

Lecture 7: List and Iterators

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Outline

- ArrayList (Vector)
- List
- Iterator

The Array List (Vector) ADT

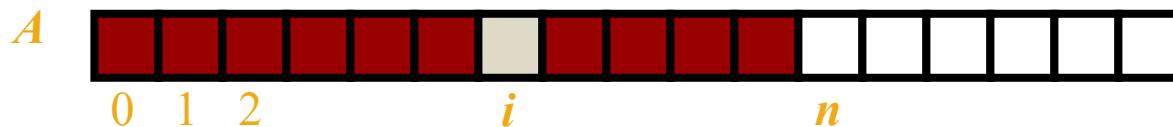
- The **Vector** or **Array List** ADT extends the notion of array by storing a sequence of objects
 - Main methods:
 - `at(integer i)`: returns the element at index *i* without removing it
 - `set(integer i, object o)`: replace the element at index *i* with *o*
 - `insert(integer i, object o)`: insert a new element *o* to have index *i*
 - `erase(integer i)`: removes element at index *i*
 - Additional methods:
 - `size()`
 - `empty()`
- An element can be accessed, inserted or removed by specifying its **index** (number of elements preceding it)
- An exception is thrown if an incorrect index is given (e.g., a negative index)

Applications of Array Lists

- Direct applications
 - Sorted collection of objects (elementary database)
- Indirect applications
 - Auxiliary data structure for algorithms
 - Component of other data structures

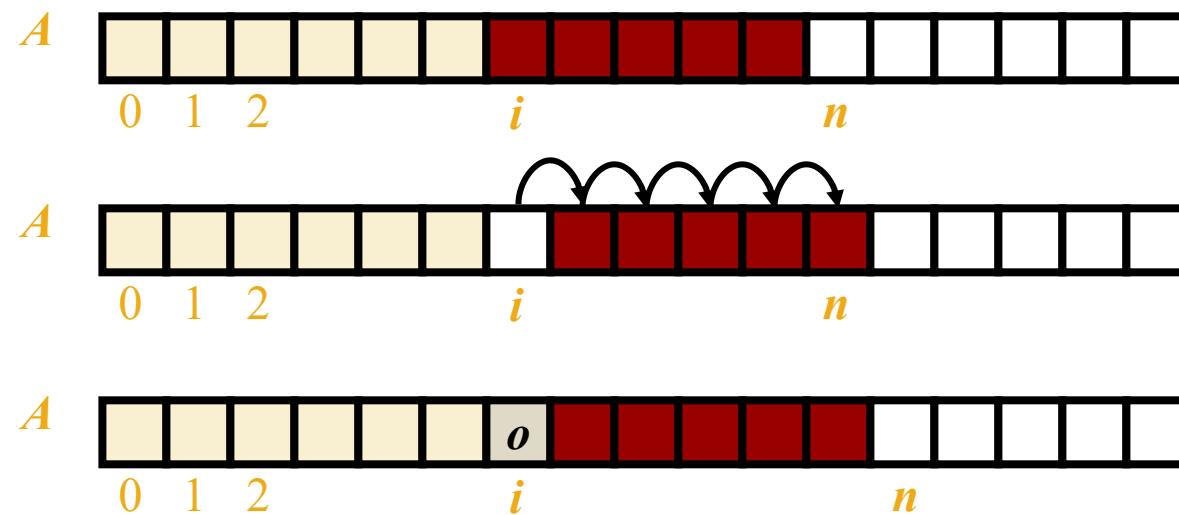
Array-based Implementation

- Use an array A of size N
- A variable n keeps track of the size of the array list (number of elements stored)
- Operation $\text{at}(i)$ is implemented in $O(1)$ time by returning $A[i]$
- Operation $\text{set}(i,o)$ is implemented in $O(1)$ time by performing $A[i] = o$



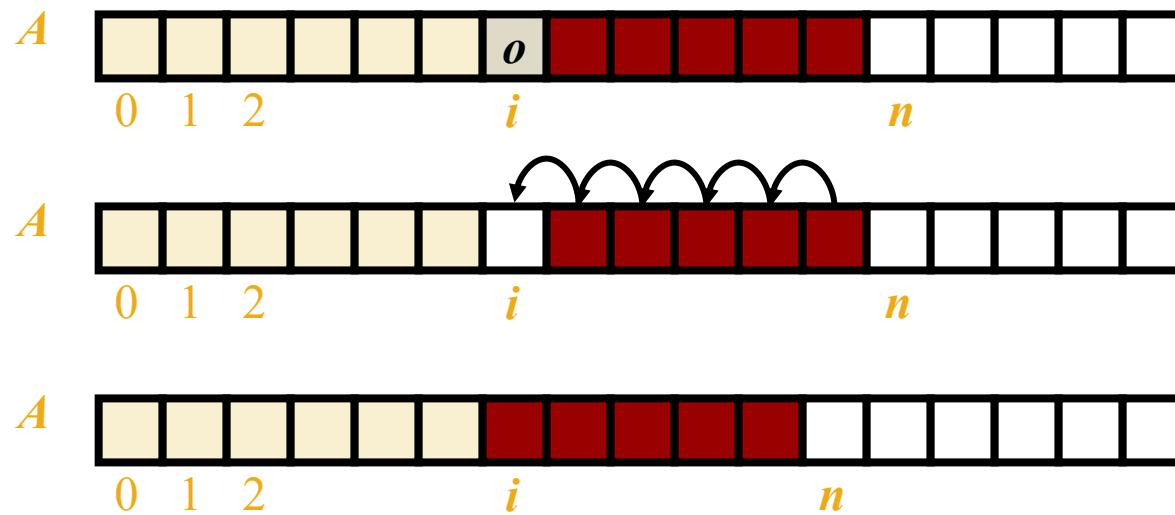
Insertion

- In operation $\text{insert}(i, o)$, we need to make room for the new element by shifting forward the $n - i$ elements $A[i], \dots, A[n - 1]$
- In the worst case ($i = 0$), this takes $O(n)$ time



Element Removal

- In operation $\text{erase}(i)$, we need to fill the hole left by the removed element by shifting backward the $n - i - 1$ elements $A[i + 1], \dots, A[n - 1]$
- In the worst case ($i = 0$), this takes $O(n)$ time



Performance

- In the array based implementation of an array list:
 - The space used by the data structure is $O(n)$
 - *size*, *empty*, *at* and *set* run in $O(1)$ time
 - *insert* and *erase* run in $O(n)$ time in worst case
- If we use the array in a circular fashion, operations *insert*(0, x) and *erase*(0, x) run in $O(1)$ time
- In an *insert* operation, when the array is full, instead of throwing an exception, we can replace the array with a larger one

Growable Array-based Array List

- In an `insert(o)` operation (without an index), we always insert at the end
- When the array is full, we replace the array with a larger one
- How large should the new array be?
 - Incremental strategy: increase the size by a constant c
 - Doubling strategy: double the size

Algorithm *insert(o)*

```
if  $t = S.length - 1$  then
     $A \leftarrow$  new array of
        size ...
    for  $i = 0$  to  $n-1$  do
         $A[i] \leftarrow S[i]$ 
     $S \leftarrow A$ 
     $n \leftarrow n + 1$ 
     $S[n-1] \leftarrow o$ 
```

Comparison of the Strategies

- We compare the incremental strategy and the doubling strategy by analyzing the total time $T(n)$ needed to perform a series of n insert(o) operations
- We assume that we start with an empty vector represented by an array of size 1
- We call amortized time of an insert operation the average time taken by an insert over the series of operations, i.e., $T(n)/n$

Incremental Strategy Analysis

- We replace the array $k = n/c$ times
- The total time $T(n)$ of a series of n insert operations is proportional to

$$n + 1 + c+1 + 2c+1 + 3c+1 \dots + (k-1)c+1 =$$

$$n + k + c(1 + 2 + 3 + \dots + k-1) =$$

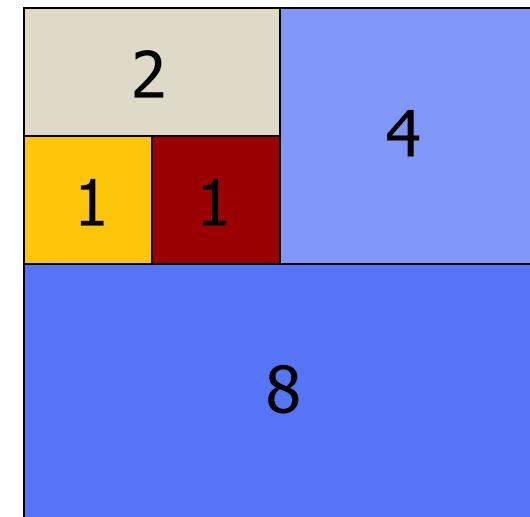
$$n + k + ck(k - 1)/2$$

- Since c is a constant, $T(n)$ is $O(n + k^2)$, i.e., $O(n^2)$
- The amortized time of an insert operation is $O(n)$

Doubling Strategy Analysis

- We replace the array $k = \log_2 n$ times
- The total time $T(n)$ of a series of n insert operations is proportional to
$$n + 1 + 2 + 4 + 8 + \dots + 2^k =$$
$$n + 2^{k+1} - 1 =$$
$$3n - 1$$
- $T(n)$ is $O(n)$
- The amortized time of an insert operation is $O(1)$

geometric series



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Position ADT

- The Position ADT models the notion of place within a data structure where a single object is stored
- It gives a unified view of diverse ways of storing data, such as
 - a cell of an array
 - a node of a linked list
- Just one method:
 - object `p.element()`: returns the element at position
 - In C++ it is convenient to implement this as `*p`

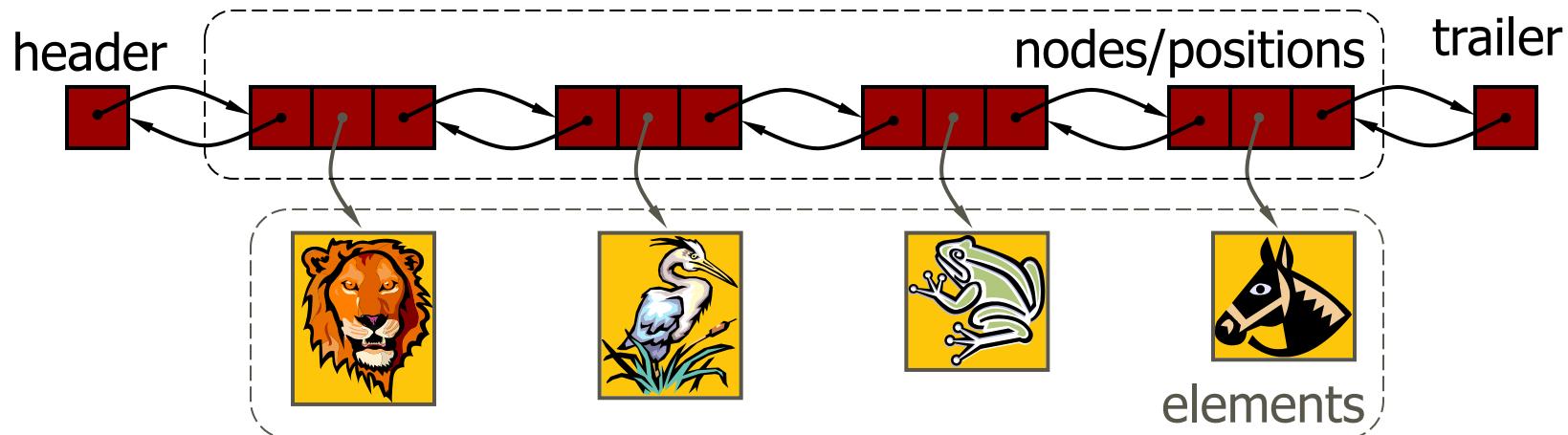
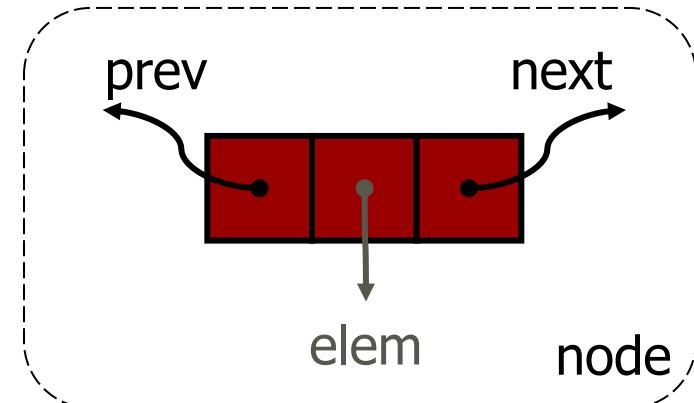
Node List ADT

- The Node List ADT models a sequence of positions storing arbitrary objects
- It establishes a before/after relation between positions
- Generic methods:
 - `size()`, `empty()`

- Iterators:
 - `begin()`, `end()`
- Update methods:
 - `insertFront(e)`,
`insertBack(e)`
 - `removeFront()`,
`removeBack()`
- Iterator-based update:
 - `insert(p, e)`
 - `remove(p)`

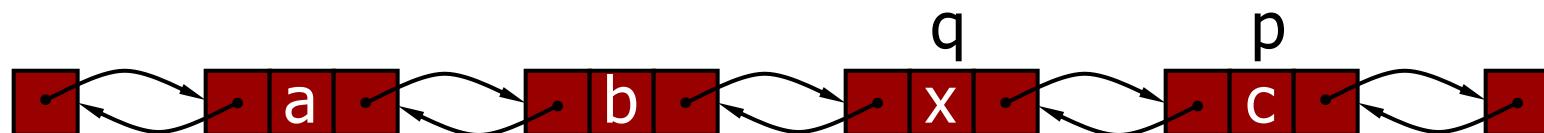
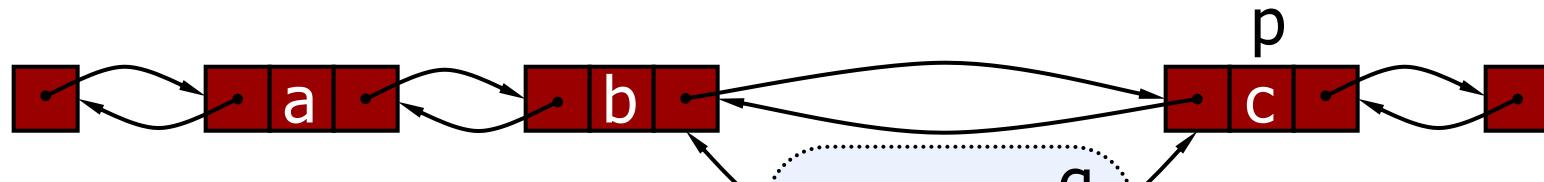
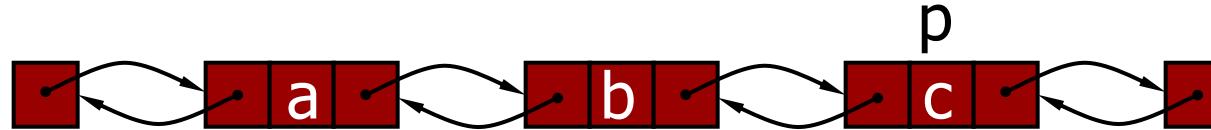
Doubly Linked List

- A doubly linked list provides a natural implementation of the Node List ADT
- Nodes implement Position and store:
 - element
 - link to the previous node
 - link to the next node
- Special trailer and header nodes



Insertion

- We visualize operation $\text{insert}(p, x)$, which inserts x before p



Insertion Algorithm

Algorithm insert(p, e): {insert e before p }

Create a new node v

$v \rightarrow \text{element} = e$

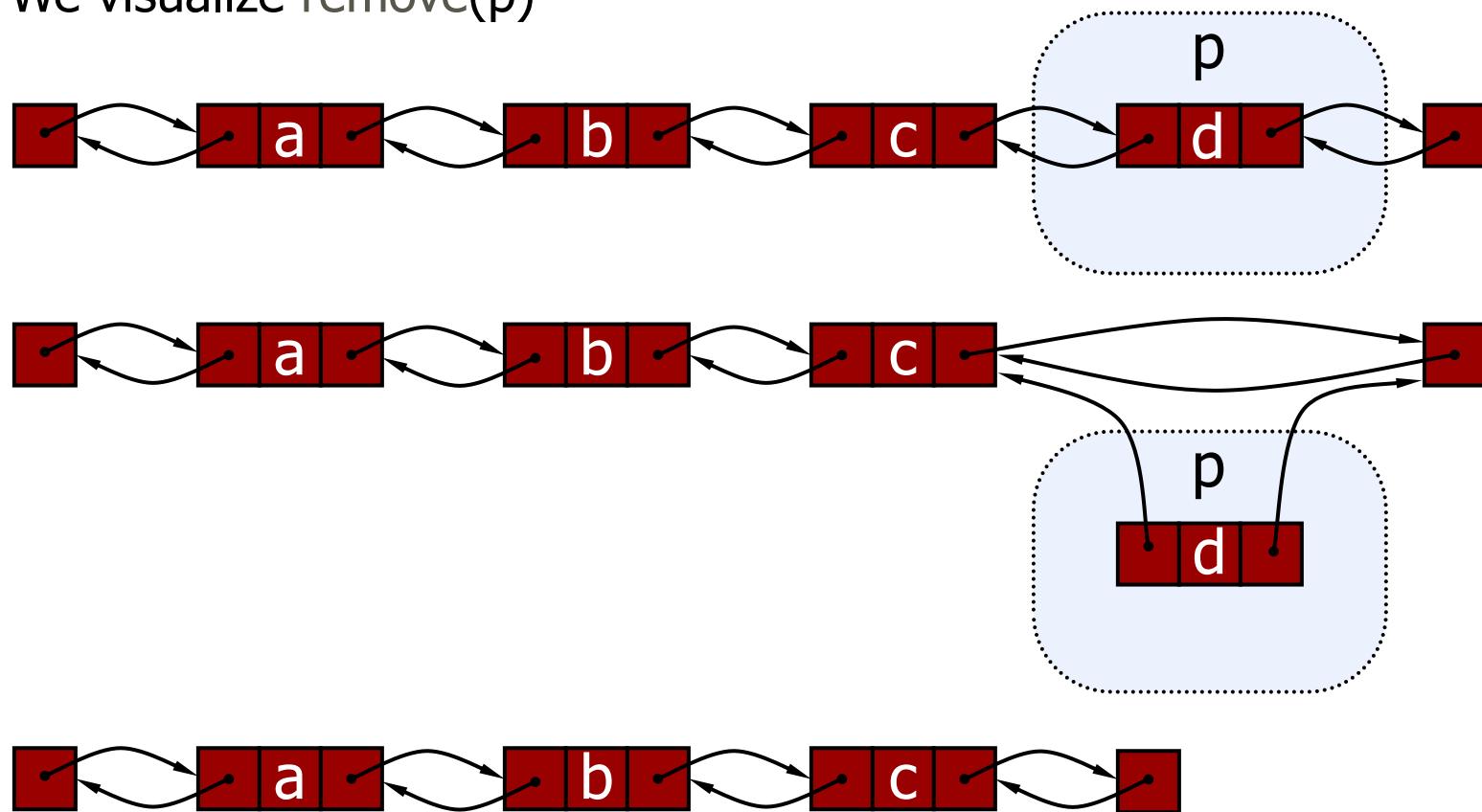
$u = p \rightarrow \text{prev}$

$v \rightarrow \text{next} = p; p \rightarrow \text{prev} = v$ {link in v before p }

$v \rightarrow \text{prev} = u; u \rightarrow \text{next} = v$ {link in v after u }

Deletion

- We visualize $\text{remove}(p)$



Deletion Algorithm

Algorithm remove(p):

$u = p->prev$

$w = p->next$

$u->next = w$ {linking out p }

$w->prev = u$

Performance

- In the implementation of the List ADT by means of a doubly linked list
 - The space used by a list with n elements is $O(n)$
 - The space used by each position of the list is $O(1)$
 - All the operations of the List ADT run in $O(1)$ time
 - Operation `element()` of the Position ADT runs in $O(1)$ time

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Containers and Iterators

- An iterator abstracts the process of scanning through a collection of elements
- A container is an abstract data structure that supports element access through iterators
 - `begin()`: returns an iterator to the first element
 - `end()`: return an iterator to an imaginary position just after the last element
- An iterator behaves like a pointer to an element
 - `*p`: returns the element referenced by this iterator
 - `++p`: advances to the next element
- Extends the concept of position by adding a traversal capability

Containers

- Data structures that support iterators are called **containers (in C++)**
- Examples include Stack, Queue, Vector, List
- Various notions of iterator:
 - (standard) iterator: allows read-write access to elements
 - const iterator: provides read-only access to elements
 - bidirectional iterator: supports both $++p$ and $--p$
 - random-access iterator: supports both $p+i$ and $p-i$

Iterating through a Container

- Let C be a container and p be an iterator for C
for ($p = C.begin(); p != C.end(); ++p)$
loop_body
- Example: (with an STL vector)

```
typedef vector<int>::iterator Iterator;  
int sum = 0;  
for (Iterator p = V.begin(); p != V.end(); ++p)  
    sum += *p;  
return sum;
```

Implementing Iterators

- Array-based
 - array A of the n elements
 - index i that keeps track of the cursor
 - $\text{begin}() = 0$
 - $\text{end}() = n$ (index following the last element)
- Linked list-based
 - doubly-linked list L storing the elements, with sentinels for header and trailer
 - pointer to node containing the current element
 - $\text{begin}() = \text{front node}$
 - $\text{end}() = \text{trailer node (just after last node)}$

STL Iterators in C++

- Each STL container type C supports iterators:
 - `C::iterator` – read/write iterator type
 - `C::const_iterator` – read-only iterator type
 - `C.begin()`, `C.end()` – return start/end iterators
- This iterator-based operators and methods:
 - `*p`: access current element
 - `++p`, `--p`: advance to next/previous element
 - `C.assign(p, q)`: replace C with contents referenced by the iterator range $[p, q]$ (from p up to, but not including, q)
 - `insert(p, e)`: insert e prior to position p
 - `erase(p)`: remove element at position p
 - `erase(p, q)`: remove elements in the iterator range $[p, q]$

Sequence ADT

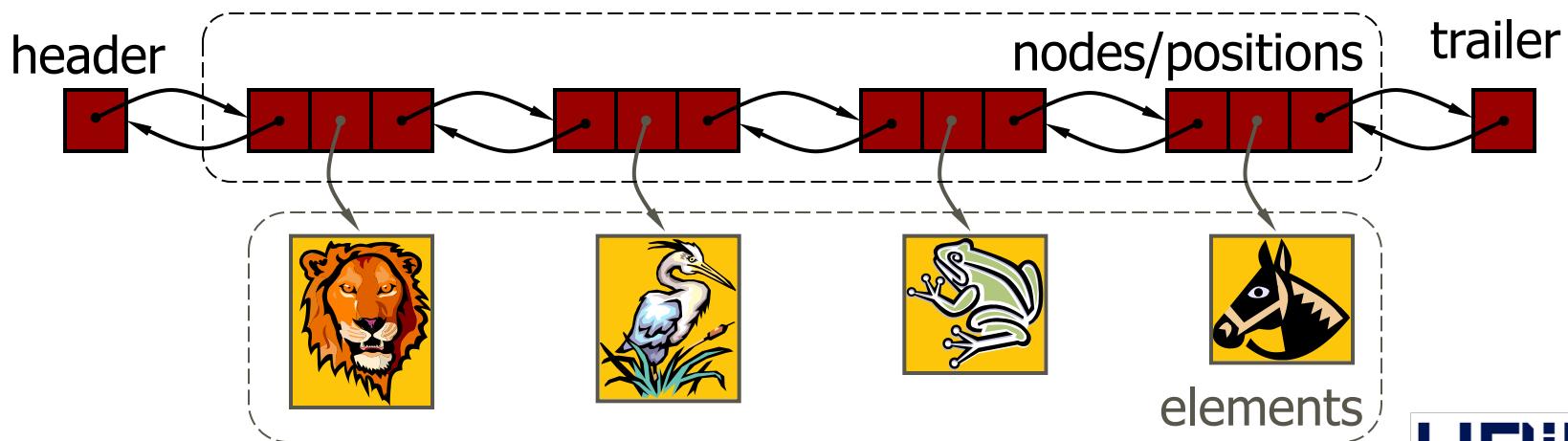
- The Sequence ADT is the union of the Array List and Node List ADTs
- Elements accessed by
 - Index, or
 - Position
- Generic methods:
 - `size()`, `empty()`
- `ArrayList`-based methods:
 - `at(i)`, `set(i, o)`, `insert(i, o)`,
`erase(i)`
- List-based methods:
 - `begin()`, `end()`
 - `insertFront(o)`,
`insertBack(o)`
 - `eraseFront()`,
`eraseBack()`
 - `insert (p, o)`, `erase(p)`
- Bridge methods:
 - `atIndex(i)`, `indexOf(p)`

Applications of Sequences

- The Sequence ADT is a basic, general-purpose, data structure for storing an ordered collection of elements
- Direct applications:
 - Generic replacement for stack, queue, vector, or list
 - small database (e.g., address book)
- Indirect applications:
 - Building block of more complex data structures

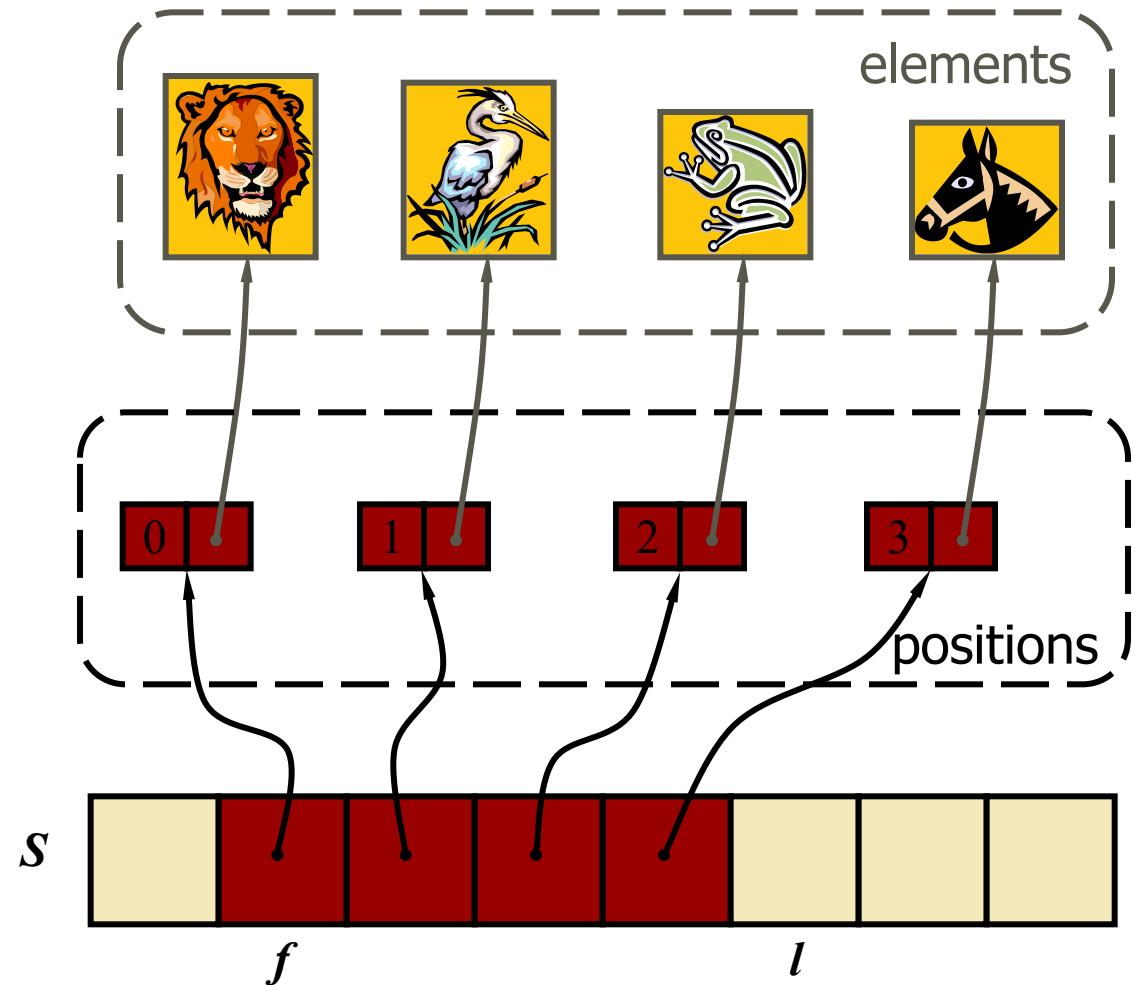
Linked List Implementation

- A doubly linked list provides a reasonable implementation of the Sequence ADT
- Nodes implement Position and store:
 - element
 - link to the previous node
 - link to the next node
- Special trailer and header nodes
 - Position-based methods run in constant time
 - Index-based methods require searching from header or trailer while keeping track of indices; hence, run in linear time



Array-based Implementation

- We use a circular array storing positions
- A position object stores:
 - Element
 - Index
- Indices f and l keep track of first and last positions



Comparing Sequence Implementations

Operation	Array	List
size, empty	1	1
atIndex, indexOf, at	1	n
begin, end	1	1
set(p,e)	1	1
set(i,e)	1	n
insert(i,e), erase(i)	n	n
insertBack, eraseBack	1	1
insertFront, eraseFront	n	1
insert(p,e), erase(p)	n	1

Bubble Sort

```
void bubbleSort1(Sequence& S) {                                // bubble-sort by indices
    int n = S.size();
    for (int i = 0; i < n; i++) {                                // i-th pass
        for (int j = 1; j < n-i; j++) {
            Sequence::Iterator prec = S atIndex(j-1);           // predecessor
            Sequence::Iterator succ = S atIndex(j);              // successor
            if (*prec > *succ) {                                // swap if out of order
                int tmp = *prec; *prec = *succ; *succ = tmp;
            }
        }
    }
}
```

Bubble Sort

```
void bubbleSort2(Sequence& S) {                                // bubble-sort by positions
    int n = S.size();
    for (int i = 0; i < n; i++) {                                // i-th pass
        Sequence::Iterator prec = S.begin();                      // predecessor
        for (int j = 1; j < n-i; j++) {
            Sequence::Iterator succ = prec;
            ++succ;                                              // successor
            if (*prec > *succ) {                                  // swap if out of order
                int tmp = *prec; *prec = *succ; *succ = tmp;
            }
            ++prec;                                              // advance predecessor
        }
    }
}
```

Questions?