

Lecture 16: Splay Trees

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Acknowledgment: The content of this file is based on the slides of the textbook as well as the slides provided by Prof. Won-Ki Jeong and Prof. Tsz-Chiu Au.

Splay Trees

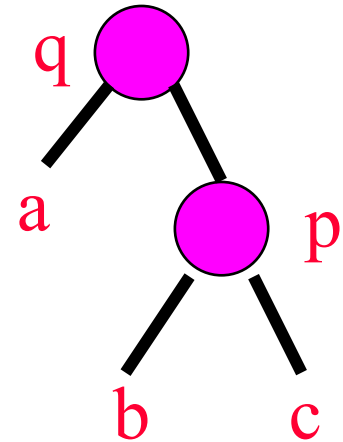
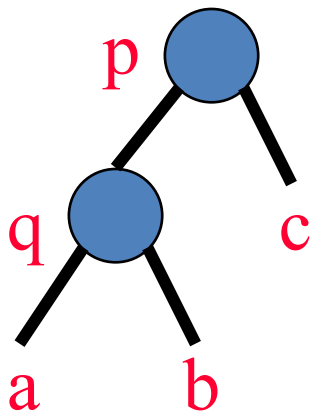
- Two heuristics to make search tree efficient
 - Make search depth shorter (AVL, RB)
 - Make frequently accessed data closer to root
- Splay trees use the latter idea
 - Rearrange tree whenever an element is accessed so that the recently used data is in the root node
- Worst-case $O(n)$ for operation, but $O(\log n)$ amortized

Splaying

- Designate splay node q
 - E.g., accessed node, inserted node ...
- Move q to the root using a series of splay steps
- In a splay step, q moves up the tree by 0, 1, or 2 levels
- Apply to all normal operations on a binary search tree

Splay Step

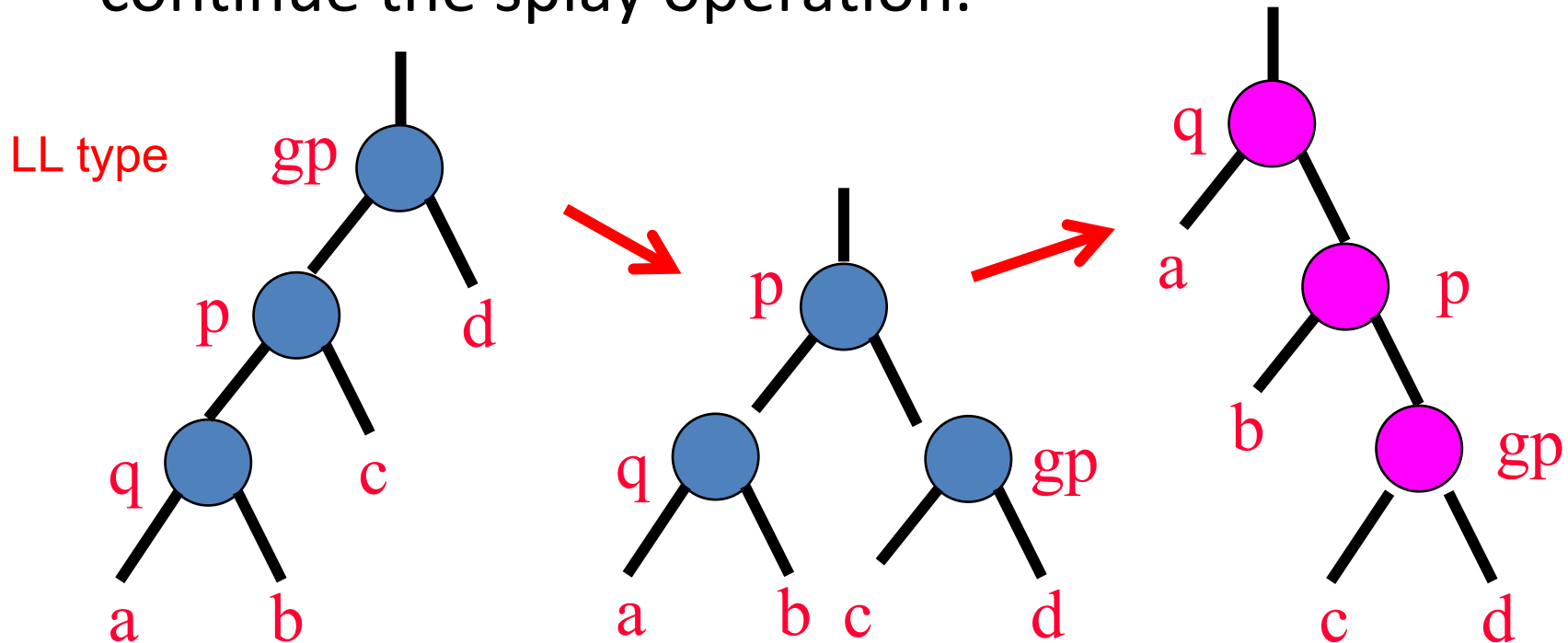
- If $q = \text{null}$ or q is the root, stop (splay is over)
- If q is at level 2, do a one-level move and terminate the splay operation



- Symmetric: right child of p

Splay Step

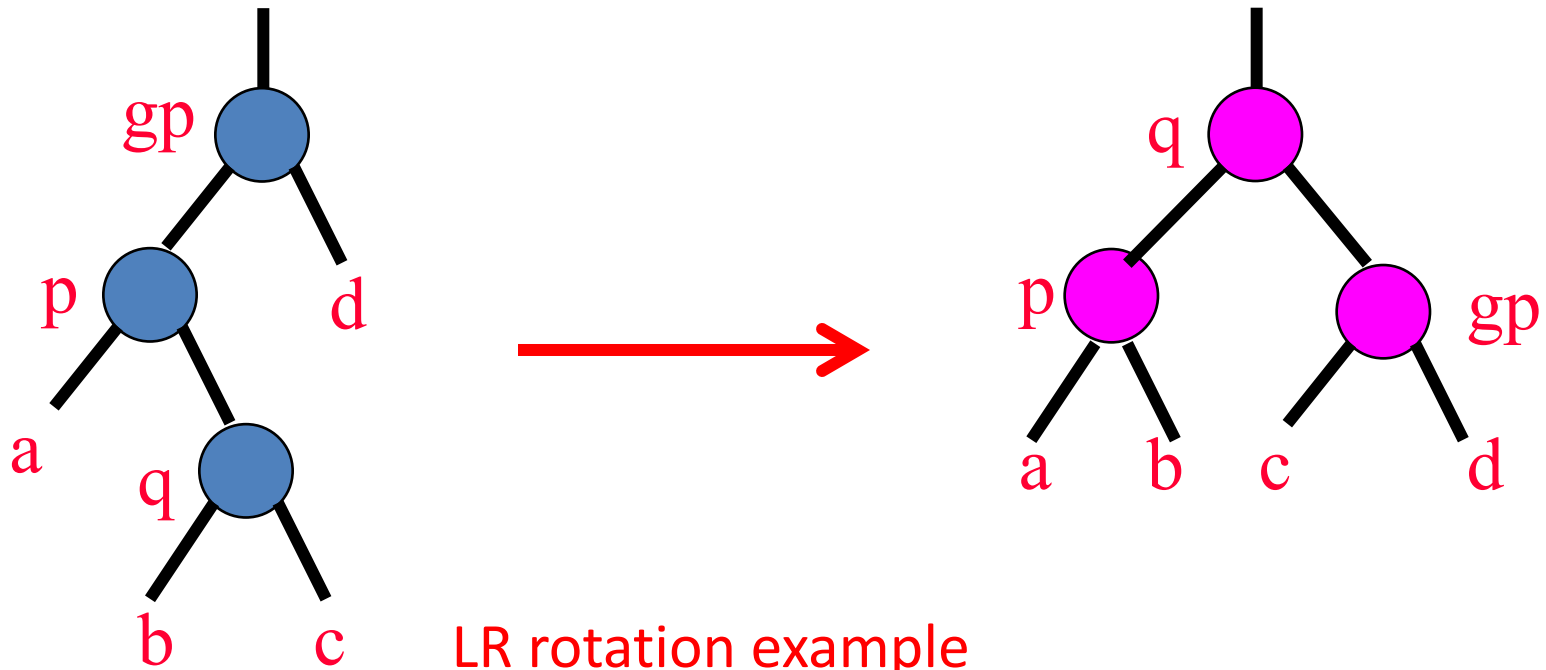
- If q is at a level > 2 , do a two-level move and continue the splay operation.



- Symmetric: right child of right child of gp (RR type)

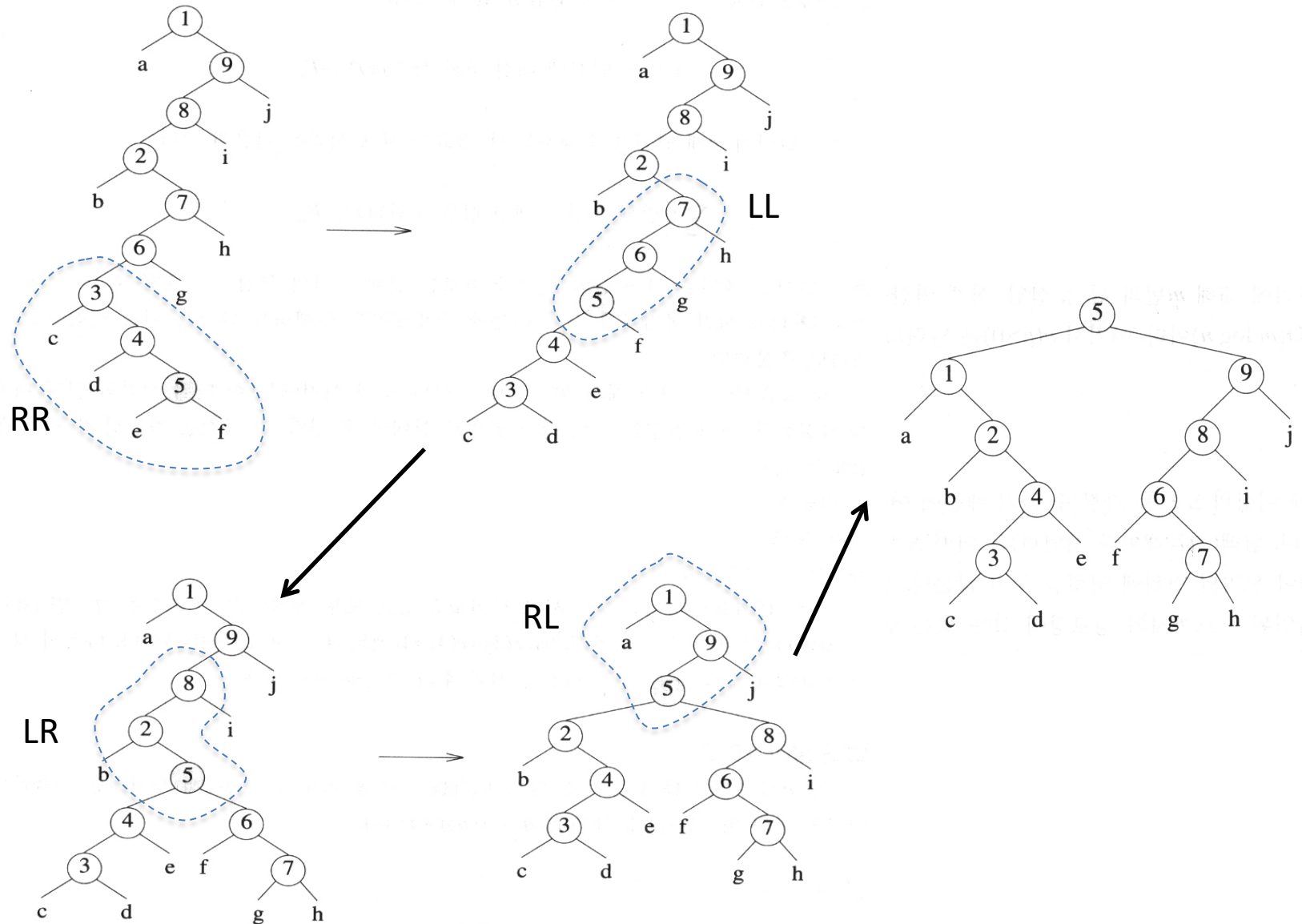
2-Level Move

- LR, RL rotations
 - Similar to AVL/Red-Black



LR rotation example

Splay node : 5

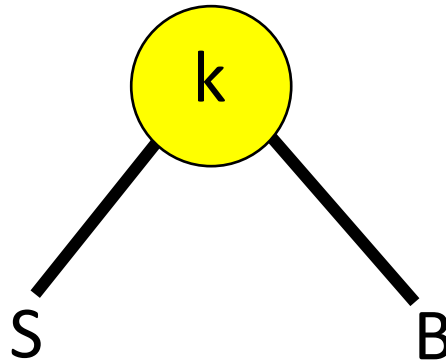


Designating Splay Node

- Search (k)
 - If there is key k , the node containing k is the splay node
- Insert (k)
 - The newly inserted node is the splay node
- Delete (k)
 - The parent of the physically deleted node is the splay node
 - If k is root, there is no splay node

Designating Splay Node

- Split (k)
 - Suppose that the key k is actually present in the tree
 - Perform a splay at the node that contains k
 - Then split the tree



Discussion

- Pros
 - Simple to implement when compared with AVL/Red-Black
 - Low memory footprint: no bookkeeping data
 - Optimized for temporal locality
 - $O(\log n)$ amortized, faster average performance
- Cons
 - Search gets more expensive since tree rotation can occur
 - No height constraint, the worst time can be $O(n)$
 - Parallel access is difficult: read-only operation will change the tree

Questions?