) = -\frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) = -\frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) = \frac{1}{5\sqrt{2}}$$

Switch combination: Left + Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Left + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}
\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\
\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\
\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\
\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}}
\end{aligned}$$

Switch combination: Right + Left + Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) = -\frac{1}{5\sqrt{2}}$$

$$\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) = -\frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) = -\frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) = -\frac{1}{5\sqrt{2}}$$

Switch combination: Right + Left + Upper

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) = \frac{1}{5\sqrt{2}}$$

$$\cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) = \frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) = \frac{1}{8\sqrt{22}}$$

$$\cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) = \frac{1}{5\sqrt{2}}$$

Switch combination: Right + Lower + Upper

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}}\end{aligned}$$

Switch combination: Left + Lower + Upper

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= \frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= -\frac{1}{5\sqrt{2}}\end{aligned}$$

Switch combination: Right + Left + Lower + Upper

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

Orthodiagonal check: $\cos(\alpha_i) \cdot \cos(\gamma_i) - \cos(\beta_i) \cdot \cos(\delta_i)$ for $i = 1..4$

$$\begin{aligned}\cos(\alpha_1) \cdot \cos(\gamma_1) - \cos(\beta_1) \cdot \cos(\delta_1) &= -\frac{1}{5\sqrt{2}} \\ \cos(\alpha_2) \cdot \cos(\gamma_2) - \cos(\beta_2) \cdot \cos(\delta_2) &= -\frac{1}{8\sqrt{22}} \\ \cos(\alpha_3) \cdot \cos(\gamma_3) - \cos(\beta_3) \cdot \cos(\delta_3) &= \frac{1}{8\sqrt{22}} \\ \cos(\alpha_4) \cdot \cos(\gamma_4) - \cos(\beta_4) \cdot \cos(\delta_4) &= \frac{1}{5\sqrt{2}}\end{aligned}$$

Out[*]=

===== NOT ISOGONAL =====

Condition (N.0) holds AND for all $i = 1..4$: $\alpha_i \neq \beta_i$,

$\alpha_i \neq \gamma_i$, $\alpha_i \neq \delta_i$, $\beta_i \neq \gamma_i$, $\beta_i \neq \delta_i$, $\gamma_i \neq \delta_i$, $\alpha_i + \beta_i \neq$

$\pi \neq \gamma_i + \delta_i$, $\alpha_i + \gamma_i \neq \pi \neq \beta_i + \delta_i$, $\alpha_i + \delta_i \neq \pi \neq \beta_i + \gamma_i \Rightarrow$ NOT

isogonal. Switching boundary strips do not change this.

Initial anglesDeg (no switches):

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned} \alpha 1 - \beta 1 &= 55.305 \\ \alpha 1 - \gamma 1 &= -45.000 \\ \alpha 1 - \delta 1 &= -26.565 \\ \beta 1 - \gamma 1 &= -100.300 \\ \beta 1 - \delta 1 &= -81.870 \\ \gamma 1 - \delta 1 &= 18.435 \\ \alpha 1 + \beta 1 - 180 &= -108.430 \\ \gamma 1 + \delta 1 - 180 &= 18.435 \\ \alpha 1 + \gamma 1 - 180 &= -8.130 \\ \beta 1 + \delta 1 - 180 &= -81.870 \\ \alpha 1 + \delta 1 - 180 &= -26.565 \\ \beta 1 + \gamma 1 - 180 &= -63.435 \\ \alpha 1 + \beta 1 - \gamma 1 - \delta 1 &= -126.870 \\ \alpha 1 + \gamma 1 - \beta 1 - \delta 1 &= 73.740 \\ \alpha 1 + \delta 1 - \beta 1 - \gamma 1 &= 36.870 \end{aligned}$$

Vertex 2

$$\begin{aligned} \alpha 2 - \beta 2 &= 76.476 \\ \alpha 2 - \gamma 2 &= -25.028 \\ \alpha 2 - \delta 2 &= -4.323 \\ \beta 2 - \gamma 2 &= -101.500 \\ \beta 2 - \delta 2 &= -80.799 \\ \gamma 2 - \delta 2 &= 20.705 \\ \alpha 2 + \beta 2 - 180 &= -85.122 \\ \gamma 2 + \delta 2 - 180 &= 20.705 \\ \alpha 2 + \gamma 2 - 180 &= 16.382 \\ \beta 2 + \delta 2 - 180 &= -80.799 \\ \alpha 2 + \delta 2 - 180 &= -4.323 \\ \beta 2 + \gamma 2 - 180 &= -60.094 \\ \alpha 2 + \beta 2 - \gamma 2 - \delta 2 &= -105.830 \\ \alpha 2 + \gamma 2 - \beta 2 - \delta 2 &= 97.181 \\ \alpha 2 + \delta 2 - \beta 2 - \gamma 2 &= 55.771 \end{aligned}$$

Vertex 3

$$\begin{aligned} \alpha 3 - \beta 3 &= 76.476 \\ \alpha 3 - \gamma 3 &= 16.382 \\ \alpha 3 - \delta 3 &= -4.323 \\ \beta 3 - \gamma 3 &= -60.094 \\ \beta 3 - \delta 3 &= -80.799 \\ \gamma 3 - \delta 3 &= -20.705 \\ \alpha 3 + \beta 3 - 180 &= -85.122 \\ \gamma 3 + \delta 3 - 180 &= -20.705 \\ \alpha 3 + \gamma 3 - 180 &= -25.028 \\ \beta 3 + \delta 3 - 180 &= -80.799 \\ \alpha 3 + \delta 3 - 180 &= -4.323 \\ \beta 3 + \gamma 3 - 180 &= -101.500 \end{aligned}$$

$$\begin{aligned}\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -64.417 \\ \alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 55.771 \\ \alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 97.181\end{aligned}$$

Vertex 4

$$\begin{aligned}\alpha_4 - \beta_4 &= 55.305 \\ \alpha_4 - \gamma_4 &= -8.130 \\ \alpha_4 - \delta_4 &= -26.565 \\ \beta_4 - \gamma_4 &= -63.435 \\ \beta_4 - \delta_4 &= -81.870 \\ \gamma_4 - \delta_4 &= -18.435 \\ \alpha_4 + \beta_4 - 180 &= -108.430 \\ \gamma_4 + \delta_4 - 180 &= -18.435 \\ \alpha_4 + \gamma_4 - 180 &= -45.000 \\ \beta_4 + \delta_4 - 180 &= -81.870 \\ \alpha_4 + \delta_4 - 180 &= -26.565 \\ \beta_4 + \gamma_4 - 180 &= -100.300 \\ \alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -90.000 \\ \alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 36.870 \\ \alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= 73.740\end{aligned}$$

Switch combination: Right*Switched anglesDeg:*

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\begin{aligned}\alpha_1 - \beta_1 &= -108.430 \\ \alpha_1 - \gamma_1 &= -8.130 \\ \alpha_1 - \delta_1 &= -26.565 \\ \beta_1 - \gamma_1 &= 100.300 \\ \beta_1 - \delta_1 &= 81.870 \\ \gamma_1 - \delta_1 &= -18.435 \\ \alpha_1 + \beta_1 - 180 &= 55.305 \\ \gamma_1 + \delta_1 - 180 &= -18.435 \\ \alpha_1 + \gamma_1 - 180 &= -45.000 \\ \beta_1 + \delta_1 - 180 &= 81.870 \\ \alpha_1 + \delta_1 - 180 &= -26.565 \\ \beta_1 + \gamma_1 - 180 &= 63.435 \\ \alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 73.740 \\ \alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -126.870 \\ \alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -90.000\end{aligned}$$

Vertex 2

$$\begin{aligned}\alpha_2 - \beta_2 &= 76.476 \\ \alpha_2 - \gamma_2 &= -25.028 \\ \alpha_2 - \delta_2 &= -4.323 \\ \beta_2 - \gamma_2 &= -101.500 \\ \beta_2 - \delta_2 &= -80.799 \\ \gamma_2 - \delta_2 &= 20.705 \\ \alpha_2 + \beta_2 - 180 &= -85.122 \\ \gamma_2 + \delta_2 - 180 &= 20.705\end{aligned}$$

$$\begin{aligned}
\alpha_2 + \gamma_2 - 180 &= 16.382 \\
\beta_2 + \delta_2 - 180 &= -80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= -60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -105.830 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 97.181 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 55.771
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= 76.476 \\
\alpha_3 - \gamma_3 &= 16.382 \\
\alpha_3 - \delta_3 &= -4.323 \\
\beta_3 - \gamma_3 &= -60.094 \\
\beta_3 - \delta_3 &= -80.799 \\
\gamma_3 - \delta_3 &= -20.705 \\
\alpha_3 + \beta_3 - 180 &= -85.122 \\
\gamma_3 + \delta_3 - 180 &= -20.705 \\
\alpha_3 + \gamma_3 - 180 &= -25.028 \\
\beta_3 + \delta_3 - 180 &= -80.799 \\
\alpha_3 + \delta_3 - 180 &= -4.323 \\
\beta_3 + \gamma_3 - 180 &= -101.500 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -64.417 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 55.771 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 97.181
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -108.430 \\
\alpha_4 - \gamma_4 &= -45.000 \\
\alpha_4 - \delta_4 &= -26.565 \\
\beta_4 - \gamma_4 &= 63.435 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= 55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= -8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565 \\
\beta_4 + \gamma_4 - 180 &= 100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 36.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -90.000 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -126.870
\end{aligned}$$

Switch combination: Left*Switched anglesDeg:*

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} \end{array} \right) \begin{array}{l} 90 \\ 90 \\ 90 \\ 90 \end{array}$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\begin{aligned}
\alpha_1 - \beta_1 &= 55.305 \\
\alpha_1 - \gamma_1 &= -45.000 \\
\alpha_1 - \delta_1 &= -26.565 \\
\beta_1 - \gamma_1 &= 63.435 \\
\beta_1 - \delta_1 &= 81.870 \\
\gamma_1 - \delta_1 &= 18.435
\end{aligned}$$

$$\begin{aligned}
\beta_1 - \gamma_1 &= -100.300 \\
\beta_1 - \delta_1 &= -81.870 \\
\gamma_1 - \delta_1 &= 18.435 \\
\alpha_1 + \beta_1 - 180 &= -108.430 \\
\gamma_1 + \delta_1 - 180 &= 18.435 \\
\alpha_1 + \gamma_1 - 180 &= -8.130 \\
\beta_1 + \delta_1 - 180 &= -81.870 \\
\alpha_1 + \delta_1 - 180 &= -26.565 \\
\beta_1 + \gamma_1 - 180 &= -63.435 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= -126.870 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= 73.740 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= 36.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -85.122 \\
\alpha_2 - \gamma_2 &= 16.382 \\
\alpha_2 - \delta_2 &= -4.323 \\
\beta_2 - \gamma_2 &= 101.500 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= -20.705 \\
\alpha_2 + \beta_2 - 180 &= 76.476 \\
\gamma_2 + \delta_2 - 180 &= -20.705 \\
\alpha_2 + \gamma_2 - 180 &= -25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= 60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 97.181 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -105.830 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -64.417
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= -85.122 \\
\alpha_3 - \gamma_3 &= -25.028 \\
\alpha_3 - \delta_3 &= -4.323 \\
\beta_3 - \gamma_3 &= 60.094 \\
\beta_3 - \delta_3 &= 80.799 \\
\gamma_3 - \delta_3 &= 20.705 \\
\alpha_3 + \beta_3 - 180 &= 76.476 \\
\gamma_3 + \delta_3 - 180 &= 20.705 \\
\alpha_3 + \gamma_3 - 180 &= 16.382 \\
\beta_3 + \delta_3 - 180 &= 80.799 \\
\alpha_3 + \delta_3 - 180 &= -4.323 \\
\beta_3 + \gamma_3 - 180 &= 101.500 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 55.771 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -64.417 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -105.830
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= 55.305 \\
\alpha_4 - \gamma_4 &= -8.130 \\
\alpha_4 - \delta_4 &= -26.565 \\
\beta_4 - \gamma_4 &= -63.435 \\
\beta_4 - \delta_4 &= -81.870 \\
\gamma_4 - \delta_4 &= -18.435 \\
\alpha_4 + \beta_4 - 180 &= -108.430 \\
\gamma_4 + \delta_4 - 180 &= -18.435 \\
\alpha_4 + \gamma_4 - 180 &= -45.000 \\
\beta_4 + \delta_4 - 180 &= -81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565 \\
\beta_4 + \gamma_4 - 180 &= -100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -90.000 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 36.870
\end{aligned}$$

$$\alpha_4 + \delta_4 - \beta_4 - \gamma_4 = 73.740$$

Switch combination: Lower

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned} \alpha_1 - \beta_1 &= -55.305 \\ \alpha_1 - \gamma_1 &= 8.130 \\ \alpha_1 - \delta_1 &= 26.565 \\ \beta_1 - \gamma_1 &= 63.435 \\ \beta_1 - \delta_1 &= 81.870 \\ \gamma_1 - \delta_1 &= 18.435 \\ \alpha_1 + \beta_1 - 180 &= 108.430 \\ \gamma_1 + \delta_1 - 180 &= 18.435 \\ \alpha_1 + \gamma_1 - 180 &= 45.000 \\ \beta_1 + \delta_1 - 180 &= 81.870 \\ \alpha_1 + \delta_1 - 180 &= 26.565 \\ \beta_1 + \gamma_1 - 180 &= 100.300 \\ \alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 90.000 \\ \alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -36.870 \\ \alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -73.740 \end{aligned}$$

Vertex 2

$$\begin{aligned} \alpha_2 - \beta_2 &= -76.476 \\ \alpha_2 - \gamma_2 &= -16.382 \\ \alpha_2 - \delta_2 &= 4.323 \\ \beta_2 - \gamma_2 &= 60.094 \\ \beta_2 - \delta_2 &= 80.799 \\ \gamma_2 - \delta_2 &= 20.705 \\ \alpha_2 + \beta_2 - 180 &= 85.122 \\ \gamma_2 + \delta_2 - 180 &= 20.705 \\ \alpha_2 + \gamma_2 - 180 &= 25.028 \\ \beta_2 + \delta_2 - 180 &= 80.799 \\ \alpha_2 + \delta_2 - 180 &= 4.323 \\ \beta_2 + \gamma_2 - 180 &= 101.500 \\ \alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 64.417 \\ \alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -55.771 \\ \alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -97.181 \end{aligned}$$

Vertex 3

$$\begin{aligned} \alpha_3 - \beta_3 &= 76.476 \\ \alpha_3 - \gamma_3 &= 16.382 \\ \alpha_3 - \delta_3 &= -4.323 \\ \beta_3 - \gamma_3 &= -60.094 \\ \beta_3 - \delta_3 &= -80.799 \\ \gamma_3 - \delta_3 &= -20.705 \\ \alpha_3 + \beta_3 - 180 &= -85.122 \\ \gamma_3 + \delta_3 - 180 &= -20.705 \\ \alpha_3 + \gamma_3 - 180 &= -25.028 \\ \beta_3 + \delta_3 - 180 &= -80.799 \end{aligned}$$

$$\begin{aligned}
\beta 3 + \delta 3 - 180 &= -80.799 \\
\alpha 3 + \delta 3 - 180 &= -4.323 \\
\beta 3 + \gamma 3 - 180 &= -101.500 \\
\alpha 3 + \beta 3 - \gamma 3 - \delta 3 &= -64.417 \\
\alpha 3 + \gamma 3 - \beta 3 - \delta 3 &= 55.771 \\
\alpha 3 + \delta 3 - \beta 3 - \gamma 3 &= 97.181
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha 4 - \beta 4 &= 55.305 \\
\alpha 4 - \gamma 4 &= -8.130 \\
\alpha 4 - \delta 4 &= -26.565 \\
\beta 4 - \gamma 4 &= -63.435 \\
\beta 4 - \delta 4 &= -81.870 \\
\gamma 4 - \delta 4 &= -18.435 \\
\alpha 4 + \beta 4 - 180 &= -108.430 \\
\gamma 4 + \delta 4 - 180 &= -18.435 \\
\alpha 4 + \gamma 4 - 180 &= -45.000 \\
\beta 4 + \delta 4 - 180 &= -81.870 \\
\alpha 4 + \delta 4 - 180 &= -26.565 \\
\beta 4 + \gamma 4 - 180 &= -100.300 \\
\alpha 4 + \beta 4 - \gamma 4 - \delta 4 &= -90.000 \\
\alpha 4 + \gamma 4 - \beta 4 - \delta 4 &= 36.870 \\
\alpha 4 + \delta 4 - \beta 4 - \gamma 4 &= 73.740
\end{aligned}$$

Switch combination: Upper*Switched anglesDeg:*

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi}
\end{array} \right) \begin{array}{l} 90 \\ 90 \\ 90 \\ 90 \end{array}$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\begin{aligned}
\alpha 1 - \beta 1 &= 55.305 \\
\alpha 1 - \gamma 1 &= -45.000 \\
\alpha 1 - \delta 1 &= -26.565 \\
\beta 1 - \gamma 1 &= -100.300 \\
\beta 1 - \delta 1 &= -81.870 \\
\gamma 1 - \delta 1 &= 18.435 \\
\alpha 1 + \beta 1 - 180 &= -108.430 \\
\gamma 1 + \delta 1 - 180 &= 18.435 \\
\alpha 1 + \gamma 1 - 180 &= -8.130 \\
\beta 1 + \delta 1 - 180 &= -81.870 \\
\alpha 1 + \delta 1 - 180 &= -26.565 \\
\beta 1 + \gamma 1 - 180 &= -63.435 \\
\alpha 1 + \beta 1 - \gamma 1 - \delta 1 &= -126.870 \\
\alpha 1 + \gamma 1 - \beta 1 - \delta 1 &= 73.740 \\
\alpha 1 + \delta 1 - \beta 1 - \gamma 1 &= 36.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha 2 - \beta 2 &= 76.476 \\
\alpha 2 - \gamma 2 &= -25.028 \\
\alpha 2 - \delta 2 &= -4.323 \\
\beta 2 - \gamma 2 &= -101.500 \\
\beta 2 - \delta 2 &= -80.799
\end{aligned}$$

$$\begin{aligned}
\gamma_2 - \delta_2 &= 20.705 \\
\alpha_2 + \beta_2 - 180 &= -85.122 \\
\gamma_2 + \delta_2 - 180 &= 20.705 \\
\alpha_2 + \gamma_2 - 180 &= 16.382 \\
\beta_2 + \delta_2 - 180 &= -80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= -60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -105.830 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 97.181 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 55.771
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= -76.476 \\
\alpha_3 - \gamma_3 &= 25.028 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= 101.500 \\
\beta_3 - \delta_3 &= 80.799 \\
\gamma_3 - \delta_3 &= -20.705 \\
\alpha_3 + \beta_3 - 180 &= 85.122 \\
\gamma_3 + \delta_3 - 180 &= -20.705 \\
\alpha_3 + \gamma_3 - 180 &= -16.382 \\
\beta_3 + \delta_3 - 180 &= 80.799 \\
\alpha_3 + \delta_3 - 180 &= 4.323 \\
\beta_3 + \gamma_3 - 180 &= 60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 105.830 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -97.181 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -55.771
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -55.305 \\
\alpha_4 - \gamma_4 &= 45.000 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= 100.300 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= -18.435 \\
\alpha_4 + \beta_4 - 180 &= 108.430 \\
\gamma_4 + \delta_4 - 180 &= -18.435 \\
\alpha_4 + \gamma_4 - 180 &= 8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= 63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 126.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -73.740 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -36.870
\end{aligned}$$

Switch combination: Right + Left*Switched anglesDeg:*

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\alpha_1 - \beta_1 = -108.430$$

$$\begin{aligned}
\alpha_1 - \beta_1 &= -108.430 \\
\alpha_1 - \gamma_1 &= -8.130 \\
\alpha_1 - \delta_1 &= -26.565 \\
\beta_1 - \gamma_1 &= 100.300 \\
\beta_1 - \delta_1 &= 81.870 \\
\gamma_1 - \delta_1 &= -18.435 \\
\alpha_1 + \beta_1 - 180 &= 55.305 \\
\gamma_1 + \delta_1 - 180 &= -18.435 \\
\alpha_1 + \gamma_1 - 180 &= -45.000 \\
\beta_1 + \delta_1 - 180 &= 81.870 \\
\alpha_1 + \delta_1 - 180 &= -26.565 \\
\beta_1 + \gamma_1 - 180 &= 63.435 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 73.740 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -126.870 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -90.000
\end{aligned}$$
Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -85.122 \\
\alpha_2 - \gamma_2 &= 16.382 \\
\alpha_2 - \delta_2 &= -4.323 \\
\beta_2 - \gamma_2 &= 101.500 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= -20.705 \\
\alpha_2 + \beta_2 - 180 &= 76.476 \\
\gamma_2 + \delta_2 - 180 &= -20.705 \\
\alpha_2 + \gamma_2 - 180 &= -25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= 60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 97.181 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -105.830 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -64.417
\end{aligned}$$
Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= -85.122 \\
\alpha_3 - \gamma_3 &= -25.028 \\
\alpha_3 - \delta_3 &= -4.323 \\
\beta_3 - \gamma_3 &= 60.094 \\
\beta_3 - \delta_3 &= 80.799 \\
\gamma_3 - \delta_3 &= 20.705 \\
\alpha_3 + \beta_3 - 180 &= 76.476 \\
\gamma_3 + \delta_3 - 180 &= 20.705 \\
\alpha_3 + \gamma_3 - 180 &= 16.382 \\
\beta_3 + \delta_3 - 180 &= 80.799 \\
\alpha_3 + \delta_3 - 180 &= -4.323 \\
\beta_3 + \gamma_3 - 180 &= 101.500 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 55.771 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -64.417 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -105.830
\end{aligned}$$
Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -108.430 \\
\alpha_4 - \gamma_4 &= -45.000 \\
\alpha_4 - \delta_4 &= -26.565 \\
\beta_4 - \gamma_4 &= 63.435 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= 55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= -8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565
\end{aligned}$$

$$\begin{aligned}
\beta_4 + \gamma_4 - 180 &= 100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 36.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -90.000 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -126.870
\end{aligned}$$

Switch combination: Right + Lower

Switched anglesDeg:

$$\left(\begin{array}{ccc}
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for i = 1..4:

Vertex 1

$$\begin{aligned}
\alpha_1 - \beta_1 &= 108.430 \\
\alpha_1 - \gamma_1 &= 45.000 \\
\alpha_1 - \delta_1 &= 26.565 \\
\beta_1 - \gamma_1 &= -63.435 \\
\beta_1 - \delta_1 &= -81.870 \\
\gamma_1 - \delta_1 &= -18.435 \\
\alpha_1 + \beta_1 - 180 &= -55.305 \\
\gamma_1 + \delta_1 - 180 &= -18.435 \\
\alpha_1 + \gamma_1 - 180 &= 8.130 \\
\beta_1 + \delta_1 - 180 &= -81.870 \\
\alpha_1 + \delta_1 - 180 &= 26.565 \\
\beta_1 + \gamma_1 - 180 &= -100.300 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= -36.870 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= 90.000 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= 126.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -76.476 \\
\alpha_2 - \gamma_2 &= -16.382 \\
\alpha_2 - \delta_2 &= 4.323 \\
\beta_2 - \gamma_2 &= 60.094 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= 20.705 \\
\alpha_2 + \beta_2 - 180 &= 85.122 \\
\gamma_2 + \delta_2 - 180 &= 20.705 \\
\alpha_2 + \gamma_2 - 180 &= 25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - 180 &= 4.323 \\
\beta_2 + \gamma_2 - 180 &= 101.500 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 64.417 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -55.771 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -97.181
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= 76.476 \\
\alpha_3 - \gamma_3 &= 16.382 \\
\alpha_3 - \delta_3 &= -4.323 \\
\beta_3 - \gamma_3 &= -60.094 \\
\beta_3 - \delta_3 &= -80.799 \\
\gamma_3 - \delta_3 &= -20.705 \\
\alpha_3 + \beta_3 - 180 &= -85.122
\end{aligned}$$

$$\begin{aligned}
\gamma_3 + \delta_3 - 180 &= -20.705 \\
\alpha_3 + \gamma_3 - 180 &= -25.028 \\
\beta_3 + \delta_3 - 180 &= -80.799 \\
\alpha_3 + \delta_3 - 180 &= -4.323 \\
\beta_3 + \gamma_3 - 180 &= -101.500 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -64.417 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 55.771 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 97.181
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -108.430 \\
\alpha_4 - \gamma_4 &= -45.000 \\
\alpha_4 - \delta_4 &= -26.565 \\
\beta_4 - \gamma_4 &= 63.435 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= 55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= -8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565 \\
\beta_4 + \gamma_4 - 180 &= 100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 36.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -90.000 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -126.870
\end{aligned}$$

Switch combination: Right + Upper*Switched anglesDeg:*

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\begin{aligned}
\alpha_1 - \beta_1 &= -108.430 \\
\alpha_1 - \gamma_1 &= -8.130 \\
\alpha_1 - \delta_1 &= -26.565 \\
\beta_1 - \gamma_1 &= 100.300 \\
\beta_1 - \delta_1 &= 81.870 \\
\gamma_1 - \delta_1 &= -18.435 \\
\alpha_1 + \beta_1 - 180 &= 55.305 \\
\gamma_1 + \delta_1 - 180 &= -18.435 \\
\alpha_1 + \gamma_1 - 180 &= -45.000 \\
\beta_1 + \delta_1 - 180 &= 81.870 \\
\alpha_1 + \delta_1 - 180 &= -26.565 \\
\beta_1 + \gamma_1 - 180 &= 63.435 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 73.740 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -126.870 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -90.000
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= 76.476 \\
\alpha_2 - \gamma_2 &= -25.028 \\
\alpha_2 - \delta_2 &= -45.000
\end{aligned}$$

$$\begin{aligned}
\alpha_2 - \delta_2 &= -4.323 \\
\beta_2 - \gamma_2 &= -101.500 \\
\beta_2 - \delta_2 &= -80.799 \\
\gamma_2 - \delta_2 &= 20.705 \\
\alpha_2 + \beta_2 - 180 &= -85.122 \\
\gamma_2 + \delta_2 - 180 &= 20.705 \\
\alpha_2 + \gamma_2 - 180 &= 16.382 \\
\beta_2 + \delta_2 - 180 &= -80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= -60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -105.830 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 97.181 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 55.771
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= -76.476 \\
\alpha_3 - \gamma_3 &= 25.028 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= 101.500 \\
\beta_3 - \delta_3 &= 80.799 \\
\gamma_3 - \delta_3 &= -20.705 \\
\alpha_3 + \beta_3 - 180 &= 85.122 \\
\gamma_3 + \delta_3 - 180 &= -20.705 \\
\alpha_3 + \gamma_3 - 180 &= -16.382 \\
\beta_3 + \delta_3 - 180 &= 80.799 \\
\alpha_3 + \delta_3 - 180 &= 4.323 \\
\beta_3 + \gamma_3 - 180 &= 60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 105.830 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -97.181 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -55.771
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= 108.430 \\
\alpha_4 - \gamma_4 &= 8.130 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= -100.300 \\
\beta_4 - \delta_4 &= -81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= -55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= 45.000 \\
\beta_4 + \delta_4 - 180 &= -81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= -63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -73.740 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 126.870 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= 90.000
\end{aligned}$$

Switch combination: Left + Lower*Switched anglesDeg:*

$$\left(\begin{array}{ccc}
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned}\alpha_1 - \beta_1 &= -55.305 \\ \alpha_1 - \gamma_1 &= 8.130 \\ \alpha_1 - \delta_1 &= 26.565 \\ \beta_1 - \gamma_1 &= 63.435 \\ \beta_1 - \delta_1 &= 81.870 \\ \gamma_1 - \delta_1 &= 18.435 \\ \alpha_1 + \beta_1 - 180 &= 108.430 \\ \gamma_1 + \delta_1 - 180 &= 18.435 \\ \alpha_1 + \gamma_1 - 180 &= 45.000 \\ \beta_1 + \delta_1 - 180 &= 81.870 \\ \alpha_1 + \delta_1 - 180 &= 26.565 \\ \beta_1 + \gamma_1 - 180 &= 100.300 \\ \alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 90.000 \\ \alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -36.870 \\ \alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -73.740\end{aligned}$$

Vertex 2

$$\begin{aligned}\alpha_2 - \beta_2 &= 85.122 \\ \alpha_2 - \gamma_2 &= 25.028 \\ \alpha_2 - \delta_2 &= 4.323 \\ \beta_2 - \gamma_2 &= -60.094 \\ \beta_2 - \delta_2 &= -80.799 \\ \gamma_2 - \delta_2 &= -20.705 \\ \alpha_2 + \beta_2 - 180 &= -76.476 \\ \gamma_2 + \delta_2 - 180 &= -20.705 \\ \alpha_2 + \gamma_2 - 180 &= -16.382 \\ \beta_2 + \delta_2 - 180 &= -80.799 \\ \alpha_2 + \delta_2 - 180 &= 4.323 \\ \beta_2 + \gamma_2 - 180 &= -101.500 \\ \alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -55.771 \\ \alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 64.417 \\ \alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 105.830\end{aligned}$$

Vertex 3

$$\begin{aligned}\alpha_3 - \beta_3 &= -85.122 \\ \alpha_3 - \gamma_3 &= -25.028 \\ \alpha_3 - \delta_3 &= -4.323 \\ \beta_3 - \gamma_3 &= 60.094 \\ \beta_3 - \delta_3 &= 80.799 \\ \gamma_3 - \delta_3 &= 20.705 \\ \alpha_3 + \beta_3 - 180 &= 76.476 \\ \gamma_3 + \delta_3 - 180 &= 20.705 \\ \alpha_3 + \gamma_3 - 180 &= 16.382 \\ \beta_3 + \delta_3 - 180 &= 80.799 \\ \alpha_3 + \delta_3 - 180 &= -4.323 \\ \beta_3 + \gamma_3 - 180 &= 101.500 \\ \alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 55.771 \\ \alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -64.417 \\ \alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -105.830\end{aligned}$$

Vertex 4

$$\begin{aligned}\alpha_4 - \beta_4 &= 55.305 \\ \alpha_4 - \gamma_4 &= -8.130 \\ \alpha_4 - \delta_4 &= -26.565 \\ \beta_4 - \gamma_4 &= -63.435 \\ \beta_4 - \delta_4 &= -81.870 \\ \gamma_4 - \delta_4 &= -18.435 \\ \alpha_4 + \beta_4 - 180 &= -108.430 \\ \gamma_4 + \delta_4 - 180 &= -18.435\end{aligned}$$

$$\begin{aligned}
\alpha_4 + \gamma_4 - 180 &= -45.000 \\
\beta_4 + \delta_4 - 180 &= -81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565 \\
\beta_4 + \gamma_4 - 180 &= -100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -90.000 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 36.870 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= 73.740
\end{aligned}$$

Switch combination: Left + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for i = 1..4:

Vertex 1

$$\begin{aligned}
\alpha_1 - \beta_1 &= 55.305 \\
\alpha_1 - \gamma_1 &= -45.000 \\
\alpha_1 - \delta_1 &= -26.565 \\
\beta_1 - \gamma_1 &= -100.300 \\
\beta_1 - \delta_1 &= -81.870 \\
\gamma_1 - \delta_1 &= 18.435 \\
\alpha_1 + \beta_1 - 180 &= -108.430 \\
\gamma_1 + \delta_1 - 180 &= 18.435 \\
\alpha_1 + \gamma_1 - 180 &= -8.130 \\
\beta_1 + \delta_1 - 180 &= -81.870 \\
\alpha_1 + \delta_1 - 180 &= -26.565 \\
\beta_1 + \gamma_1 - 180 &= -63.435 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= -126.870 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= 73.740 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= 36.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -85.122 \\
\alpha_2 - \gamma_2 &= 16.382 \\
\alpha_2 - \delta_2 &= -4.323 \\
\beta_2 - \gamma_2 &= 101.500 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= -20.705 \\
\alpha_2 + \beta_2 - 180 &= 76.476 \\
\gamma_2 + \delta_2 - 180 &= -20.705 \\
\alpha_2 + \gamma_2 - 180 &= -25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - 180 &= -4.323 \\
\beta_2 + \gamma_2 - 180 &= 60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 97.181 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -105.830 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -64.417
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= 85.122 \\
\alpha_3 - \gamma_3 &= -16.382 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= -101.500
\end{aligned}$$

$$\begin{aligned}
\beta 3 - \gamma 3 &= -101.300 \\
\beta 3 - \delta 3 &= -80.799 \\
\gamma 3 - \delta 3 &= 20.705 \\
\alpha 3 + \beta 3 - 180 &= -76.476 \\
\gamma 3 + \delta 3 - 180 &= 20.705 \\
\alpha 3 + \gamma 3 - 180 &= 25.028 \\
\beta 3 + \delta 3 - 180 &= -80.799 \\
\alpha 3 + \delta 3 - 180 &= 4.323 \\
\beta 3 + \gamma 3 - 180 &= -60.094 \\
\alpha 3 + \beta 3 - \gamma 3 - \delta 3 &= -97.181 \\
\alpha 3 + \gamma 3 - \beta 3 - \delta 3 &= 105.830 \\
\alpha 3 + \delta 3 - \beta 3 - \gamma 3 &= 64.417
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha 4 - \beta 4 &= -55.305 \\
\alpha 4 - \gamma 4 &= 45.000 \\
\alpha 4 - \delta 4 &= 26.565 \\
\beta 4 - \gamma 4 &= 100.300 \\
\beta 4 - \delta 4 &= 81.870 \\
\gamma 4 - \delta 4 &= -18.435 \\
\alpha 4 + \beta 4 - 180 &= 108.430 \\
\gamma 4 + \delta 4 - 180 &= -18.435 \\
\alpha 4 + \gamma 4 - 180 &= 8.130 \\
\beta 4 + \delta 4 - 180 &= 81.870 \\
\alpha 4 + \delta 4 - 180 &= 26.565 \\
\beta 4 + \gamma 4 - 180 &= 63.435 \\
\alpha 4 + \beta 4 - \gamma 4 - \delta 4 &= 126.870 \\
\alpha 4 + \gamma 4 - \beta 4 - \delta 4 &= -73.740 \\
\alpha 4 + \delta 4 - \beta 4 - \gamma 4 &= -36.870
\end{aligned}$$

Switch combination: Lower + Upper*Switched anglesDeg:*

$$\left(\begin{array}{ccc}
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} \quad 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} \quad 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} \quad 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} \quad 90
\end{array} \right)$$

*Angle relation checks for i = 1..4:***Vertex 1**

$$\begin{aligned}
\alpha 1 - \beta 1 &= -55.305 \\
\alpha 1 - \gamma 1 &= 8.130 \\
\alpha 1 - \delta 1 &= 26.565 \\
\beta 1 - \gamma 1 &= 63.435 \\
\beta 1 - \delta 1 &= 81.870 \\
\gamma 1 - \delta 1 &= 18.435 \\
\alpha 1 + \beta 1 - 180 &= 108.430 \\
\gamma 1 + \delta 1 - 180 &= 18.435 \\
\alpha 1 + \gamma 1 - 180 &= 45.000 \\
\beta 1 + \delta 1 - 180 &= 81.870 \\
\alpha 1 + \delta 1 - 180 &= 26.565 \\
\beta 1 + \gamma 1 - 180 &= 100.300 \\
\alpha 1 + \beta 1 - \gamma 1 - \delta 1 &= 90.000 \\
\alpha 1 + \gamma 1 - \beta 1 - \delta 1 &= -36.870 \\
\alpha 1 + \delta 1 - \beta 1 - \gamma 1 &= -73.740
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -76.476 \\
\alpha_2 - \gamma_2 &= -16.382 \\
\alpha_2 - \delta_2 &= 4.323 \\
\beta_2 - \gamma_2 &= 60.094 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= 20.705 \\
\alpha_2 + \beta_2 - 180 &= 85.122 \\
\gamma_2 + \delta_2 - 180 &= 20.705 \\
\alpha_2 + \gamma_2 - 180 &= 25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - 180 &= 4.323 \\
\beta_2 + \gamma_2 - 180 &= 101.500 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 64.417 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -55.771 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -97.181
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= -76.476 \\
\alpha_3 - \gamma_3 &= 25.028 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= 101.500 \\
\beta_3 - \delta_3 &= 80.799 \\
\gamma_3 - \delta_3 &= -20.705 \\
\alpha_3 + \beta_3 - 180 &= 85.122 \\
\gamma_3 + \delta_3 - 180 &= -20.705 \\
\alpha_3 + \gamma_3 - 180 &= -16.382 \\
\beta_3 + \delta_3 - 180 &= 80.799 \\
\alpha_3 + \delta_3 - 180 &= 4.323 \\
\beta_3 + \gamma_3 - 180 &= 60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 105.830 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -97.181 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -55.771
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -55.305 \\
\alpha_4 - \gamma_4 &= 45.000 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= 100.300 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= -18.435 \\
\alpha_4 + \beta_4 - 180 &= 108.430 \\
\gamma_4 + \delta_4 - 180 &= -18.435 \\
\alpha_4 + \gamma_4 - 180 &= 8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= 63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 126.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -73.740 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -36.870
\end{aligned}$$

Switch combination: Right + Left + Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{pmatrix}$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned} \alpha_1 - \beta_1 &= 108.430 \\ \alpha_1 - \gamma_1 &= 45.000 \\ \alpha_1 - \delta_1 &= 26.565 \\ \beta_1 - \gamma_1 &= -63.435 \\ \beta_1 - \delta_1 &= -81.870 \\ \gamma_1 - \delta_1 &= -18.435 \\ \alpha_1 + \beta_1 - 180 &= -55.305 \\ \gamma_1 + \delta_1 - 180 &= -18.435 \\ \alpha_1 + \gamma_1 - 180 &= 8.130 \\ \beta_1 + \delta_1 - 180 &= -81.870 \\ \alpha_1 + \delta_1 - 180 &= 26.565 \\ \beta_1 + \gamma_1 - 180 &= -100.300 \\ \alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= -36.870 \\ \alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= 90.000 \\ \alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= 126.870 \end{aligned}$$

Vertex 2

$$\begin{aligned} \alpha_2 - \beta_2 &= 85.122 \\ \alpha_2 - \gamma_2 &= 25.028 \\ \alpha_2 - \delta_2 &= 4.323 \\ \beta_2 - \gamma_2 &= -60.094 \\ \beta_2 - \delta_2 &= -80.799 \\ \gamma_2 - \delta_2 &= -20.705 \\ \alpha_2 + \beta_2 - 180 &= -76.476 \\ \gamma_2 + \delta_2 - 180 &= -20.705 \\ \alpha_2 + \gamma_2 - 180 &= -16.382 \\ \beta_2 + \delta_2 - 180 &= -80.799 \\ \alpha_2 + \delta_2 - 180 &= 4.323 \\ \beta_2 + \gamma_2 - 180 &= -101.500 \\ \alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -55.771 \\ \alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 64.417 \\ \alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 105.830 \end{aligned}$$

Vertex 3

$$\begin{aligned} \alpha_3 - \beta_3 &= -85.122 \\ \alpha_3 - \gamma_3 &= -25.028 \\ \alpha_3 - \delta_3 &= -4.323 \\ \beta_3 - \gamma_3 &= 60.094 \\ \beta_3 - \delta_3 &= 80.799 \\ \gamma_3 - \delta_3 &= 20.705 \\ \alpha_3 + \beta_3 - 180 &= 76.476 \\ \gamma_3 + \delta_3 - 180 &= 20.705 \\ \alpha_3 + \gamma_3 - 180 &= 16.382 \\ \beta_3 + \delta_3 - 180 &= 80.799 \\ \alpha_3 + \delta_3 - 180 &= -4.323 \\ \beta_3 + \gamma_3 - 180 &= 101.500 \\ \alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= 55.771 \\ \alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= -64.417 \\ \alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= -105.830 \end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -108.430 \\
\alpha_4 - \gamma_4 &= -45.000 \\
\alpha_4 - \delta_4 &= -26.565 \\
\beta_4 - \gamma_4 &= 63.435 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= 55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= -8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= -26.565 \\
\beta_4 + \gamma_4 - 180 &= 100.300 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 36.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -90.000 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -126.870
\end{aligned}$$

Switch combination: Right + Left + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned}
\alpha_1 - \beta_1 &= -108.430 \\
\alpha_1 - \gamma_1 &= -8.130 \\
\alpha_1 - \delta_1 &= -26.565 \\
\beta_1 - \gamma_1 &= 100.300 \\
\beta_1 - \delta_1 &= 81.870 \\
\gamma_1 - \delta_1 &= -18.435 \\
\alpha_1 + \beta_1 - 180 &= 55.305 \\
\gamma_1 + \delta_1 - 180 &= -18.435 \\
\alpha_1 + \gamma_1 - 180 &= -45.000 \\
\beta_1 + \delta_1 - 180 &= 81.870 \\
\alpha_1 + \delta_1 - 180 &= -26.565 \\
\beta_1 + \gamma_1 - 180 &= 63.435 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 73.740 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -126.870 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -90.000
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= -85.122 \\
\alpha_2 - \gamma_2 &= 16.382 \\
\alpha_2 - \delta_2 &= -4.323 \\
\beta_2 - \gamma_2 &= 101.500 \\
\beta_2 - \delta_2 &= 80.799 \\
\gamma_2 - \delta_2 &= -20.705 \\
\alpha_2 + \beta_2 - 180 &= 76.476 \\
\gamma_2 + \delta_2 - 180 &= -20.705 \\
\alpha_2 + \gamma_2 - 180 &= -25.028 \\
\beta_2 + \delta_2 - 180 &= 80.799 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -4.323
\end{aligned}$$

$$\begin{aligned}
\alpha_2 + \gamma_2 - 180 &= -11.929 \\
\beta_2 + \gamma_2 - 180 &= 60.094 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= 97.181 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= -105.830 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= -64.417
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= 85.122 \\
\alpha_3 - \gamma_3 &= -16.382 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= -101.500 \\
\beta_3 - \delta_3 &= -80.799 \\
\gamma_3 - \delta_3 &= 20.705 \\
\alpha_3 + \beta_3 - 180 &= -76.476 \\
\gamma_3 + \delta_3 - 180 &= 20.705 \\
\alpha_3 + \gamma_3 - 180 &= 25.028 \\
\beta_3 + \delta_3 - 180 &= -80.799 \\
\alpha_3 + \delta_3 - 180 &= 4.323 \\
\beta_3 + \gamma_3 - 180 &= -60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -97.181 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 105.830 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 64.417
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= 108.430 \\
\alpha_4 - \gamma_4 &= 8.130 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= -100.300 \\
\beta_4 - \delta_4 &= -81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= -55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= 45.000 \\
\beta_4 + \delta_4 - 180 &= -81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= -63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -73.740 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 126.870 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= 90.000
\end{aligned}$$

Switch combination: Right + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc}
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for i = 1..4:

Vertex 1

$$\begin{aligned}
\alpha_1 - \beta_1 &= 108.430 \\
\alpha_1 - \gamma_1 &= 45.000 \\
\alpha_1 - \delta_1 &= 26.565 \\
\beta_1 - \gamma_1 &= -63.435 \\
\beta_1 - \delta_1 &= -81.870 \\
\gamma_1 - \delta_1 &= -18.435
\end{aligned}$$

$$\begin{aligned}
\alpha 1 + \beta 1 - 180 &= -55.305 \\
\gamma 1 + \delta 1 - 180 &= -18.435 \\
\alpha 1 + \gamma 1 - 180 &= 8.130 \\
\beta 1 + \delta 1 - 180 &= -81.870 \\
\alpha 1 + \delta 1 - 180 &= 26.565 \\
\beta 1 + \gamma 1 - 180 &= -100.300 \\
\alpha 1 + \beta 1 - \gamma 1 - \delta 1 &= -36.870 \\
\alpha 1 + \gamma 1 - \beta 1 - \delta 1 &= 90.000 \\
\alpha 1 + \delta 1 - \beta 1 - \gamma 1 &= 126.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha 2 - \beta 2 &= -76.476 \\
\alpha 2 - \gamma 2 &= -16.382 \\
\alpha 2 - \delta 2 &= 4.323 \\
\beta 2 - \gamma 2 &= 60.094 \\
\beta 2 - \delta 2 &= 80.799 \\
\gamma 2 - \delta 2 &= 20.705 \\
\alpha 2 + \beta 2 - 180 &= 85.122 \\
\gamma 2 + \delta 2 - 180 &= 20.705 \\
\alpha 2 + \gamma 2 - 180 &= 25.028 \\
\beta 2 + \delta 2 - 180 &= 80.799 \\
\alpha 2 + \delta 2 - 180 &= 4.323 \\
\beta 2 + \gamma 2 - 180 &= 101.500 \\
\alpha 2 + \beta 2 - \gamma 2 - \delta 2 &= 64.417 \\
\alpha 2 + \gamma 2 - \beta 2 - \delta 2 &= -55.771 \\
\alpha 2 + \delta 2 - \beta 2 - \gamma 2 &= -97.181
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha 3 - \beta 3 &= -76.476 \\
\alpha 3 - \gamma 3 &= 25.028 \\
\alpha 3 - \delta 3 &= 4.323 \\
\beta 3 - \gamma 3 &= 101.500 \\
\beta 3 - \delta 3 &= 80.799 \\
\gamma 3 - \delta 3 &= -20.705 \\
\alpha 3 + \beta 3 - 180 &= 85.122 \\
\gamma 3 + \delta 3 - 180 &= -20.705 \\
\alpha 3 + \gamma 3 - 180 &= -16.382 \\
\beta 3 + \delta 3 - 180 &= 80.799 \\
\alpha 3 + \delta 3 - 180 &= 4.323 \\
\beta 3 + \gamma 3 - 180 &= 60.094 \\
\alpha 3 + \beta 3 - \gamma 3 - \delta 3 &= 105.830 \\
\alpha 3 + \gamma 3 - \beta 3 - \delta 3 &= -97.181 \\
\alpha 3 + \delta 3 - \beta 3 - \gamma 3 &= -55.771
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha 4 - \beta 4 &= 108.430 \\
\alpha 4 - \gamma 4 &= 8.130 \\
\alpha 4 - \delta 4 &= 26.565 \\
\beta 4 - \gamma 4 &= -100.300 \\
\beta 4 - \delta 4 &= -81.870 \\
\gamma 4 - \delta 4 &= 18.435 \\
\alpha 4 + \beta 4 - 180 &= -55.305 \\
\gamma 4 + \delta 4 - 180 &= 18.435 \\
\alpha 4 + \gamma 4 - 180 &= 45.000 \\
\beta 4 + \delta 4 - 180 &= -81.870 \\
\alpha 4 + \delta 4 - 180 &= 26.565 \\
\beta 4 + \gamma 4 - 180 &= -63.435 \\
\alpha 4 + \beta 4 - \gamma 4 - \delta 4 &= -73.740 \\
\alpha 4 + \gamma 4 - \beta 4 - \delta 4 &= 126.870 \\
\alpha 4 + \delta 4 - \beta 4 - \gamma 4 &= 90.000
\end{aligned}$$

Switch combination: Left + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned} \alpha_1 - \beta_1 &= -55.305 \\ \alpha_1 - \gamma_1 &= 8.130 \\ \alpha_1 - \delta_1 &= 26.565 \\ \beta_1 - \gamma_1 &= 63.435 \\ \beta_1 - \delta_1 &= 81.870 \\ \gamma_1 - \delta_1 &= 18.435 \\ \alpha_1 + \beta_1 - 180 &= 108.430 \\ \gamma_1 + \delta_1 - 180 &= 18.435 \\ \alpha_1 + \gamma_1 - 180 &= 45.000 \\ \beta_1 + \delta_1 - 180 &= 81.870 \\ \alpha_1 + \delta_1 - 180 &= 26.565 \\ \beta_1 + \gamma_1 - 180 &= 100.300 \\ \alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= 90.000 \\ \alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= -36.870 \\ \alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= -73.740 \end{aligned}$$

Vertex 2

$$\begin{aligned} \alpha_2 - \beta_2 &= 85.122 \\ \alpha_2 - \gamma_2 &= 25.028 \\ \alpha_2 - \delta_2 &= 4.323 \\ \beta_2 - \gamma_2 &= -60.094 \\ \beta_2 - \delta_2 &= -80.799 \\ \gamma_2 - \delta_2 &= -20.705 \\ \alpha_2 + \beta_2 - 180 &= -76.476 \\ \gamma_2 + \delta_2 - 180 &= -20.705 \\ \alpha_2 + \gamma_2 - 180 &= -16.382 \\ \beta_2 + \delta_2 - 180 &= -80.799 \\ \alpha_2 + \delta_2 - 180 &= 4.323 \\ \beta_2 + \gamma_2 - 180 &= -101.500 \\ \alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -55.771 \\ \alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 64.417 \\ \alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 105.830 \end{aligned}$$

Vertex 3

$$\begin{aligned} \alpha_3 - \beta_3 &= 85.122 \\ \alpha_3 - \gamma_3 &= -16.382 \\ \alpha_3 - \delta_3 &= 4.323 \\ \beta_3 - \gamma_3 &= -101.500 \\ \beta_3 - \delta_3 &= -80.799 \\ \gamma_3 - \delta_3 &= 20.705 \\ \alpha_3 + \beta_3 - 180 &= -76.476 \\ \gamma_3 + \delta_3 - 180 &= 20.705 \\ \alpha_3 + \gamma_3 - 180 &= 25.028 \\ \beta_3 + \delta_3 - 180 &= -80.799 \\ \alpha_3 + \delta_3 - 180 &= 4.323 \end{aligned}$$

$$\begin{aligned}
\beta_3 + \gamma_3 - 180 &= -60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -97.181 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 105.830 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 64.417
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= -55.305 \\
\alpha_4 - \gamma_4 &= 45.000 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= 100.300 \\
\beta_4 - \delta_4 &= 81.870 \\
\gamma_4 - \delta_4 &= -18.435 \\
\alpha_4 + \beta_4 - 180 &= 108.430 \\
\gamma_4 + \delta_4 - 180 &= -18.435 \\
\alpha_4 + \gamma_4 - 180 &= 8.130 \\
\beta_4 + \delta_4 - 180 &= 81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= 63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= 126.870 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= -73.740 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= -36.870
\end{aligned}$$

Switch combination: Right + Left + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{cccc}
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\
180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90
\end{array} \right)$$

Angle relation checks for $i = 1..4$:

Vertex 1

$$\begin{aligned}
\alpha_1 - \beta_1 &= 108.430 \\
\alpha_1 - \gamma_1 &= 45.000 \\
\alpha_1 - \delta_1 &= 26.565 \\
\beta_1 - \gamma_1 &= -63.435 \\
\beta_1 - \delta_1 &= -81.870 \\
\gamma_1 - \delta_1 &= -18.435 \\
\alpha_1 + \beta_1 - 180 &= -55.305 \\
\gamma_1 + \delta_1 - 180 &= -18.435 \\
\alpha_1 + \gamma_1 - 180 &= 8.130 \\
\beta_1 + \delta_1 - 180 &= -81.870 \\
\alpha_1 + \delta_1 - 180 &= 26.565 \\
\beta_1 + \gamma_1 - 180 &= -100.300 \\
\alpha_1 + \beta_1 - \gamma_1 - \delta_1 &= -36.870 \\
\alpha_1 + \gamma_1 - \beta_1 - \delta_1 &= 90.000 \\
\alpha_1 + \delta_1 - \beta_1 - \gamma_1 &= 126.870
\end{aligned}$$

Vertex 2

$$\begin{aligned}
\alpha_2 - \beta_2 &= 85.122 \\
\alpha_2 - \gamma_2 &= 25.028 \\
\alpha_2 - \delta_2 &= 4.323 \\
\beta_2 - \gamma_2 &= -60.094 \\
\beta_2 - \delta_2 &= -80.799 \\
\gamma_2 - \delta_2 &= -20.705
\end{aligned}$$

$$\begin{aligned}
\alpha_2 + \beta_2 - 180 &= -76.476 \\
\gamma_2 + \delta_2 - 180 &= -20.705 \\
\alpha_2 + \gamma_2 - 180 &= -16.382 \\
\beta_2 + \delta_2 - 180 &= -80.799 \\
\alpha_2 + \delta_2 - 180 &= 4.323 \\
\beta_2 + \gamma_2 - 180 &= -101.500 \\
\alpha_2 + \beta_2 - \gamma_2 - \delta_2 &= -55.771 \\
\alpha_2 + \gamma_2 - \beta_2 - \delta_2 &= 64.417 \\
\alpha_2 + \delta_2 - \beta_2 - \gamma_2 &= 105.830
\end{aligned}$$

Vertex 3

$$\begin{aligned}
\alpha_3 - \beta_3 &= 85.122 \\
\alpha_3 - \gamma_3 &= -16.382 \\
\alpha_3 - \delta_3 &= 4.323 \\
\beta_3 - \gamma_3 &= -101.500 \\
\beta_3 - \delta_3 &= -80.799 \\
\gamma_3 - \delta_3 &= 20.705 \\
\alpha_3 + \beta_3 - 180 &= -76.476 \\
\gamma_3 + \delta_3 - 180 &= 20.705 \\
\alpha_3 + \gamma_3 - 180 &= 25.028 \\
\beta_3 + \delta_3 - 180 &= -80.799 \\
\alpha_3 + \delta_3 - 180 &= 4.323 \\
\beta_3 + \gamma_3 - 180 &= -60.094 \\
\alpha_3 + \beta_3 - \gamma_3 - \delta_3 &= -97.181 \\
\alpha_3 + \gamma_3 - \beta_3 - \delta_3 &= 105.830 \\
\alpha_3 + \delta_3 - \beta_3 - \gamma_3 &= 64.417
\end{aligned}$$

Vertex 4

$$\begin{aligned}
\alpha_4 - \beta_4 &= 108.430 \\
\alpha_4 - \gamma_4 &= 8.130 \\
\alpha_4 - \delta_4 &= 26.565 \\
\beta_4 - \gamma_4 &= -100.300 \\
\beta_4 - \delta_4 &= -81.870 \\
\gamma_4 - \delta_4 &= 18.435 \\
\alpha_4 + \beta_4 - 180 &= -55.305 \\
\gamma_4 + \delta_4 - 180 &= 18.435 \\
\alpha_4 + \gamma_4 - 180 &= 45.000 \\
\beta_4 + \delta_4 - 180 &= -81.870 \\
\alpha_4 + \delta_4 - 180 &= 26.565 \\
\beta_4 + \gamma_4 - 180 &= -63.435 \\
\alpha_4 + \beta_4 - \gamma_4 - \delta_4 &= -73.740 \\
\alpha_4 + \gamma_4 - \beta_4 - \delta_4 &= 126.870 \\
\alpha_4 + \delta_4 - \beta_4 - \gamma_4 &= 90.000
\end{aligned}$$

Out[]=

===== NOT CONJUGATE-MODULAR =====

$M_i < 1$ and $p_i \in \mathbb{R}$ for all $i = 1..4 \Rightarrow$ NOT

conjugate-modular. Boundary-strip switches preserve this.

Initial configuration (no switches applied):

$$\left(\begin{array}{ccc}
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} \\
\frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi}
\end{array} \right) \begin{array}{l} 90 \\ 90 \\ 90 \\ 90 \end{array}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Left

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{\frac{7}{22}}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Left

Switched anglesDeg:

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Lower

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Left + Lower

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Left + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Lower + Upper

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Left + Lower

Switched anglesDeg:

$$\begin{pmatrix} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Left + Upper

Switched anglesDeg:

$$\begin{pmatrix} \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \\ \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{10}}\right]}{\pi} & 90 \end{pmatrix}$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Left + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Switch combination: Right + Left + Lower + Upper

Switched anglesDeg:

$$\left(\begin{array}{ccc} 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[-\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{4\sqrt{11}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7\sqrt{22}}{4}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{2\sqrt{2}}\right]}{\pi} & 90 \\ 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{5}}\right]}{\pi} & \frac{180 \operatorname{ArcCos}\left[\frac{7}{5\sqrt{2}}\right]}{\pi} & 180 - \frac{180 \operatorname{ArcCos}\left[\frac{1}{\sqrt{18}}\right]}{\pi} & 90 \end{array} \right)$$

M_i values:

$$M_1 = \frac{1}{2}, M_2 = \frac{1}{2}, M_3 = \frac{1}{2}, M_4 = \frac{1}{2}$$

M_i < 1 for all i = 1, ..., 4

Out[*]=

===== NOT CHIMERA =====

Fails conic, orthodiagonal & isogonal tests for all
i=1, ..., 4 ⇒ NOT chimera. Boundary-strip switches
 preserve these failures as demonstrated in the NOT
 CONIC, NOT ORTHODIAGONAL, and NOT ISOGONAL sections.

