

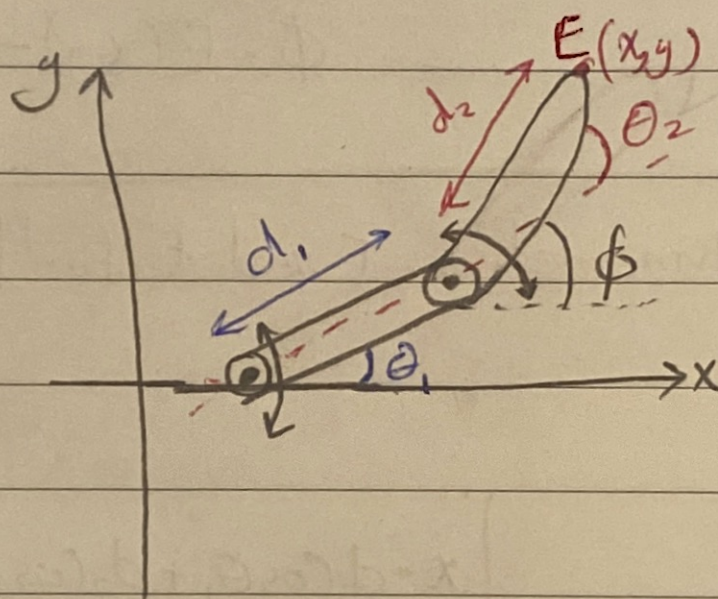
Forward Kinematics ~~Base~~ degree of freedom (DOF)

↳ Given joint angles $\rightarrow \theta_1, \theta_2, d_1, d_2$

↳ We want to find a location of a point in different frame.

* What is Forward Kinematics?

It is a system can be 2D or 3D consist of two rods with a joint that can move in a specific motion specified by an angle.



NOTE:

\ominus : Anti clock $\rightarrow +ve$

\oplus : Clockwise $\rightarrow -ve$

Joint Space

World Space

* $\theta_1, \theta_2 \Rightarrow$ it represents the coordinates attached to the joints.

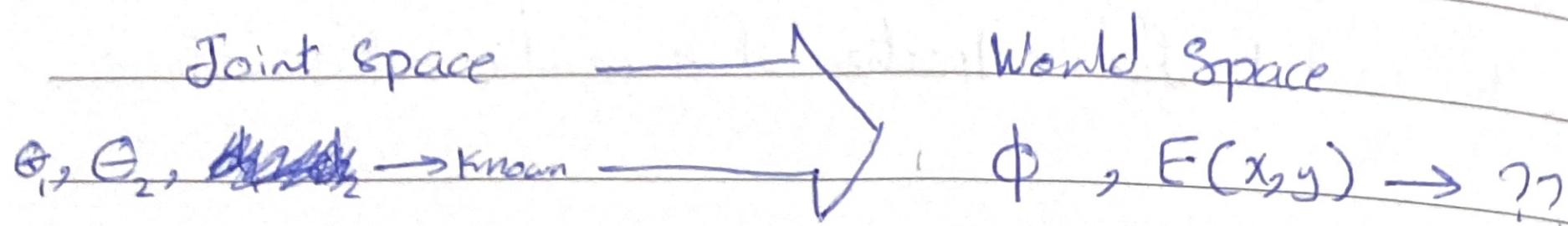
* $\phi, E(x,y) \Rightarrow$ it represents the absolute coordinates of position of end effector.

* $\phi \rightarrow$ represents the overall position of rod " d_2 "

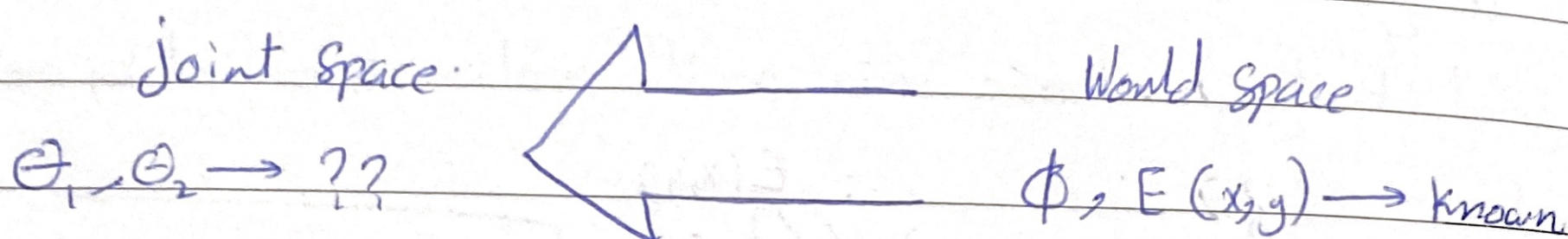
Forward Kinematics \Rightarrow It is a system that goes from joint space to world space in order to find the unknowns.

Summary:

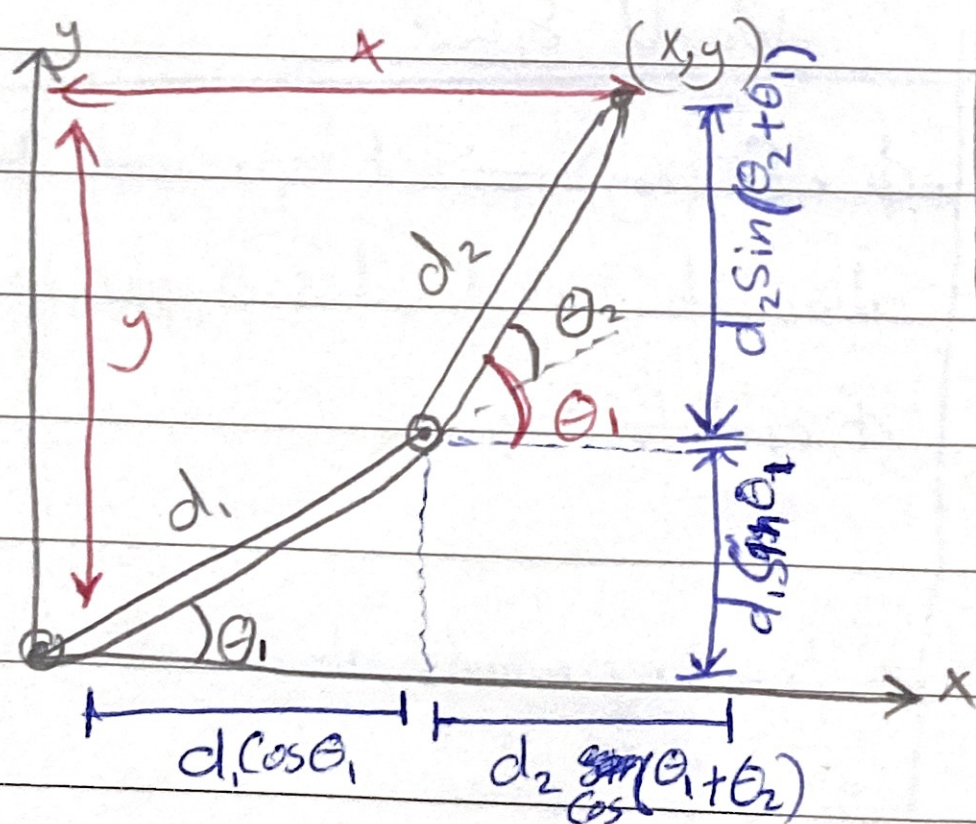
Forward / Direct Kinematics:



Reverse / Indirect Kinematics:



* Two DOF Forward Kinematics. I need to find $[x, y, \phi]$:



$$x = d_1 \cos \theta_1 + d_2 \cos (\theta_1 + \theta_2)$$

$$y = d_1 \sin \theta_1 + d_2 \sin (\theta_1 + \theta_2)$$

$$\boxed{\phi = \theta_1 + \theta_2}$$

$$\sin \theta = \text{opp} / \text{hyp}$$

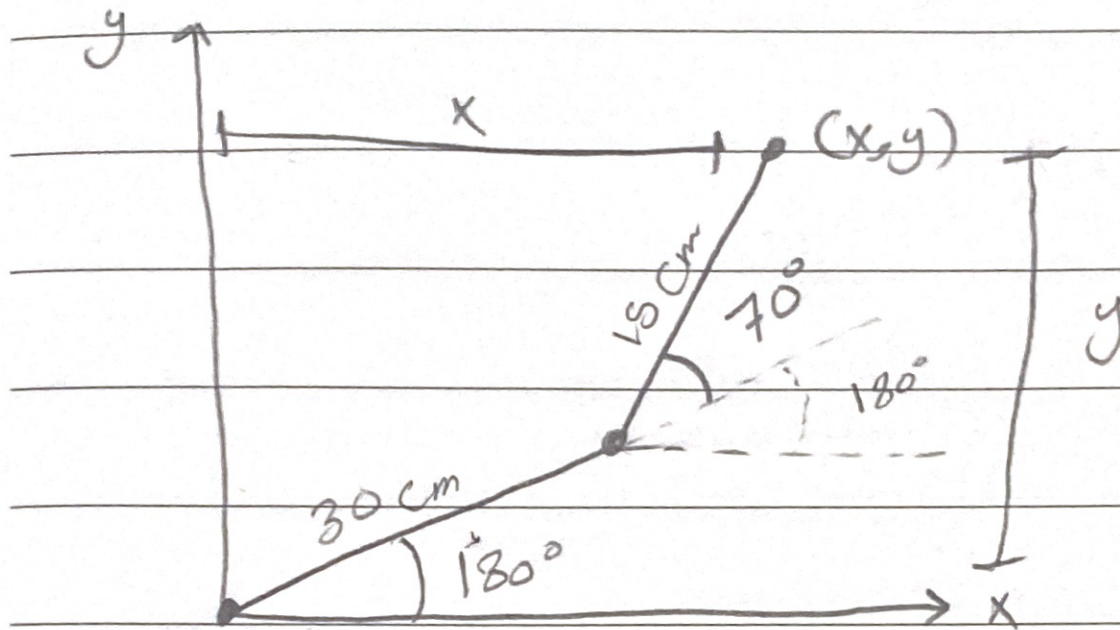
$$\cos \theta = \text{adj} / \text{hyp}$$

$$\tan \theta = \text{opp} / \text{adj}$$

* Calculation of 2 DOF to find $\phi, (x, y)$: Assuming:

$$L_1 = 30 \text{ cm}, L_2 = 15 \text{ cm}, \theta_1 = 180^\circ, \theta_2 = 70^\circ$$

① Design:



② Calculation:

→ Find ϕ :

$$\phi = \theta_1 + \theta_2$$

$$= 180 + 70 = 250^\circ$$

→ Find x :

$$x = L_1 \cos \theta_1 + L_2 \cos (\theta_1 + \theta_2)$$

$$= 30 \cos (180) + 15 \cos (250)$$

$$= -30 - 5.13$$

$$= -35.130 \text{ cm}$$

→ Find y :

$$y = L_1 \sin \theta_1 + L_2 \sin (\theta_1 + \theta_2)$$

$$= 30 \sin (180) + 15 \sin (250)$$

$$= 0 + (-14.095)$$

$$= -14.095 \text{ cm}$$